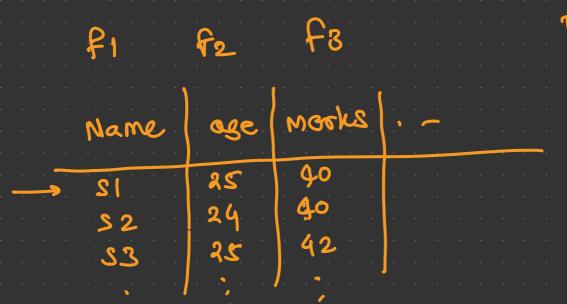
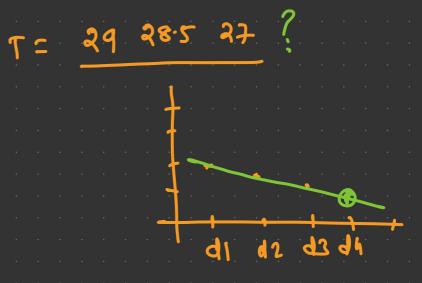


Measures of Correlation





$$\frac{\alpha l}{y}$$
 $\frac{y}{y} = \frac{x^2}{x^2}$
between $\frac{x}{k}$
 $\frac{y}{y} = \frac{x^2}{y}$
 $\frac{y}{y} = \frac{x^2}{y}$
 $\frac{y}{y} = \frac{x^2}{y}$
 $\frac{y}{y} = \frac{x}{y}$
 $\frac{y}{y} = \frac{x}{y}$

Terminologies



Univariate

- This type of data consists of only one variable
- It does not deal with causes or relationships
- the main purpose of the analysis is to describe the data and find patterns that exist within it
- Bivariate -> two variables in the dataset
 - This type of data involves two different variables
 - The analysis of this type of data deals with causes and relationships
 - the analysis is done to find out the relationship among the two variables

pood al	(formula)
model	(LD. C. A.) Com

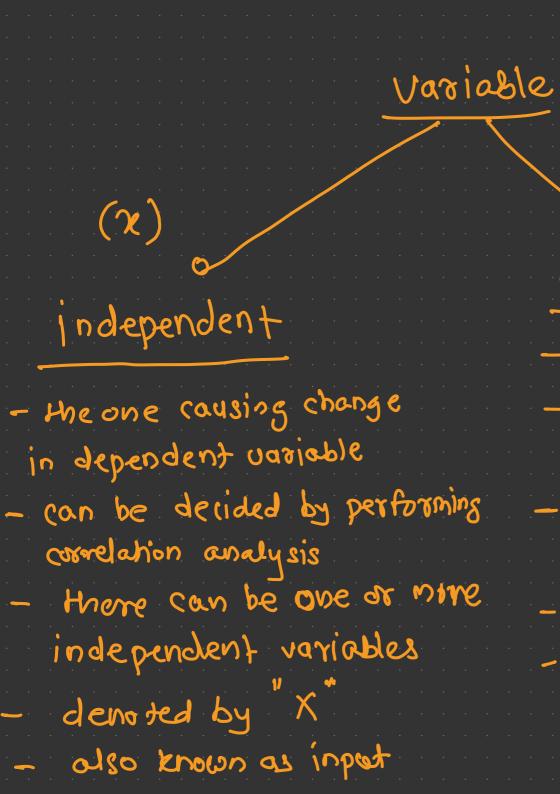
K I	22
KAP	Edory
1.1	50 k
1.2	ssk
1.8	65k
3,0	1 80 k
•	لند

one variable is coursing thange in other ver.

