

SPATIAL-SPECTRAL
PROCESSING, FEATURE
EXTRACTION AND
CLASSIFICATION OF
MNIST AND FASHION
MNIST DATASETS

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TABLE OF CONTENTS

INTRODUCTION.....	3
PROCESSING TECHNIQUES.....	3
FEATURE EXTRACTION METHOD.....	8
METHOD OF CLASSIFICATION.....	16
RESULTS AND DISCUSSION.....	19
CONCLUSION.....	43
REFERENCE.....	43
APPENDIX.....	17

INTRODUCTION

In my project, I have used MNIST dataset which comprises of hand-written digits and Fashion MNIST which comprises of clothing images. Both the dataset are of the same dimension and size i.e. 28X28 and 70,000 images. The images shown below depicts the sample images of MNIST and Fashion MNIST dataset.

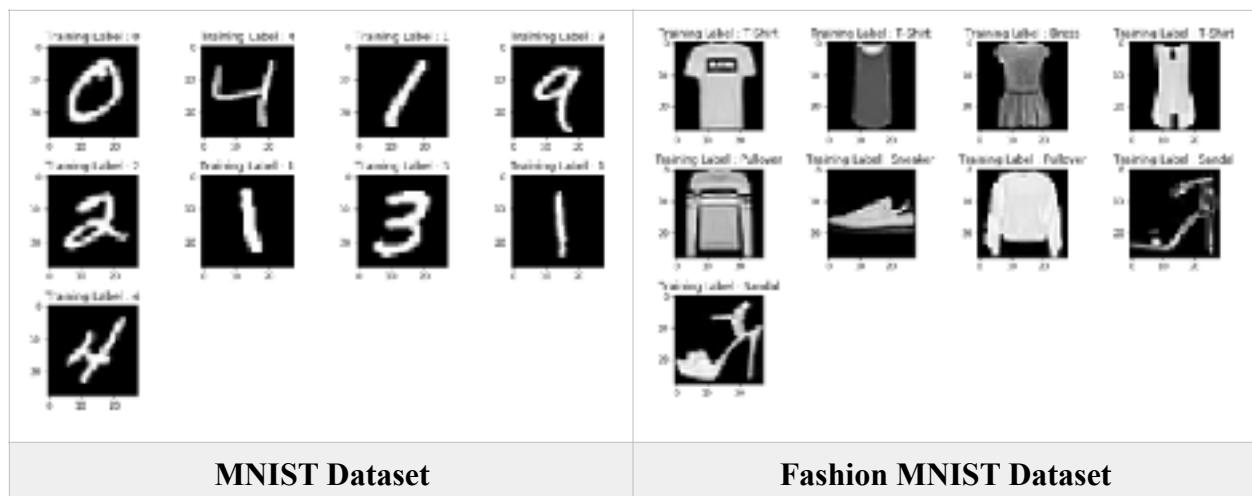


Figure 1 : Sample images of MNIST(left) AND Fashion MNIST(right) dataset.

PROCESSING TECHNIQUES

SPATIAL PROCESSING TECHNIQUES

1. DILATION

The basic effect of the operator on a binary image is to gradually enlarge the boundaries of regions of foreground pixels(*i.e.* white pixels, typically). Thus areas of foreground pixels grow in size while holes within those regions become smaller.

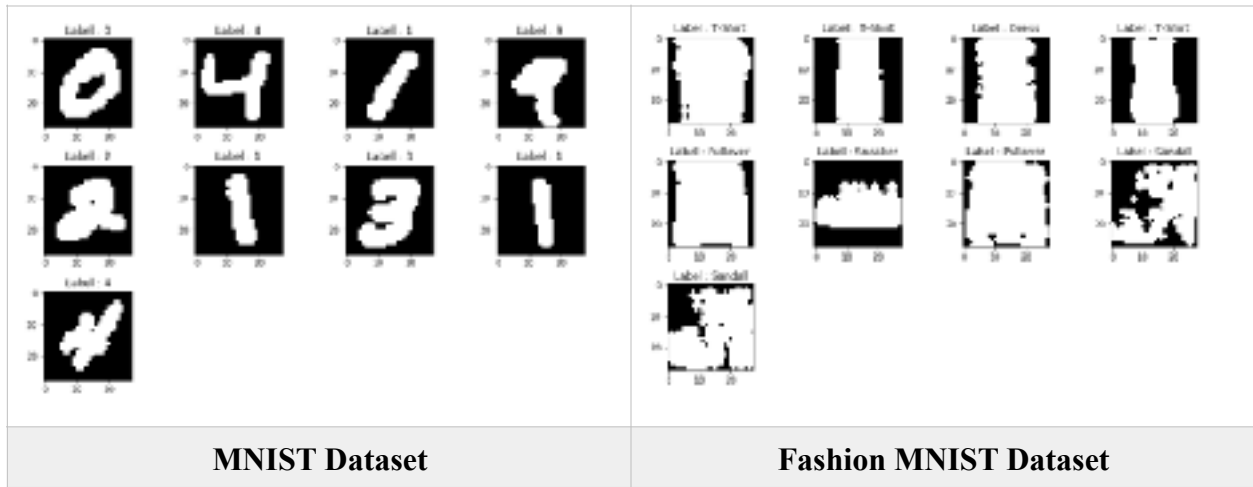


Figure 2 : Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation.

2. EROSION

The basic effect of the operator on a binary image is to erode away the boundaries of regions of foreground pixels (*i.e.* white pixels, typically). Thus areas of foreground pixels shrink in size, and holes within those areas become larger.

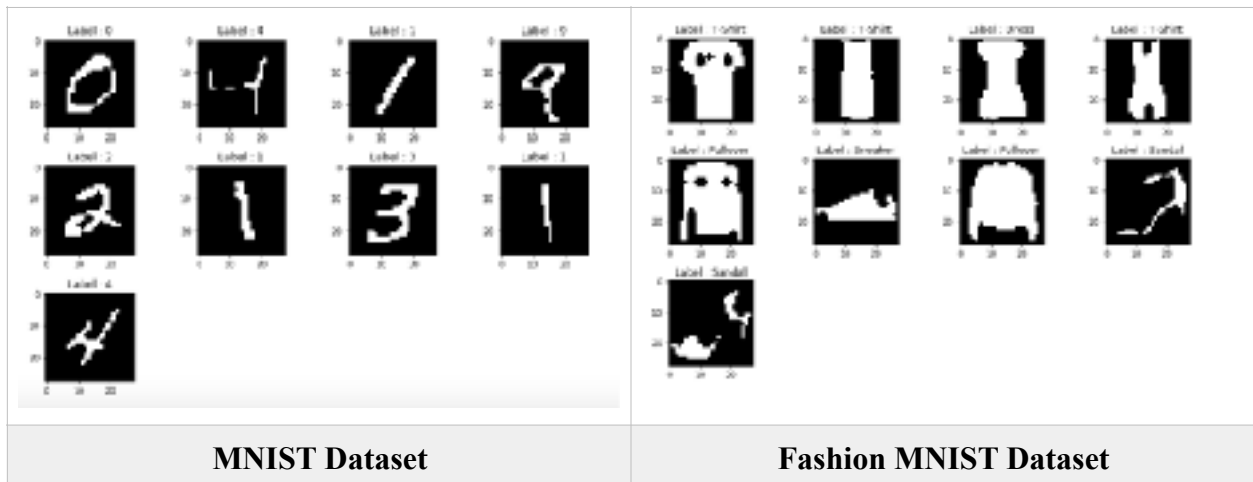


Figure 3 : Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion.

SPECTRAL PROCESSING TECHNIQUES

1. FOURIER TRANSFORM

The Fourier Transform is an important image processing tool which is used to decompose an image into its sine and cosine components. The output of the transformation represents the image in the Fourier or frequency domain, while the input image is the spatial domain equivalent.

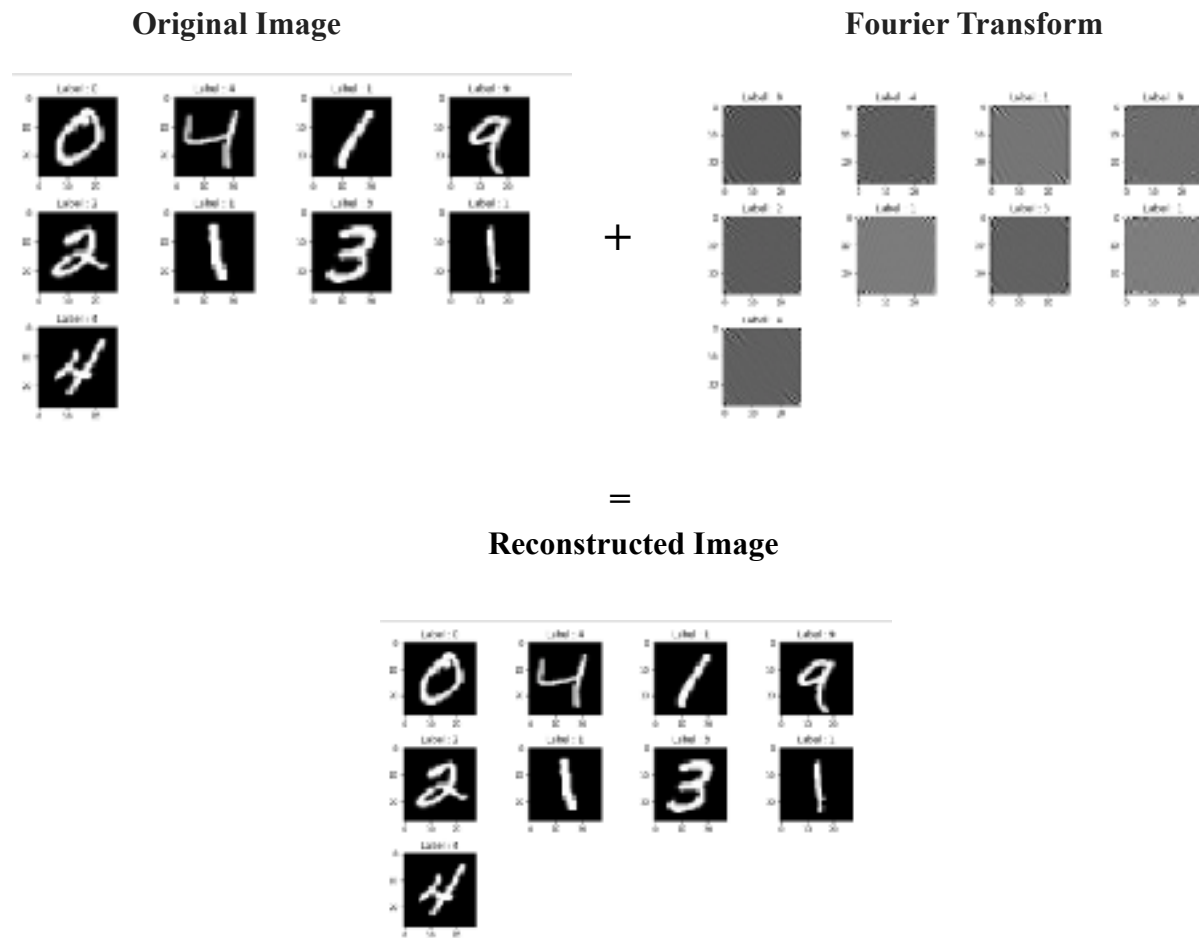


Figure 4 : Sample images of MNIST dataset after applying Fourier Transform.

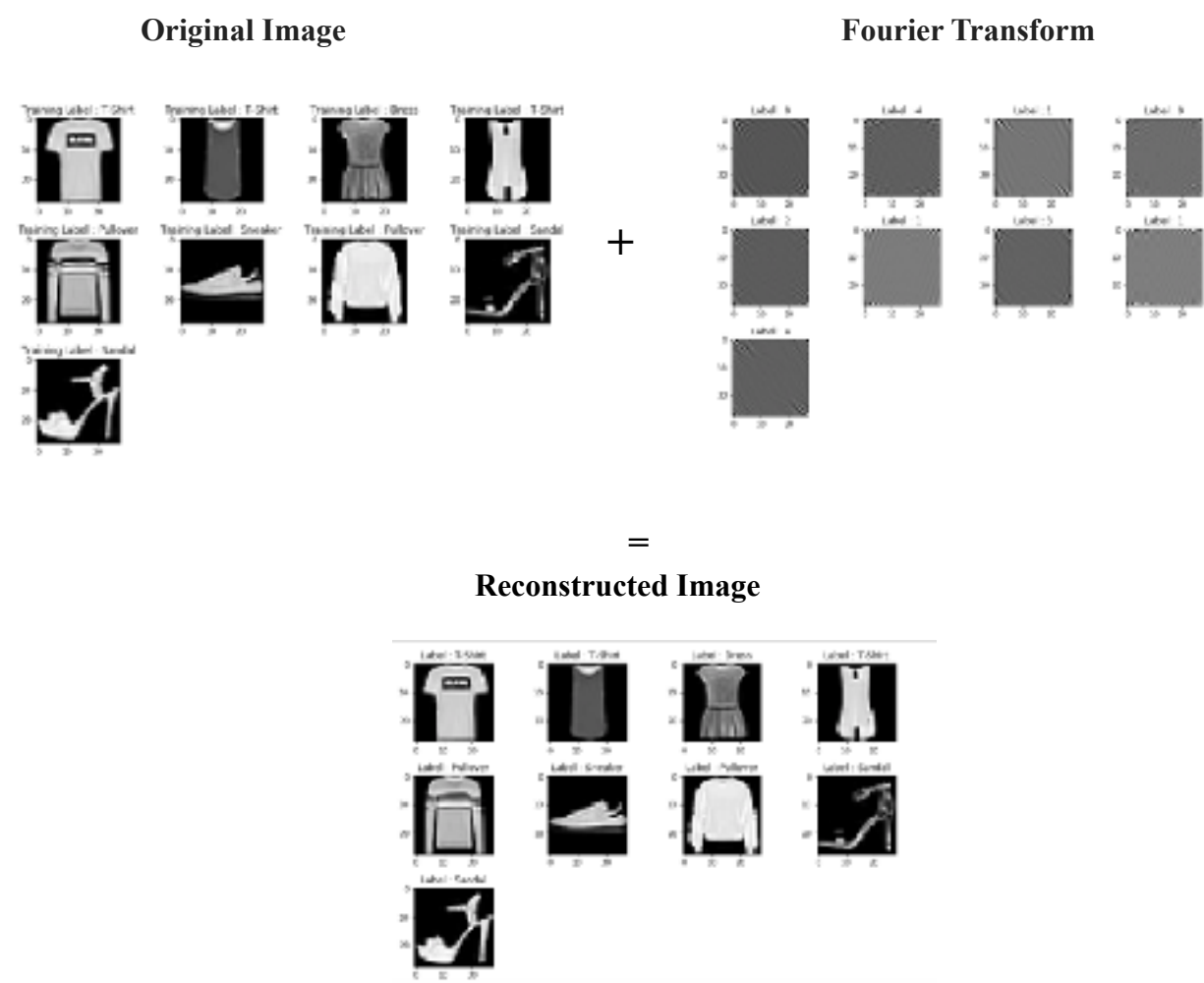


Figure 5 : Sample images of Fashion MNIST dataset after applying Fourier Transform.

2. PRINCIPAL COMPONENT ANALYSIS

It is used to compress high dimension data to low dimension data space. The size of the data was reduced from 784 components to 154 components.

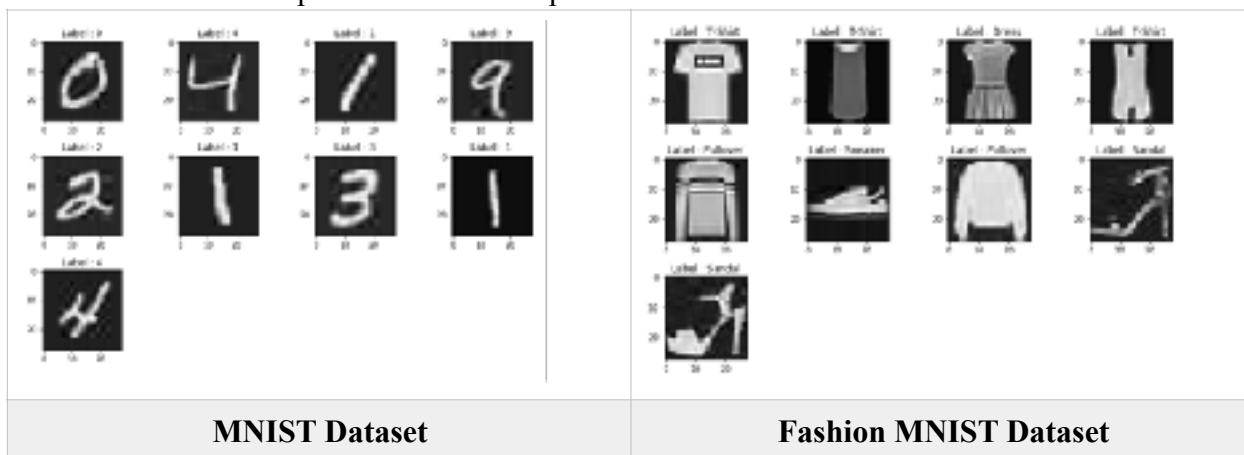


Figure 6 : Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying PCA.

SPATIAL-SPECTRAL PROCESSING TECHNIQUES

This section comprises of the combination of techniques used for spatial-spectral processing on the MNIST and Fashion MNIST Dataset

1. Dilation followed by Fourier Transform

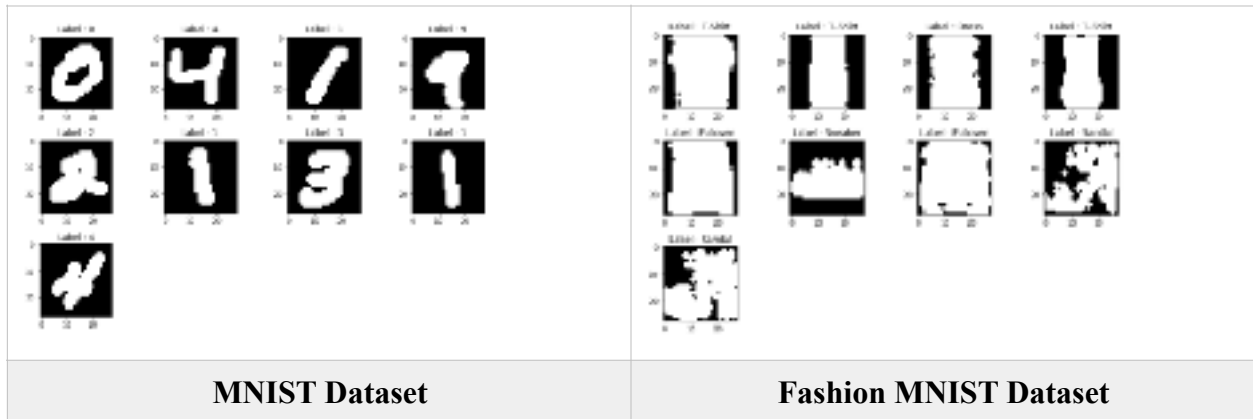


Figure 7: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation followed by Fourier Transform.

