Class 09 Mini-Project

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read in data fna.data <- "WisconsinCancer.csv"</pre> wisc.df <- read.csv(fna.data, row.names=1)</pre> show dataframe #wisc.df remove first column(expert diagonosis) wisc.data <- wisc.df[,-1]</pre> expert diagnosis diagnosis <- as.factor(wisc.df[,1])</pre> Q1. How many observations are in this dataset? nrow(wisc.data) ## [1] 569 Q2. How many of the observations have a malignant diagnosis? length(which(diagnosis == "M")) ## [1] 212 Q3. How many variables/features in the data are suffixed with _mean? sum(grepl("*_mean", colnames(wisc.data)))

checking means and standard devs for each column to see if it needs to be scaled

[1] 10

colMeans(wisc.data)

```
##
               radius mean
                                        texture mean
                                                               perimeter mean
##
               1.412729e+01
                                        1.928965e+01
                                                                  9.196903e+01
##
                                     smoothness mean
                                                             compactness mean
                  area mean
##
               6.548891e+02
                                        9.636028e-02
                                                                 1.043410e-01
##
            concavity_mean
                                 concave.points_mean
                                                                symmetry_mean
##
               8.879932e-02
                                        4.891915e-02
                                                                  1.811619e-01
##
    fractal_dimension_mean
                                           radius_se
                                                                    texture_se
##
                                                                 1.216853e+00
              6.279761e-02
                                        4.051721e-01
##
              perimeter_se
                                             area_se
                                                                 smoothness_se
##
               2.866059e+00
                                                                 7.040979e-03
                                        4.033708e+01
                                                            concave.points_se
##
            compactness_se
                                        concavity_se
##
              2.547814e-02
                                        3.189372e-02
                                                                 1.179614e-02
                               fractal_dimension_se
##
               symmetry_se
                                                                 radius worst
                                        3.794904e-03
                                                                 1.626919e+01
##
               2.054230e-02
##
             texture_worst
                                     perimeter_worst
                                                                    area_worst
##
               2.567722e+01
                                        1.072612e+02
                                                                  8.805831e+02
##
                                                              concavity_worst
          smoothness_worst
                                   compactness_worst
##
               1.323686e-01
                                        2.542650e-01
                                                                  2.721885e-01
##
      concave.points_worst
                                      symmetry_worst fractal_dimension_worst
##
               1.146062e-01
                                        2.900756e-01
                                                                 8.394582e-02
```

apply(wisc.data,2,sd)

```
##
               radius_mean
                                        texture_mean
                                                               perimeter_mean
##
              3.524049e+00
                                        4.301036e+00
                                                                 2.429898e+01
##
                 area mean
                                     smoothness mean
                                                             compactness_mean
              3.519141e+02
##
                                        1.406413e-02
                                                                 5.281276e-02
##
            concavity_mean
                                concave.points_mean
                                                                symmetry_mean
##
              7.971981e-02
                                        3.880284e-02
                                                                 2.741428e-02
##
    fractal_dimension_mean
                                                                   texture_se
                                           radius_se
##
              7.060363e-03
                                        2.773127e-01
                                                                 5.516484e-01
##
                                                                smoothness_se
              perimeter_se
                                             area_se
##
              2.021855e+00
                                        4.549101e+01
                                                                 3.002518e-03
            compactness_se
##
                                        concavity_se
                                                            concave.points_se
##
              1.790818e-02
                                        3.018606e-02
                                                                 6.170285e-03
##
               symmetry_se
                               fractal_dimension_se
                                                                 radius_worst
              8.266372e-03
                                        2.646071e-03
                                                                 4.833242e+00
##
##
             texture_worst
                                    perimeter_worst
                                                                   area_worst
##
              6.146258e+00
                                        3.360254e+01
                                                                 5.693570e+02
##
          smoothness_worst
                                   compactness_worst
                                                              concavity_worst
##
              2.283243e-02
                                        1.573365e-01
                                                                 2.086243e-01
##
      concave.points worst
                                      symmetry worst fractal dimension worst
##
              6.573234e-02
                                        6.186747e-02
                                                                 1.806127e-02
```