Multivariate

- When the data involves three or more variables
- It is similar to bivariate but contains more than one

		X.	(2)	(3)	1
city	agguss	phone	size	# TUDMS	byce
ableure		98	500	7	1.504
7	boot club	34	700	2	857
puse		70	800	3	30L
pure	wokad	10	:	:	
		•	\		



model= y=fn) (4) dependent - the one under study the requirement decides the dependent variable there can be one and only one dependent var in a dataset denoted by y" also known as output

Introduction



- In practice, we come across a large number of problems involving the use of two or more number of variables multivatione data
- If two quantities vary in such a way that, movements in one are accompanied by movements in the other, these quantities are correlated
- E.g. price of commodity and its demand, experience of an employee and his salary etc.
- The degree of relationship is measured between the variables under consideration is measured through the correlation analysis
 → ようしはy q re)のけっつらりなり。

covariance

carrel ation

- The problem of analyzing relationship between variables can be divided into following steps
 - Determine if the relationship exists between the variables
 - If it exists, then measure it using measure of correlation
 - Testing whether it is significant -> strong selationship
 - Establish the cause and effect relation if any

Significance of study of correlation



- Most of the variables show some kind of relationship. With the help of correlation analysis, we can measure its degree of relationship in one figure
 - E.g. relationship between price and supply
- Once we know that two variables are closely related, we can estimate the value of one variable given the value of another

 \[
 \text{value of another}
 \]

 \[
 \text{value of another}
 \]
- Correlation analysis contributes to the understanding of economic behavior, aid in locating the critically important variables on which other depends whether there is any releasing the
- In business, the correlation analysis enables the execution to estimate costs, sales, prices and other variables on the basis of some other series with which these my be functionally related

Correlation and Causation





- Correlation analysis helps us in determining the degree of relationship between two or more variables
- It does not tell us anything about the cause and effect relationship
- Even a high degree of correlation does not necessarily mean that the relationship of cause and effect exists between the variables
- The explanation of significant degree of correlation may be one or both of the following
 - The correlation may be due to pure chance, especially in a small sample
 - Both the correlated variables may be influenced by one or more other variables
 - Both the correlated variables are mutually influencing each other