2. Erosion followed by Fourier Transform

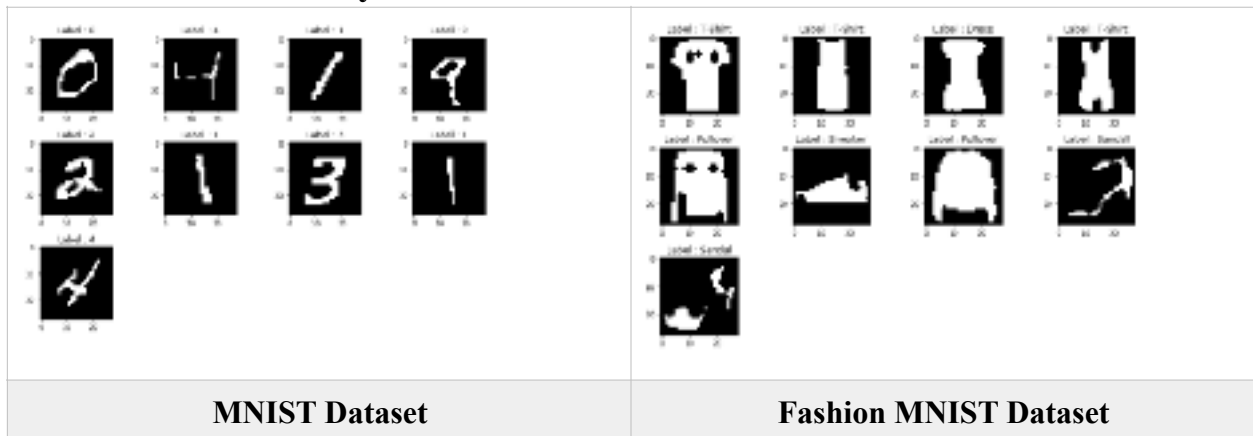


Figure 8: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion followed by Fourier Transform.

3. Dilation followed by Principal Component Analysis

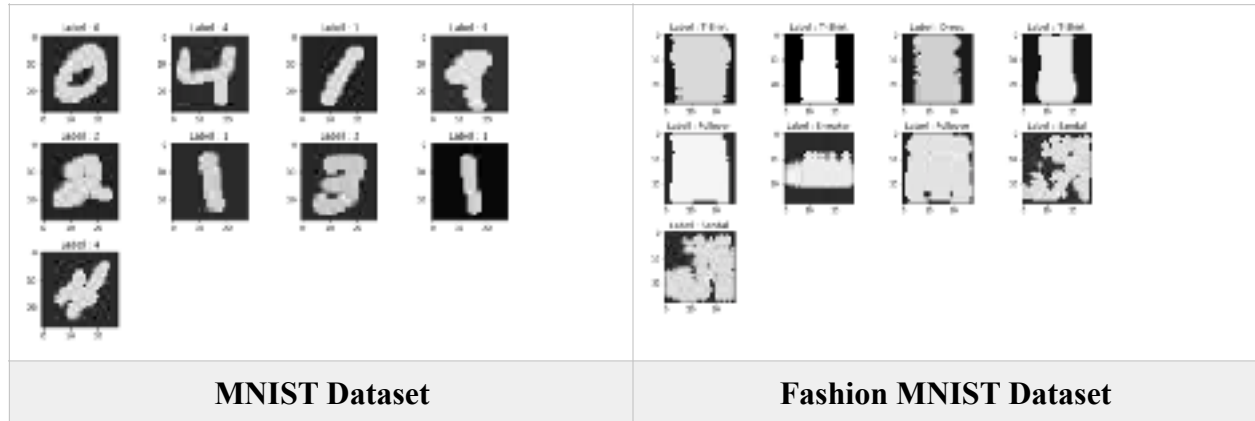


Figure 9: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation followed by Principal Component Analysis.

4. Erosion followed by Principal Component Analysis

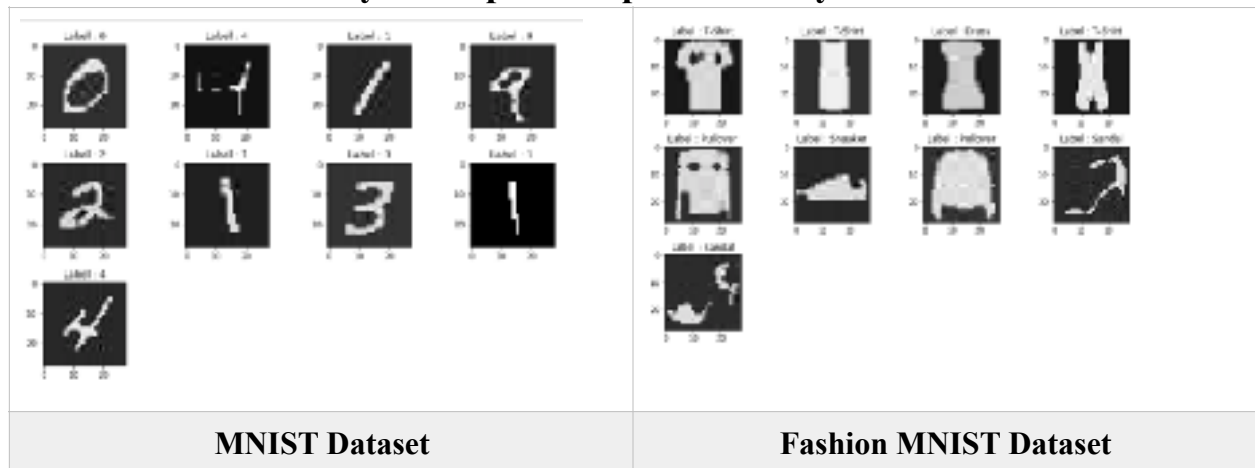


Figure 10: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion followed by Principal Component Analysis.

FEATURE EXTRACTION METHODS

SOBEL EDGE DETECTOR METHOD

It is a discrete differentiation operator, computing an approximation of the gradient of the image intensity function. At each point in the image, the result of the Sobel–Feldman operator is either the corresponding gradient vector or the norm of this vector.

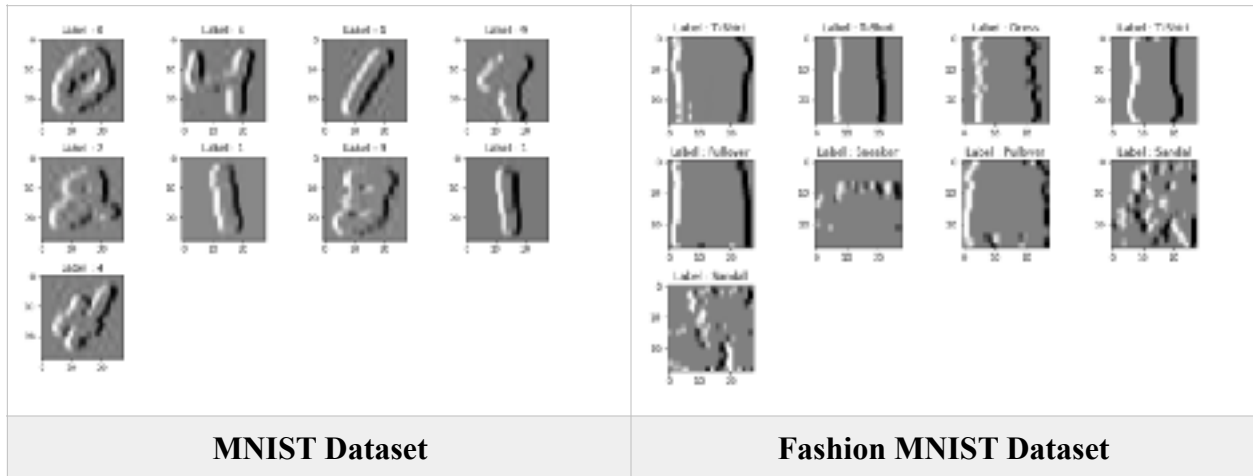


Figure 11: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation followed by Fourier Transform and Sobel Edge Detector.

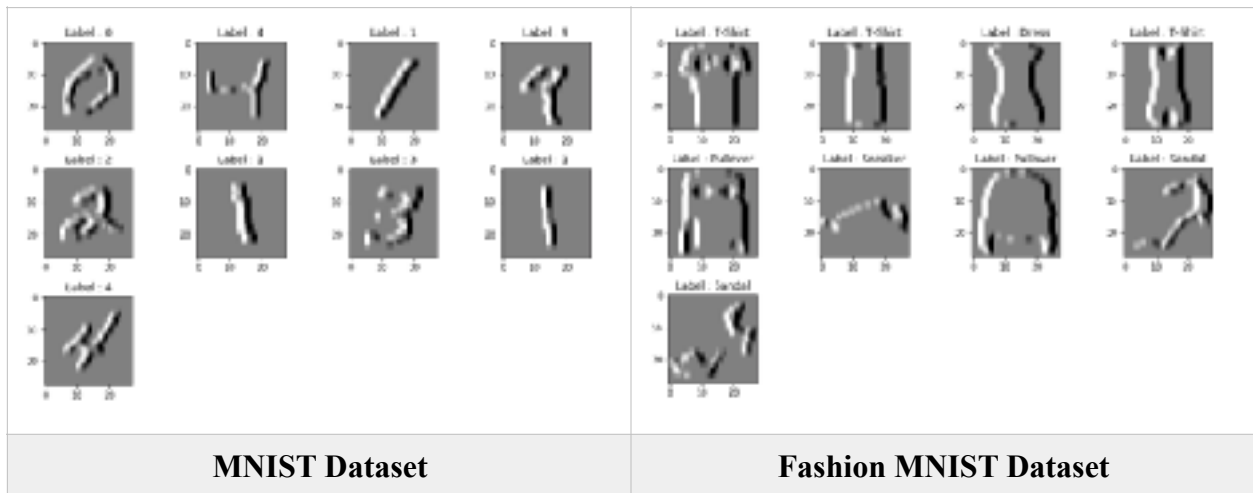


Figure 12: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion followed by Fourier Transform and Sobel Edge Detector.

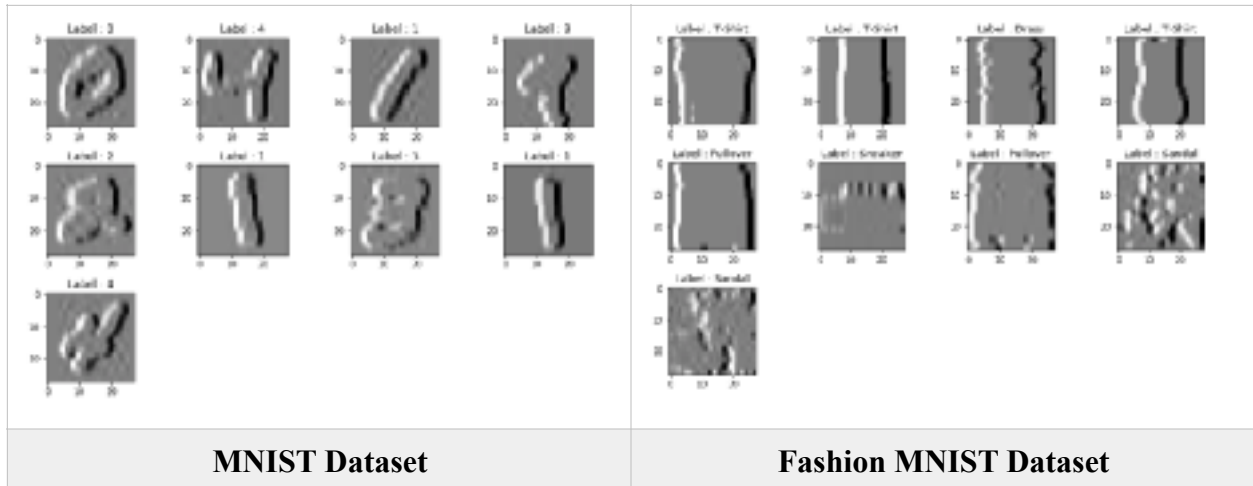


Figure 13: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation followed by Principal Component Analysis and Sobel Edge Detector.

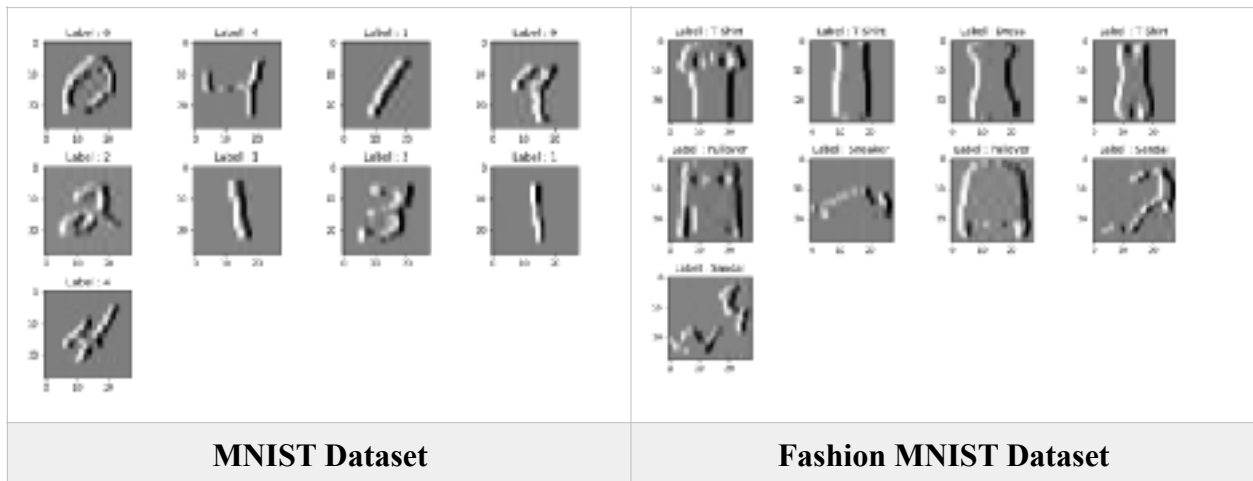


Figure 14: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion followed by Principal Component Analysis and Sobel Edge Detector.

CANNY EDGE DETECTOR METHOD

The Canny edge detector is an edge detection operator that uses a multi-stage algorithm to detect a wide range of edges in images. It uses a filter based on the derivative of a Gaussian in order to compute the intensity of the gradients. The Gaussian reduces the effect of noise present in the image.

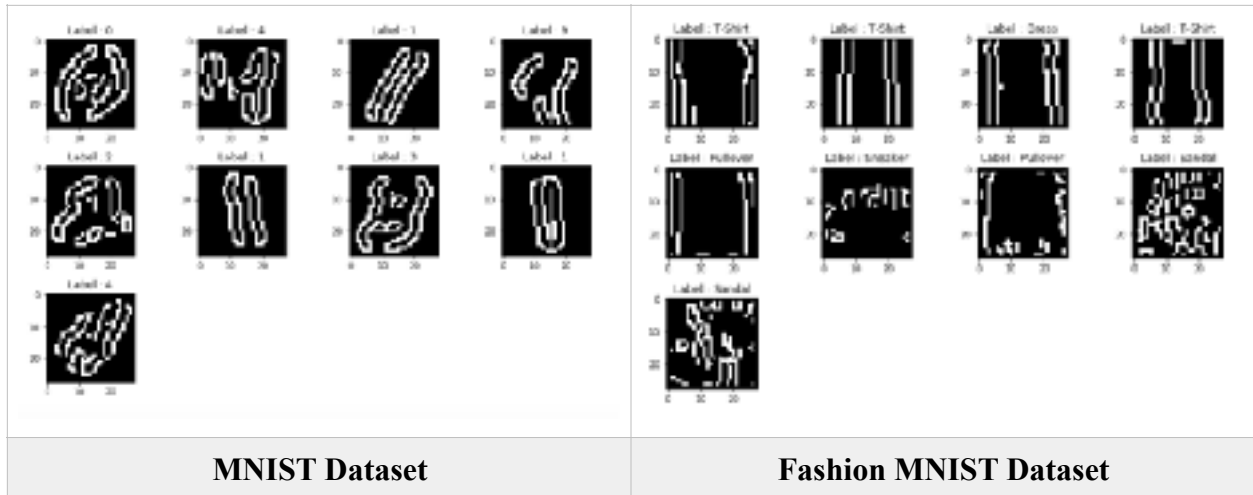


Figure 15: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation followed by Fourier Transform and Canny Edge Detector.

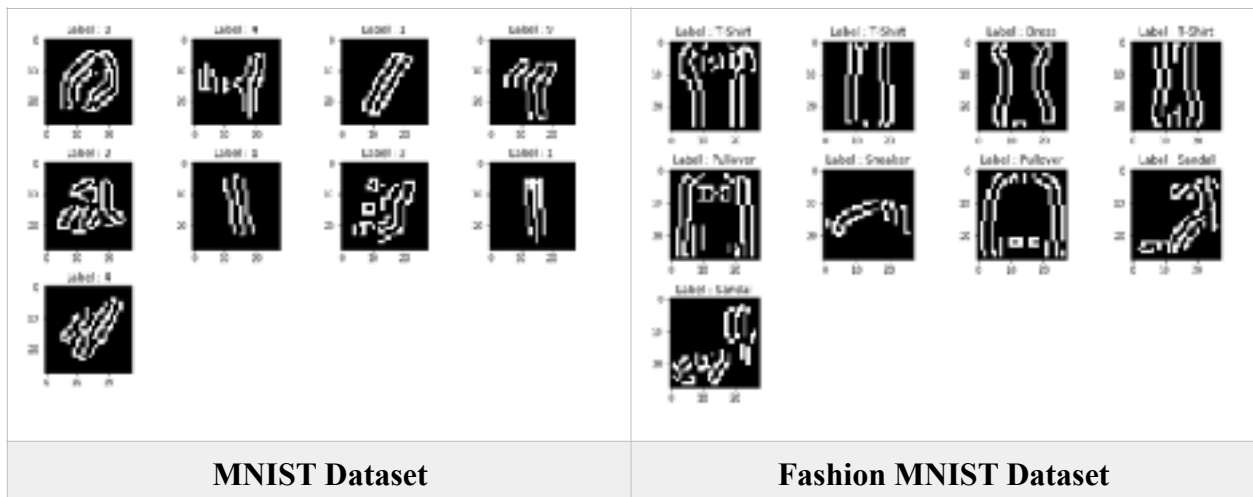


Figure 16: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion followed by Fourier Transform and Canny Edge Detector.