need to scale because values are vastly different among columns

```
wisc.pr <- prcomp(wisc.data, scale = TRUE)
wisc.pr</pre>
```

```
## Standard deviations (1, .., p=30):
```

```
[1] 3.64439401 2.38565601 1.67867477 1.40735229 1.28402903 1.09879780
   [7] 0.82171778 0.69037464 0.64567392 0.59219377 0.54213992 0.51103950
## [13] 0.49128148 0.39624453 0.30681422 0.28260007 0.24371918 0.22938785
  [19] 0.22243559 0.17652026 0.17312681 0.16564843 0.15601550 0.13436892
  [25] 0.12442376 0.09043030 0.08306903 0.03986650 0.02736427 0.01153451
##
## Rotation (n x k) = (30 \times 30):
                                            PC2
##
                                PC1
                                                        PC3
                                                                    PC4
## radius_mean
                        -0.21890244 0.233857132 -0.008531243
                                                            0.041408962
## texture_mean
                        ## perimeter_mean
                        -0.22753729
                                    0.215181361 -0.009314220
                                                            0.041983099
## area_mean
                        -0.22099499
                                   0.231076711 0.028699526
                                                            0.053433795
## smoothness_mean
                        -0.14258969 -0.186113023 -0.104291904 0.159382765
                        -0.23928535 -0.151891610 -0.074091571
## compactness_mean
                                                            0.031794581
                        -0.25840048 -0.060165363 0.002733838 0.019122753
## concavity_mean
## concave.points_mean
                        -0.26085376
                                    0.034767500 -0.025563541
                                                            0.065335944
## symmetry_mean
                        -0.13816696 -0.190348770 -0.040239936 0.067124984
## fractal_dimension_mean
                        -0.06436335 -0.366575471 -0.022574090 0.048586765
## radius se
                        -0.20597878 0.105552152 0.268481387
                                                            0.097941242
## texture se
                        -0.01742803 -0.089979682 0.374633665 -0.359855528
## perimeter_se
                        -0.21132592   0.089457234   0.266645367   0.088992415
                        -0.20286964 0.152292628 0.216006528
## area se
                                                            0.108205039
## smoothness_se
                        -0.01453145 -0.204430453 0.308838979
                                                            0.044664180
## compactness se
                        -0.17039345 -0.232715896 0.154779718 -0.027469363
## concavity se
                        -0.15358979 -0.197207283 0.176463743 0.001316880
## concave.points_se
                        -0.18341740 -0.130321560 0.224657567
                                                            0.074067335
                        -0.04249842 -0.183848000 0.288584292 0.044073351
## symmetry_se
## fractal_dimension_se
                        -0.10256832 -0.280092027
                                                0.211503764
                                                            0.015304750
                        -0.22799663 0.219866379 -0.047506990 0.015417240
## radius_worst
                        ## texture_worst
## perimeter_worst
                        -0.23663968 0.199878428 -0.048546508 0.013802794
## area_worst
                        0.025894749
## smoothness_worst
                        -0.12795256 -0.172304352 -0.259797613 0.017652216
## compactness_worst
                        -0.21009588 -0.143593173 -0.236075625 -0.091328415
                        -0.22876753 -0.097964114 -0.173057335 -0.073951180
## concavity worst
                        -0.25088597 \quad 0.008257235 \ -0.170344076 \quad 0.006006996
## concave.points_worst
## symmetry worst
                        -0.12290456 -0.141883349 -0.271312642 -0.036250695
## fractal_dimension_worst -0.13178394 -0.275339469 -0.232791313 -0.077053470
##
                                 PC5
                                              PC6
                                                           PC7
                                                                       PC8
                        ## radius_mean
## texture mean
                         0.049468850 - 0.0321788366 \ 0.0113995382 - 0.130674825
## perimeter mean
                        ## area mean
                        -0.010331251 -0.0018877480 -0.0516534275 -0.034673604
                         0.365088528 -0.2863744966 -0.1406689928 0.288974575
## smoothness_mean
## compactness_mean
                        -0.011703971 -0.0141309489 0.0309184960 0.151396350
                        -0.086375412 -0.0093441809 -0.1075204434 0.072827285
## concavity_mean
## concave.points_mean
                         0.043861025 -0.0520499505 -0.1504822142 0.152322414
## symmetry_mean
                         ## fractal_dimension_mean
                         0.044424360 -0.1194306679 0.2957600240 0.177121441
## radius_se
                         0.154456496 -0.0256032561 0.3124900373 -0.022539967
## texture_se
                         0.191650506 -0.0287473145 -0.0907553556
                                                               0.475413139
## perimeter se
                         0.120990220 0.0018107150 0.3146403902 0.011896690
## area_se
                         0.127574432 -0.0428639079 0.3466790028 -0.085805135
## smoothness se
                         0.232065676 - 0.3429173935 - 0.2440240556 - 0.573410232
```

```
-0.279968156  0.0691975186  0.0234635340  -0.117460157
## compactness se
                    -0.353982091 0.0563432386 -0.2088237897 -0.060566501
## concavity_se
## concave.points se
                    -0.195548089 -0.0312244482 -0.3696459369 0.108319309
                    ## symmetry_se
## fractal dimension se
                    -0.263297438 -0.0531952674 0.1913949726 -0.011168188
## radius worst
                    0.004406592 -0.0002906849 -0.0097099360 -0.042619416
                    0.092883400 -0.0500080613 0.0098707439 -0.036251636
## texture worst
                    ## perimeter worst
## area worst
                    0.027390903 -0.0251643821 0.0678316595 -0.079394246
                    0.324435445 -0.3692553703 -0.1088308865 -0.205852191
## smoothness_worst
## compactness_worst
                    -0.188518727 0.0283792555 -0.0604880561 -0.072467871
## concavity_worst
## concave.points_worst
                    -0.043332069 -0.0308734498 -0.1679666187 0.036170795
                     ## symmetry_worst
## fractal_dimension_worst -0.094423351 -0.0802235245 0.3746576261 -0.048360667
##
                           PC9
                                    PC10
                                             PC11
                                                       PC12
                    -0.223109764 0.095486443 -0.04147149 0.051067457
## radius_mean
                     0.112699390 0.240934066 0.30224340 0.254896423
## texture mean
## perimeter_mean
                    ## area mean
                    ## smoothness_mean
                     0.006424722 -0.069292681 0.13702184 0.316727211
