

1. An infinitely long cylindrical cavity of radius b is bored into a bigger cylinder of radius a . The axes of the two cylinders are parallel but the cylinders are not concentric. The remaining part of the cylinder has a constant volume charge density ρ . Show that the electric field inside the cavity is uniform and directed along the line joining the center of the two cylinders.
2. A hollow spherical shell carries a uniform charge density ρ_0 in the region $a \leq r \leq b$. Find the electric potential as a function of r .
3. The electric field in a region is cylindrically symmetric, given as follows:

$$\begin{aligned}\vec{E}(\vec{r}) &= \frac{cs}{s}; & \text{when } s \geq a \\ &= 0; & \text{when } s < a\end{aligned}$$

Find the charge distribution in the region using the differential form of Gauss' law $\vec{\nabla} \cdot \vec{E} = \frac{\rho}{\epsilon_0}$.

4. Prove the mean value theorem in electrostatics which states that in a chargeless region, the average of the potential over the surface of any sphere is equal to the potential at the center of the sphere.
This is true for any regular polyhedron. If the faces of a regular polyhedron having n faces are maintained at potentials V_1, V_2, \dots, V_n then the potential at the center of the polyhedron is $(V_1 + V_2 + \dots + V_n)/n$. How many such regular polyhedron do you think are possible? Look for platonic solids. Tetrahedron, cube, octahedron, dodecahedron and icosahedron.
5. Prove that in a chargeless region electrostatic potential cannot have a maxima or a minima.