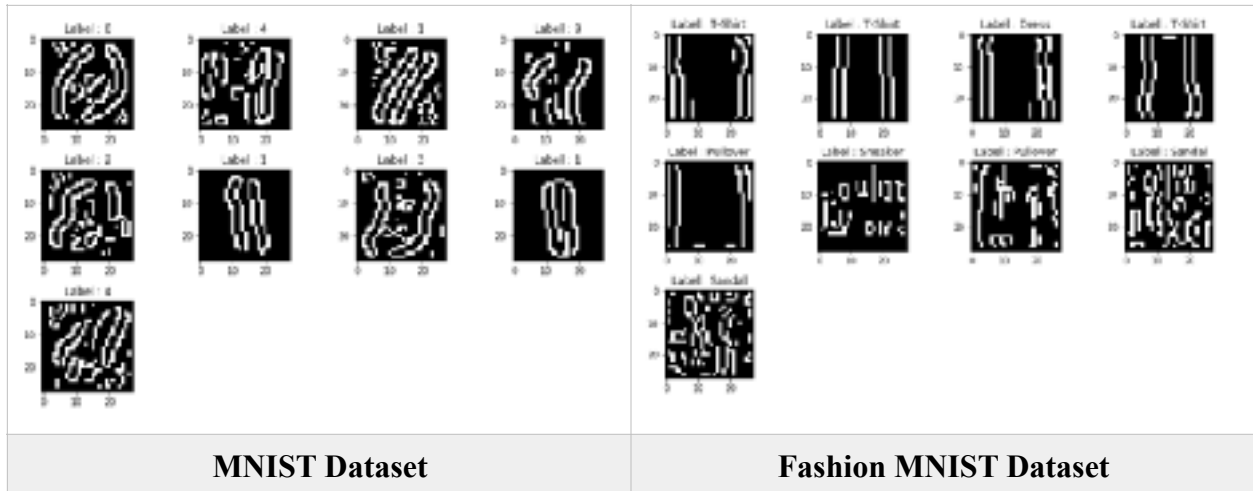


Figure 17: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation followed by Principal Component Analysis and Canny Edge Detector.

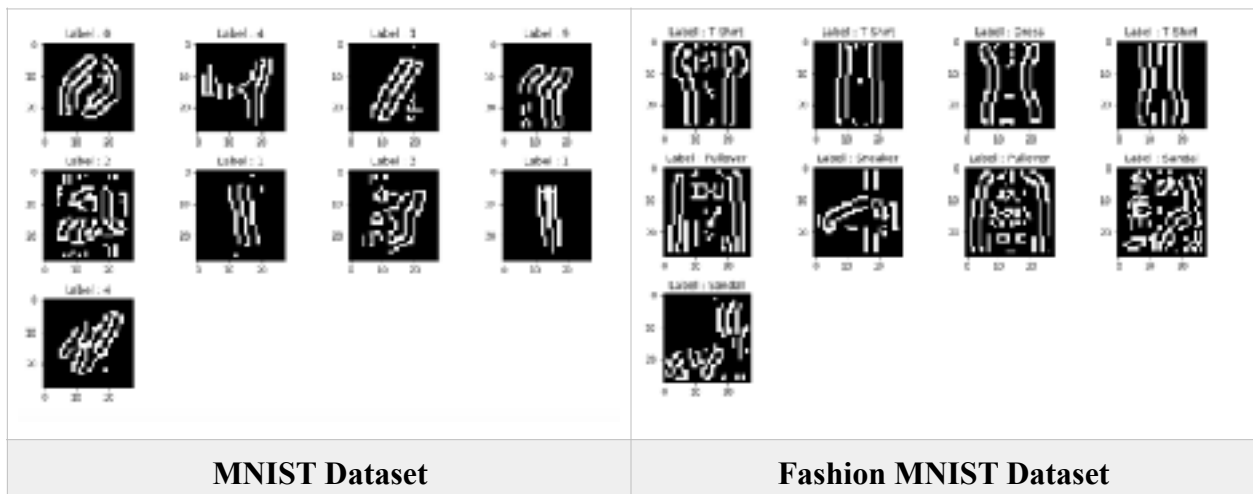


Figure 18: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion followed by Principal Component Analysis and Canny Edge Detector.

LOCAL BINARY PATTERN

Local Binary Pattern (LBP) looks at points surrounding a central point and tests whether the surrounding points are greater than or less than the central point (i.e. gives a binary result). The Images below depicts the processed images after applying the LBP.

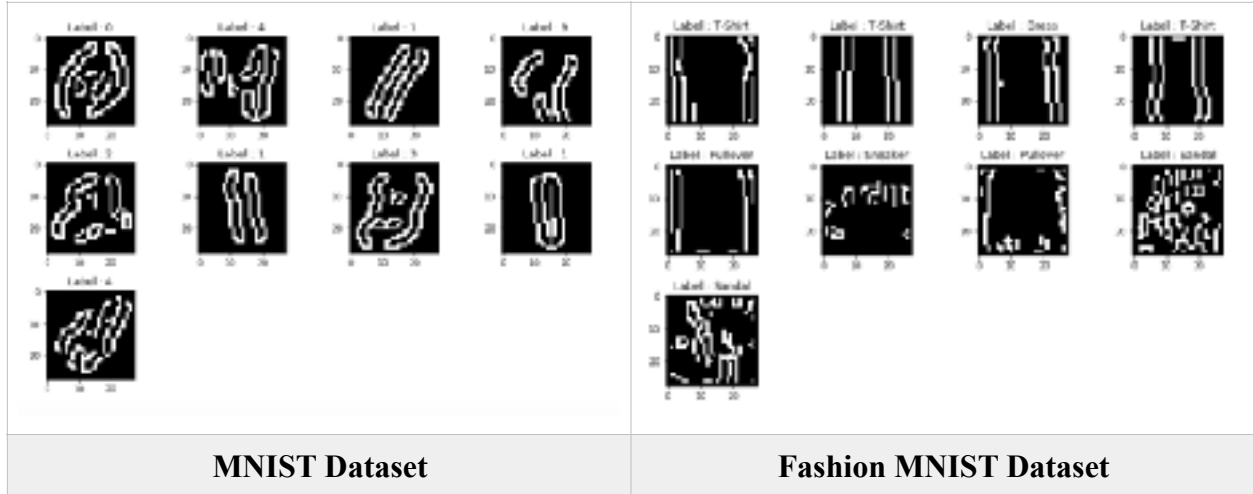


Figure 19: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation followed by Fourier Transform and Local Binary Pattern

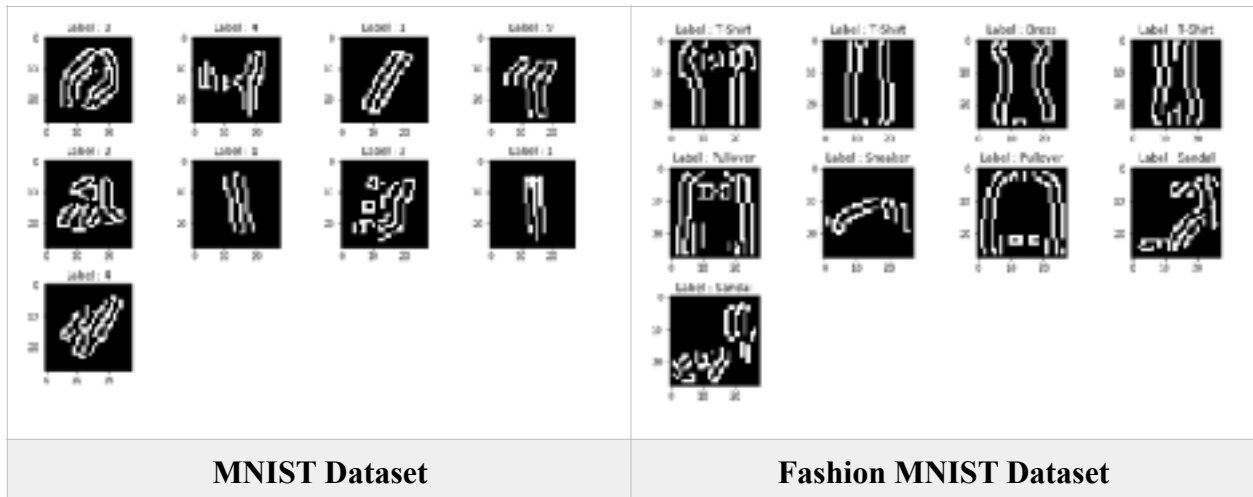


Figure 20: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion followed by Fourier Transform and Local Binary Pattern

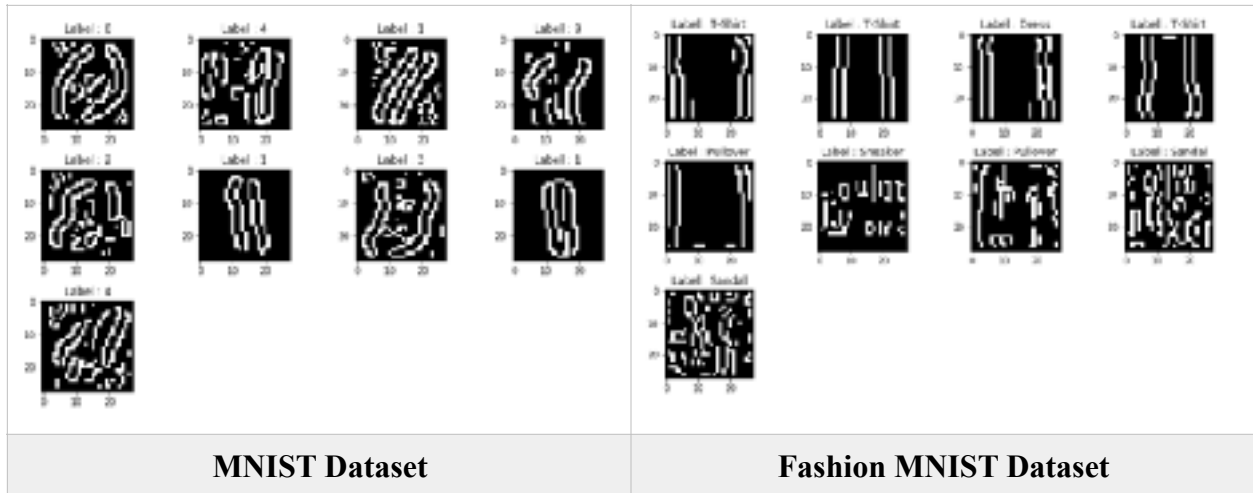


Figure 21: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation followed by Principal Component Analysis and Local Binary Pattern

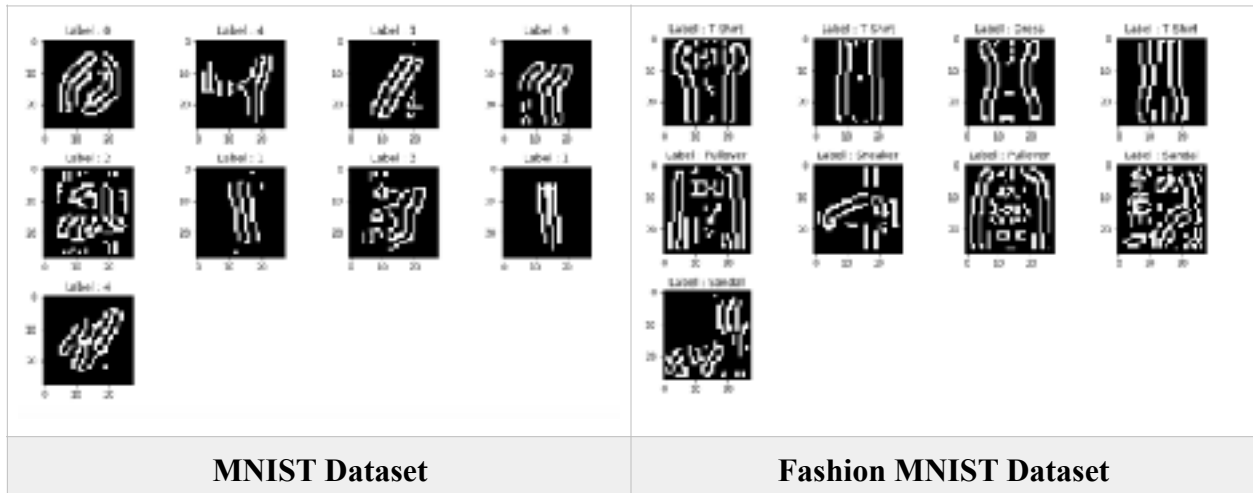


Figure 22: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion followed by Principal Component Analysis and Local Binary Pattern

PEAK LOCAL MAXIMA METHOD

Find peaks in an image as coordinate list or boolean mask.

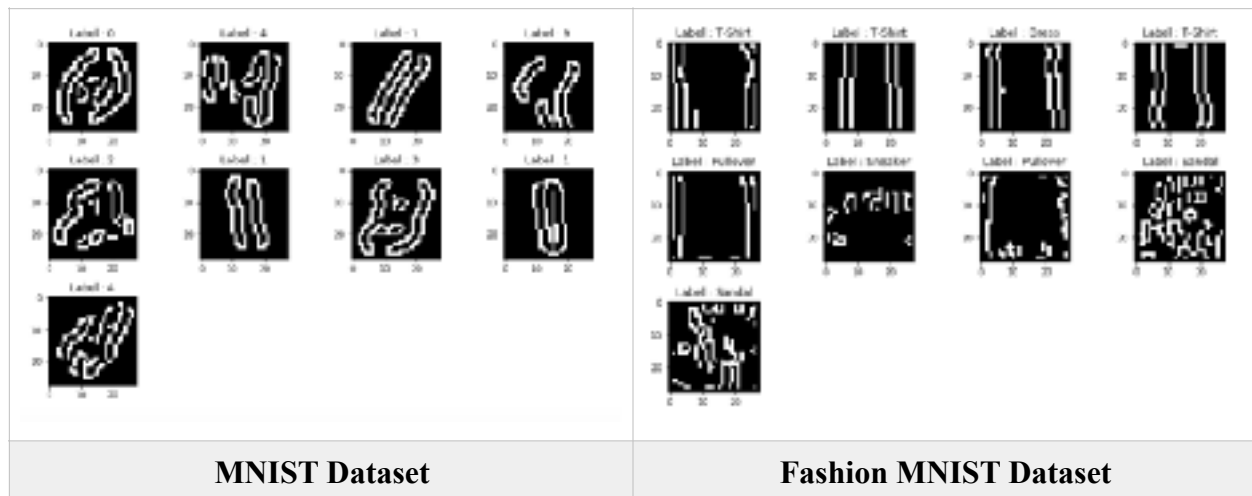


Figure 23: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation followed by Fourier Transform and Peak Local Maxima

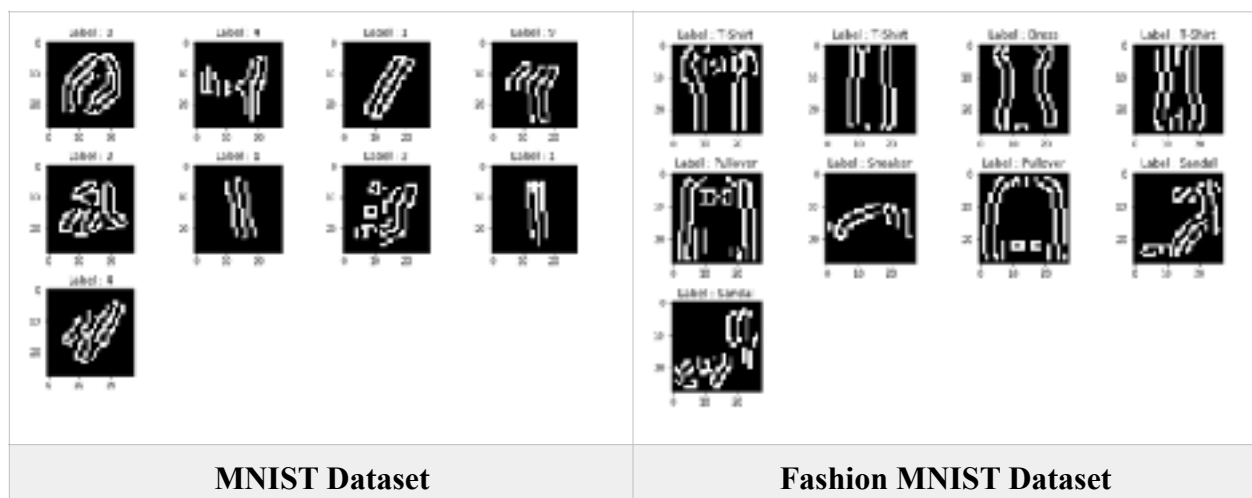


Figure 24: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion followed by Fourier Transform and Peak Local Maxima

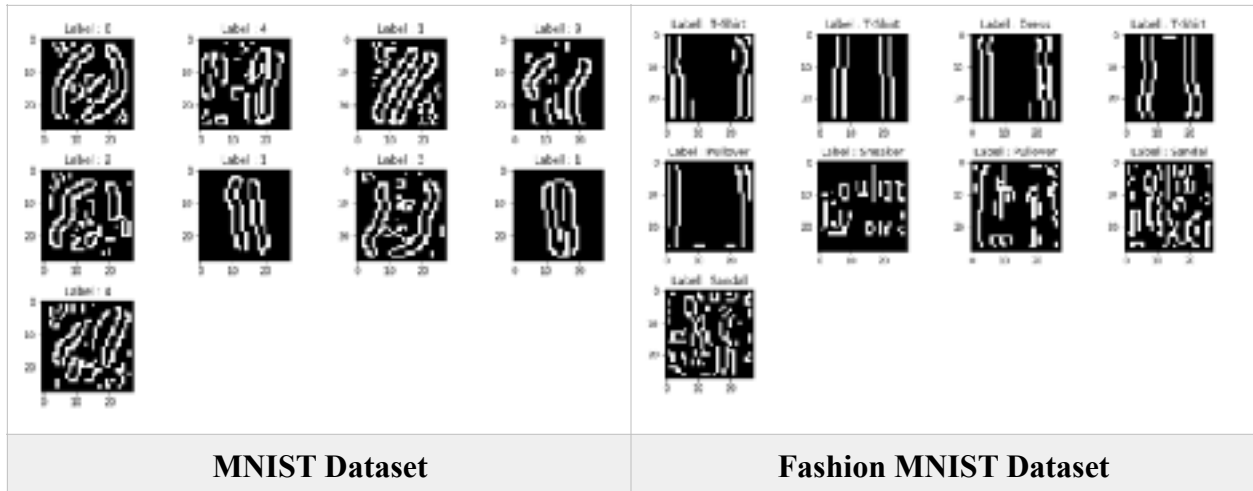


Figure 25: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Dilation followed by Principal Component Analysis and Peak Local Maxima

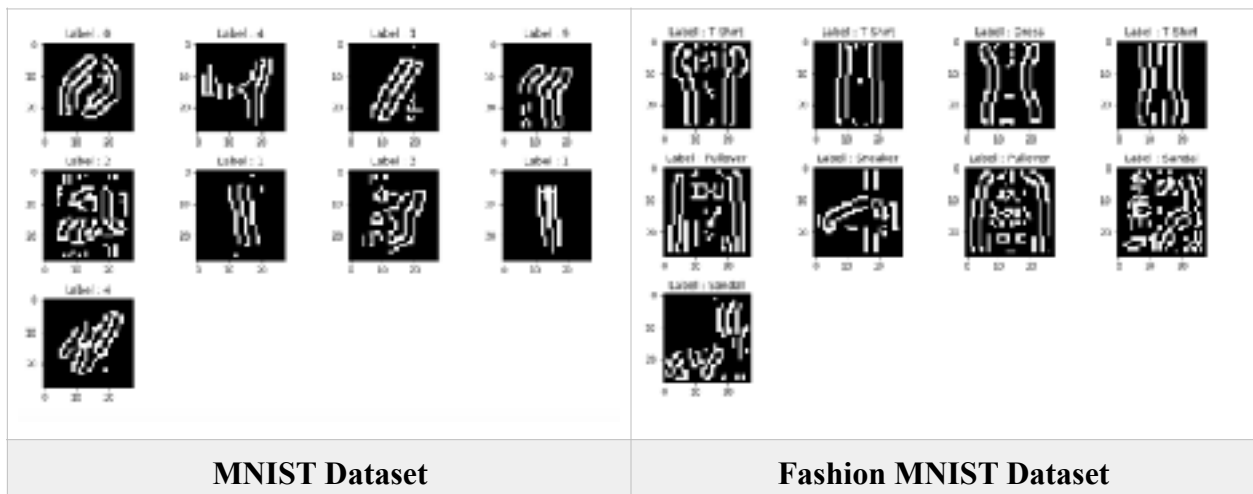


Figure 26: Sample images of MNIST(left) AND Fashion MNIST(right) dataset after applying Erosion followed by Principal Component Analysis and Peak Local Maxima

METHOD OF CLASSIFICATION

MULTI-LAYER PERCEPTRON

It is a class of Feed-forward network. It consists of at least three Hidden layers of nodes. Each node is a neuron that uses a non-linear activation function. The figure given below shows the Architecture of the Multi-Layer perceptron used for this project.

