

Assignment #8

**Exercise 9.11.2**

Sentence #3:  $\forall x (\text{Tet}(x) \wedge \text{Small}(x))$

Sentence #4:  $\forall x (\text{Tet}(x) \rightarrow \text{Small}(x))$

When looking at sentence 3 we evaluate it left to right starting with the inside parentheses. Since  $x$  is a tetrahedron must be true, then  $x$  being small also must be true to satisfy the inside of the “and”. So we can say for all  $x$ ,  $x$  is a tetrahedron and is small. Thus sentence #3 is true.

When we take a look at sentence 4, we interpret  $\rightarrow$  as  $x$  is a tetrahedron if and only if  $x$  is small. Therefore  $x$  must be small so that also means  $x$  is a tetrahedron thus resulting in a true value, sentence #4 is true.

There is no world that exists where sentence #3 is true and sentence #4 is false because they both evaluate truth values.

**Exercise 9.11.3**

Sentence #1:  $\exists x (\text{Dodec}(x) \wedge \text{Large}(x))$

Sentence #2:  $\exists x (\text{Dodec}(x) \rightarrow \text{Large}(x))$

When looking at sentence 3 we evaluate it left to right starting with the inside parentheses. Since  $x$  is a dodec must be true, then  $x$  being large also must be true to satisfy the inside of the “and”. So we can say for all  $x$ ,  $x$  is a dodec and is large. Thus sentence #3 is true.

When we take a look at sentence 4, we interpret  $\rightarrow$  as  $x$  is a dodec if and only if  $x$  is large. Therefore  $x$  must be large so that also means  $x$  is a dodec thus resulting in a true value, sentence #4 is true.

There is no world that exists where sentence #3 is true and sentence #4 is false because they both evaluate truth values.