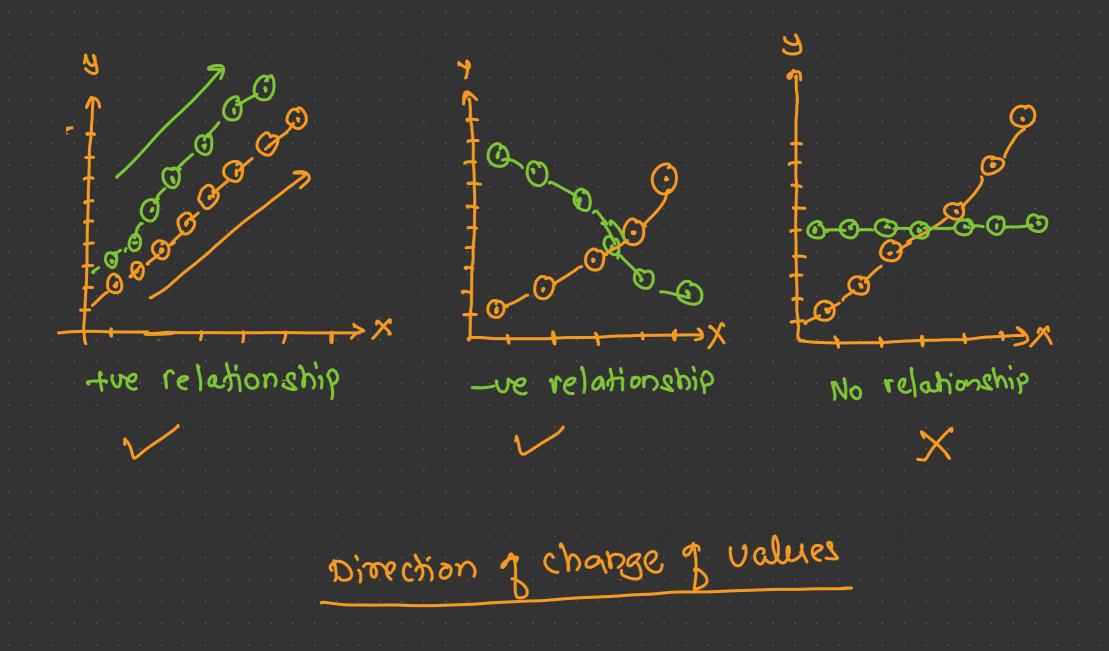
Types of Correlation

Positive and Negative Correlation



- Whether the correlation is positive or negative would depend upon the direction of the change of the variables
- If both he variables are varying in the same direction i.e., if as one variable is increasing and the other one is also increasing or vice-a-versa, is said to be positive correlation
- On the other hand, if the variables are varying in opposite directions, the correlation is said to be negative correlation

■ E.g.								
Positive	X	10	12	15	18	20	24	30
- Positive	Y	15	20	25	30	35	40	45
- Nagativa	Х	10	12	15	18	20	24	30
Negative	Υ	45	40	35	30	25	20	15



Simple, Partial and Multiple Correlation



- The distinction between simple, partial and multiple correlation is based upon the number of variables under study
- When only two variables are studied, it is a problem of simple correction to the independent
- When three or more variable are studied, it is a problem of either multiple or partial correlation
- In multiple correlation, three or more are studied simultaneously
 - E.g. studying relationship between yield of rice per acre and amount of rainfall and amount of fertilizers used
- On the other hand, in partial correlation, we recognize more than two variables, but consider only two
 variables keeping other constant

Linear and Non-Linear Correlation

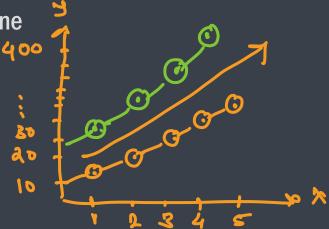


 The distinction between line and non-linear correlation is based upon the constancy of the ratio of change between the variables

Linear Correlation

- If the change in one variable tends to bear constant ratio to the amount of change in the other variable, then the correlation is said to be linear
- If the variables are plotted on graph, all potted points would fall on a straight line

X	10	20	30	40	50
Υ	70	140	210	280	350



Non-Linear Correlation

Correlation is called as non-linear of curvilinear if the amount of change in one variable does not bear a constant ratio
to the amount of change in other

If the variables are plotted on graph, the points will never fall on a straight line

X	10	20	30	40	50
Υ	10	40	80	30	49 500

7=0.41





Methods of Studying Correlation

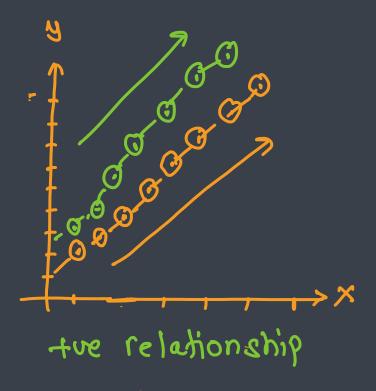
graphical Mon-graphical

Scatter plot correlation Covariance

Scatter Diagram -> chart with dots



- The simplest way of asserting whether two variables are related or not is to prepare a dot chart called as scatter diagram
- When this method is used, the dataset is plotted on the graph (for every value we simply put a dot)
- By looking at the scatter of the of the various points, we can form an idea as to whether the variables are related or not



Merit and Limitations of Scatter Method



Merits

- It is a simple and non-mathematical method of studying the correlation between the variables
- It can be easily understood and a rough idea can very quickly can be formed about the relationship
- It is not influenced by the size of extreme items whereas most mathematical methods are influenced by them
- Making a scatter diagram is usually the first step in investigating the relationship
- If he variables are related, we can see what kind of line or estimating equation describes the relationship

Limitations

 By applying this method, we can get an idea about the direction of correlation, but we can not establish the exact degree of correlation between two variables