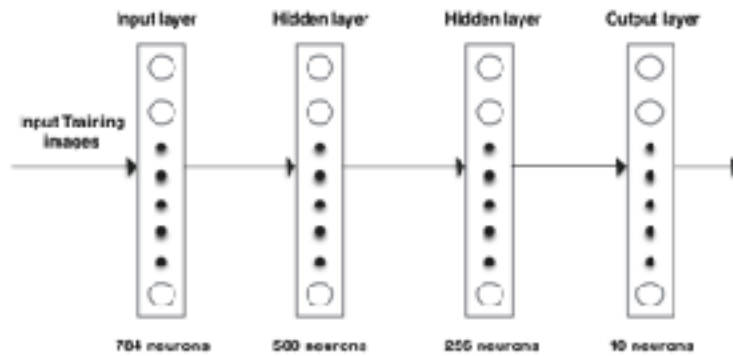


Figure 27: Multi-layer Perceptron Model

CONVOLUTIONAL NEURAL NETWORK

It is a class of deep, feed-forward network. They require relatively less pre-processing compared to other image classification algorithms. The figure given below shows the Architecture of the Convolution neural network used for this project.

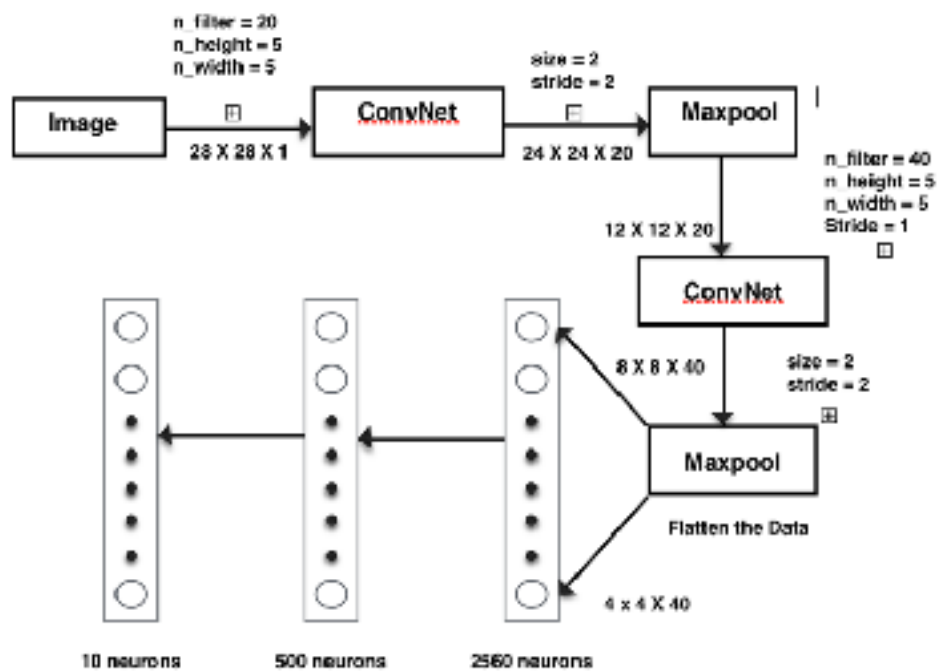


Figure 28: Convolutional Neural network model

At Each layer except the output Layer, I have used ReLu(Rectified Linear Unit) as the Non-

linear Activation Function. Softmax is applied at the output layer and Cross Entropy Loss is used to calculate the loss at each epoch.

ReLU Function:

$$f(x) = \max(0, x)$$

Softmax Function:

$$P(y = j \mid \mathbf{x}) = \frac{e^{\mathbf{x}^T \mathbf{w}_j}}{\sum_{k=1}^K e^{\mathbf{x}^T \mathbf{w}_k}}$$

Cross Entropy Loss Function:

$$\text{Loss} = -(y * \log(p) + (1 - y) * \log(1 - p))$$

RESULTS AND DISCUSSION

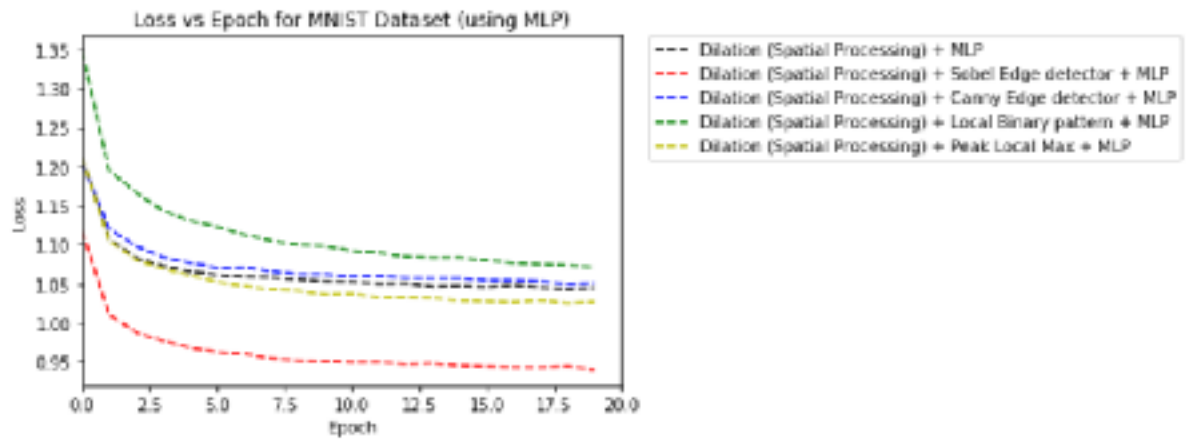


Figure 29 : The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Dilation and Feature Extraction with MLP as Classifier

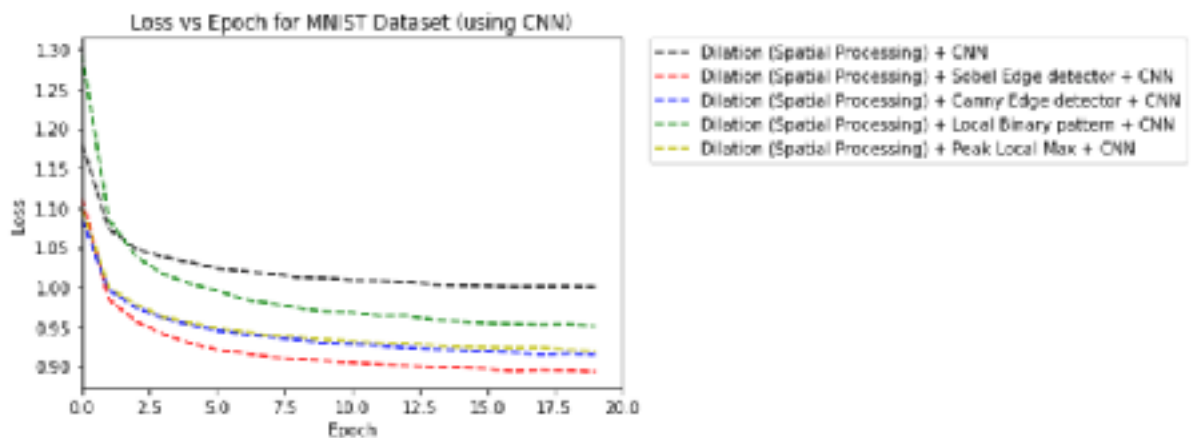


Figure 30 : The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Dilation and Feature Extraction with CNN as Classifier

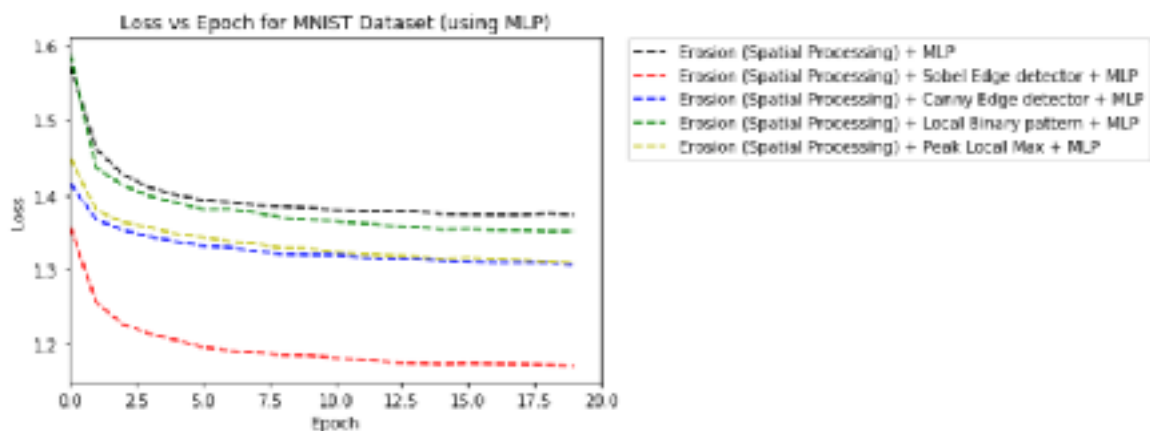


Figure 31 : The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Erosion and Feature Extraction with MLP as Classifier

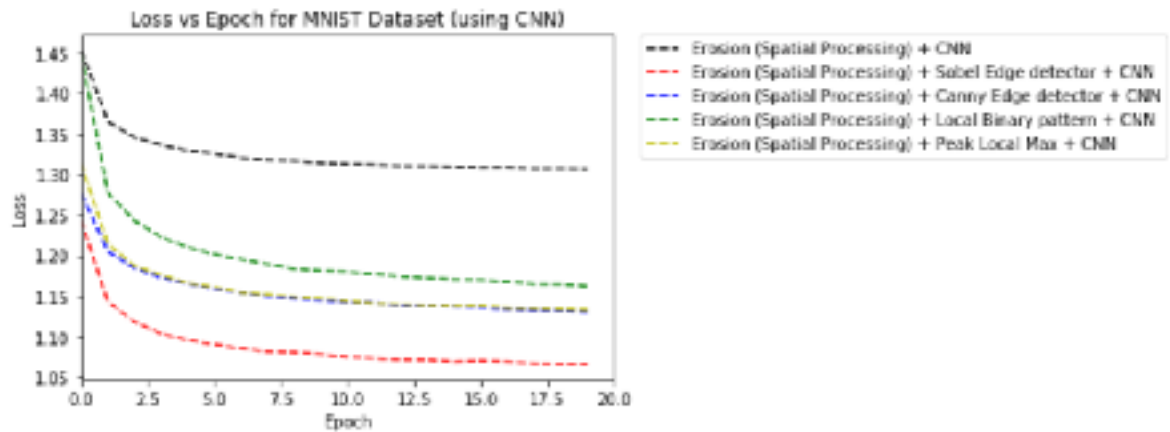


Figure 32: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Erosion and Feature Extraction with CNN as Classifier

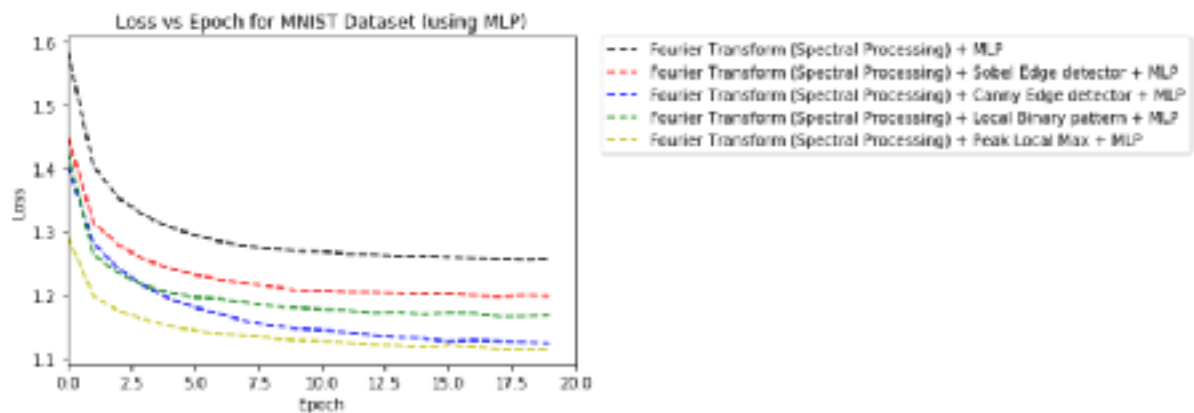


Figure 33: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Fourier transform and Feature Extraction with MLP as Classifier

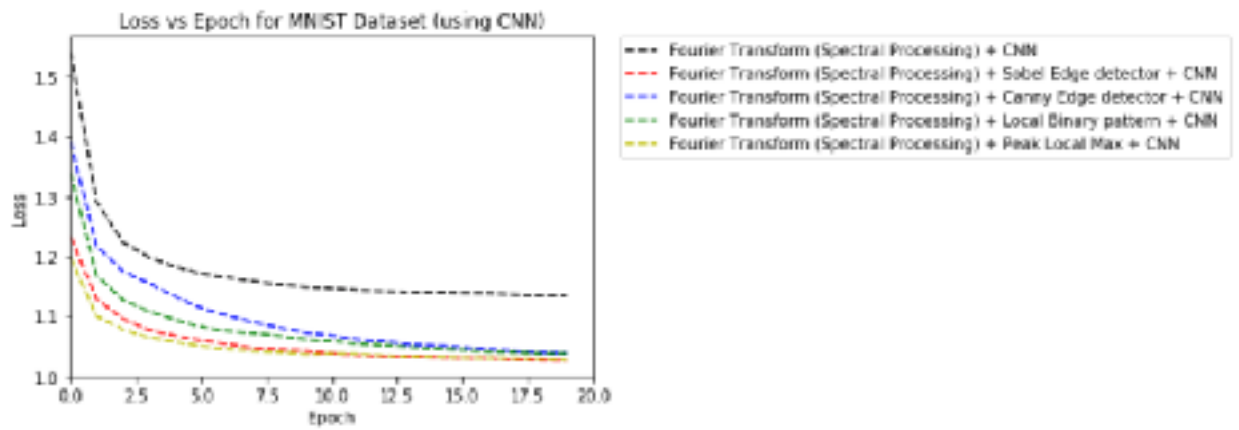


Figure 34: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Fourier transform and Feature Extraction with CNN as Classifier

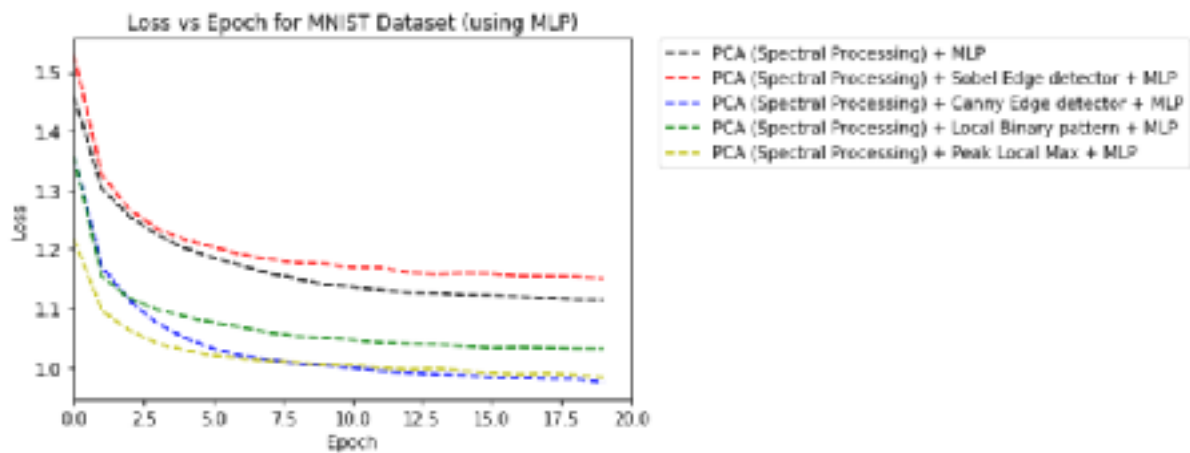


Figure 35: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying PCA and Feature Extraction with MLP as Classifier

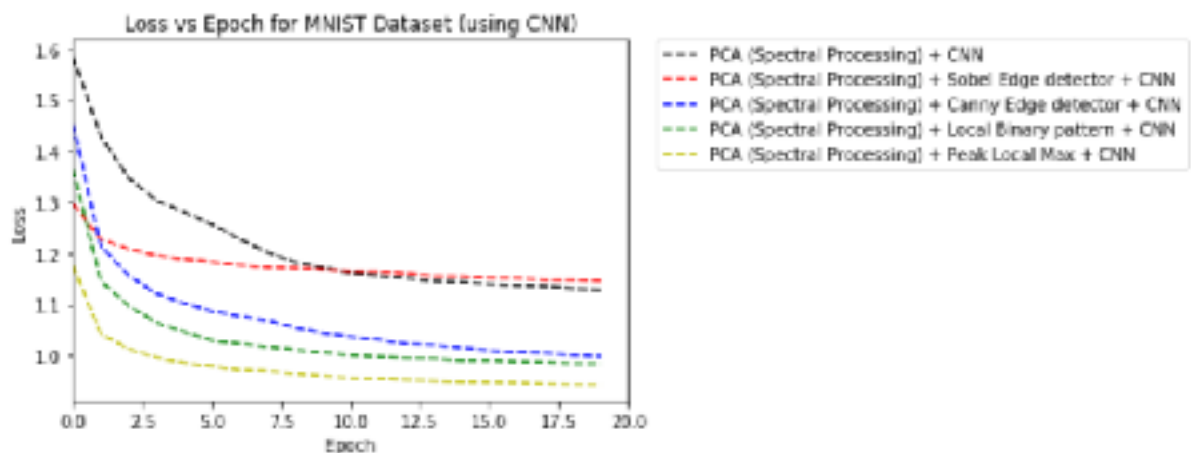


Figure 36: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying PCA and Feature Extraction with CNN as Classifier

