02/07/2020 EECS 16a Homework 02 Shivani Patel 3033800943

1. Mechanical Gaussian Elimination & Linear Independence

1a)

$$\left[\begin{array}{ccccc|c} 4 & 4 & 4 & 1 & 1 & 1 \\ 1 & 1 & 2 & 4 & 1 & 2 \\ 5 & 5 & 5 & 1 & 1 & 0 \end{array}\right]$$

$R_2 \longleftrightarrow R_1$

$$\left[\begin{array}{ccccc|c} 1 & 1 & 2 & 4 & 1 & 2 \\ 4 & 4 & 4 & 1 & 1 & 1 \\ 5 & 5 & 5 & 1 & 1 & 0 \end{array}\right]$$

$R_2 \leftarrow -4R_1 + R_2$

$$\left[\begin{array}{ccccc|c} 1 & 1 & 2 & 4 & 1 & 2 \\ 0 & 0 & -4 & -15 & -3 & -7 \\ 5 & 5 & 5 & 1 & 1 & 0 \end{array}\right]$$

$R_3 \leftarrow -5R_1 + R_2$

$$\left[\begin{array}{ccccc|c} 1 & 1 & 2 & 4 & 1 & 2 \\ 0 & 0 & -4 & -15 & -3 & -7 \\ 0 & 0 & -5 & -19 & -4 & -10 \end{array}\right]$$

$R_2 \leftarrow R_2 / -4$

$$\left[\begin{array}{ccccc|c} 1 & 1 & 2 & 4 & 1 & 2 \\ 0 & 0 & 1 & \frac{15}{4} & 3/4 & 7/4 \\ 0 & 0 & -5 & -19 & -4 & -10 \end{array}\right]$$

$R_1 \leftarrow -2R_2 + R_1$
$R_3 \leftarrow 5R_2 + R_3$

$$\left[\begin{array}{ccccc|c} 1 & 1 & 0 & -7/2 & -1/2 & -3/2 \\ 0 & 0 & 1 & 15/4 & 3/4 & 7/4 \\ 0 & 0 & 0 & -1/4 & -\frac{1}{4} & -\frac{5}{4} \end{array}\right]$$

$R_3 \leftarrow R_3 / -\frac{1}{4}$

$$\left[\begin{array}{ccccc|c} 1 & 1 & 0 & -7/2 & -\frac{1}{2} & -3/2 \\ 0 & 0 & 1 & \frac{15}{4} & \frac{3}{4} & 7/4 \\ 0 & 0 & 0 & 1 & 1 & 5 \end{array}\right]$$

$R_1 \leftarrow 7/2\, R_3 + R_1$
$R_2 \leftarrow -\frac{15}{4} R_3 + R_2$

$$\left[\begin{array}{ccccc|c} 1 & 1 & 0 & 0 & 3 & 16 \\ 0 & 0 & 1 & 0 & -3 & -17 \\ 0 & 0 & 0 & 1 & 1 & 5 \end{array}\right]$$

1b. basic variables:

x, z, w

free variables

y and v

1c. parameterize the solution

$x = 16 - y - 3v$

$z = -17 - 3v$

$w = 5 - v$

1di) $\left\{ \begin{bmatrix} -5 \\ 2 \end{bmatrix}, \begin{bmatrix} 5 \\ 2 \end{bmatrix} \right\}$

$$\Downarrow$$

$$\begin{array}{cc} x_1 & x_2 \end{array}$$
$$\begin{bmatrix} -5 & 5 \\ 2 & 2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

rref:

$$\left[\begin{array}{cc|c} -5 & 5 & 0 \\ 2 & 2 & 0 \end{array}\right] \Rightarrow \left[\begin{array}{cc|c} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array}\right]$$

$\boxed{\text{Dependent } x_1 = 0, \ x_2 = 0}$

1dii

$$\left\{ \begin{bmatrix} -1 \\ 5 \\ 0 \\ -3 \\ \frac{1}{2} \end{bmatrix}, \begin{bmatrix} -7 \\ 20 \\ 24 \\ -12 \\ 0 \end{bmatrix}, \begin{bmatrix} \frac{1}{2} \\ 0 \\ -4 \\ 0 \\ \frac{1}{3} \end{bmatrix} \right\}$$

$$\left[\begin{array}{ccc|c} -1 & -7 & \frac{1}{2} & 0 \\ 5 & 20 & 0 & 0 \\ 0 & 24 & -4 & 0 \\ -3 & -12 & 6 & 0 \\ \frac{1}{2} & 0 & \frac{1}{3} & 0 \end{array}\right]$$

2 Finding charges from potential measurements

① Pythagorean Theorem

$r_{11} = \sqrt{2}$	$r_{12} = \sqrt{5}$	$r_{13} = 2$
$r_{21} = 1$	$r_{22} = \sqrt{2}$	$r_{23} = 1$
$r_{31} = 2$	$r_{23} = \sqrt{5}$	$r_{33} = \sqrt{2}$

② then potential(V)

$$V_1 = K\left(\frac{Q_1}{\sqrt{2}} + \frac{Q_2}{\sqrt{5}} + \frac{Q_3}{2}\right)$$
$$V_2 = K\left(Q_1 + \frac{Q_2}{\sqrt{2}} + Q_3\right)$$
$$V_3 = K\left(\frac{Q_1}{2} + \frac{Q_2}{\sqrt{5}} + \frac{Q_3}{\sqrt{2}}\right)$$

