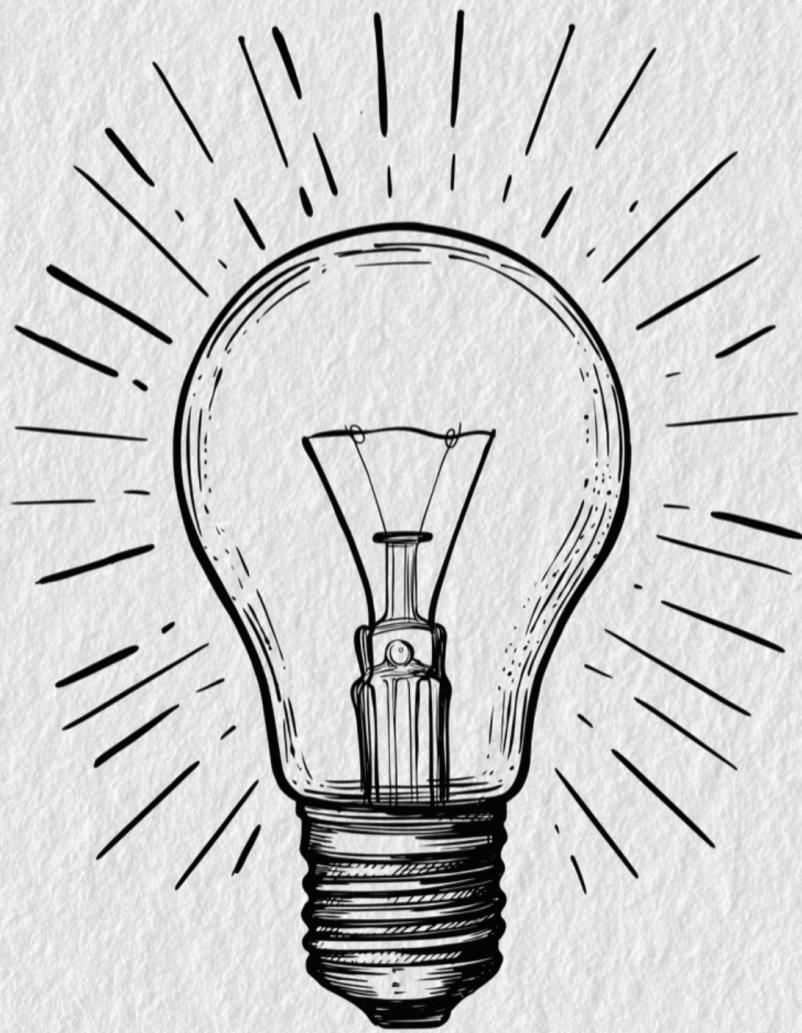


NOTEBOOK



Creative notes

By reading we enrich the mind;
by writing we polish it.

~~Bubble sort~~ → Stable

Intuition: push the maximum element to the last by adjacent swapping.

```

public static void bubbleSort(int a[], int n) {
    // Iterate over the entire array
    for (int i = 0; i < n; i++) { → Here i=0 to n-1 is enough
        boolean swap = true; // Initially assume no swaps have occurred
        // Compare adjacent elements up to the unsorted portion of the array
        for (int j = 0; j < n - i - 1; j++) {
            if (a[j] > a[j + 1]) { → Swap technique
                // Swap a[j] and a[j+1]
                int temp = a[j];
                a[j] = a[j + 1];
                a[j + 1] = temp;
                swap = false; // A swap occurred, so mark the flag accordingly
            }
        }
        // If no swaps occurred during the inner loop, the array is sorted
        if (!swap) { → Best case
            break;
        }
    }
}

```

Time complexity Derivation => For example $n = 5$

$i=0 \rightarrow j=0 \text{ to } n-1 (4)$

$i=1 \rightarrow j=0 \text{ to } n-2 (3)$

$i=2 \rightarrow j=0 \text{ to } n-3 (2)$

$i=3 \rightarrow j=0 \text{ to } n-4 (1)$

$i=4 \rightarrow j=0 \text{ to } n-5 (0) \times (\text{Not running } j \text{ loop})$