## compactness_mean
                    ## concavity_mean
                    0.040591006 -0.135602298 -0.12419024 0.065653480
## concave.points mean
                    -0.111971106 0.008054528
                                        0.07244603 0.042589267
## symmetry_mean
                     ## fractal dimension mean -0.123740789 0.081103207 0.03804827 0.236358988
## radius_se
                     0.249985002 -0.049547594 0.02535702 -0.016687915
                    -0.246645397 -0.289142742 -0.34494446 -0.306160423
## texture_se
                    ## perimeter_se
## area_se
                    0.229160015 -0.091927889 -0.05161946 -0.017679218
                    -0.141924890 0.160884609 -0.08420621 -0.294710053
## smoothness_se
## compactness_se
                    -0.145322810 0.043504866 0.20688568 -0.263456509
## concavity_se
                    0.358107079 -0.141276243 -0.34951794 0.251146975
                    ## concave.points_se
## symmetry se
                    -0.304077200 -0.316529830 0.18784404 0.320571348
## fractal_dimension_se
                    ## radius worst
                    ## texture_worst
                    ## perimeter worst
                    0.048088657
## area_worst
                    -0.080732461 0.069921152 -0.18459894
                     0.112315904 -0.128304659 -0.14389035
## smoothness worst
                                                0.056514866
## compactness worst
                    -0.100677822 -0.172133632 0.19742047 -0.371662503
                    0.161908621 -0.311638520 -0.18501676 -0.087034532
## concavity worst
                    0.060488462 -0.076648291 0.11777205 -0.068125354
## concave.points_worst
                     0.064637806 -0.029563075 -0.15756025 0.044033503
## symmetry_worst
##
                         PC13
                                   PC14
                                             PC15
                                                      PC16
                     ## radius_mean
## texture_mean
                     0.20346133 -0.021560100 -0.107922421 -0.15784196
## perimeter_mean
                     0.04410950 0.048513812 -0.039902936 -0.11445396
                     0.06737574 0.010830829 0.013966907 -0.13244803
## area_mean
## smoothness_mean
                    ## compactness_mean
                    0.22928130 0.008101057 0.230899962 0.17017837
                    0.38709081 -0.189358699 -0.128283732 0.26947021
## concavity mean
```

```
## concave.points_mean
                    0.13213810 -0.244794768 -0.217099194 0.38046410
                    ## symmetry_mean
## fractal dimension mean
                    0.10623908 -0.377078865 0.517975705 -0.04079279
## radius_se
                   ## texture se
                   -0.16822238 -0.010849347 0.032752721 -0.03450040
                   -0.03784399 -0.045523718 -0.008268089 0.02651665
## perimeter se
                   ## area se
                    0.15044143 -0.201152530 0.018559465 -0.05803906
## smoothness se
## compactness se
                    0.01004017
                            0.491755932 0.168209315 0.18983090
## concavity_se
                    ## concave.points_se
                   -0.49402674 -0.199666719 0.062079344 -0.19881035
                    0.01033274 -0.046864383 -0.113383199 -0.15771150
## symmetry_se
## fractal_dimension_se
                   ## radius_worst
                   -0.13789053 0.023101281 0.166567074 -0.08156057
                   ## texture_worst
## perimeter_worst
                   -0.09696571
                            0.012219382
                                      0.182755198 -0.05485705
                   ## area_worst
## smoothness worst
                   ## compactness_worst
## concavity worst
                    0.21798433 -0.066798931 -0.204835886 -0.21502195
                   -0.25438749 -0.276418891 -0.169499607 0.17814174
## concave.points_worst
## symmetry_worst
                   -0.25653491 0.005355574 0.139888394 0.25789401
## fractal_dimension_worst -0.17281424 -0.212104110 -0.256173195 -0.40555649
                         PC17
                                   PC18
                                            PC19
                    ## radius mean
## texture mean
                   -0.038706119 -0.0411029851 0.02978864 -0.244134993
                    ## perimeter_mean
                    ## area_mean
                    0.167929914 -0.3522268017 -0.16456584 0.017100960
## smoothness_mean
## compactness_mean
                   ## concavity_mean
                   -0.001598353 -0.0269681105 0.00226636 -0.033387086
## concave.points_mean
                    0.034509509 -0.0828277367 -0.15497236 -0.235407606
## symmetry_mean
                   ## fractal_dimension_mean
## radius se
                   -0.139396866 -0.2362165319 0.17588331 -0.090800503
                    0.043963016 -0.0098586620 0.03600985 -0.071659988
## texture se
## perimeter se
                   -0.024635639 -0.0259288003 0.36570154 -0.177250625
## area_se
                    ## smoothness se
                    0.139595006 -0.2312599432 -0.01326009
                                               0.090061477
                   ## compactness_se
                    0.084616716 -0.0001954852 0.12638102 0.066946174
## concavity se
                    ## concave.points_se
                   -0.274059129 0.1870147640 -0.08903929
## symmetry se
                                                0.107385289
                   -0.122733398 -0.0598230982 0.08660084 0.222345297
## fractal_dimension_se
## radius_worst
                   -0.240049982 -0.2161013526 0.01366130 -0.005626909
                   0.300599798
## texture_worst
## perimeter_worst
                   -0.234164147 -0.1885435919 0.09081325
                                                0.011003858
                   -0.273399584 -0.1420648558 -0.41004720 0.060047387
## area_worst
## smoothness_worst
                   ## compactness_worst
                   -0.004037123 -0.0735745143 0.02020070
                                               0.229280589
                   -0.191313419 -0.1039079796 -0.04578612 -0.046482792
## concavity_worst
## concave.points_worst
                   -0.075485316  0.0758138963  -0.26022962  0.033022340
## symmetry_worst
                    0.430658116 -0.2787138431 0.11725053 -0.116759236
## fractal dimension worst 0.159394300 0.0235647497 -0.01149448 -0.104991974
```

```
PC23
##
                              PC21
                                        PC22
                                                             PC24
## radius mean
                      -0.0685700057 -0.07292890 -0.0985526942 -0.18257944
## texture mean
                       0.4483694667 -0.09480063 -0.0005549975
                                                        0.09878679
                      -0.0697690429 -0.07516048 -0.0402447050 -0.11664888
## perimeter_mean
## area mean
                      -0.0184432785 -0.09756578
                                            0.0077772734
                                                        0.06984834
## smoothness mean
                      -0.1194917473 -0.06382295 -0.0206657211 0.06869742
## compactness mean
                       0.1926213963  0.09807756  0.0523603957 -0.10413552
