

Solution to Homework #2

I am going to skip q1 and 2

- 3. a. $\forall x \text{ Mush}(x) \rightarrow \text{Pois}(x)$
- 3 b. $\forall x \text{ Mus}(x) \text{ and } \text{Pois}(x) \rightarrow \text{Col}(x, \text{Purple})$
- 3 c. $\forall x \text{ Mus}(x) \text{ and } \text{Pois}(x) \rightarrow (\text{col}(x, \text{Purple}) \vee \text{col}(x, \text{Gray}) \vee \text{col}(x, \text{White}))$
- 3 d. $\forall x \forall y \text{ Veg}(x) \text{ and } \text{Likes}(x, \text{Pizza}) \text{ and } \text{Mus}(y) \text{ and not } \text{Pois}(y) \rightarrow \text{Likes}(x, y)$

4. Interpretation

$\text{Per}(x)$: x is a person
 $\text{TT}(x)$: x is a truth teller
 $\text{Li}(x)$: x is a liar

Domain knowledge:

$\forall x \text{ Per}(x) \rightarrow (\text{TT}(x) \vee \text{Li}(x))$
 $\forall x \text{ Per}(x) \rightarrow \text{not}(\text{TT}(x) \text{ and } \text{Li}(x))$

$\text{Per}(\text{Mark})$

$\text{Per}(\text{Mary})$

$\text{Per}(\text{John})$

Statements:

$\text{TT}(\text{John}) \rightarrow (\text{TT}(\text{Mark}) \text{ and } \text{TT}(\text{Mary}))$
 $\text{Li}(\text{John}) \rightarrow \text{not}(\text{TT}(\text{Mark}) \text{ and } \text{TT}(\text{Mary}))$

$\text{TT}(\text{Mark}) \rightarrow \text{Li}(\text{John}) \text{ and } (\text{Li}(\text{John}) \vee \text{Li}(\text{Mary}))$
 $\text{Li}(\text{Mark}) \rightarrow \text{not}(\text{Li}(\text{John}) \text{ and } (\text{Li}(\text{John}) \vee \text{Li}(\text{Mary})))$

$\text{TT}(\text{Mary}) \rightarrow (\text{TT}(\text{John}) \text{ and } \text{TT}(\text{Mark})) \vee (\text{TT}(\text{John}) \text{ and } \text{Li}(\text{Mark})) \vee (\text{Li}(\text{John}) \text{ and } \text{TT}(\text{Mark}))$
 $\text{Li}(\text{Mary}) \rightarrow \text{not}((\text{TT}(\text{John}) \text{ and } \text{TT}(\text{Mark})) \vee (\text{TT}(\text{John}) \text{ and } \text{Li}(\text{Mark})) \vee (\text{Li}(\text{John}) \text{ and } \text{TT}(\text{Mark})))$

5. Interpretation

$\text{Per}(x)$: x is a person
 $\text{TT}(x)$: x is a truth teller
 $\text{Li}(x)$: x is a liar
 $\text{Nor}(x)$: x is a normal person

Domain knowledge:

$\forall x \text{ Per}(x) \rightarrow (\text{TT}(x) \vee \text{Li}(x) \vee \text{Nor}(x))$

$\text{All } x \text{ Per}(x) \rightarrow \text{not } (\text{TT}(x) \text{ and } \text{Li}(x) \text{ and } \text{Nor}(x))$

(not strong enough to capture the fact that a person belongs exclusively to only one category)

$\text{All } x \text{ Per}(x) \rightarrow (\text{TT}(x) \text{ and not } \text{Li}(x) \text{ and not } \text{Nor}(x)) \vee (\text{not } \text{TT}(x) \text{ and } \text{Li}(x) \text{ and not } \text{Nor}(x)) \vee$
 $(\text{not } \text{TT}(x) \text{ and not } \text{Li}(x) \text{ and } \text{Nor}(x))$

(correctly encode the facts that a person belongs to exactly only one category)

$\text{All } x \ y \text{ TT}(x) \text{ and Marry}(x, y) \rightarrow \text{Li}(y)$

$\text{All } x \ y \text{ Li}(x) \text{ and Marry}(x, y) \rightarrow \text{TT}(y)$

$\text{All } x \ y \text{ Nor}(x) \text{ and Marry}(x, y) \rightarrow \text{Nor}(y)$

$\text{Per}(\text{MrA})$

$\text{Per}(\text{MrsA})$

$\text{Marry}(\text{MrA}, \text{MrsA})$

$\text{Marry}(\text{MrsA}, \text{MrA})$

Statements:

$\text{TT}(\text{MrA}) \rightarrow \text{not } (\text{Nor}(\text{MrsA}))$

$\text{Li}(\text{MrA}) \rightarrow \text{Nor}(\text{MrsA})$

$\text{TT}(\text{MrsA}) \rightarrow \text{not}(\text{Nor}(\text{MrA}))$

$\text{Li}(\text{MrsA}) \rightarrow \text{Nor}(\text{MrA})$

6.

a. Those who hesitate "to act" will lose.

b. There is no business-like show business.

c. not all glitters are gold.

d. There is a person who can fool all the time.

(d is for what is written. It is supposed to be Can't Fool implying
a person can't be fooled all the time)