From Above, for $n=5$

$$4 + 3 + 2 + 1 = 10$$

$$\frac{5 \times 4}{2} = 10$$

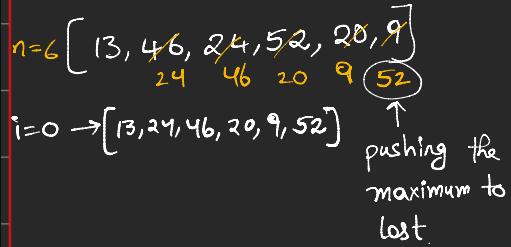
$$\text{So, } \Rightarrow \frac{n(n-1)}{2} \Rightarrow \frac{n^2-n}{2} \Rightarrow \frac{n^2}{2} - \frac{n}{2} \Rightarrow O(N^2)$$

⊗ Time complexity is $O(N^2)$

Time Complexity $\Rightarrow O(N^2)$ Worst case
Average case

$O(N)$ Best case.

Space complexity $\Rightarrow O(1)$



Note :-

$j=0 \text{ to } n-i-1 ?$

→ Every large element pushed to end
for every i th iteration.

⊗ Sorting from right side to left side.

⇒ Best case:

$$[2, 3, 4, 5, 6, 7]$$

Swap = true;

If any swap occurs,

Swap = false;

⊗ selection sort → unstable

⇒ select minimum numbers and push to first end.

```
SelectionSort
public static void insertionSort(int a[], int n){
    for(int i = 0; i<n; i++){           → n-1 is enough.
        int minIdx = i;                 → initial minIdx
        for(int j = i+1; j<n; j++){
            if(a[minIdx]>a[j]){       → if any min value found
                minIdx = j;             update minIdx.
            }
        }
        int temp = a[minIdx];          } swap that min value with
        a[minIdx] = a[i];              current ith value.
        a[i] = temp;
    }
}
```

Time complexity derivation: → for example $n=5$

$$i=0 \Rightarrow j=1 \text{ to } n \quad (4)$$

$$i=1 \Rightarrow j=2 \text{ to } n \quad (3)$$

$$i=2 \Rightarrow j=3 \text{ to } n \quad (2)$$

$$i=3 \Rightarrow j=4 \text{ to } n \quad (1)$$

$$i=4 \Rightarrow j=5 \text{ to } n \quad (0) \quad \text{Not running } j^{\text{th}} \text{ loop}$$

so $i=0$ to $n-1$ is enough

⇒ for $n=5$, $4+3+2+1 = 10$

$$\frac{5(5-1)}{2} = 10$$

$$\frac{n(n-1)}{2} \Rightarrow \frac{n^2-n}{2} \Rightarrow \frac{n^2}{2} - \frac{n}{2} \Rightarrow n^2$$

Time complexity ⇒ $O(n^2)$

Best case, {
Average, } $O(n^2)$
Worst

Space complexity ⇒ $O(1)$

$\downarrow i=0$
 $[13, 46, 24, 52, 20, 9]$
 $\minIdx = i$; $a[minIdx] > a[i]$ then
 $\minIdx = j$;

$\underline{At} \Rightarrow i=0$
 $\minIdx = 0 \quad 5$
swap ⇒ $\text{temp} = a[minIdx];$
 $a[minIdx] = a[i];$
 $a[i] = \text{temp};$

→ why ⇒ $j=i$ to n ?
→ pushing min element to first for
every i^{th} iteration.
⊗ sorting from left side to right.

Time complexity ⇒ $O(n^2)$

Space complexity ⇒ $O(1)$

④ Insertion Sort

⇒ Taking an element, place it in its correct position.

```
public static void insertionSort(int a[], int n){
    for(int i = 1; i < n; i++){
        int j = i; → 1 to n-1
        while(j > 0 && a[j] < a[j-1]){
            int temp = a[j];
            a[j] = a[j-1]; } swap → put that in
            a[j-1] = temp; its correct
            j--; position.
        }
    }
```

Run | Debug

Time Complexity Derivation ⇒ for ex: n=5

- i=1 ⇒ j=1 to 1 (1)
- i=2 ⇒ j=2 to 1 (2)
- i=3 ⇒ j=3 to 1 (3)
- i=4 ⇒ j=4 to 1 (4)