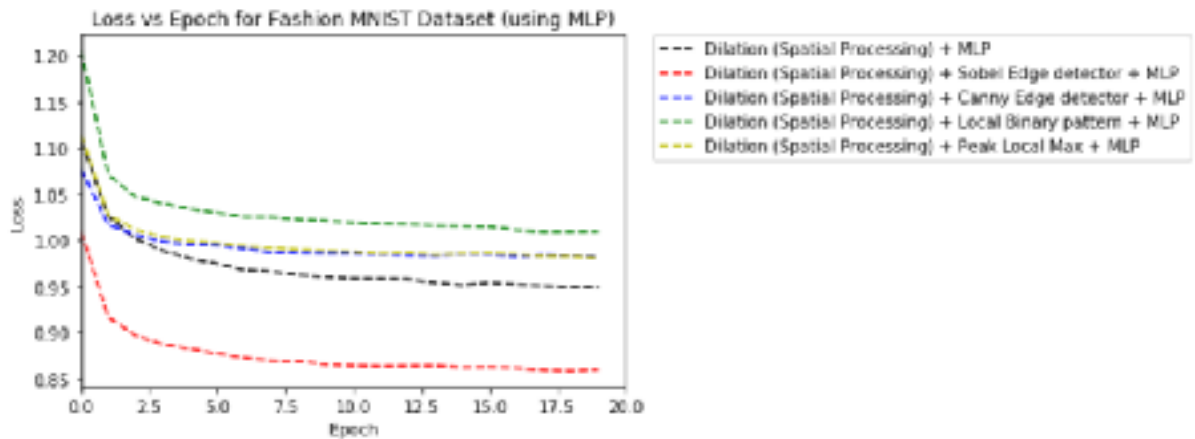


Figure 37 : The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Dilation and Feature Extraction with MLP as Classifier

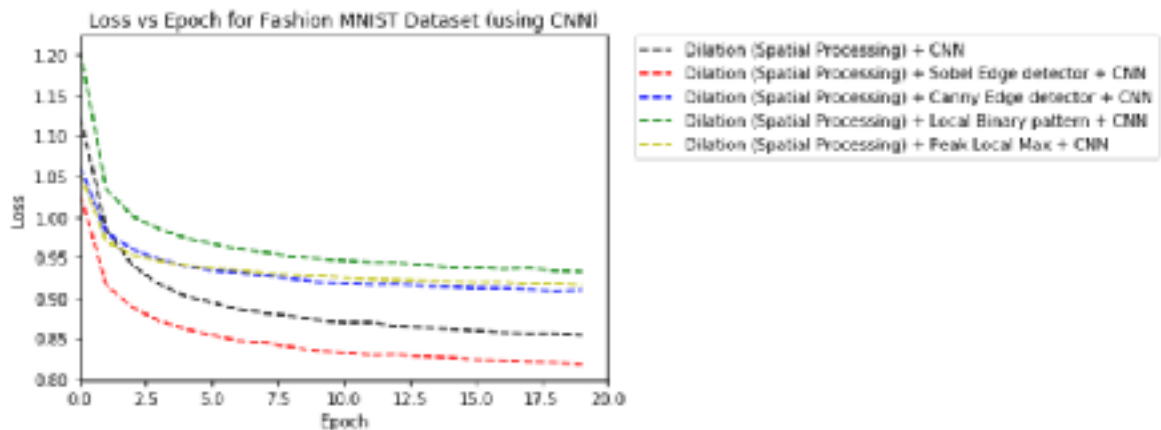


Figure 38 : The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Dilation and Feature Extraction with CNN as Classifier

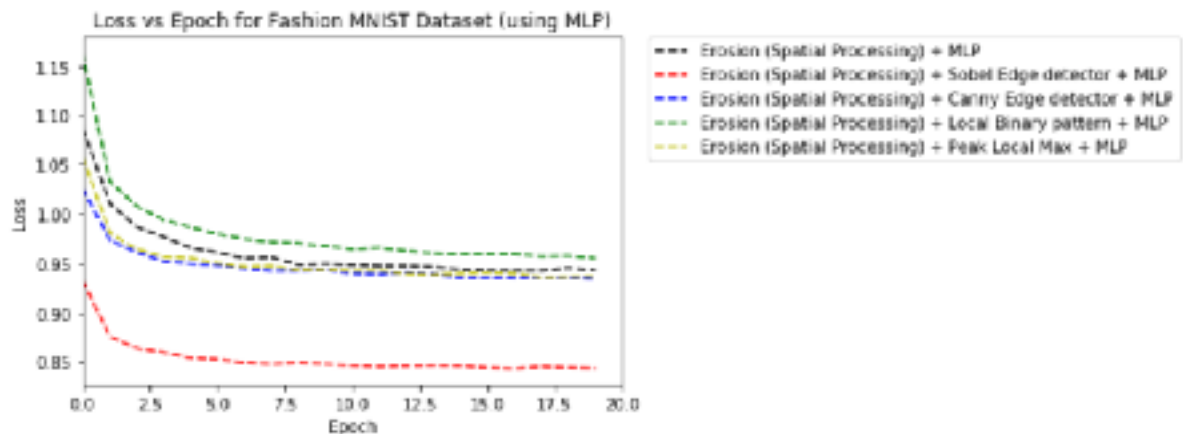


Figure 39 : The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Erosion and Feature Extraction with MLP as Classifier

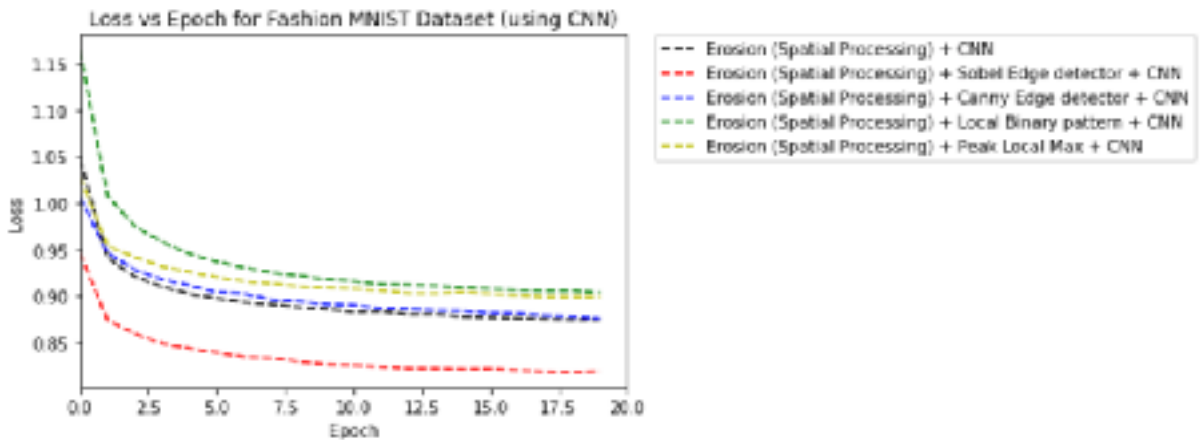


Figure 40 : The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Erosion and Feature Extraction with CNN as Classifier

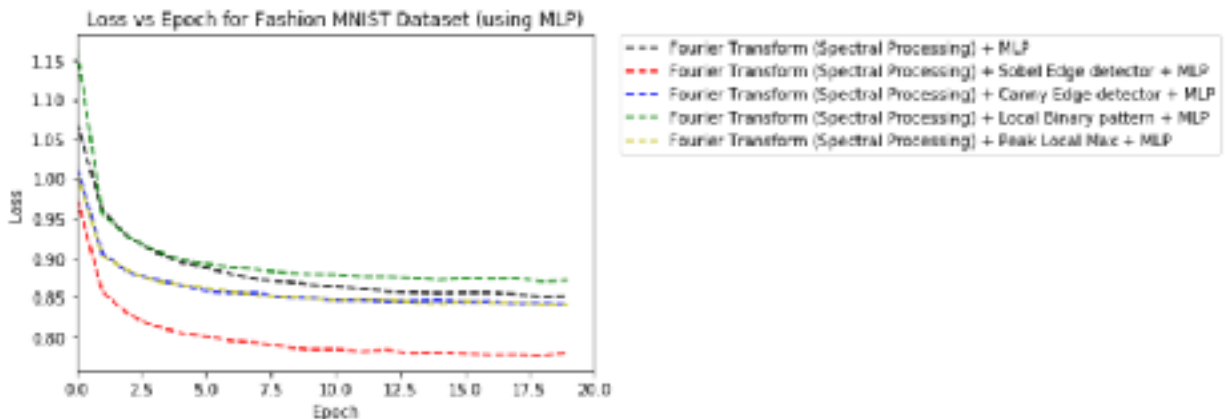


Figure 41: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Fourier transform and Feature Extraction with MLP as Classifier

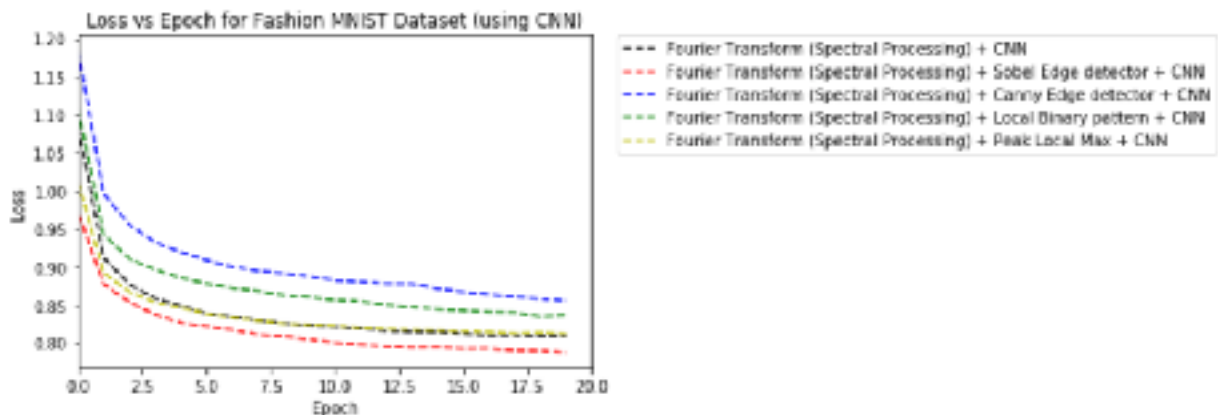


Figure 42: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Fourier transform and Feature Extraction with CNN as Classifier

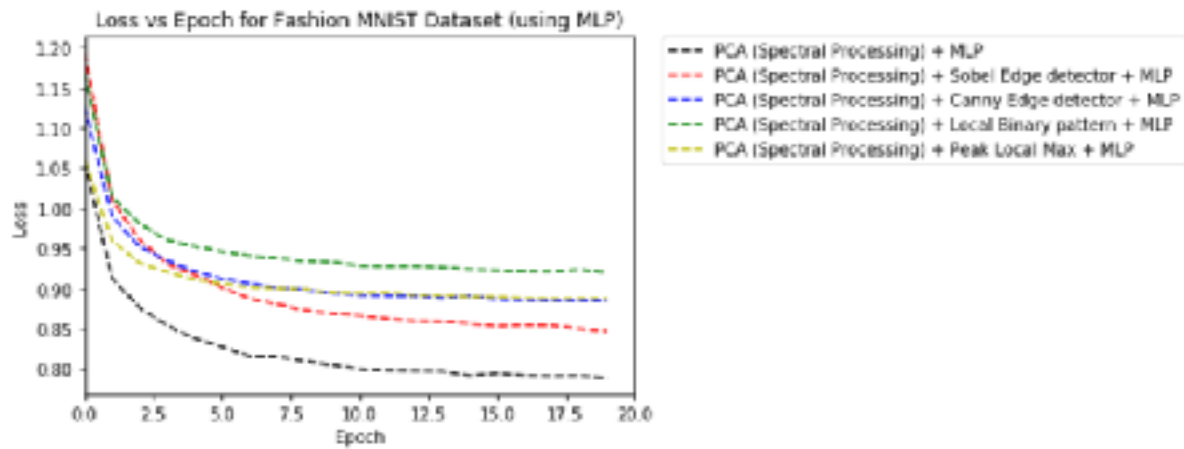


Figure 43: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying PCA and Feature Extraction with MLP as Classifier

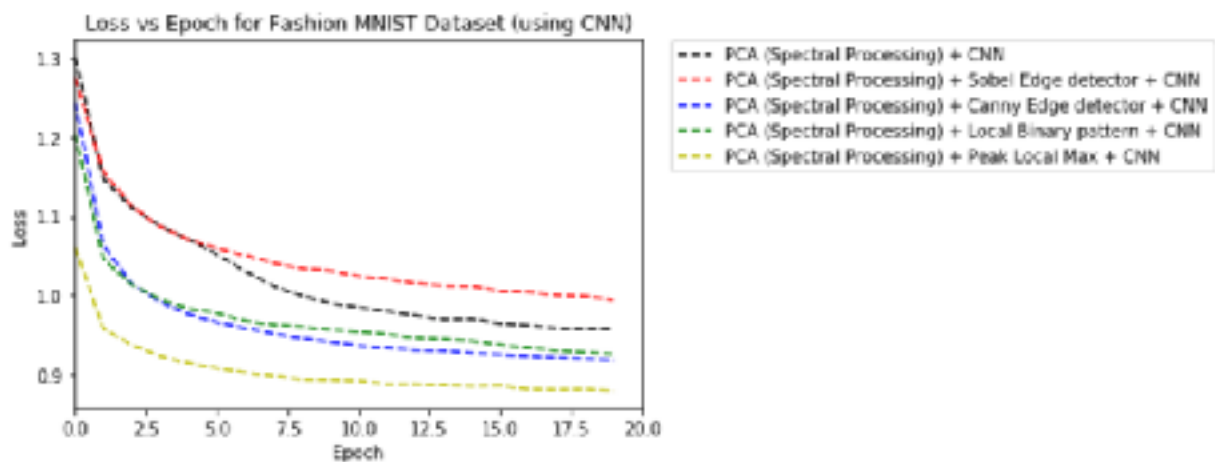


Figure 44: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying PCA and Feature Extraction with CNN as Classifier

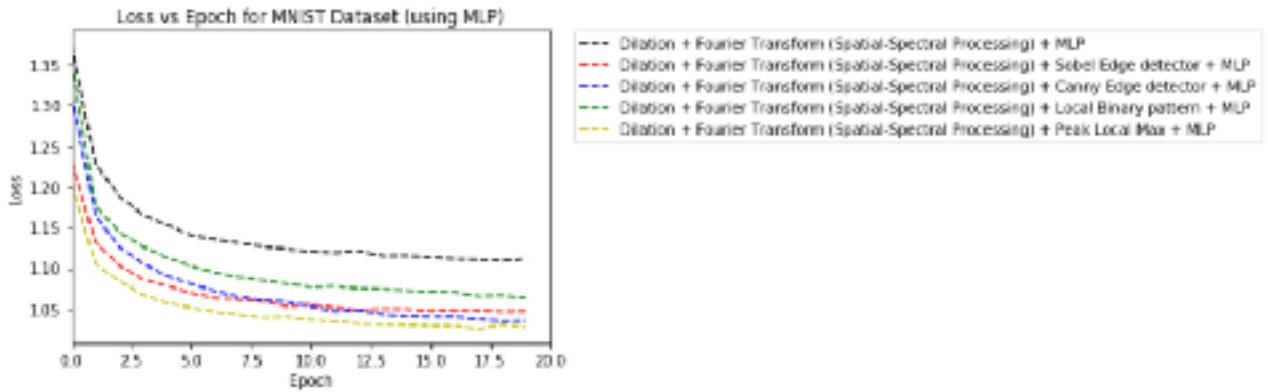


Figure 45: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Dilation followed by Fourier Transform and Feature Extraction with MLP as Classifier

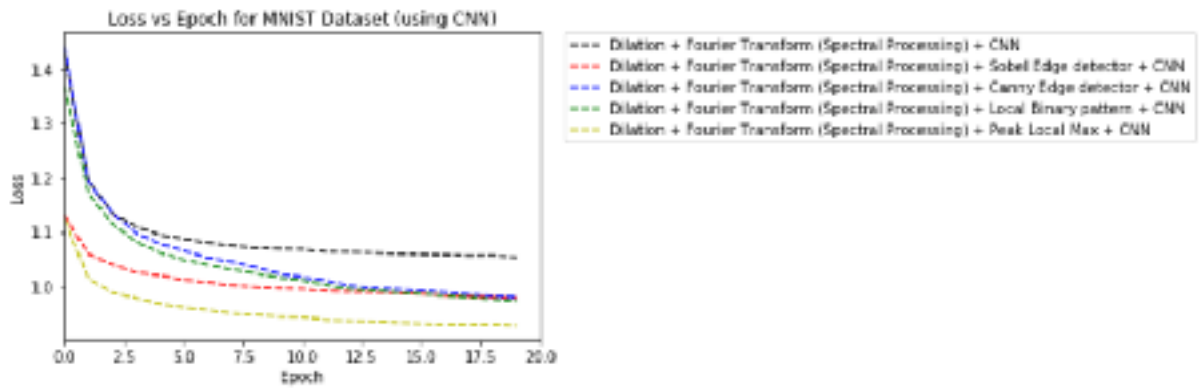


Figure 46: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Dilation followed by Fourier Transform and Feature Extraction with CNN as Classifier

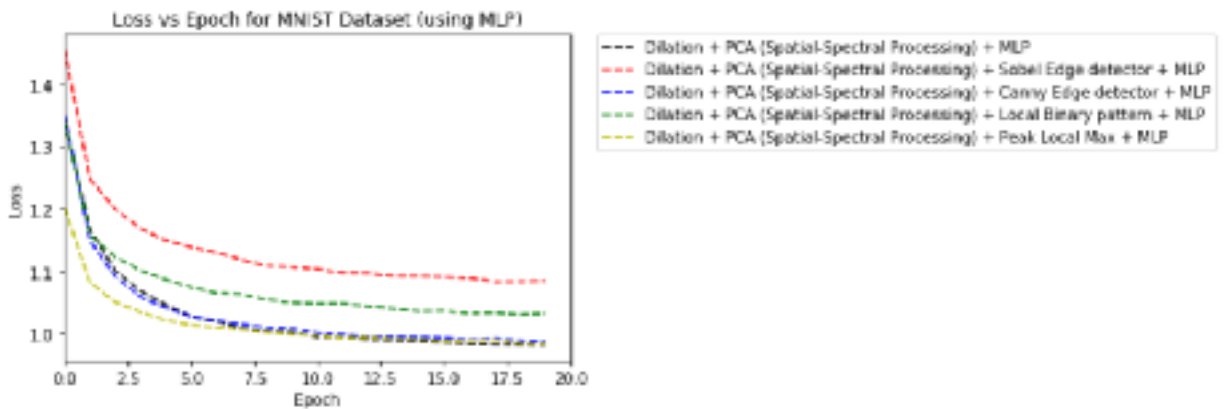


Figure 47: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Dilation followed by PCA and Feature Extraction with MLP as Classifier

