1-1.11-3

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Question: If a line makes 60° and 45° angles with the positive directions of the X-axis and Z-axis respectively, then find the angle that it makes with the positive direction of the Y-axis. Hence, write the direction cosines of the line.

Solution: Let α , β and γ be the angles made by the line with the X, Y and Z axes respectively. Now the unit direction vector \mathbf{x} can be expressed as

$$\mathbf{x} = \begin{pmatrix} \cos \alpha \\ \cos \beta \\ \cos \gamma \end{pmatrix}$$
$$||\mathbf{x}|| = 1$$

$$\sqrt{\mathbf{x}\mathbf{x}^{\mathrm{T}}} = 1$$

$$\cos^{2}\alpha + \cos^{2}\beta + \cos^{2}\gamma = 1$$

$$\cos^{2}60^{\circ} + \cos^{2}\beta + \cos^{2}45^{\circ} = 1$$

$$\frac{1}{4} + \cos^{2}\beta + \frac{1}{2} = 1$$

$$\cos^{2}\beta = \frac{1}{4}$$

$$\cos\beta = \pm \frac{1}{2}$$

$$\beta = 60^{\circ}$$

Hence the direction cosines are

$$\mathbf{x} = \begin{pmatrix} \cos \alpha \\ \cos \beta \\ \cos \gamma \end{pmatrix} = \begin{pmatrix} \cos 60^{\circ} \\ \cos 60^{\circ} \\ \cos 45^{\circ} \end{pmatrix} = \begin{pmatrix} \frac{1}{2} \\ \frac{1}{2} \\ \frac{1}{\sqrt{2}} \end{pmatrix}$$

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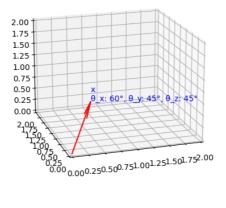


Fig. 0: Plot of the described vector

Code for this plot can be found at:

Codes/main.py Codes/main.c