By analysing above, for 5 ⇒ 4+3+2+1 ⇒ 10

$$\frac{5 \times 4}{2} = 10$$

$$\frac{n(n-1)}{2} \Rightarrow \frac{n^2 - n}{2} \Rightarrow O(N^2)$$

Time complexity is $O(N^2)$

Space complexity is $O(1)$

Time Complexity $\Rightarrow O(N^2)$ Average
Worst

⇒ Best case $\Rightarrow O(N)$

Space Complexity $\Rightarrow O(1)$

[14, 9, 15, 12, 6, 8, 13]
i=1
j=2

[9, 14, 15, 12, 6, 8, 13]
i=2
j=2 & 0

[9, 12, 14, 15, 6, 8, 13]
i=3 → ↑ i, ↑ j → 15 is in its position
j=3 ⇒ here ($j < j-1$) → false

[9, 12, 14, 15, 6, 8, 13]
i=4 → ↑ i, ↑ j → 15 is in its position
j=4 & 2 & 0

[6, 8, 12, 14, 15, 9, 13]
i=5 → ↑ i, ↑ j → 15 is in its position
j=5 & 4 & 2 & 1

[6, 8, 9, 12, 14, 15, 13]
i=6 < n-1 → loop terminates. ↓
final sorted array.

Best case $\Rightarrow O(N)$

Worst, Average $\Rightarrow O(N^2)$

② merge sort Algorithm \Rightarrow Divide and merge

4/2/25

```
// Recursive method to perform merge sort on a subarray from index 'start' to 'end'
public static int[] mergeSort(int arr[], int start, int end) {
    // Base case: if the subarray has one element or is empty, return it as a single-element array
    if (start >= end) {
        return new int[]{arr[start]};
    }

    // Calculate the middle index to divide the array into two halves
    int mid = (start + end) / 2;

    // Recursively sort the left half (from start to mid)
    int left[] = mergeSort(arr, start, mid);
    // Recursively sort the right half (from mid+1 to end)
    int right[] = mergeSort(arr, mid + 1, end);

    // Merge the two sorted halves and return the result
    return merge(left, right);
}
```

\rightarrow Divide the array
recursively

\rightarrow merge the array
before returning

④ Time complexity derivation

\rightarrow why $N \times \log N$

① For dividing $\log N$

For every subpart of
array, we call merge().

Merge() fun takes $O(N)$

\Rightarrow Overall time complexity

is $O(N \times \log N)$

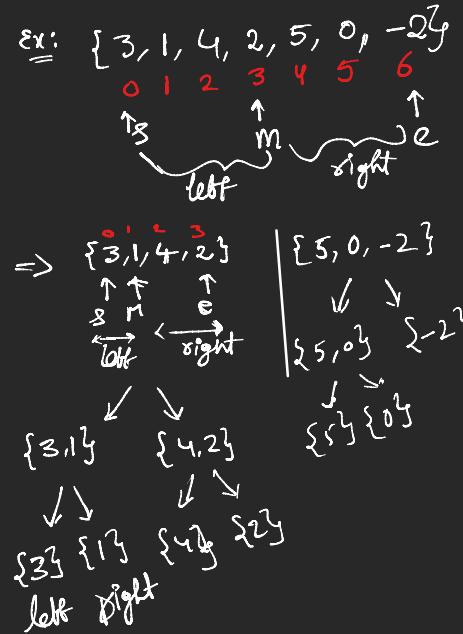
```
// Helper method to merge two sorted arrays into one sorted array
private static int[] merge(int left[], int right[]) {
    // Create a new array to hold the merged result
    int ans[] = new int[left.length + right.length];
    int i = 0; // Index for the left array
    int j = 0; // Index for the right array
    int k = 0; // Index for the merged array

    // Merge elements from left and right arrays into ans in sorted order
    while (i < left.length && j < right.length) {
        // Compare current elements of left and right
        // Add the smaller element to the merged array
        if (left[i] < right[j]) {
            ans[k] = left[i];
            i++;
        } else {
            ans[k] = right[j];
            j++;
        }
        k++;
    }

    // Add any remaining elements from the left array (if any)
    while (i < left.length) {
        ans[k] = left[i];
        i++;
        k++;
    }

    // Add any remaining elements from the right array (if any)
    while (j < right.length) {
        ans[k] = right[j];
        j++;
        k++;
    }

    // Return the merged sorted array
    return ans;
}
```