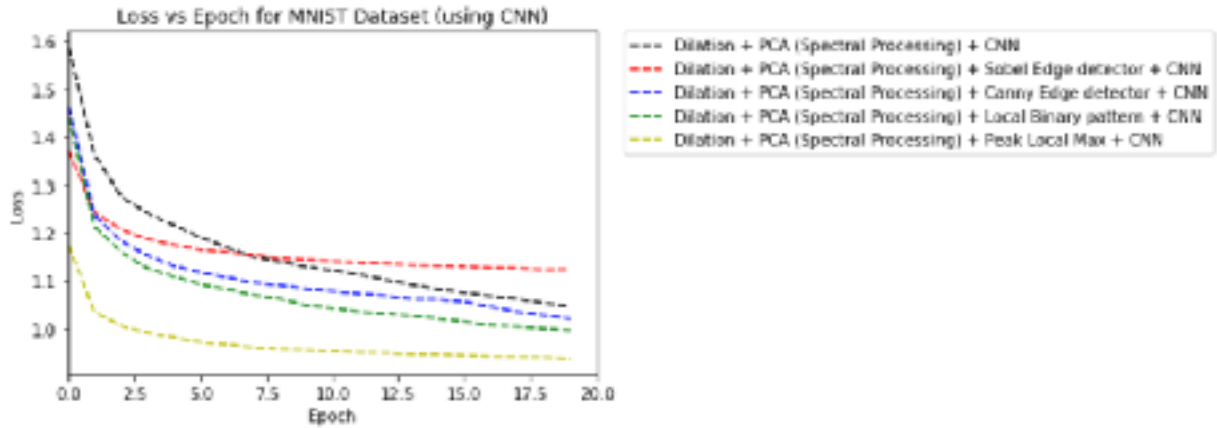


Figure 48: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Dilation followed by PCA and Feature Extraction with CNN as Classifier

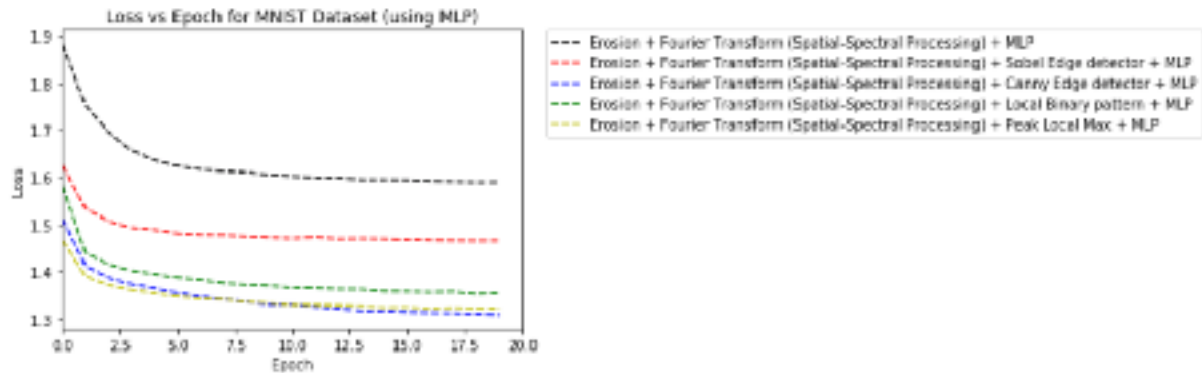


Figure 49: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Erosion followed by Fourier Transform and Feature Extraction with MLP as Classifier

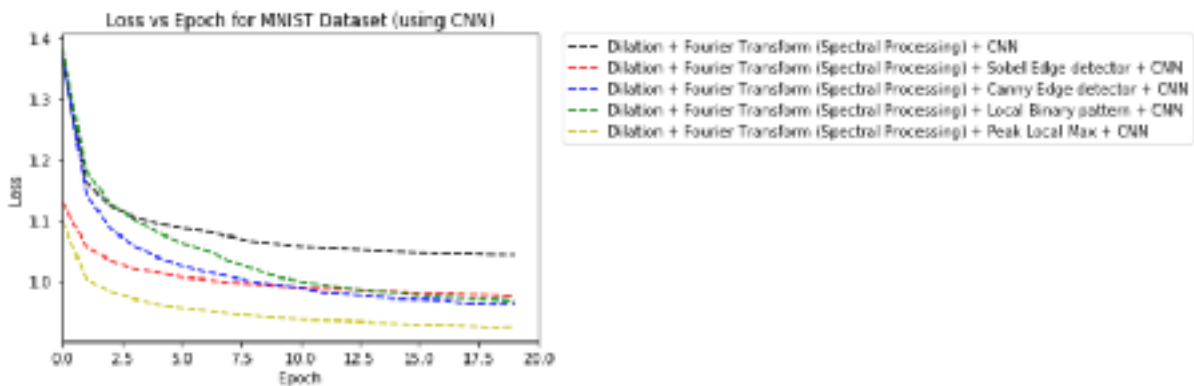


Figure 50: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Erosion followed by Fourier Transform and Feature Extraction with CNN as Classifier

Note : Forgot to change Legend values and noticed it very late to run the entire code again

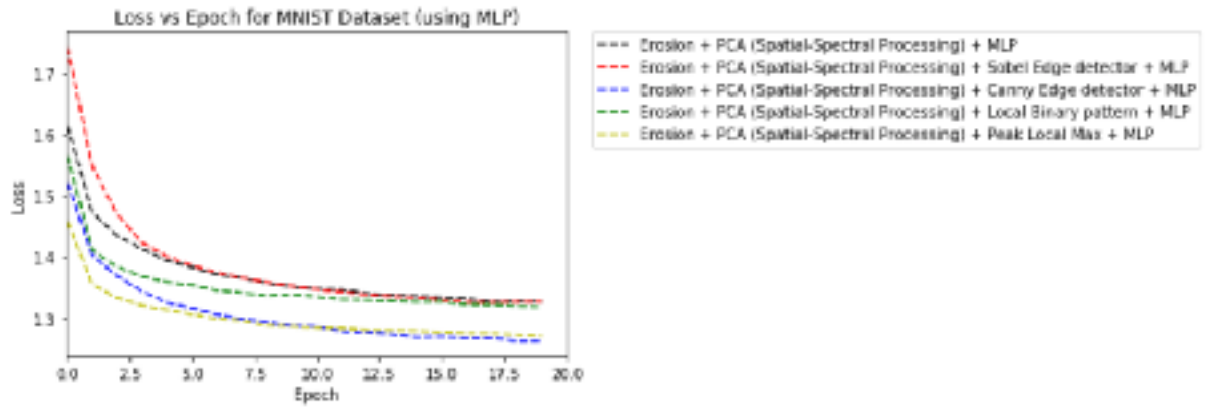


Figure 51: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Erosion followed by PCA and Feature Extraction with MLP as Classifier

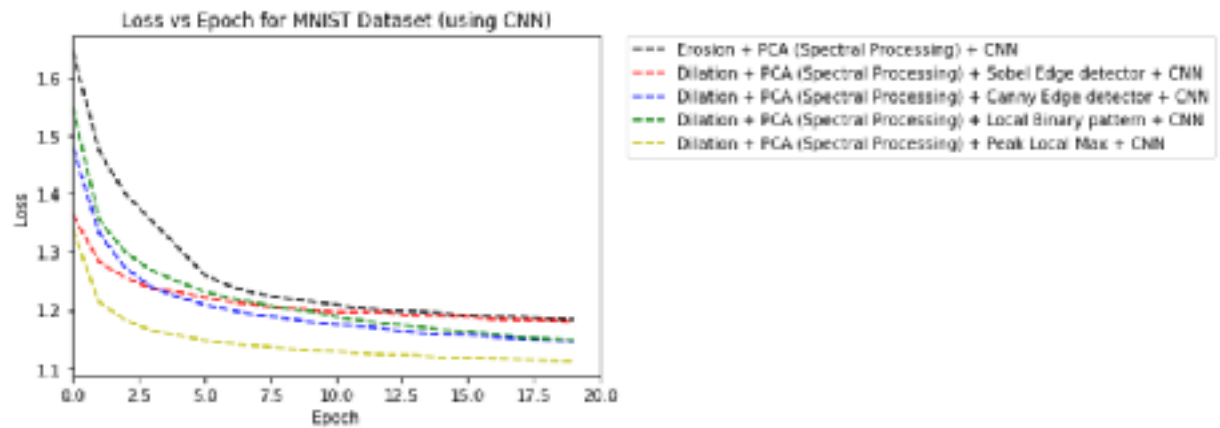


Figure 52: The Image above shows the Loss versus Epoch graph for MNIST dataset after applying Erosion followed by PCA and Feature Extraction with MLP as Classifier

Note : Forgot to change Legend values and noticed it very late to run the entire code again

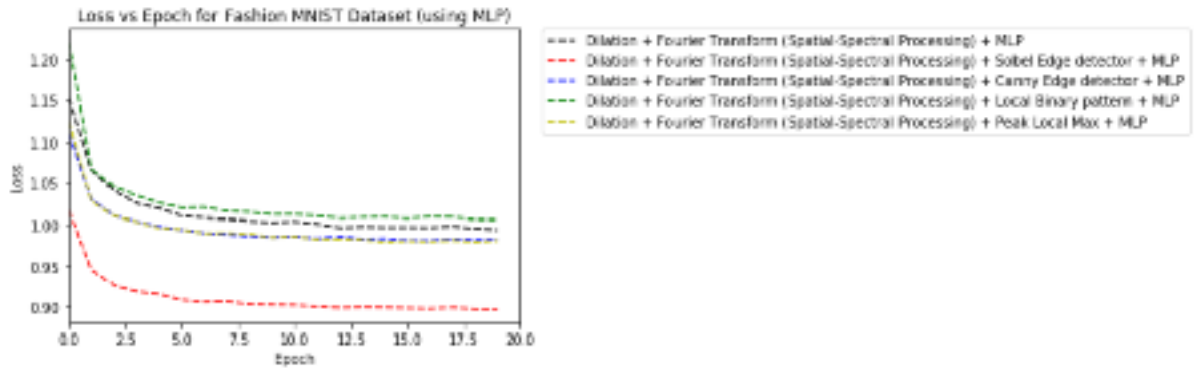


Figure 53: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Dilation followed by Fourier Transform and Feature Extraction with MLP as Classifier

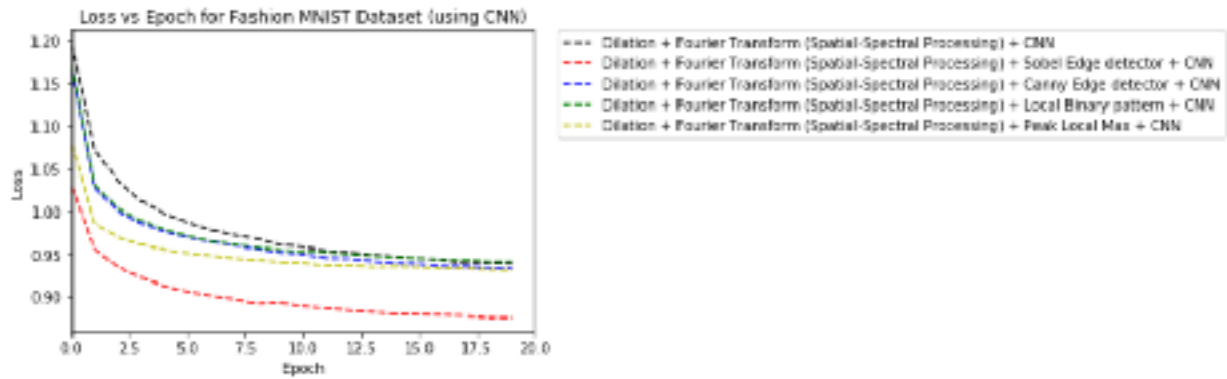


Figure 54: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Dilation followed by Fourier Transform and Feature Extraction with CNN as Classifier

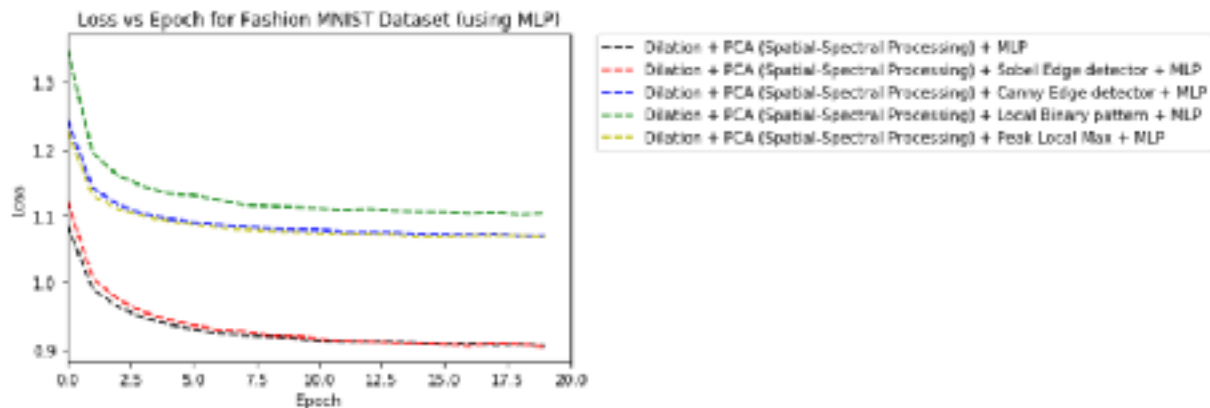


Figure 55: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Dilation followed by PCA and Feature Extraction with MLP as Classifier

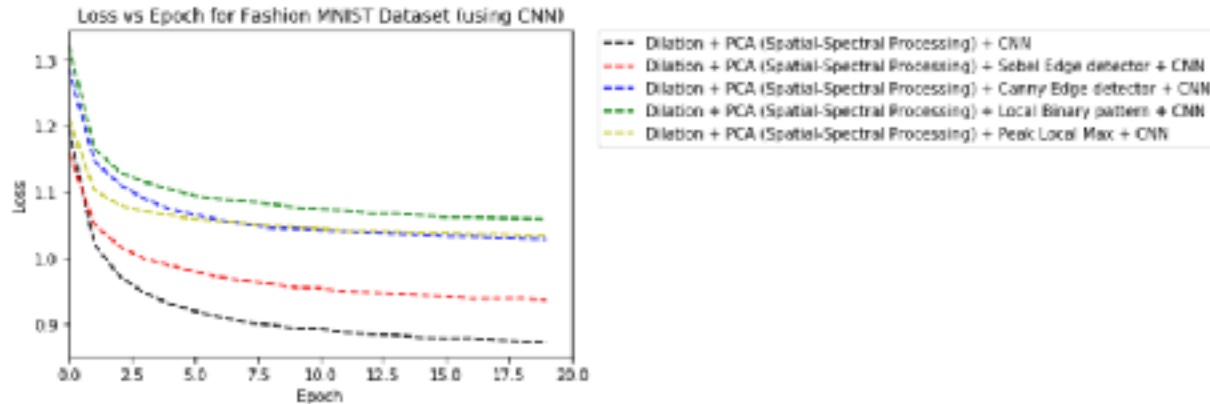


Figure 56: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Dilation followed by PCA and Feature Extraction with CNN as Classifier

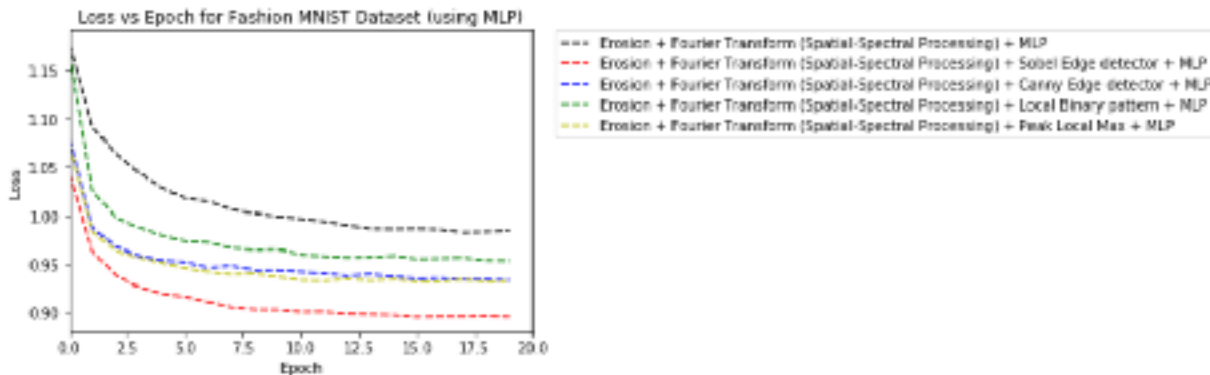


Figure 57: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Erosion followed by Fourier Transform and Feature Extraction with MLP as Classifier

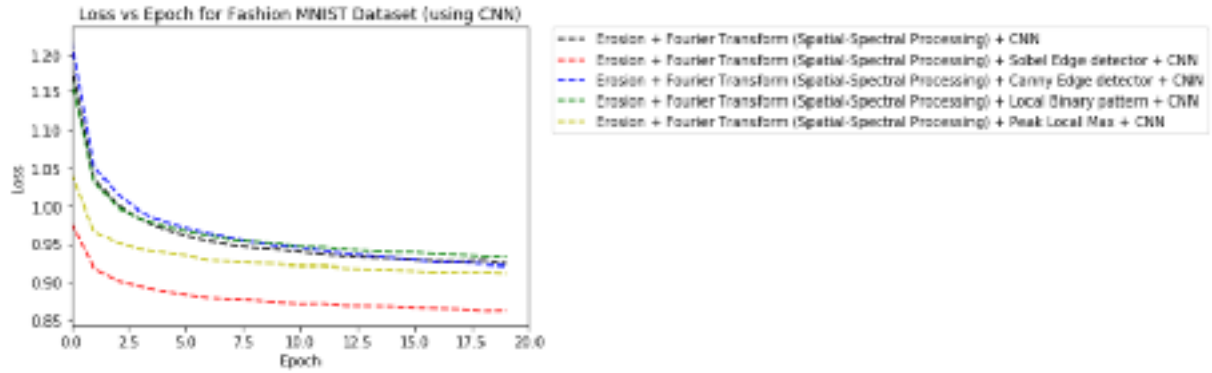


Figure 58: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Erosion followed by Fourier Transform and Feature Extraction with CNN as Classifier

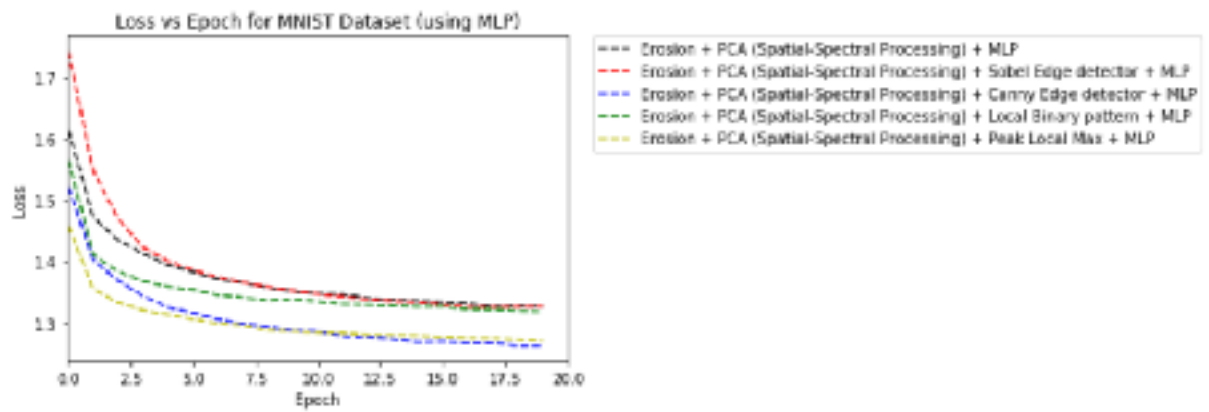


Figure 59: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Erosion followed by PCA and Feature Extraction with MLP as Classifier