## concavity_mean
                       0.0055717533 0.18521200 0.3248703785
                                                        0.04474106
## concave.points_mean
                      0.08402770
## symmetry_mean
                      -0.0869384844 0.01840673 -0.0512005770
                                                        0.01933947
## fractal_dimension_mean
                      -0.0762718362 -0.28786888 -0.0846898562 -0.13326055
                       ## radius se
## texture_se
                       0.2170719674 -0.04845693 -0.0008738805
                                                        0.02426730
## perimeter_se
                      -0.3049501584 -0.15935280 0.0900742110
                                                        0.51675039
                       0.1925877857 -0.06423262
                                             0.0982150746 -0.02246072
## area_se
## smoothness_se
                      -0.0720987261 -0.05054490 -0.0598177179
                                                        0.01563119
                      -0.1403865724 0.04528769
                                            0.0091038710 -0.12177779
## compactness_se
## concavity se
                       0.0630479298  0.20521269  -0.3875423290
                                                        0.18820504
                       ## concave.points_se
## symmetry se
                      -0.0976995265 0.08465443 -0.0423628949
                                                        0.00322620
## fractal_dimension_se
                       0.0628432814 -0.24470508 0.0857810992 0.07519442
## radius worst
                       ## texture_worst
                      -0.0920235990 -0.01722163
                                             0.0633448296
                                                        0.23711317
## perimeter worst
                       ## area worst
## smoothness worst
                       ## compactness_worst
                       0.1813748671 -0.02967641 -0.1479209247
                                                        0.18674995
## concavity_worst
                      -0.1321005945 -0.46042619
                                            0.2864331353 -0.28885257
## concave.points_worst
                       0.0008860815 -0.29984056 -0.5675277966 0.10734024
## symmetry_worst
                       0.1627085487 -0.09714484 0.1213434508 -0.01438181
## fractal_dimension_worst -0.0923439434 0.46947115 0.0076253382 0.03782545
##
                            PC25
                                       PC26
                                                  PC27
                                                              PC28
                      -0.01922650 -0.129476396 -0.131526670 2.111940e-01
## radius_mean
                       0.08474593 -0.024556664 -0.017357309 -6.581146e-05
## texture_mean
## perimeter mean
                       0.02701541 -0.125255946 -0.115415423 8.433827e-02
                      ## area mean
## smoothness mean
                       0.02895489 -0.037003686 0.069689923 1.479269e-03
## compactness_mean
                       ## concavity mean
                      -0.09697732 -0.548876170 0.364808397 4.553864e-02
## concave.points_mean
                      ## symmetry mean
                      -0.02458369 -0.016044038 -0.015164835 1.433026e-03
## fractal dimension mean
                      -0.20722186 -0.097404839 -0.101244946 -6.311687e-03
                      -0.17493043 0.049977080 0.212982901 -1.922239e-01
## radius se
                       0.05698648 -0.011237242 -0.010092889 -5.622611e-03
## texture_se
## perimeter_se
                       0.07292764 0.103653282 0.041691553 2.631919e-01
                       0.13185041 -0.155304589 -0.313358657 -4.206811e-02
## area_se
## smoothness_se
                       0.03121070 -0.007717557 -0.009052154 9.792963e-03
                       0.17316455 -0.049727632 0.046536088 -1.539555e-02
## compactness_se
## concavity_se
                       ## concave.points_se
                      -0.12954655 -0.017941919 -0.011165509 -2.900930e-02
                      -0.01951493 -0.017267849 -0.019975983 -7.636526e-03
## symmetry_se
## fractal_dimension_se
                      -0.08417120 0.035488974 -0.012036564 1.975646e-02
## radius worst
                       0.07070972 -0.197054744 -0.178666740 4.126396e-01
                      ## texture worst
```

```
## perimeter worst
                           0.11803403 -0.244103670 -0.241031046 -7.286809e-01
## area worst
                          -0.03828995 0.231359525 0.237162466 2.389603e-01
                          -0.04796476 0.012602464 -0.040853568 -1.535248e-03
## smoothness worst
## compactness_worst
                          -0.62438494 -0.100463424 -0.070505414 4.869182e-02
## concavity worst
                           ## concave.points worst
                           0.26319634 -0.133574507 0.230901389 2.247567e-02
## symmetry worst
                           0.04529962 0.028184296 0.022790444 4.920481e-03
## fractal_dimension_worst 0.28013348 0.004520482 0.059985998 -2.356214e-02
##
                                   PC29
                                                PC30
                           2.114605e-01 0.7024140910
## radius_mean
## texture_mean
                          -1.053393e-02 0.0002736610
                           3.838261e-01 -0.6898969685
## perimeter_mean
## area_mean
                          -4.227949e-01 -0.0329473482
                          -3.434667e-03 -0.0048474577
## smoothness_mean
## compactness_mean
                          -4.101677e-02 0.0446741863
## concavity_mean
                          -1.001479e-02 0.0251386661
## concave.points_mean
                          -4.206949e-03 -0.0010772653
## symmetry_mean
                          -7.569862e-03 -0.0012803794
## fractal_dimension_mean
                          7.301433e-03 -0.0047556848
## radius se
                           1.184421e-01 -0.0087110937
                          -8.776279e-03 -0.0010710392
## texture_se
## perimeter se
                          -6.100219e-03 0.0137293906
## area_se
                          -8.592591e-02 0.0011053260
## smoothness_se
                          1.776386e-03 -0.0016082109
## compactness se
                          3.158134e-03 0.0019156224
## concavity_se
                          1.607852e-02 -0.0089265265
                          -2.393779e-02 -0.0021601973
## concave.points_se
## symmetry_se
                          -5.223292e-03 0.0003293898
                          -8.341912e-03 0.0017989568
## fractal_dimension_se
## radius_worst
                          -6.357249e-01 -0.1356430561
## texture_worst
                           1.723549e-02 0.0010205360
## perimeter_worst
                          2.292180e-02 0.0797438536
## area_worst
                           4.449359e-01 0.0397422838
                          7.385492e-03 0.0045832773
## smoothness_worst
## compactness worst
                          3.566904e-06 -0.0128415624
                          -1.267572e-02 0.0004021392
## concavity_worst
## concave.points worst
                           3.524045e-02 -0.0022884418
## symmetry_worst
                           1.340423e-02 0.0003954435
## fractal_dimension_worst 1.147766e-02 0.0018942925
```