Graphic Method



- When this method is used, the individual values of the two variables are plotted on the graph paper
- We thus obtain two curves, one for X variable and another for Y variable
- By examining the direction and closeness of the two curves so drawn, we can infer whether or not the variables are related
- If both the curves drawn on the graph are moving in the same direction (either upward or downward), correlation is said to be positive
- On the other hand, if the curves are moving in the opposite directions, correlation is said to be negative

Covariance -> does not have any scale



- A measure of the relationship between two random variables
- The metric evaluates how much to what extent the variables change together
- A positive covariance would indicate a positive linear relationship between the variables
- A negative covariance would indicate the opposite

$$cov(x,y) = \frac{\sum (x - \bar{x})(y - \bar{y})}{N}$$

- Where
 - X_i the values of the X-variable
 - Y_i the values of the Y-variable
 - \overline{x} the mean (average) of the X-variable
 - \overline{y} the mean (average) of the Y-variable
 - n the number of the data points in sample
 - N the number of the data points in Population

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84 40 5.58 10 85.8 $(ov(x,y) = 63.57)$	3 6	35	1.28	5 1 5 1 1		· · · · · · · · · · · · · · · · · · ·
	2 6	40	5.58	0.010	8.28	63.57
30 33	30	45	11.58) 5	1737	