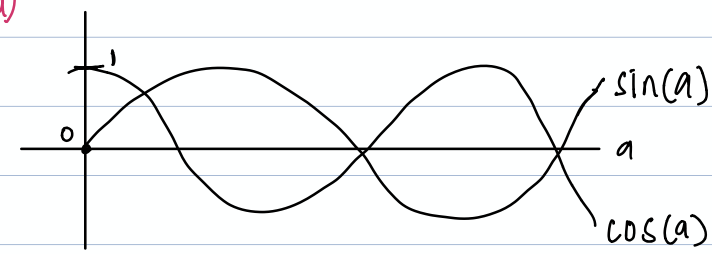
③ plug in given potential and cancel out k

$$\frac{Q_1}{\sqrt{2}} + \frac{Q_2}{\sqrt{5}} + \frac{Q_3}{2} = \frac{4+3\sqrt{5}+\sqrt{10}}{2\sqrt{5}}$$
$$Q_1 + \frac{Q_2}{\sqrt{2}} + Q_3 = \frac{2+4\sqrt{2}}{\sqrt{2}}$$
$$\frac{Q_1}{2} + \frac{Q_2}{\sqrt{5}} + \frac{Q_3}{\sqrt{2}} = \frac{4+\sqrt{5}+3\sqrt{10}}{2\sqrt{5}}$$

Final Answer $\longrightarrow$ $Q_1 = 1$, $Q_2 = 2$, $Q_3 = 3$ IPython code

3. Kinematic Model for a simple car

3a)



when a is small the cos(a) graph approaches 1 and the sin(a) graph approaches Ø.

3b)

A = np.array([[1, 0, 0, 0],
[0, 1, 0, 0],
[0, 0, 1, 0],
[0, 0, 0, 1]])

B = np.array $\begin{bmatrix} 0, 0 \\ 0, 0 \\ 0, 0 \\ 1, 0 \end{bmatrix}$

3c) x-init = 5

y-init = 10

theta-init = 0.0

v-init = 2.0

a-init = 1.0

phi-init = 0.0001

extremely small from 3a description

3d) x-init = 5

y-init = 10

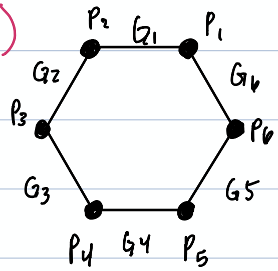
theta_init = 0

v_init = 2

a_init = 1

phi_input = 0.5

4 Figuring out the tips

4a) 

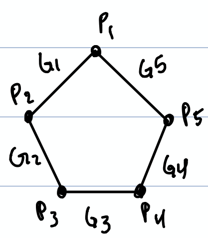
you cannot determine this in general

$$\underbrace{\begin{matrix}(P_1, P_2, P_3, P_4, P_5, P_6) = (2,0,2,0,2,0) \\ (P_1, P_2, P_3, P_4, P_5, P_6) = (0,2,0,2,0,2)\end{matrix}}$$

$(P_1, P_2, P_3, P_4, P_5, P_6) = (1,1,1,1,1,1)$

$$\begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} P_1 \\ P_2 \\ P_3 \\ P_4 \\ P_5 \\ P_6 \end{bmatrix} = \begin{bmatrix} 2G_1 \\ 2G_2 \\ 2G_3 \\ 2G_4 \\ 2G_5 \\ 2G_6 \end{bmatrix} \longrightarrow$$

this shows that every other seat tips the associated amount. the six-sided table is symetric so it is not possible to conclude everyone's tip

4b) 

can be reduced to the system of equations:

Row reduced form

$$\begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} P_1 \\ P_2 \\ P_3 \\ P_4 \\ P_5 \end{bmatrix} = \begin{bmatrix} 2G1 \\ 2G2 \\ 2G3 \\ 2G4 \\ 2G5 \end{bmatrix} = \left.\begin{bmatrix} G_1 - G_2 + G_3 - G_4 + G_5 \\ G_2 - G_3 + G_4 - G_5 + G_1 \\ G_3 - G_4 + G_5 - G_1 + G_2 \\ G_4 - G_5 + G_1 - G_2 + G_3 \\ G_5 - G_1 + G_2 - G_3 + G_4 \end{bmatrix}\right\}$$

unique solution for $P_1 - P_5$ through $G_1 - G_5$

conclusion:

there is an odd number of seats so we would be able to calculate the tips through the matrix.

4(c) we can only determine odd values of tips. A possible way to do this is through Gaussian Elimination solution.

$$\begin{bmatrix} 1 & 1 & 0 & 0 & \cdots & 0 \\ 0 & 1 & 1 & \cdots & & 0 \\ & & \ddots & & & \\ 0 & \cdots & & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 & \cdots & 1 \end{bmatrix}$$

① subtract odd numbered rows from row n and add even rows to row n

we are looking for the ith item in row n. through ① we know that n is odd so we can figure out that $Row_{n,n-1} = 0$ and $Row_{n,n} = 2$. this shows linear independence

5. Proof: Linear Dependence is a square matrix

I could not figure out this problem

5a)

5b)

6. Image stitching

6a) $$\vec{v_2} = \begin{bmatrix} 2 & 2 \\ -2 & 2 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 2 \\ 2 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 3 \\ 3 \end{bmatrix}$$

through this we see that $\vec{v_2}$ is rotated by 45° and scaled by 3!