summary of PCA

summary(wisc.pr)

```
## Importance of components:
##
                             PC1
                                    PC2
                                            PC3
                                                    PC4
                                                             PC5
                                                                     PC6
                                                                             PC7
## Standard deviation
                          3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172
## Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251
## Cumulative Proportion 0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
##
                              PC8
                                     PC9
                                            PC10
                                                   PC11
                                                           PC12
                                                                    PC13
                                                                            PC14
## Standard deviation
                          0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
## Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
## Cumulative Proportion 0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
```

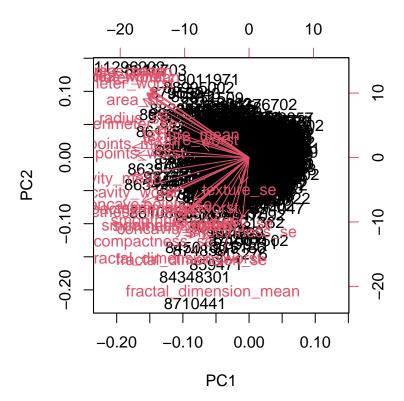
```
PC15
##
                                     PC16
                                             PC17
                                                      PC18
                                                              PC19
                                                                      PC20
                                                                             PC21
## Standard deviation
                          0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
## Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
## Cumulative Proportion
                          0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
                             PC22
                                     PC23
                                            PC24
                                                     PC25
                                                             PC26
                                                                     PC27
                                                                             PC28
## Standard deviation
                          0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
## Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
                          0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
## Cumulative Proportion
##
                             PC29
                                     PC30
## Standard deviation
                          0.02736 0.01153
## Proportion of Variance 0.00002 0.00000
## Cumulative Proportion 1.00000 1.00000
```

Q4. From your results, what proportion of the original variance is captured by the first principal components (PC1)?

44.27%

- Q5. How many principal components (PCs) are required to describe at least 70% of the original variance in the data?
- 3 PCs, this gives 72.6% of the variance
 - Q6. How many principal components (PCs) are required to describe at least 90% of the original variance in the data?
- 7 PCs, this gives 91% of the variance

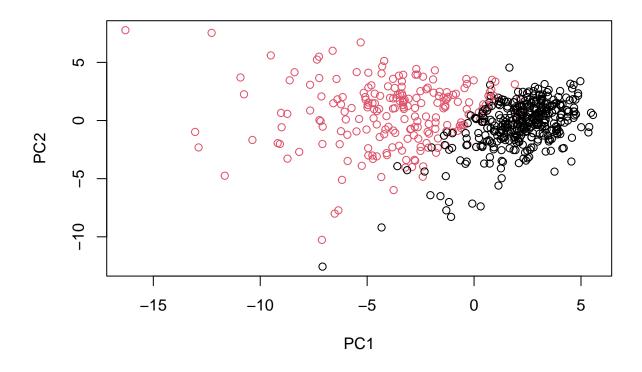
biplot(wisc.pr)

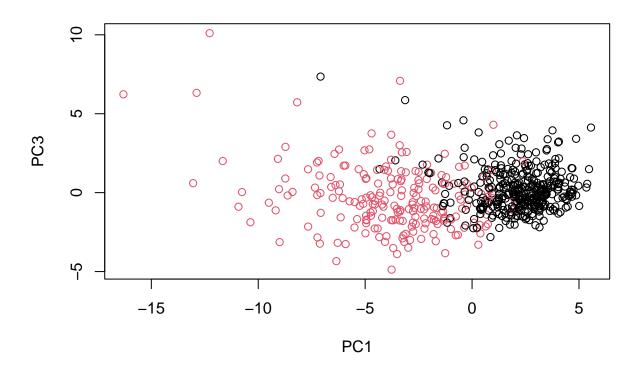


> Q7. What stands out to you about this plot? Is it easy or difficult to understand? Why?

The column labels are blocking the points, which are listed as numeric values rather than dots. This is very difficult to understand.

plot for PC1 and PC2



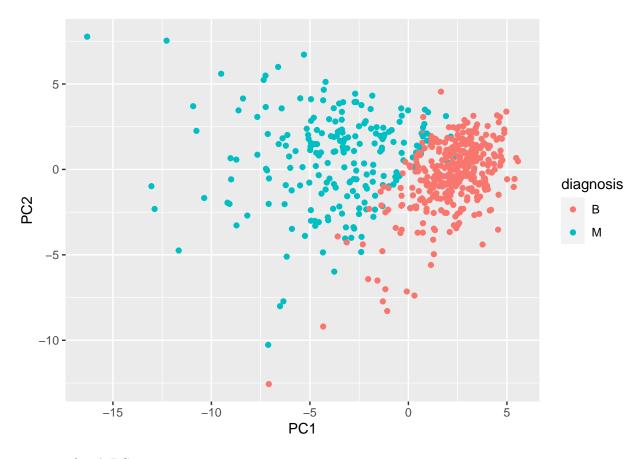


making ggplot scatterplot for PC1 vs PC2 $\,$

```
df <- as.data.frame(wisc.pr$x)
df$diagnosis <- diagnosis

library(ggplot2)

ggplot(df) +
  aes(PC1, PC2, col=diagnosis) +
  geom_point()</pre>
```