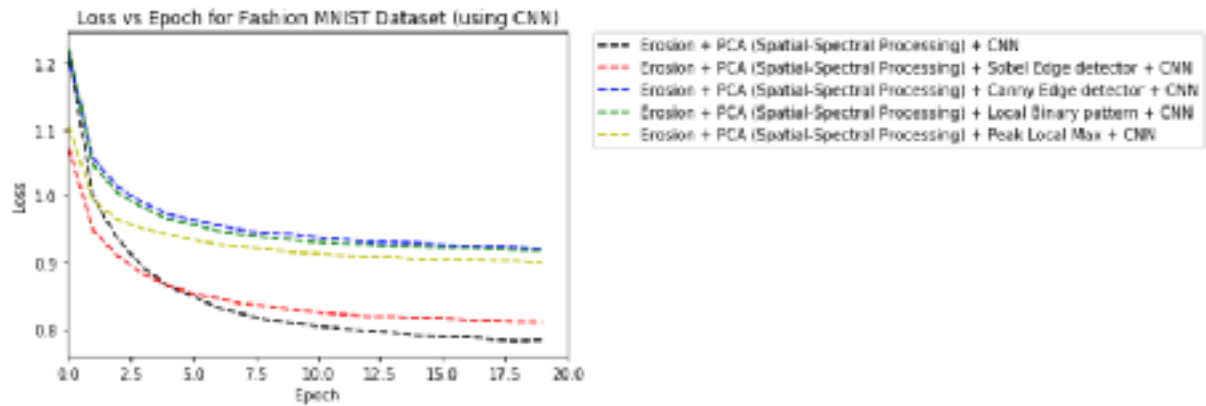


Figure 60: The Image above shows the Loss versus Epoch graph for Fashion MNIST dataset after applying Erosion followed by PCA and Feature Extraction with CNN as Classifier

	MLP	CNN
Dilation	62	64
Erosion	49	52
Fourier transform	54	59
PCA	58	58
Dilation+Fourier	57	62
Dilation+PCA	64	52
Erosion+Fourier	37	62
Erosion+PCA	51	57

Table 1 : Accuracy of MNIST data using different processing methods and no Feature Extraction Technique

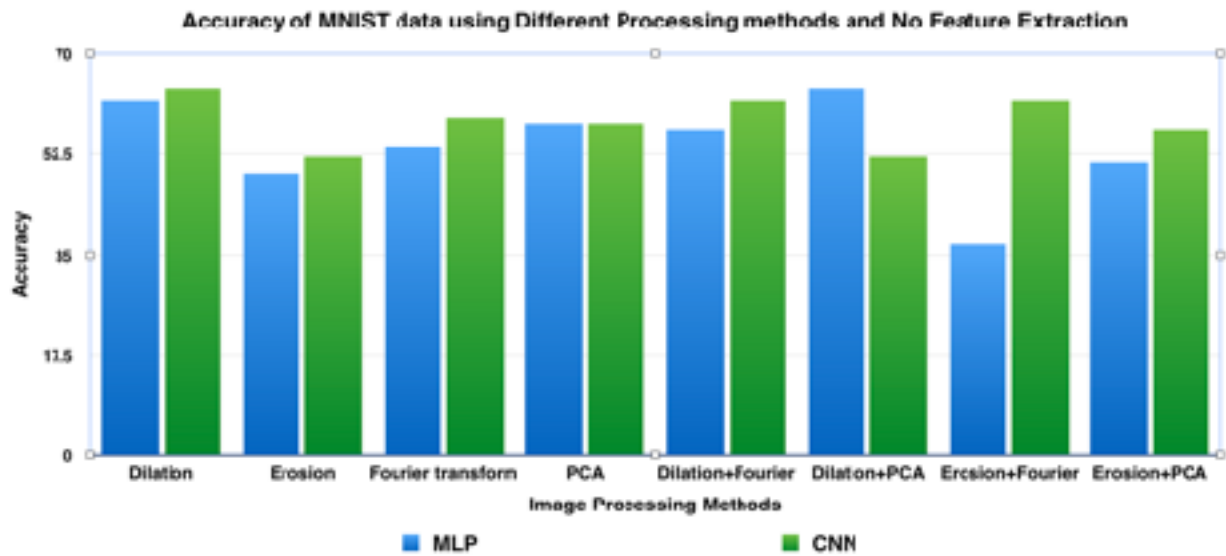


Figure 61 : Accuracy of MNIST data using different processing methods and no Feature Extraction Technique

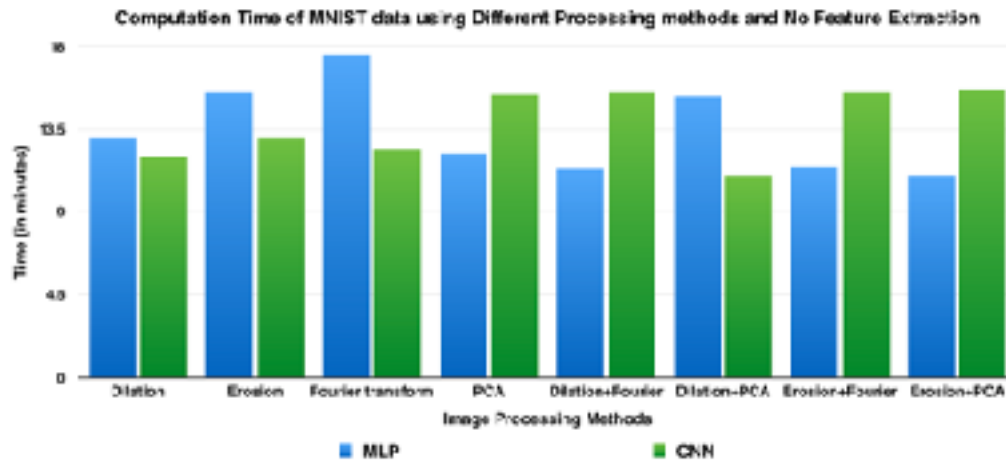


Figure 62 : Computation time of MNIST data using different processing methods and no Feature Extraction Technique

	MLP	CNN
Dilation	67	67
Erosion	60	62
Fourier transform	51	62
PCA	55	57
Dilation+Fourier	59	62
Dilation+PCA	58	58
Erosion+Fourier	44	64
Erosion+PCA	49	57

Table 2 : Accuracy of MNIST data using different processing methods and Sobel Edge Detector for Feature Extraction

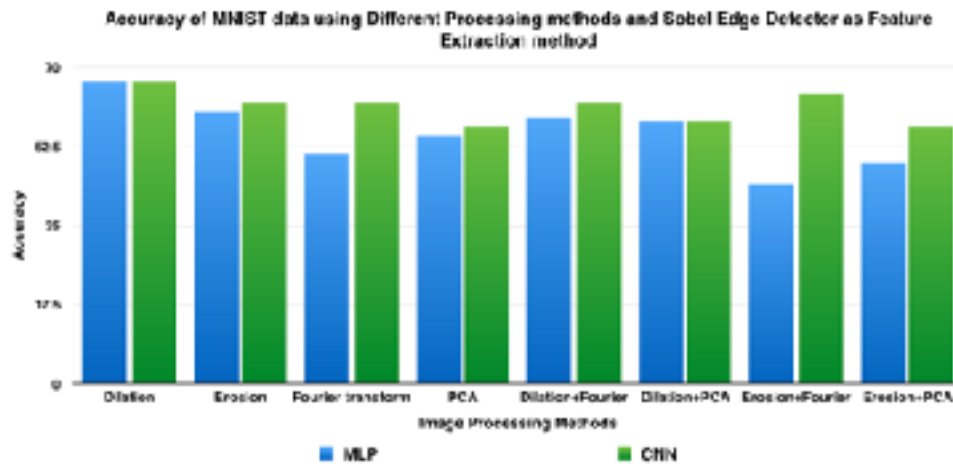


Figure 63 : Accuracy of MNIST data using different processing methods and Sobel Edge Detector for Feature Extraction

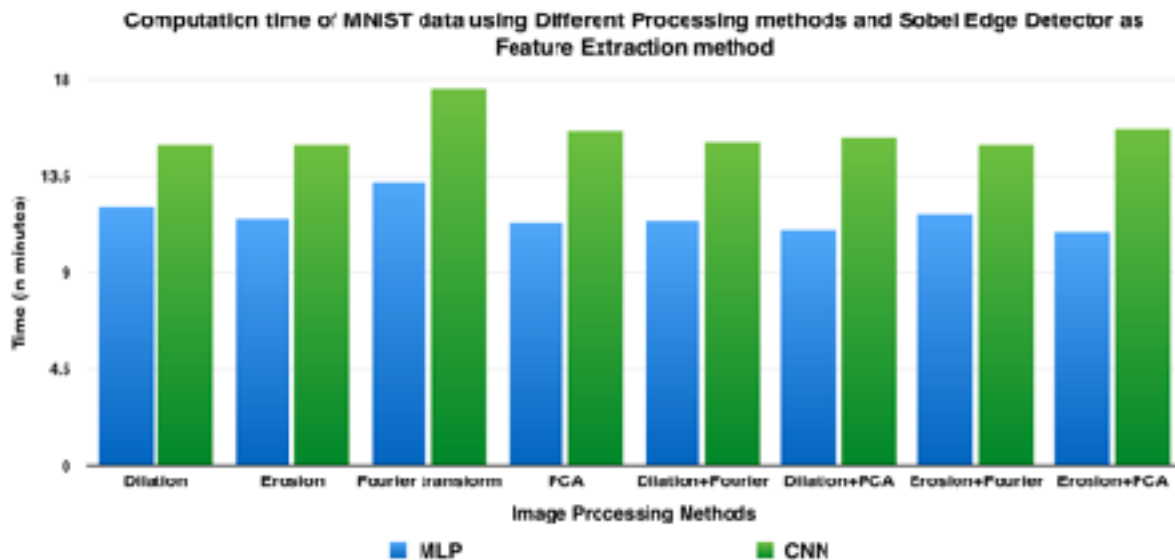


Figure 64 : Computation time of MNIST data using different processing methods and Sobel Edge Detector for Feature Extraction

	MLP	CNN
Dilation	64	65
Erosion	54	59
Fourier transform	61	63
PCA	64	64
Dilation+Fourier	62	65
Dilation+PCA	65	64
Erosion+Fourier	54	66
Erosion+PCA	68	66

Table 3 : Accuracy of MNIST data using different processing methods and Canny Edge Detector for Feature Extraction

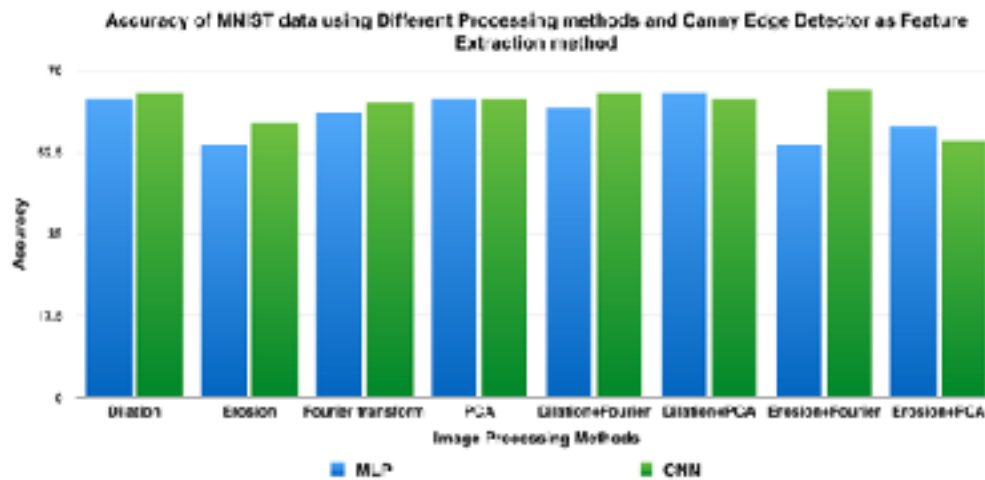


Figure 65 : Accuracy of MNIST data using different processing methods and Canny Edge Detector for Feature Extracti

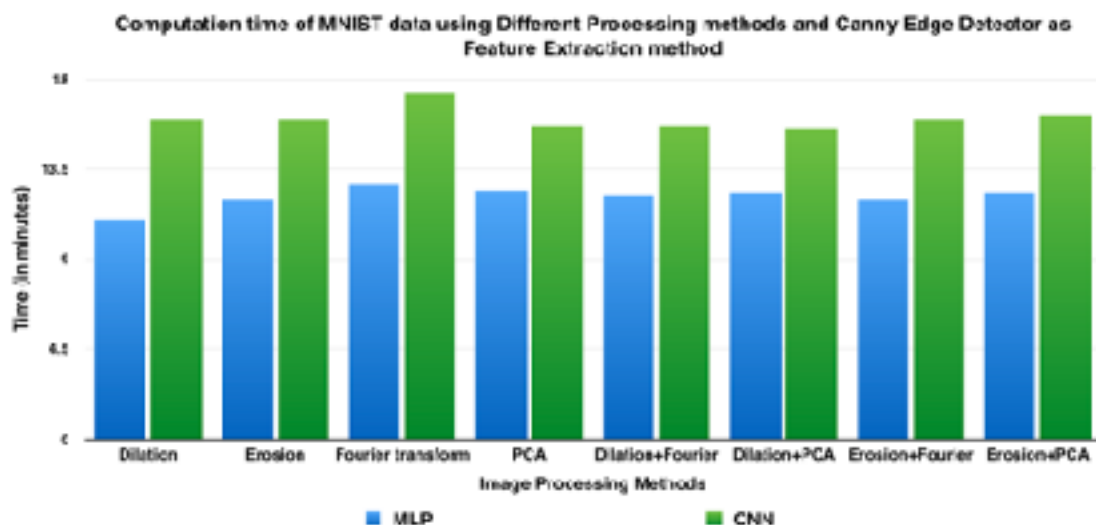


Figure 66 : Computation time of MNIST data using different processing methods and Canny Edge Detector for Feature Extraction

	MLP	CNN
Dilation	62	65
Erosion	62	58
Fourier transform	50	62
PCA	64	65
Dilation+Fourier	61	64
Dilation+PCA	65	64
Erosion+Fourier	50	65
Erosion+PCA	51	58

Table 4 : Accuracy of MNIST data using different processing methods and Local binary pattern for Feature Extraction

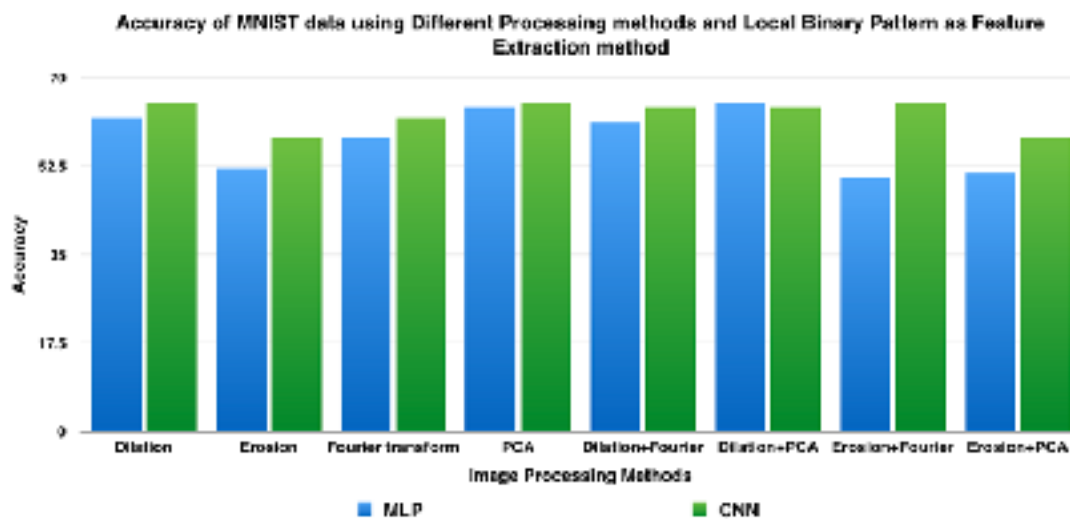


Figure 67 : Accuracy of MNIST data using different processing methods and Local binary pattern for Feature Extraction

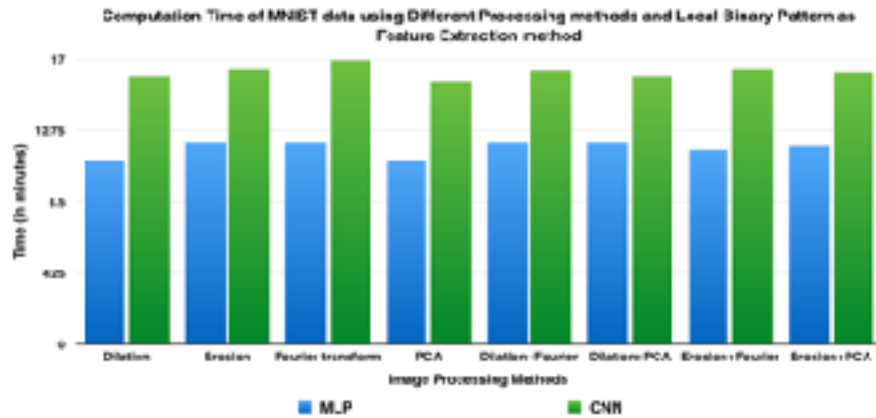


Figure 68 : Computation time of MNIST data using different processing methods and Local binary pattern for Feature Extraction

	MLP	CNN
Dilation	64	65
Erosion	54	58
Fourier transform	59	62
PCA	63	65
Dilation+Fourier	64	65
Dilation+PCA	66	65
Erosion+Fourier	53	67
Erosion+PCA	54	59

Table 5 : Accuracy of MNIST data using different processing methods and Peak Local Maxima for Feature Extraction

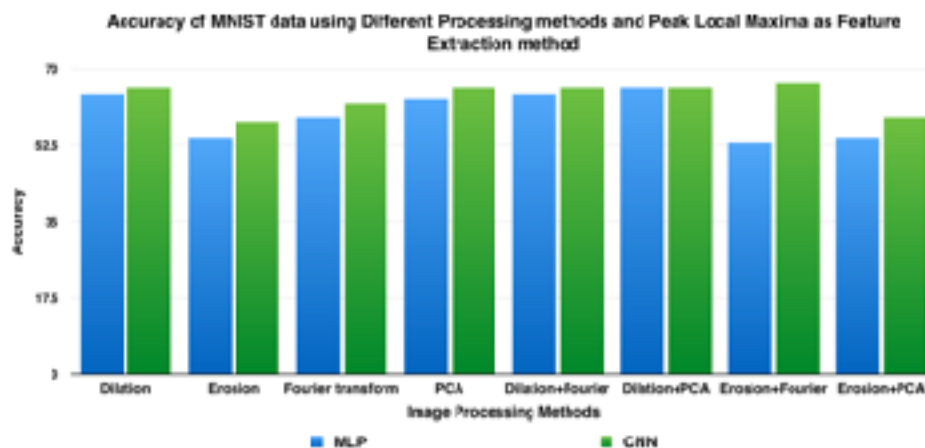


Figure 69 : Accuracy of MNIST data using different processing methods and Peak Local Maxima for Feature Extraction