6b) $$\begin{bmatrix} q_x \\ q_y \end{bmatrix} = \begin{bmatrix} R_{xx} & R_{xy} \\ R_{yx} & R_{yy} \end{bmatrix} \begin{bmatrix} p_x \\ p_y \end{bmatrix} + \begin{bmatrix} T_x \\ T_y \end{bmatrix}$$

$$q_x = p_x R_{xx} + p_y R_{xy} + T_x$$

$$q_y = p_x R_{yx} + p_y R_{yy} + T_y$$

There are 6 unknowns and they lie in R matrix ($R_{xx}, R_{xy}, R_{yx}, R_{yy}$) and $\vec{T}$ (t_x, T_y). This means we would need 6 equations to solve them. We would need 3 pairs of common points $\vec{p}$ and $\vec{q}$ to solve for the unknowns

6c) (q_1, p_1) (q_2, p_2) (q_2, p_3)

$$\begin{bmatrix} q_{1x} \\ q_{1y} \\ q_{2x} \\ q_{2y} \\ q_{3x} \\ q_{3y} \end{bmatrix} = \begin{bmatrix} p_{1x} & p_{1y} & 0 & 0 & 1 & 0 \\ 0 & 0 & p_{1x} & p_{1y} & 0 & 1 \\ p_{2x} & p_{2y} & 0 & 0 & 1 & 0 \\ 0 & 0 & p_{2x} & p_{2y} & 0 & 1 \\ p_{3x} & p_{3y} & 0 & 0 & 1 & 0 \\ 0 & 0 & p_{3x} & p_{3y} & 0 & 1 \end{bmatrix} \begin{bmatrix} R_{xx} \\ R_{xy} \\ R_{yx} \\ R_{yy} \\ T_x \\ T_y \end{bmatrix} = \begin{bmatrix} q_{1x} \\ q_{1y} \\ q_{2x} \\ q_{2y} \\ q_{3x} \\ q_{3y} \end{bmatrix}$$

7. Homework Process and Study Group

I worked with Sadia Qureshi (3034541667)

I did it by myself for roughly 6-8 hours then I worked with sadia for an hour

EECS16A: Homework 2

Problem 2: Finding Charges from Potential Measurements

In [4]:
```
import numpy as np
r11 = np.sqrt(2); r12 = np.sqrt(5); r13 = 2
r21 = 1; r22 = np.sqrt(2); r23 = 1
r31 = 2; r32 = np.sqrt(5); r33 = np.sqrt(2);
y1 = (4 + 3*np.sqrt(5) + np.sqrt(10))/(2*np.sqrt(5))
y2 = (2 + 4*np.sqrt(2))/( np.sqrt(2) )
y3 = (4 + np.sqrt(5) + 3*np.sqrt(10)) / ( 2*np.sqrt(5) )

a = np.array([
    [1/r11, 1/r12, 1/r13],
    [1/r21, 1/r22, 1/r23],
    [1/r31, 1/r32, 1/r33]
])
b= np.array([y1, y2, y3])
x= np.linalg.solve(a,b)
print(x)
```

```
[1. 2. 3.]
```

Problem 3: Kinematic Model for a Simple Car

This script helps to visualize the difference between a nonlinear model and a corresponding linear approximation for a simple car. What you should notice is that the linear model is similar to the nonlinear model when you are close to the point where the approximation is made.

First, run the following block to set up the helper functions needed to simulate the vehicle models and plot the trajectories taken.

In [3]:
```
# DO NOT MODIFY THIS BLOCK!
''' Problem/Model Setup'''
import numpy as np
import matplotlib.pyplot as plt
%matplotlib inline

# Vehicle Model Constants
L = 1.0  # length of the car, meters
dt = 0.1 # time difference between timestep (k+1) and timestep k, second
s

''' Nonlinear Vehicle Model Update Equation '''
def nonlinear_vehicle_model(initial_state, inputs, num_steps):
    x     = initial_state[0] # x position, meters
    y     = initial_state[1] # y position, meters
    theta = initial_state[2] # heading (wrt x-axis), radians
    v     = initial_state[3] # speed, meters per second

    a = inputs[0]            # acceleration, meters per second squared
    phi = inputs[1]          # steering angle, radians

    state_history = []       # array to hold state values as the time st
ep k advances.
    state_history.append([x,y,theta,v]) # add the initial state (i.e. k
 = 0) to history.

    for i in range(0, num_steps):
        # Find the next state, at time k+1, by applying the nonlinear mo
del to the current state, at time k.
        x_next     = x     + v * np.cos(theta) * dt
        y_next     = y     + v * np.sin(theta) * dt
        theta_next = theta + v/L * np.tan(phi) * dt
        v_next     = v     + a * dt

        # Add the next state to the history.
        state_history.append([x_next,y_next,theta_next,v_next])

        # Advance to the next state, at time k+1, to get ready for next
 loop iteration.
        x = x_next
        y = y_next
        theta = theta_next
        v = v_next

    return np.array(state_history)

''' Linear Vehicle Model Update Equation '''
def linear_vehicle_model(A, B, initial_state, inputs, num_steps):
    # Note: A should be a 4x4 matrix, B should be a 4x2 matrix for this
 linear model.

    x     = initial_state[0] # x position, meters
    y     = initial_state[1] # y position, meters
    theta = initial_state[2] # heading (wrt x-axis), radians
    v     = initial_state[3] # speed, meters per second
```

```
    a = inputs[0]              # acceleration, meters per second squared
    phi = inputs[1]            # steering angle, radians

    state_history = []         # array to hold state values as the time st
ep k advances.
    state_history.append([x,y,theta,v]) # add the initial state (i.e. k
 = 0) to history.

    for i in range(0, num_steps):
        # Find the next state, at time k+1, by applying the nonlinear mo
del to the current state, at time k.
        state_next = np.dot(A, state_history[-1]) + np.dot(B, inputs)

        # Add the next state to the history.
        state_history.append(state_next)

        # Advance to the next state, at time k+1, to get ready for next
 loop iteration.
        state = state_next

    return np.array(state_history)

''' Plotting Setup'''
def make_model_comparison_plot(state_predictions_nonlinear, state_predic
tions_linear):
    f = plt.figure()
    plt.plot(state_predictions_nonlinear[0,0], state_predictions_nonline
ar[0,1], 'go', label='Start')
    plt.plot(state_predictions_nonlinear[:,0], state_predictions_nonline
ar[:,1], 'r', label='Nonlinear')
    plt.plot(state_predictions_linear[:,0], state_predictions_linear[:,1
], 'k.', label='Linear')
    plt.legend(loc='upper left')
    plt.xlim([4, 8])
    plt.ylim([9, 12])
    plt.show()
```