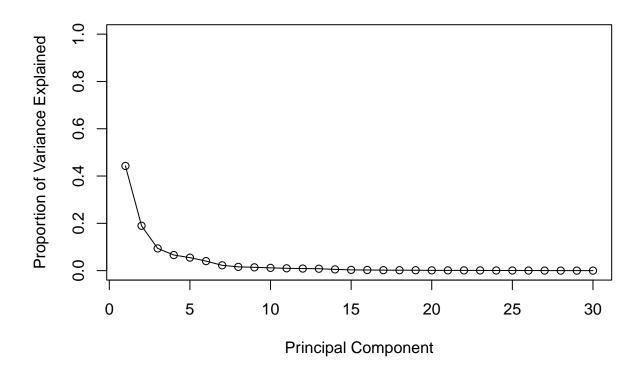
variance of each PC

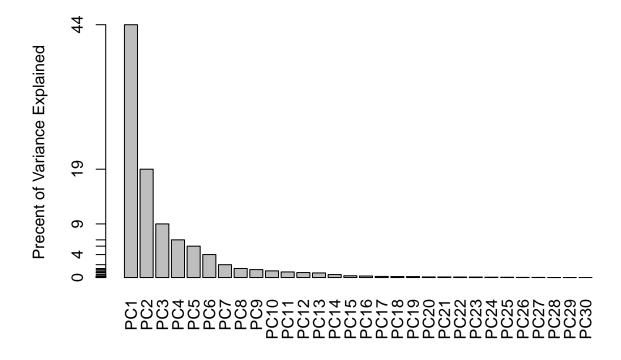
```
pr.var <- wisc.pr$sdev^2
head(pr.var)</pre>
```

[1] 13.281608 5.691355 2.817949 1.980640 1.648731 1.207357

```
# Variance explained by each principal component: pve
pve <- pr.var / sum(pr.var)

# Plot variance explained for each principal component
plot(pve, xlab = "Principal Component",
    ylab = "Proportion of Variance Explained",
    ylim = c(0, 1), type = "o")</pre>
```





Q9. For the first principal component, what is the component of the loading vector (i.e. wisc.pr\$rotation[,1]) for the feature concave.points_mean?

wisc.pr\$rotation[,1]

radius_mean	texture_mean	perimeter_mean
-0.21890244	-0.10372458	-0.22753729
area_mean	${\tt smoothness_mean}$	compactness_mean
-0.22099499	-0.14258969	-0.23928535
concavity_mean	concave.points_mean	symmetry_mean
-0.25840048	-0.26085376	-0.13816696
fractal_dimension_mean	radius_se	texture_se
-0.06436335	-0.20597878	-0.01742803
perimeter_se	area_se	smoothness_se
-0.21132592	-0.20286964	-0.01453145
compactness_se	concavity_se	concave.points_se
-0.17039345	-0.15358979	-0.18341740
symmetry_se	fractal_dimension_se	radius_worst
-0.04249842	-0.10256832	-0.22799663
texture_worst	perimeter_worst	area_worst
-0.10446933	-0.23663968	-0.22487053
smoothness_worst	compactness_worst	${\tt concavity_worst}$
-0.12795256	-0.21009588	-0.22876753
concave.points_worst	symmetry_worst	${\tt fractal_dimension_worst}$
-0.25088597	-0.12290456	-0.13178394
	-0.21890244	-0.21890244 -0.10372458 area_mean smoothness_mean -0.22099499 -0.14258969 concavity_mean concave.points_mean -0.25840048 -0.26085376 fractal_dimension_mean radius_se -0.06436335 -0.20597878 perimeter_se area_se -0.21132592 -0.20286964 compactness_se concavity_se -0.17039345 -0.15358979 symmetry_se fractal_dimension_se -0.04249842 -0.10256832 texture_worst perimeter_worst -0.10446933 -0.23663968 smoothness_worst compactness_worst -0.12795256 -0.21009588 concave.points_worst symmetry_worst

-0.26085376

Q10. What is the minimum number of principal components required to explain 80% of the variance of the data?

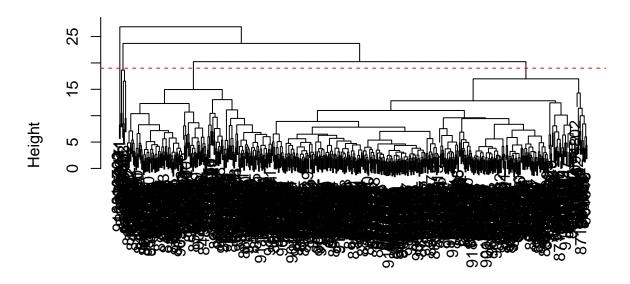
```
summary(wisc.pr)
## Importance of components:
                                                              PC5
##
                              PC1
                                     PC2
                                              PC3
                                                      PC4
                                                                       PC6
                                                                               PC7
                           3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172
## Standard deviation
## Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251
## Cumulative Proportion 0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
##
                               PC8
                                      PC9
                                             PC10
                                                     PC11
                                                             PC12
                                                                      PC13
## Standard deviation
                           0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
## Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
## Cumulative Proportion 0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
##
                              PC15
                                      PC16
                                               PC17
                                                       PC18
                                                               PC19
                                                                        PC20
## Standard deviation
                           0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
## Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
## Cumulative Proportion 0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
##
                              PC22
                                      PC23
                                              PC24
                                                      PC25
                                                              PC26
                                                                       PC27
## Standard deviation
                           0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
## Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
## Cumulative Proportion 0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
##
                              PC29
                                      PC30
## Standard deviation
                           0.02736 0.01153
## Proportion of Variance 0.00002 0.00000
## Cumulative Proportion 1.00000 1.00000
5
data.scaled <- scale(wisc.data)</pre>
data.dist <- dist(data.scaled)</pre>
\#data.dist
wisc.hclust <- hclust(data.dist)</pre>
wisc.hclust
##
## Call:
## hclust(d = data.dist)
##
## Cluster method
                     : complete
## Distance
                     : euclidean
## Number of objects: 569
     Q11. Using the plot() and abline() functions, what is the height at which the clustering model
```