$$\frac{7}{20} = 18.42 \quad \frac{7}{9} = 30$$

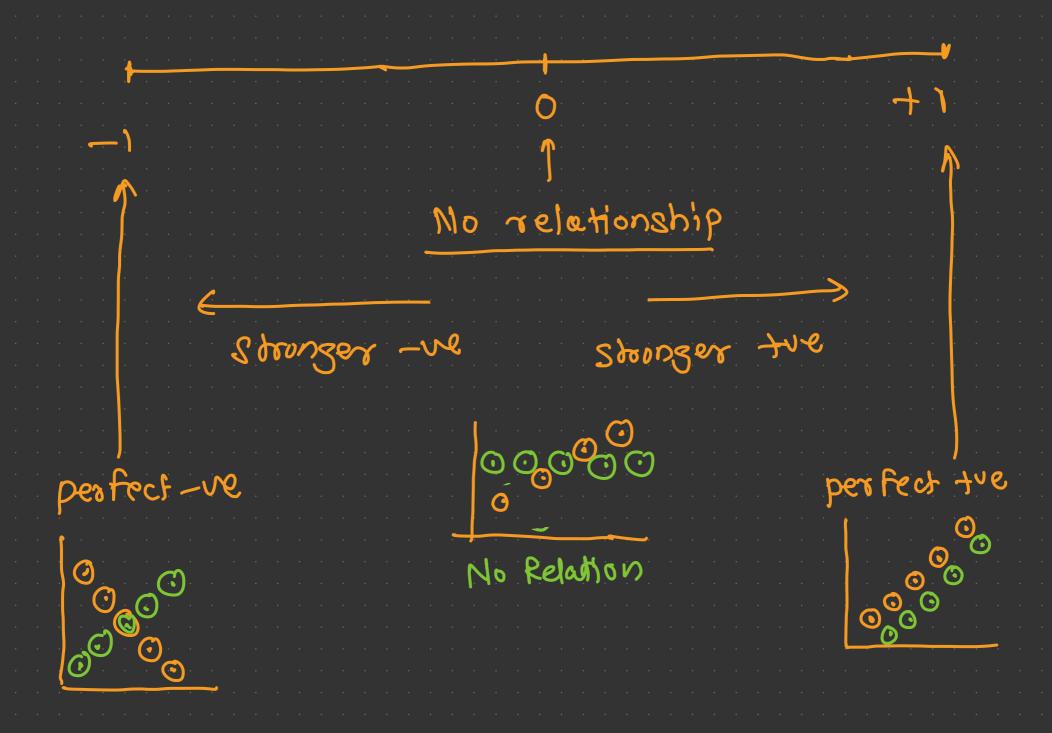
445

O if (ov is the then relationship is the

@ if cov is -ve, relation is -ve

1 if cou = 6, No relationship

X	y	(2-元)	(4-4)	(2-2) (4-9)	(ルが)2	(4-3)2
12 15 18 20 24	15 20 25 30 35 40 5	-8.42 -6.42 -3.42 -0.42 1.58 5.58	-15 -10 -5 0	126.3 64.2 17.1 0 7.9 85.8	76.89 41.21 11.69 0:17 2.49 31.13 134.09	225 100 25 100 25
	18.42	2 (2-4) ²	1291.6 7 7	<u>445</u> 7 = 6.45	~ ~ ~ ~	700 (2-2) (4-9) (6,62 (45) (6,45) (6,45) (45) (45)



$$(ov(x,y) = (ov(y,x))$$
 $(ov(x,y) = (ov(y,x))$

Karl Pearson Coefficient of Correlation



- Of the several mathematical methods of measuring correlation, the Karl Pearson's method popularly known as Pearson's coefficient of correlation, is most widely used in practice
- It is denoted as r



$$r = \frac{\sum (x - \bar{x})(y - \bar{y})}{N\sigma_1\sigma_2}$$

(orrelation



$$r = \frac{\sum (x - \bar{x})(y - \bar{y})}{N\sqrt{\sum (x - \bar{x})^2 \sum (y - \bar{y})^2}}$$

Direct Method of finding Correlation Coefficient



 Correlation Coefficient can be calculated without taking deviations of the items either from the actual mean or assumed mean



$$r = \frac{N \sum XY - \sum X \sum Y}{\sqrt{N \sum X^2 - (\sum X)^2} \sqrt{N \sum Y^2 - (\sum Y)^2}}$$

Assumptions of Pearsonian Coefficient



- There is a linear relationship between the variables, i.e., when the two variables are plotted on a scatter diagram, a straight line will be formed by the points so plotted
- The two variables under study are affected by a large number of independent causes so as to form a normal distribution. Variables like height, weight, price, demand, supply, etc, are affected by such forces that a normal distribution is formed
- There is a cause and effect relationship between the forces affecting the distribution of the items in the two series
- If such a relationship is not formed between the variables, i.e, if the variables are independent, there cannot be any correlation
 - For example, there is no relationship between income and height because the forces that affect these variables are not common

Merits and Limitations of Pearsonian Coefficient



Merits

- Amongst the mathematical methods used for measuring the degree of relationship, Karl Pearson's method is the most popular one
- The correlation coefficient summarizes in one figure not only the degree of correlation but also the direction, i.e.,
 whether correlation is positive or negative

Limitations

- The correlation coefficient always assumes linear relationship regardless of the fact whether that assumption is correct or not
- Great care must be exercised in interpreting the value of this coefficient as very often the coefficient is misinterpreted
- The value of the coefficient is unduly affected by the extreme items
- As compared with other methods, this method takes more time to compute the value of correlation coefficient

Interpreting Coefficient of Correlation



- The coefficient of correlation measures the degree of relationship between two sets of figures
- As the reliability of estimates depends upon the closeness of the relationship, it is imperative that utmost care must be taken while interpreting the value of coefficient of correlation, otherwise, fallacious conclusions can be drawn
- following general rules are given which would help in interpreting the value of r
 - When r = +1, it means that there is perfect positive relationship between the variables
 - When r =-1, it means that there is perfect negative relationship between the variables
 - When r = 0, it means that there is no relationship between the variables, i.e., the variables are uncorrelated.
- The closer r is to +1 or -1, the closer the relationship between the variables and the closer r is to 0, the less close the relationship

Properties of Correlation Coefficient



- The coefficient of correlation lies between -1 and +1, symbolically -1 <= r <= +1
- The coefficient of correlation is independent of the change of scale and origin of the variables
- It is the geometric mean of two regression coefficient
- The degree of relationship between two variables is symmetric

$$r_{xy} = r_{yx}$$

$$(on(x_1) = (orr(y_1))$$