Part B

Task: Fill in the matrices A and B for the linear system approximating the nonlinear vehicle model under small heading and steering angle approximations.

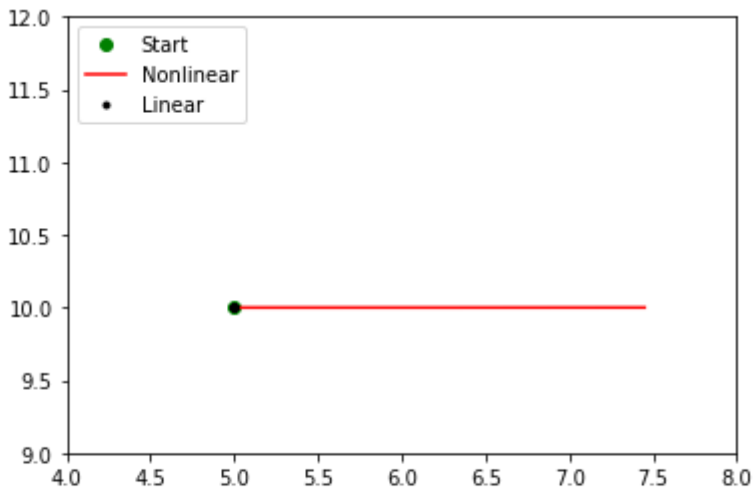
In [4]:

```
# Your code here.
A = np.array([[1, 0, 0, 0],
              [0, 1, 0, 0],
              [0, 0, 1, 0],
              [0, 0, 0, 1]])

B = np.array([[ 0, 0],
              [ 0, 0],
              [ 0, 0],
              [ 1, 0]])
```

Part C

Task: Fill out the state and input values from Part C and look at the resulting plot. The plot should help you to visualize the difference between using a linear model and a nonlinear model for this specific starting state and input.

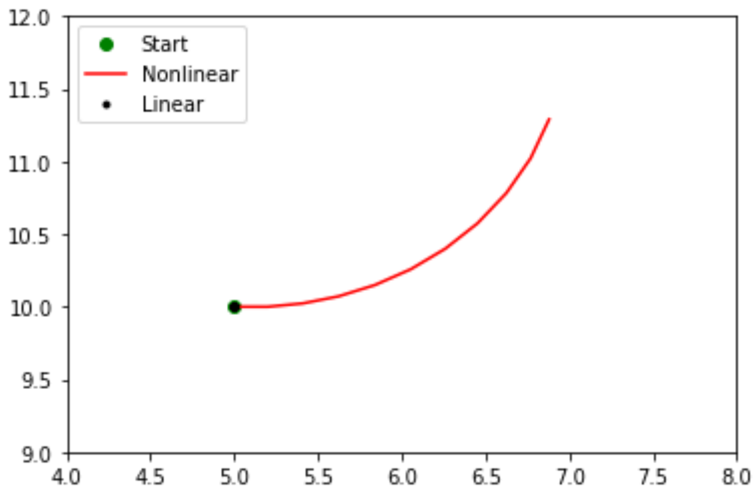
In [6]:
```
# Your code here.
x_init   = 5
y_init   = 10
theta_init = 0
v_init     = 2
a_input    = 1
phi_input  = 0.0001

state_init = [x_init, y_init, theta_init, v_init]
state_predictions_nonlinear = nonlinear_vehicle_model(state_init, [a_inp
ut, phi_input], 10)
state_predictions_linear = linear_vehicle_model(A, B, state_init, [a_inp
ut, phi_input], 10)

make_model_comparison_plot(state_predictions_nonlinear, state_prediction
s_linear)
```



Part D

Task: Fill out the state and input values from Problem D and look at the resulting plot. The plot should help you to visualize the difference between using a linear model and a nonlinear model for this specific starting state and input.