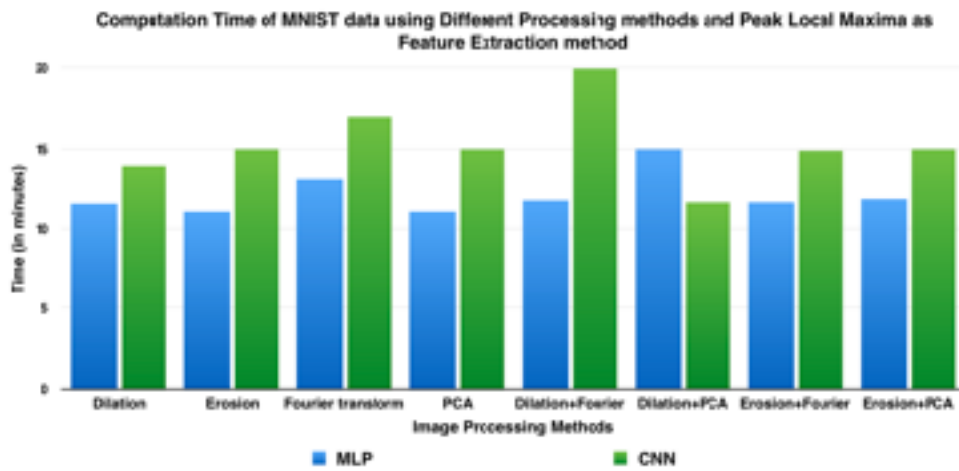


Figure 70 : Computation time of MNIST data using different processing methods and Peak Local Maxima for Feature Extraction

	MLP	CNN
Dilation	58	63
Erosion	59	62
Fourier transform	61	65
PCA	64	59
Dilation+Fourier	56	61
Dilation+PCA	60	64
Erosion+Fourier	37	62
Erosion+PCA	51	57

Table 6 : Accuracy of Fashion MNIST data using different processing methods and No Feature Extraction

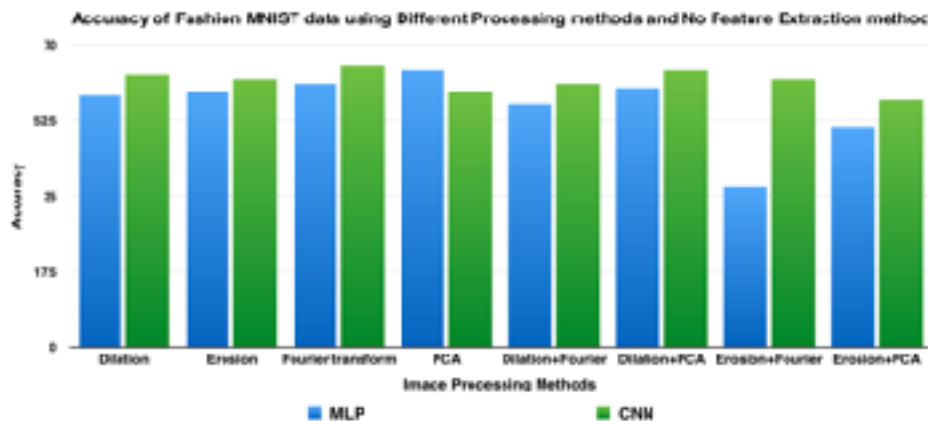


Figure 71 : Accuracy of Fashion MNIST data using different processing methods and No Feature Extraction

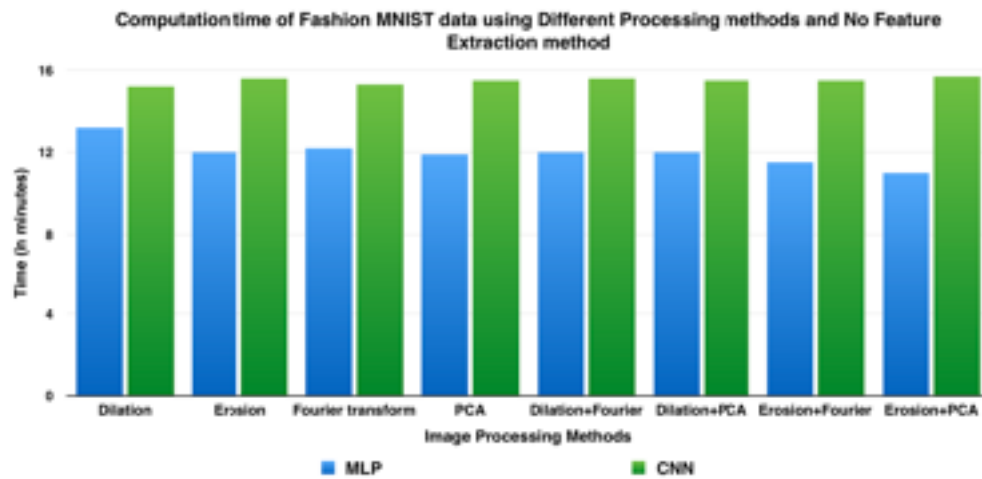


Figure 72 : Computation time of Fashion MNIST data using different processing methods and No Feature Extraction

	MLP	CNN
Dilation	64	64
Erosion	65	65
Fourier transform	64	65
PCA	62	61
Dilation+Fourier	61	62
Dilation+PCA	60	61
Erosion+Fourier	44	64
Erosion+PCA	49	57

Table 7 : Accuracy of Fashion MNIST data using different processing methods and Sobel Edge detector for Feature Extraction

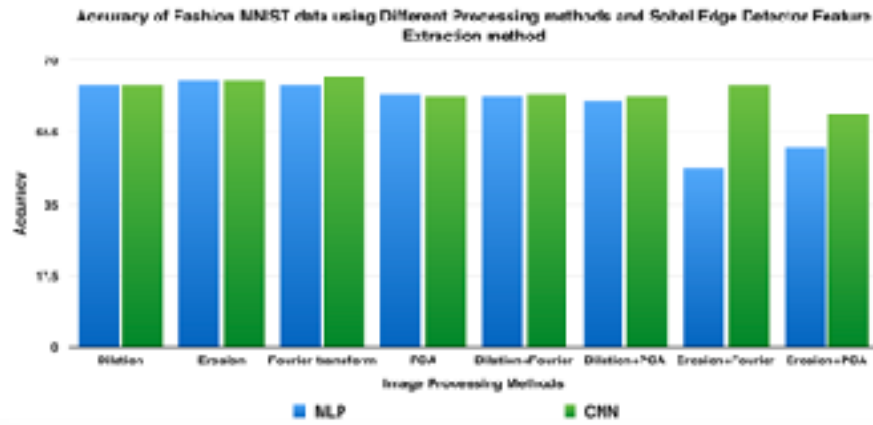


Figure 73 : Accuracy of Fashion MNIST data using different processing methods and Sobel Edge detector for Feature Extraction

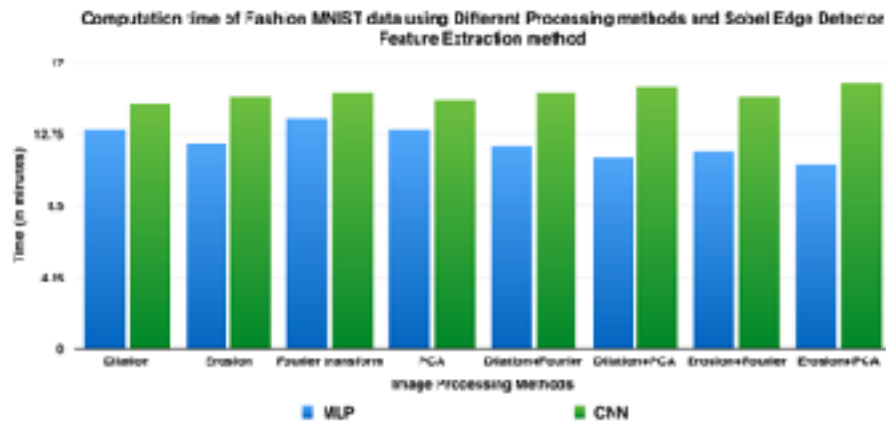


Figure 74 : Computation time of Fashion MNIST data using different processing methods and Sobel Edge detector for Feature Extraction

	MLP	CNN
Dilation	58	61
Erosion	51	52
Fourier transform	54	54
PCA	54	51
Dilation+Fourier	59	59
Dilation+PCA	55	55
Erosion+Fourier	54	56
Erosion+PCA	55	58

Table 8 : Accuracy of Fashion MNIST data using different processing methods and Canny Edge detector for Feature Extraction

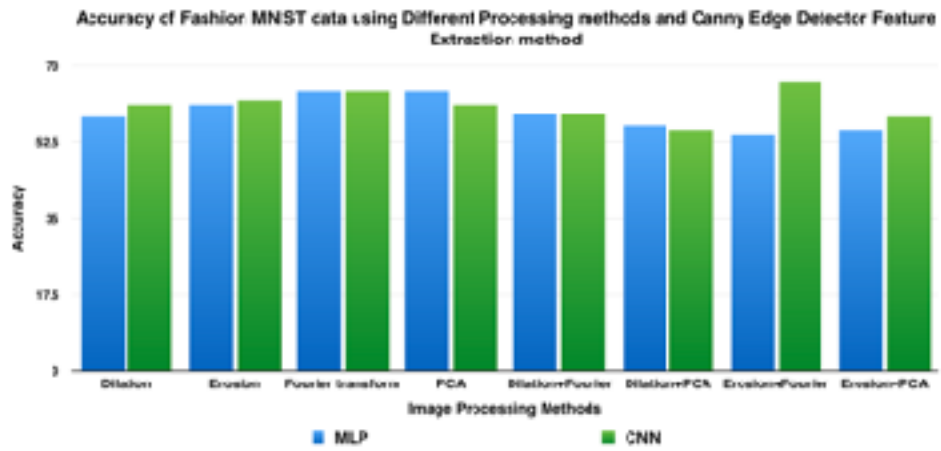


Figure 75 : Accuracy of Fashion MNIST data using different processing methods and Canny Edge detector for Feature Extraction

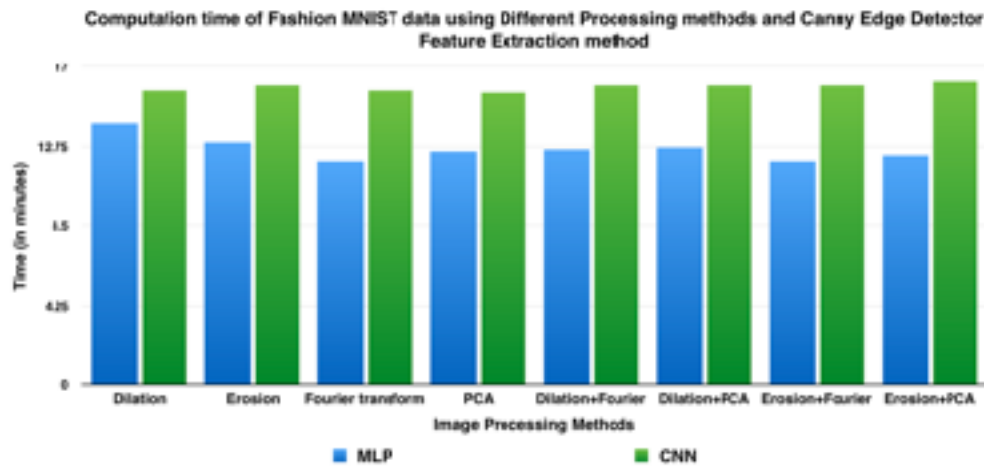


Figure 76 : Computation time of Fashion MNIST data using different processing methods and Canny Edge detector for Feature Extraction

	MLP	CNN
Dilation	58	59
Erosion	59	62
Fourier transform	63	64
PCA	62	62
Dilation+Fourier	57	60
Dilation+PCA	54	55
Erosion+Fourier	54	65
Erosion+PCA	51	58

Table 8 : Accuracy of Fashion MNIST data using different processing methods and Local Binary Pattern for Feature Extraction

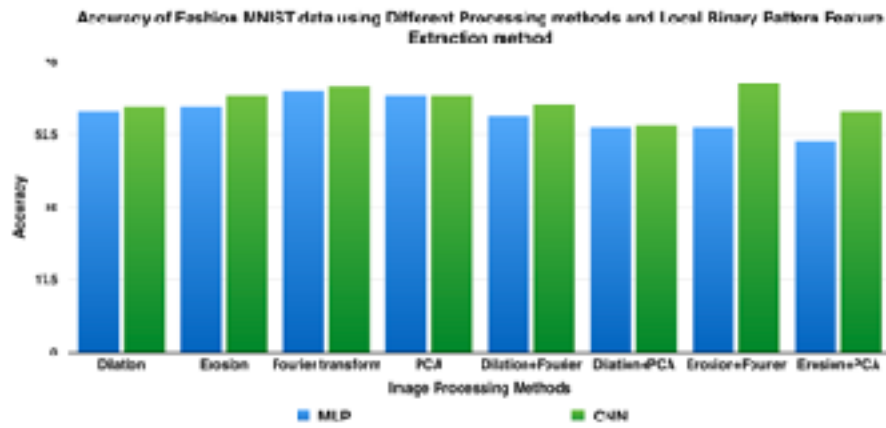


Figure 77 : Accuracy of Fashion MNIST data using different processing methods and Local Binary Pattern for Feature Extraction

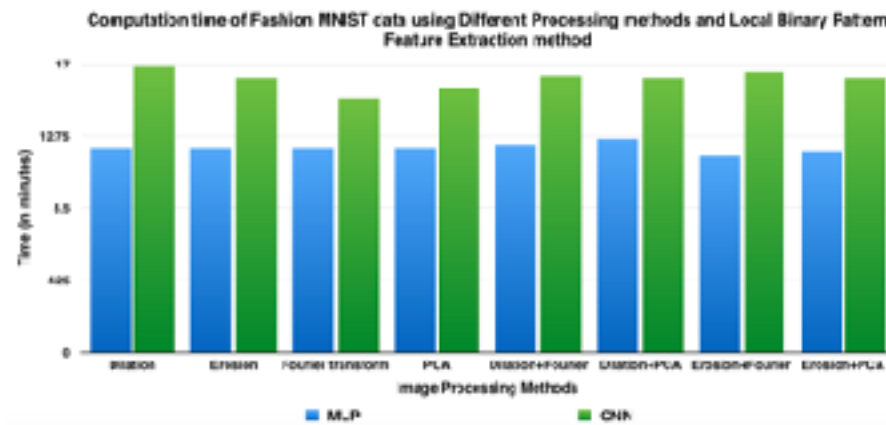


Figure 78 : Computation time of Fashion MNIST data using different processing methods and Local Binary Pattern for Feature Extraction

	MLP	CNN
Dilation	59	59
Erosion	61	61
Fourier transform	65	65
PCA	65	63
Dilation+Fourier	59	60
Dilation+PCA	54	56
Erosion+Fourier	60	61
Erosion+PCA	61	61

Table 10 : Accuracy of Fashion MNIST data using different processing methods and Peak Local Maxima for Feature Extraction

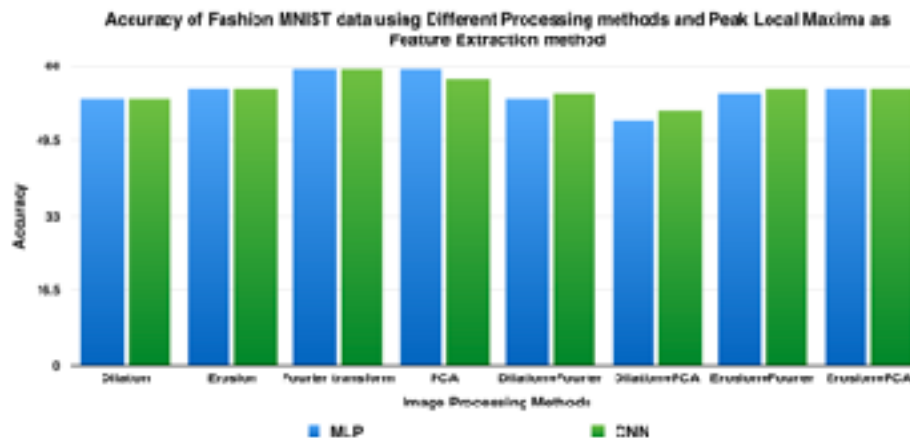


Figure 79 : Accuracy of Fashion MNIST data using different processing methods and Peak Local Maxima for Feature Extraction

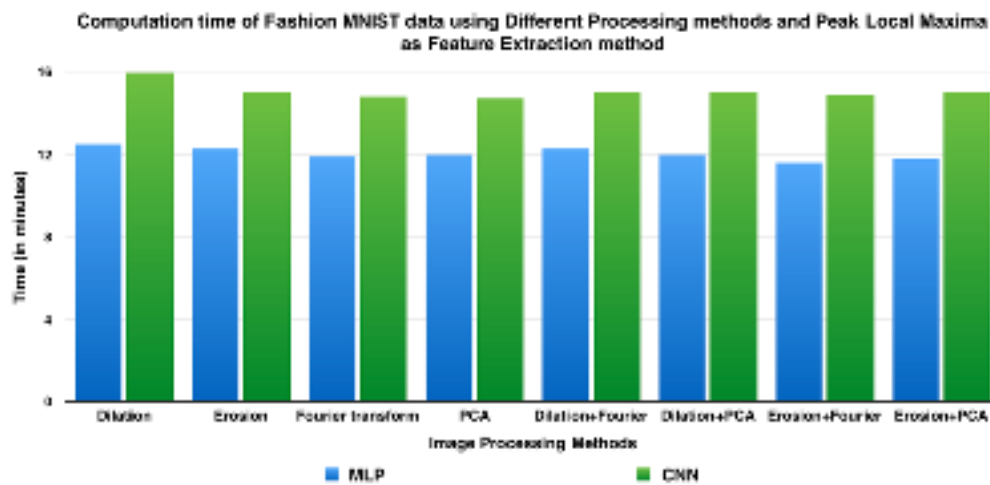


Figure 80 : Computation time of Fashion MNIST data using different processing methods and Peak Local Maxima for Feature Extraction

CONCLUSION

From the above results, it can be observed that Classification using that the Accuracy of the dataset is not very good after processing it, but the Computation time was found to be decreased.

After processing of the dataset, Sobel edge detection feature extraction method performed better overall in comparison to other methods.

It can also be observed, that even though some datasets look similar after applying Feature Extraction method, they have different accuracies.

Overall, MNIST and Fashion MNIST dataset do not require any kind of processing but they can be classified using an appropriate Feature Extraction technique as shown in my previous project, as they had better results.

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