h = 19

has 4 clusters?

```
plot(wisc.hclust)
abline(h=19, col="red", lty=2)
```

Cluster Dendrogram



data.dist hclust (*, "complete")

wisc.hclust.clusters <- cutree(wisc.hclust, 4)
wisc.hclust.clusters</pre>

##	842302	842517	84300903	84348301	84358402	843786	844359	84458202
##	1	1	1	2	1	1	1	1
##	844981	84501001	845636	84610002	846226	846381	84667401	84799002
##	1	2	3	1	1	3	1	1
##	848406	84862001	849014	8510426	8510653	8510824	8511133	851509
##	3	1	1	3	3	3	1	1
##	852552	852631	852763	852781	852973	853201	853401	853612
##	1	1	1	1	1	3	1	1
##	85382601	854002	854039	854253	854268	854941	855133	855138
##	1	1	1	1	1	3	3	1
##	855167	855563	855625	856106	85638502	857010	85713702	85715
##	3	1	1	1	1	1	3	1
##	857155	857156	857343	857373	857374	857392	857438	85759902
##	3	3	3	3	3	1	3	3
##	857637	857793	857810	858477	858970	858981	858986	859196
##	1	1	3	3	3	3	1	3
##	85922302	859283	859464	859465	859471	859487	859575	859711
##	1	1	3	3	2	3	1	3
##	859717	859983	8610175	8610404	8610629	8610637	8610862	8610908

## ##	1 861103	1 8611161	3 8611555	3 8611792	3 8612080	1 8612399	2 86135501	3 86135502
##	3	1	1	1	3	1	3	1
##	861597	861598	861648	861799	861853	862009	862028	86208
##	3	1	3	3	3	3	1	1
##	86211	862261	862485	862548	862717	862722	862965	862980
##	3	3	3	3	3	3	3	3
##	862989	863030	863031	863270	86355	864018	864033	86408
##	3	1	1	3	1	3	3	3
##	86409	864292	864496	864685	864726	864729	864877	865128
##	3	3	3	3	3	1	1	3
##	865137	86517	865423	865432	865468	86561	866083	866203
##	3	1	2	3	3	3	1	3
##	866458	866674	866714	8670	86730502	867387	867739	868202
##	1	1	3	1	1	3	1	3
##	868223	868682	868826	868871	868999	869104	869218	869224
##	3	3	1	3	3	3	3	3
##	869254	869476	869691	86973701	86973702		871001501	
##	3	3	1	3	3	3	3	3
##	8710441	87106	8711002	8711003	8711202	8711216	871122	871149
##	2	3	3	3	1	3	3	3
##	8711561	8711803	871201	8712064	8712289	8712291	87127	
##	3 8712766	0710052	1 87139402	3	07164	071641	3	070112
## ##	0/12/00	8712853 3	87139402	87163 3	87164 1	871641 3	871642 3	872113 3
##	872608	87281702	873357	873586	873592	873593	873701	873843
##	3	1	3	3	1	1	1	3
##	873885	874158	874217	874373	874662	874839	874858	875093
##	1	3	3	3	3	3	2	
##	875099	875263	87556202	875878	875938	877159	877486	877500
##	3	1	1	3	1	3	1	1
##	877501	877989	878796	87880	87930	879523	879804	879830
##	3	3	1	1	3	3	3	3
##	8810158	8810436	881046502	8810528	8810703	881094802	8810955	8810987
##	1	3	1	3	4	3	1	1
##	8811523	8811779	8811842	88119002	8812816	8812818	8812844	8812877
##	3	3	1	1	3	3	3	1
##			88147101					
##			3					
			882488					
##								1
			883852					
			3 884948					3
								3
			887181					
##			1					
			8910251					
			3					
			8911163					
			3					
			89122					
			1					
			89143602					