In [7]:
```
# Your code here.
x_init   = 5
y_init   = 10
theta_init = 0
v_init     = 2
a_input    = 1
phi_input  = 0.5

state_init = [x_init, y_init, theta_init, v_init]
state_predictions_nonlinear = nonlinear_vehicle_model(state_init, [a_inp
ut, phi_input], 10)
state_predictions_linear = linear_vehicle_model(A, B, state_init, [a_inp
ut, phi_input], 10)

make_model_comparison_plot(state_predictions_nonlinear, state_prediction
s_linear)
print(state_predictions_nonlinear[10])
print(state_predictions_linear[10])
```




```
[ 6.87984693 11.28998941  1.3384411   3.        ]
[ 5. 10.  0. 12.]
```

Problem 6: Image Stitching

This section of the notebook continues the image stitching problem. Be sure to have a `figures` folder in the same directory as the notebook. The `figures` folder should contain the files:

```
Berkeley_banner_1.jpg
Berkeley_banner_2.jpg
stacked_pieces.jpg
lefthalfpic.jpg
righthalfpic.jpg
```

Note: This structure is present in the provided HW2 zip file.

Part D

Run the next block of code before proceeding

In [8]:
```
import numpy as np
import numpy.matlib
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
from numpy import pi, cos, exp, sin
import matplotlib.image as mpimg
import matplotlib.transforms as mtransforms


#%matplotlib inline

#loading images
image1=mpimg.imread('figures/Berkeley_banner_1.jpg')
image1=image1/255.0
image2=mpimg.imread('figures/Berkeley_banner_2.jpg')
image2=image2/255.0
image_stack=mpimg.imread('figures/stacked_pieces.jpg')
image_stack=image_stack/255.0


image1_marked=mpimg.imread('figures/lefthalfpic.jpg')
image1_marked=image1_marked/255.0
image2_marked=mpimg.imread('figures/righthalfpic.jpg')
image2_marked=image2_marked/255.0

def euclidean_transform_2to1(transform_mat,translation,image,position,LL
,UL):
    new_position=np.round(transform_mat.dot(position)+translation)
    new_position=new_position.astype(int)


    if (new_position>=LL).all() and (new_position<UL).all():
        values=image[new_position[0][0],new_position[1][0],:]
    else:
        values=np.array([2.0,2.0,2.0])

    return values

def euclidean_transform_1to2(transform_mat,translation,image,position,LL
,UL):
    transform_mat_inv=np.linalg.inv(transform_mat)
    new_position=np.round(transform_mat_inv.dot(position-translation))
    new_position=new_position.astype(int)

    if (new_position>=LL).all() and (new_position<UL).all():
        values=image[new_position[0][0],new_position[1][0],:]
    else:
        values=np.array([2.0,2.0,2.0])

    return values

def solve(A,b):
    try:
        z = np.linalg.solve(A,b)
    except:
        raise ValueError('Rows are not linearly independent. Cannot solv
```

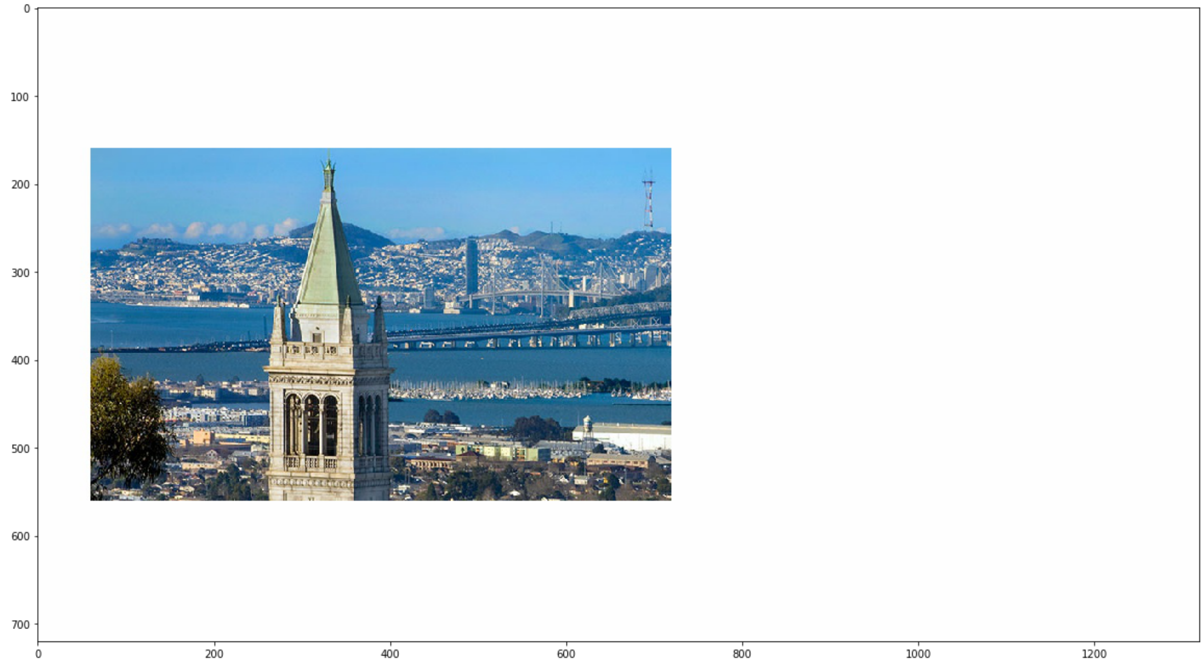
```
e system of linear equations uniquely. :)')
    return z
```

We will stick to a simple example and just consider stitching two images (if you can stitch two pictures, then you could conceivably stitch more by applying the same technique over and over again).