\Rightarrow Base condition (single element)

(start \geq end)

return new int[] {arr[start]}

left [] = divided ()
right [] = divided ()
return merge (left, right);

Time complexity : $O(N \times \log N)$

Space complexity ; $O(\log N) \Rightarrow$ stack space

$O(N) \Rightarrow$ for merging

⊗ Quick Sort (pivot & partition)

Approach

→① Take pivot (Any element) (Here I took mid)

→② partition (place pivot element in its position)

- $a[i[start]] < \text{pivot}$, then move $\text{start}++$
- $a[i[end]] > \text{pivot}$, then move $\text{end}--$
- Swap (start, end)
- Do, above three until ($\text{start} < \text{end}$)

* Partition logic

```
public static void quickSort(int a[], int low, int high){
    if (low < high) {
        int pivotIdx = partition(a, low, high);
        quickSort(a, low, pivotIdx - 1); // left part after placing pivot at its correct
        quickSort(a, pivotIdx + 1, high); // right part after placing pivot at its corre
    }
}

private static int partition(int a[], int low, int high) {
    int start_Idx = low;
    int end_Idx = high;
    int mid = (start_Idx + end_Idx) / 2; // Here you can take any element as pivot. In th
    int pivot = a[mid];
    while (start_Idx < end_Idx) {
        while (start_Idx < high && a[start_Idx] <= pivot) { // see these cases carefully,
            start_Idx++;
        }
        while (end_Idx > low && a[end_Idx] > pivot){           why we return endIdx
            end_Idx--;
        }
        if (start_Idx < end_Idx) { // swap
            int temp = a[start_Idx];
            a[start_Idx] = a[end_Idx];
            a[end_Idx] = temp;
        }
    }
    // place pivot at its position. so swap a[pivotIdx] with a[end_idx]
    int temp = a[end_Idx];
    a[end_Idx] = a[pivotIdx]; // which is pivot; pivot;
    a[pivotIdx] = temp;

    return end_Idx; // return pivot position.
}
```

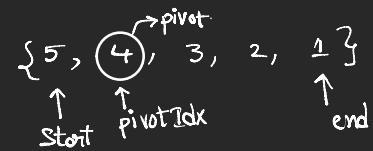
⊗ Time complexity \Rightarrow Worst case $\Rightarrow O(N^2)$
 Average case $\Rightarrow O(N \times \log N)$

⊗ space complexity $\Rightarrow O(1)$ (constant space)

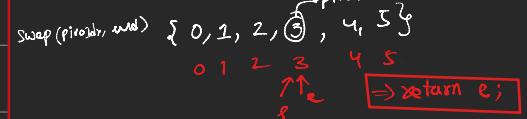
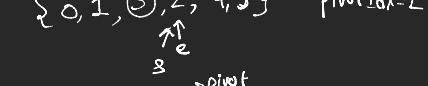
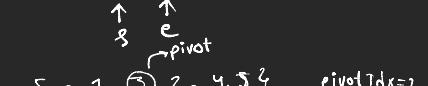
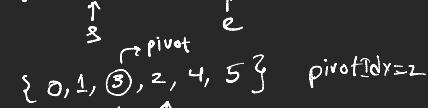
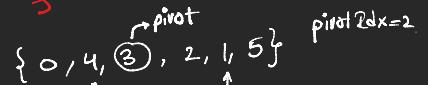
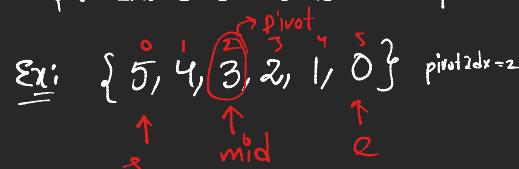
Time complexity $\Rightarrow O(N \times \log N)$

Space complexity $\Rightarrow O(1)$

⊗ How to put pivot At correct pos?



Aim put larger elements to right of pivot
put smaller element to left of pivot



Recursively for

left $\{0, 1, 2\}$ and right $\{4, 5\}$

⊗ Why should we return end? (Important)

→ Reason is we check $a[startIdx] \leq \text{pivot}$

→ So, All lesser than equal elements go left.

→ If we use, $a[endIdx] \geq \text{pivot}$,

then swap ($a[startIdx], \text{pivot}$)