##	3	3	3	3	3	3	3	3
##	891936	892189	892214	892399	892438	892604	89263202	892657
##	3	3	3	3	1	3	1	3
##	89296	893061	89344	89346	893526	893548	893783	89382601
##	3	3	3	3	3	3	3	3
##	89382602	893988	894047	894089	894090	894326	894329	894335
##	3	3	3	3	3	1	3	3
##	894604 3	894618 3	894855 3	895100 1	89511501 3	89511502	89524 3	895299 3
##	8953902	895633	ى 896839	896864	897132	897137	897374	89742801
##	1	1	1	1	3	3	3	1
##	897604	897630	897880	89812	89813	898143	89827	898431
##	3	1	3	1	3	3	3	1
##	89864002	898677	898678	89869	898690	899147	899187	899667
##	3	3	3	3	3	3	3	1
##	899987	9010018	901011	9010258	9010259	901028	-	901034301
##	1	3010010	301011	3010230	3010233	301028	3010333	301034301
##	901034302	901041	9010598	9010872	9010877	901088	9011494	9011495
##	301004002	301041	3010330	3010072	3010077	1	1	3011433
##	9011971	9012000	9012315	9012568	9012795	901288	9013005	901303
##	1	1	1	3012000	1	1	3010000	3
##	901315	9013579	9013594	9013838	901549	901836	90250	90251
##	301010	3	3	1	301043	301000	30200	30201
##	902727	90291	902975	902976	903011	90312	90317302	903483
##	3	3	3	3	3	1	3	3
##	903507	903516	903554	903811	90401601	90401602	904302	904357
##	1	1	3	3	3	3	3	3
##	90439701	904647	904689	9047	904969	904971	905189	905190
##	1	3	3	3	3	3	3	3
##	90524101	905501	905502	905520	905539	905557	905680	905686
##	1	3	3	3	3	3	3	3
##	905978	90602302	906024	906290	906539	906564	906616	906878
##	3	1	3	3	3	1	3	3
##	907145	907367	907409	90745	90769601	90769602	907914	907915
##	3	3	3	3	3	3	1	3
##	908194	908445	908469	908489	908916	909220	909231	909410
##	1	1	3	1	3	3	3	3
##	909411	909445	90944601	909777	9110127	9110720	9110732	9110944
##	3	3	3	3	3	3	1	3
##	911150	911157302	9111596	9111805	9111843	911201	911202	9112085
##	3	1	3	1	3	3	3	3
##	9112366	9112367	9112594	9112712	911296201	911296202	9113156	911320501
##		3						
##	911320502	9113239	9113455	9113514	9113538	911366	9113778	9113816
##		3						
		9113846						
								1
		91227						
##								1
		913535						
##		3						
		914580						
##								1
##	915186	915276	91544001	91544002	915452	915460	91550	915664

```
##
            3
                        3
                                    3
                                               3
                                                           3
                                                                                  3
                                                                      1
##
      915691
                  915940
                           91594602
                                         916221
                                                     916799
                                                                 916838
                                                                            917062
                                                                                        917080
##
            1
                        3
                                    3
                                               3
                                                                      1
                                                                                  3
                                                                                              3
##
      917092
                91762702
                               91789
                                         917896
                                                     917897
                                                                  91805
                                                                          91813701
                                                                                     91813702
##
            3
                        1
                                    3
                                               3
                                                           3
                                                                      3
                                                                                  1
      918192
                  918465
                               91858
                                       91903901
                                                   91903902
                                                              91930402
                                                                            919537
                                                                                        919555
##
                                    3
                                                           3
                                                                                  3
##
            3
                        3
                                               3
                                                                      1
                                                                                              1
    91979701
                              921092
                                                                                        922296
##
                  919812
                                         921362
                                                     921385
                                                                 921386
                                                                            921644
##
            3
                                    3
                                               3
                                                           3
                                                                                  3
                                                                                              3
                        1
                                                                      1
                                         922840
      922297
                  922576
                              922577
                                                                            923748
                                                                                        923780
##
                                                     923169
                                                                 923465
##
            3
                        3
                                    3
                                               3
                                                           3
                                                                      3
                                                                                  3
                                                                                              3
                                                                                        925291
      924084
                  924342
                              924632
                                         924934
                                                     924964
                                                                 925236
                                                                            925277
##
##
            3
                        3
                                    3
                                               3
                                                           3
                                                                      3
                                                                                  3
                                                                                              3
                              925622
                                                     926424
##
      925292
                  925311
                                         926125
                                                                 926682
                                                                            926954
                                                                                        927241
##
                        3
                                                                                  3
            3
                                    1
                                               1
                                                           1
                                                                      1
                                                                                              1
##
        92751
##
            3
```

table(wisc.hclust.clusters, diagnosis)

```
##
                          diagnosis
## wisc.hclust.clusters
                             В
                                  М
                            12 165
##
                             2
                                  5
##
                         2
##
                         3
                           343
                                 40
##
                             0
                                  2
```

Q12. Can you find a better cluster vs diagnoses match by cutting into a different number of clusters between 2 and 10?

Our group determined that a cluster of 4 is optimal, from trying different values. There is good separation between B and M.

```
wisc.hclust.clusters2 <- cutree(wisc.hclust, 5)
table(wisc.hclust.clusters2, diagnosis)</pre>
```

```
##
                           diagnosis
##
   wisc.hclust.clusters2
                               В
                                   Μ
                              12 165
##
##
                          2
                               0
                                    5
                          3
                            343
                                  40
##
##
                          4
                               2
                                   0
##
                          5
                                    2
```

Q13. Which method gives your favorite results for the same data.dist dataset? Explain your reasoning.

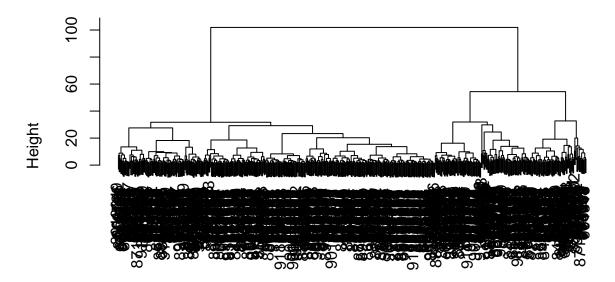
Our group decided that the ward.D2 method splits the data more cleanly than the other methods

```
wisc.hclust2 <- hclust(data.dist, method = "ward.D2")
wisc.hclust2</pre>
```

```
##
## Call:
## hclust(d = data.dist, method = "ward.D2")
##
## Cluster method : ward.D2
## Distance : euclidean
## Number of objects: 569
```

plot(wisc.hclust2)

Cluster Dendrogram



data.dist hclust (*, "ward.D2")