Daniel decided to take an amazing picture of the Campanile overlooking the bay. Unfortunately, the field of view of his camera was not large enough to capture the entire scene, so he decided to take two pictues and stitch them together.

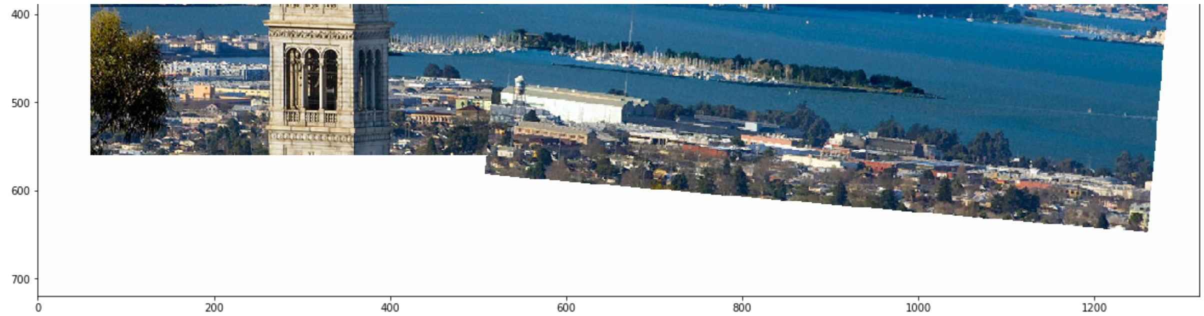
The next block will display the two images.

In [9]:
```
plt.figure(figsize=(20,40))

plt.subplot(311)
plt.imshow(image1)

plt.subplot(312)
plt.imshow(image2)

plt.subplot(313)
plt.imshow(image_stack)

plt.show()
```


