

1. An infinitely long cylindrical cavity of radius b is bored into a bigger cylinder of radius a . The axes of the two cylinders are parallel but the cylinders are not concentric. The remaining part of the cylinder has a constant volume charge density ρ . Show that the electric field inside the cavity is uniform and directed along the line joining the center of the two cylinders.
2. A hollow spherical shell carries a uniform charge density ρ_0 in the region $a \leq r \leq b$. Find the electric potential as a function of r .
3. The electric field in a region is cylindrically symmetric, given as follows:

$$\begin{aligned}\vec{E}(\vec{r}) &= \frac{c\hat{s}}{s}; & \text{when } s \geq a \\ &= 0; & \text{when } s < a\end{aligned}$$

Find the charge distribution in the region using Gauss' law.

4. Prove the mean value theorem in electrostatics which states that in a chargeless region, the average of the potential over the surface of any sphere is equal to the potential at the center of the sphere.
5. Prove that in a chargeless region electrostatic potential cannot have a maxima or a minima.