0
100
200
300
400
500
600
700
0
200
400
600
800
1000
1200


0
100
200
300
400
500
600
700
0
200
400
600
800
1000
1200

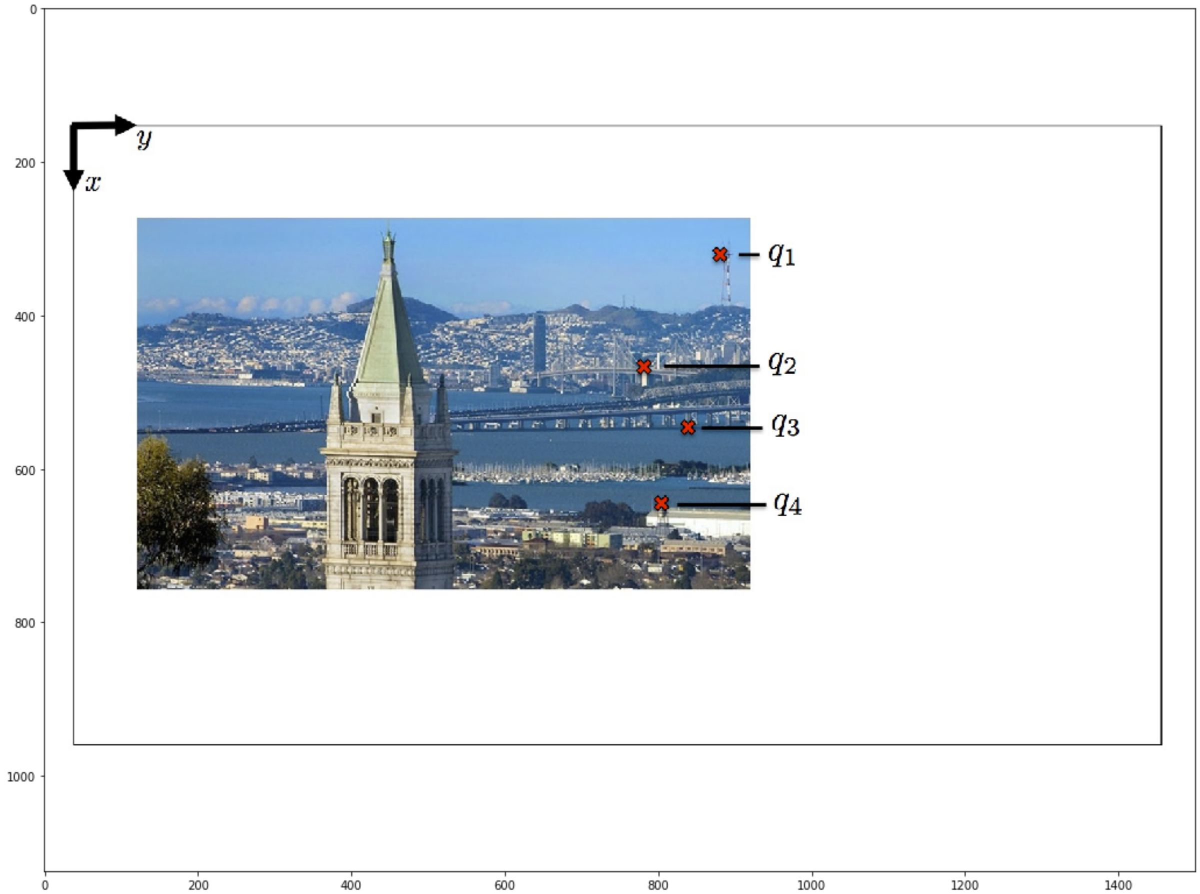

0
100
200
300

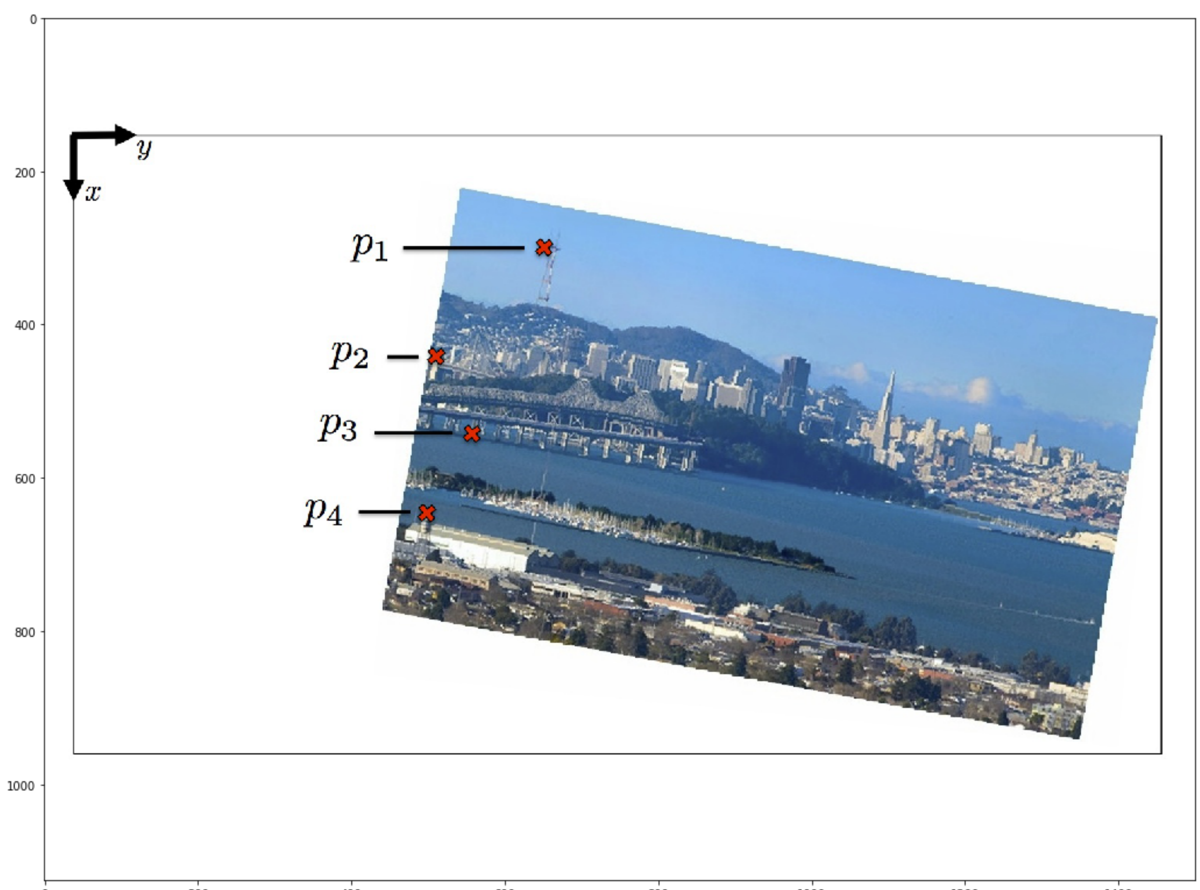


Once you apply Marcela's algorithm on the two images you get the following result (run the next block):

In [10]:
```
plt.figure(figsize=(20,30))

plt.subplot(211)
plt.imshow(image1_marked)

plt.subplot(212)
plt.imshow(image2_marked)
```

Out[10]: <matplotlib.image.AxesImage at 0x1157c3f90>


0
200
400
600
800
1000
0
200
400
600
800
1000
1200
1400
y
x
q_1
q_2
q_3
q_4


0
200
400
600
800
1000
0
200
400
600
800
1000
1200
1400
y
x
p_1
p_2
p_3
p_4

As you can see Marcela's algorithm was able to find four common points between the two images. These points expressed in the coordinates of the first image and second image are

$$\vec{p_1} = \begin{bmatrix} 200 \\ 700 \end{bmatrix} \qquad \vec{p_2} = \begin{bmatrix} 310 \\ 620 \end{bmatrix} \qquad \vec{p_3} = \begin{bmatrix} 390 \\ 660 \end{bmatrix} \qquad \vec{p_4} = \begin{bmatrix} 460 \\ 630 \end{bmatrix}$$

$$\vec{q_1} = \begin{bmatrix} 162.2976 \\ 565.8862 \end{bmatrix} \qquad \vec{q_2} = \begin{bmatrix} 285.4283 \\ 458.7469 \end{bmatrix} \qquad \vec{q_3} = \begin{bmatrix} 385.2465 \\ 498.1973 \end{bmatrix} \qquad \vec{q_4} = \begin{bmatrix} 465.7892 \\ 455.0132 \end{bmatrix}$$

It should be noted that in relation to the image the positive x-axis is down and the positive y-axis is right. This will have no bearing as to how you solve the problem, however it helps in interpreting what the numbers mean relative to the image you are seeing.

Using the points determine the parameters $R_{11}, R_{12}, R_{21}, R_{22}, T_x, T_y$ that map the points from the first image to the points in the second image by solving an appropriate system of equations. Hint: you do not need all the points to recover the parameters.

In [12]:

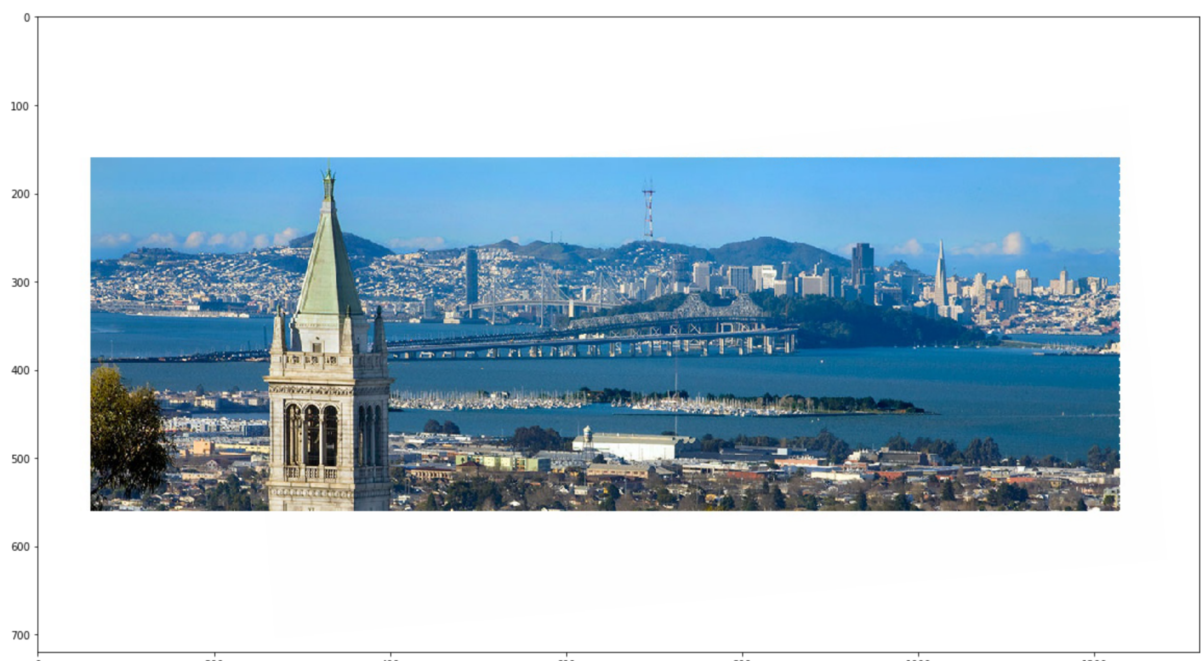
```
# Note that the following is a general template for solving for 6 unknowns from 6 equations represented as Az = b.
# You do not have to use the following code exactly.
# All you need to do is to find parameters R_11, R_12, R_21, R_22, T_x, T_y.
# If you prefer finding them another way it is fine.

# fill in the entries
A = np.array([[200, 700, 0, 0, 1, 0],
              [0, 0, 200, 700, 0, 1],
              [310, 620, 0, 0, 1, 0],
              [0, 0, 310, 620, 0, 1],
              [390, 660, 0, 0, 1, 0],
              [0, 0, 390, 660, 0, 1]])

# fill in the entries
b = np.array([[162.2976],[565.8862],[285.4283],[458.7469],[385.2465],[498.1973]])

A = A.astype(float)
b = b.astype(float)

# solve the linear system for the coefficiens
z = solve(A,b)

#Parameters for our transformation
R_11 = z[0,0]
R_12 = z[1,0]
R_21 = z[2,0]
R_22 = z[3,0]
T_x  = z[4,0]
T_y  = z[5,0]
```

Stitch the images using the transformation you found by running the code below.

Note that it takes about 40 seconds for the block to finish running on a modern laptop.

In [13]:
```
matrix_transform=np.array([[R_11,R_12],[R_21,R_22]])
translation=np.array([T_x,T_y])

#Creating image canvas (the image will be constructed on this)
num_row,num_col,blah=image1.shape
image_rec=1.0*np.ones((int(num_row),int(num_col),3))

#Reconstructing the original image

LL=np.array([[0],[0]]) #lower limit on image domain
UL=np.array([[num_row],[num_col]]) #upper limit on image domain

for row in range(0,int(num_row)):
    for col in range(0,int(num_col)):
        #notice that the position is in terms of x and y, so the c
        position=np.array([[row],[col]])
        if image1[row,col,0] > 0.995 and image1[row,col,1] > 0.995 and i
mage1[row,col,2] > 0.995:
            temp = euclidean_transform_2to1(matrix_transform,translation
,image2,position,LL,UL)
            image_rec[row,col,:] = temp
        else:
            image_rec[row,col,:] = image1[row,col,:]


plt.figure(figsize=(20,20))
plt.imshow(image_rec)
plt.axis('on')
plt.show()
```

```
Clipping input data to the valid range for imshow with RGB data ([0..1]
for floats or [0..255] for integers).
```



In [ ]: