
Indoor localization using Local Positioning Systems.

MSc.

By

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ABSTRACT

Here goes the abstract

DEDICATION AND ACKNOWLEDGEMENTS

Here goes the dedication.

AUTHOR'S DECLARATION

I declare that the work in this dissertation was carried out in accordance with the requirements of the University's Regulations and Code of Practice for Research Degree Programmes and that it has not been submitted for any other academic award. Except where indicated by specific reference in the text, the work is the candidate's own work. Work done in collaboration with, or with the assistance of, others, is indicated as such. Any views expressed in the dissertation are those of the author.

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NOMENCLATURE

- UAV - Unmanned Aerial Vehicle.
- GPS - Global Positioning System.
- LPS - Local Positioning System.
- FCU - Flight Controller Unit.
- UWB - Ultra-WideBand.
- TOF - Time of Flight.
- PSoC - Programmable System on Chip.
- NLOS - No Line of Sight.
- TWR - Two Way Ranging.
- I2C- Inter-Integrated Circuit Bus.
- SPI - Serial Peripheral Interface.

TABLE OF CONTENTS

	Page
List of Tables	ix
List of Figures	xi
1 Introduction	1
1.1 Aims & Objectives	4
1.2 Background Research	5
2 Literature Review	7
2.1 Indoor Localisation Systems	7
2.1.1 Passive Systems	7
2.1.2 Active Systems	8
2.2 Pozyx - Behind the Scenes	9
2.2.1 Ultra-WideBand (UWB)	9
2.2.2 Pozyx Localisation	10
2.2.3 Pozyx - Arduino Implementation	12
2.2.4 Summary	12
3 Research Methodology	13
3.1 Anchor Configurations	13
A Appendix A	19
Bibliography	23

LIST OF TABLES

TABLE	Page
3.1 Statistics of the data recorded for each configuration.	16

LIST OF FIGURES

FIGURE	Page
1.1 The typical setup for an autonomous UAV.	2
2.1 VISON setup for position of a UAV. (https://aerial-robotics-iitk.gitbook.io/wiki/estimation/setup-with-vicon)	8
2.2 Setup used to compare UWB and BLE performance in a museum.	9
2.3 Simplified Block Diagram of the Pozyx tag.	9
2.4 The experimental setups for both a dog and a student.	11
2.5 Data collected from a student walking in a circle.	11
3.1 Birds eye view of the test environment.	14
3.2 Sample plots of several anchor configurations.	17
A.1 Packet transfer in TWR.	19
A.2 4 Anchor and 1 Tag trilateration in 2D.	20

INTRODUCTION

In recent years Unmanned aerial vehicle(UAV) usages has grown exponentially becoming common in industry and households Custers (2016). A major part of UAV applications is their ability to localise themselves in the given environment with acceptable precision and accuracy. This is a common requirement in any robotic system but UAV's are often limited by strict payload requirements and therefore have to rely on sensors that are lightweight and robust. (Mendoza-Mendoza et al. 2020) gives a good summary of physical components that are used in various vehicles but a UAV system, specifically, a quadrotor system cab be summarised as follows:

- Rotor build - This section contains parts that should be researched based on the size and physical requirements of the drone. These include: brushless motors, electronic speed controllers, frame size.
- Flight controller unit(FCU) - This acts as the mother board and brain of the quadrotor system. It collates data from various sensors, sends commands to the motors and if there is a companion computer is attached collects and sends data to it. Commercial FCU's contain the various control systems and laws required for stable flight and movement. Most have an array of sensors built in.
- Sensors - These vary from from inertial, positioning, barometric and camera. Aside from inertial and barometric sensors that are present in most FCU's, sensors are chosen based on the environment and use case of the system.
- Companion computer - In some cases higher level processing is required by the system to execute autonomy and a secondary computer is used to do this.

- Transmitter and Receiver - This is used to implement manual control over the drone by a user.

Further delving into the sensors, we can classify UAV's based on their operating environment, indoors or outdoors. These give rise to two forms of localisation and navigation systems:

- Global Positioning Systems (GPS) - As the name suggests this setup uses GPS as well as other sensors.
- GPS-denied - These systems do not have access to GPS due to their operating environment.

In outdoor applications GPS provides a reliable and fairly accurate way to localise with use of several other sensors. However, indoor applications are denied the benefits of GPS and often must use other sensors for the task of localisation. Utilizing a similar concept of triangulation used by GPS a local positioning system(LPS) can be used for indoor environments. (Pozyx Labs 2018) has developed a commercial system that utilizes Ultra-WideBand technology(UWB) with a bandwidth of $\approx 500MHz$.

With indoor environments users have more control of the environment so a LPS can create a feasible solution for indoor localisation for UAV's/robots operating there. The core idea of this research would be to integrate a commercial LPS directly into an existing FCU to produce accurate position estimates that can be used for autonomy. The measurements from the LPS would then be transformed into observations of the state of the UAV and fused with other observations from other sensors. This fused pose estimate would then be fed into the companion computer for off-board processing.

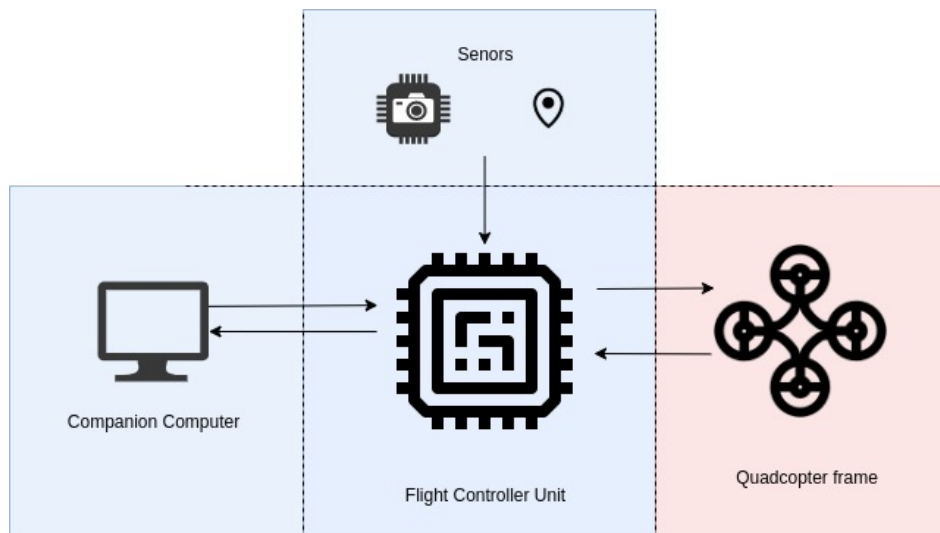


Figure 1.1: The typical setup for an autonomous UAV.

Figure: 1.1 shows a typical setup for UAV. Parts of the system highlighted in blue represent systems that would be worked on during the course of this research. The idea is that the system

being designed should provide localisation data which should be independent of the rotor build. These will be further scoped in the upcoming sections but it will involve doing a quality exercise of the LPS to determine measurement uncertainty and limitations, writing additions or modifying the firmware of the FCU to integrate the LPS and setting up the pipelines for a companion computer to receive the pose estimates and use them.

1.1 Aims & Objectives

In 1 we briefly touched on what would be addressed over the course of this research. Expanding on that, the research would entail the use of the commercial version of an UWB sensor for positioning from Pozyx Labs (2018). At a high level the project and be split into three modules that must be researched, unit tested and finally integrated. Figure 1.1 highlights the major systems within the project and are as follows:

- The Pozyx LPS providing measurements that will be used in localisation.
- A flight controller collating fusing various observations from sensors to provide a pose estimate.
- A companion computer to visualise and utilise the pose information in a meaningful manner.

From these systems and the overall aim of indoor localisation the following objectives were created:

- Evaluation and qualitative analysis of the LPS, documentation limitations from previous done work and current physical setups as well as compare with other ranging standards.
- Based on the qualitative analysis and experiments determine the best configuration in a household to place the anchors for the system.
- Use the incoming data from the sensors to produce a suitable measurement/observation model for the pose of the system.
- Relay the data to a flight controller unit via a suitable hardware interface.
- Delve into the firmware of the flight controller and apply sensor fusion algorithms on the flight controller to provide pose estimates.
- Pipe the pose estimates to a companion computer for visualisation and higher level control of a UAV.

All of these objectives can be completed without flying the UAV autonomously. Given the current situation and time-frame it was determined that setting up the pipelines to visualise the localisation in realtime from the companion computer is adequate for the last objective. Furthermore, with the autonomous flight being out of scope of this project much of the work fell into software engineering to achieve the overall aim. Broadly, this means delving into the software libraries and interfaces for the Pozyx sensor, modifying and making additions to the Ardupilot flight stack to integrate the Pozyx sensor with the (pixhawk?) FCU, and finally digging into the MAVLINK protocol and libraries to use the pose estimates on a Raspberry Pi 3 Model B+ PSoC. To achieve these objectives a solid software engineering approach would need to be applied with familiarity of Python and C++ programming languages.

1.2 Background Research

Indoor localisation has become a core part of many system in recent years. These range from robotics, multimedia, logistics and sporting systems. Modern localisation systems can be split in active or passive systems, active systems require the system being localised to have electronics to either process or send information that will be used to determine location. In passive systems the position is determine based on a variance of a measured signal or image data. As noted by Deak et al. (2012), some of these techniques include, Received Signal Strength Indicator (RSSI), Time of Arrival (TOA), Time Difference of Arrival (TDOA) and Angle of Arrival (AOA). The Pozyx commercial system uses UWB signals with a TOF technique in order to determine the position of a receiver (tag) in a network of transmitters (anchors). Since processing is done on-board the tag, it falls under the active localisation category. Active systems are ideal for indoor localisation systems for drones since the positional data can be fed directly to FCU's or companion computers in order to correct pose estimates calculated by the system directly.

As noted by the producers of Pozyx the core of the system uses a communication bandwidth of $\approx 500MHz$, this results in pulses of $0.16ns$ wide. Assuming that speed of light is $299792458ms^{-1}$ we get pulses of length $0.04797m$ which is very small and hence robust to noise from reflections. The major factors affecting the performance of the system would be materials that would slow down the signals before they reach the tag. So No Line of Sight (NLOS), conductors and changing mediums of travel are noted to affect the performance the most.

With increasing complexity of FCU's it is possible to do relatively dense calculations in a real time scenario without delegating them to a separate processing system. This is beneficial to indoor drone systems since they need to be small and maneuverable. A standard FCU comes equipped with several standard communication interfaces (I2C, Serial, SPI) so integrating external sensors is possible. Furthermore, multiple autopilot firmware provides a Hardware Abstraction Layer (HAL) making any sensor integration developed on one unit easily ported to another system. Additionally, on board libraries contain sensor fusion implementations (Extended Kalman Filter (EKF)) that can combine the Pozyx data and on-board sensor data to provide fairly accurate positional data while in motion.

LITERATURE REVIEW

2.1 Indoor Localisation Systems

2.1.1 Passive Systems

In summary, passive systems do not require the object being tracked to have some of electronics on them to do positioning. Some examples of passive systems are (Deak et al. 2012):

- Computer Vision and Imaging systems.
- Tactile and contact sensors.
- Attenuation of signals.
- Differential air pressure.

A common example of computer vision based localisation is to use a setup consisting of multiple cameras in a space trying to detecting a single object. Using the intrinsic and extrinsic properties of each camera it is possible to determine the transform to the object in a given frame with relatively high accuracy. A prime example of this is the commercial VICON motion capture systems. Aerial Robotics IITK (n.d.) shows a drone application in which the UAV is positioned via using a VICON motion capture system. Figure 2.1 shows the simplified setup, it should be noted that the UAV must be equipped with specialised marker that is used to identify it. Furthermore, the positions are fed to a companion computer connected to the autopilot system. The VICON setup provides highly accurate positions and is often used to gather ground truth positional data to compare to other positioning systems. The additional requirements of the VICON systems, however, do not make it feasible for indoor applications.

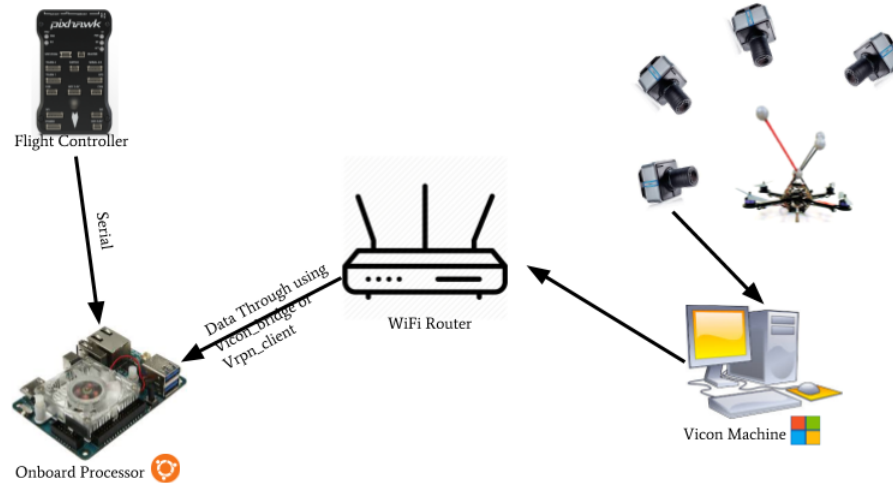


Figure 2.1: VICON setup for position of a UAV. (<https://aerial-robotics-iitk.gitbook.io/wiki/estimation/setup-with-vicon>)

2.1.2 Active Systems

In contrast to passive systems, active systems have the object being positioned equipped with electronics. Many indoor localisation techniques use this and some examples are (Deak et al. 2012)

- Radio-frequency identification
- UWB
- Wireless Local Area Network
- Bluetooth Low energy (BLE)

Many of these setups use an anchor and tag configuration. The tag receives signals from multiple anchors and triangulates the tag.

An approach using and comparing UWB and BLE is developed by Jiménez & Seco (2017) to do localisation in a museum. Both methods are combined with a dead reckoning system to improve accuracy. Six paintings are equipped with both a BLE and UWB tag. The test setup first did a calibration where both sensors were placed at fixed points in the museum with a clear line of sight to each tag. From initial ranging performance, the UWB setup was shown to perform better with a distance variance of $\pm 0.4m$ while the BLE setup had errors of over $10m$. It is noted by the authors that a ranging approach with BLE is challenging since it uses an RSSI method

but can match the accuracy of the UWB setup when combined a dead reckoning system after some initial steps by the user.

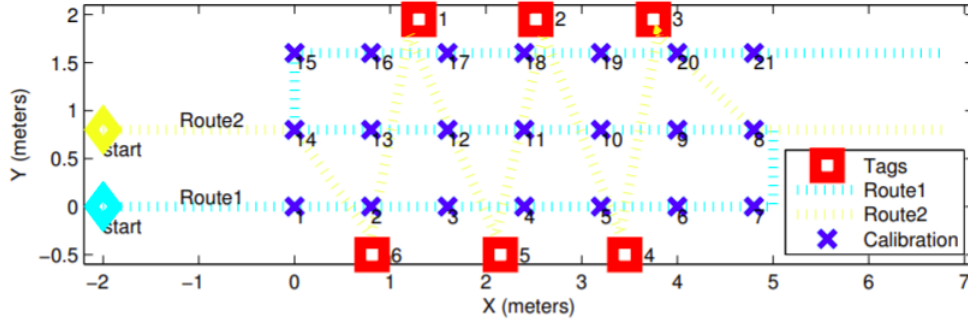


Figure 2.2: Setup used to compare UWB and BLE performance in a museum.

2.2 Pozyx - Behind the Scenes

For this research project a commercially available, active UWB sensor system is proposed to aid in localisation of an indoor UAV system.

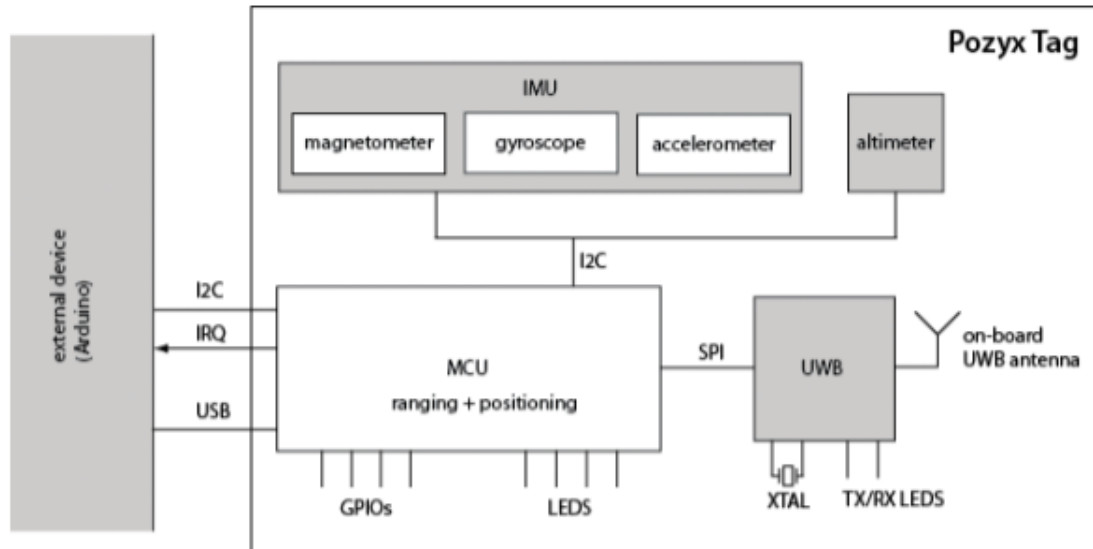


Figure 2.3: Simplified Block Diagram of the Pozyx tag.

2.2.1 Ultra-WideBand (UWB)

The core of the Pozyx system operates using an UWB approach. UWB is a short range, low energy, high bandwidth communication radio technology. Radio waves travel at the speed of light

($c = 299792458ms^{-1}$) so using a TOF approach the range between a tag and an anchor can be obtained simply by:

$$d = c * TOF$$

Knowing the position of each anchor in a given reference frame, Mimoune et al. (2019) discuss a method to use raw range readings in order to determine the position of the tag. The positions can be described by the following system of equations:

$$(2.1) \quad \begin{bmatrix} (x - x_1)^2 + (y - y_1)^2 + (z - z_1)^2 = d_1^2 \\ \vdots \\ (x - x_n)^2 + (y - y_n)^2 + (z - z_n)^2 = d_n^2 \end{bmatrix}$$

Where n represents an index of an anchor and (x, y, z) represents the position of the tag. This can be converted into matrix form of $\mathbf{A} \cdot \mathbf{x} = \mathbf{B}$:

$$(2.2) \quad \begin{bmatrix} 1 - 2x_1 - 2y_1 - 2z_1 \\ \vdots \\ 1 - 2x_n - 2y_n - 2z_n \end{bmatrix} * \begin{bmatrix} x^2 + y^2 + z^2 \\ x \\ y \\ z \end{bmatrix} = \begin{bmatrix} d_1^2 - x_1^2 - y_1^2 - z_1^2 \\ \vdots \\ d_n^2 - x_n^2 - y_n^2 - z_n^2 \end{bmatrix}$$

The position of the tag can be calculated as:

$$\hat{x} = (\mathbf{A}^T \mathbf{A})^{-1} \mathbf{A}^T \mathbf{B}$$

From the algorithms and work presented we can confirm that the Pozyx system can achieve an accuracy of $\pm 10cm$ in standard environments with LOS. The work confirms that LOS of the anchors to tag is a major factor in accuracy and this will be taken into account when anchors are being placed in the research. Furthermore, the work mentioned in this section proposes an algorithm with raw range readings in order to do localisation, my research will focus on the integration of the Pozyx tag with a standard FCU, so the pose data coming directly from the tag can be used. The pose can be obtained via two modes: 1). A pure Two Way Ranging (TWR) Approach or 2.) A tracking approach using a Kalman prediction filter in addition to the TWR pose.

Additional work done by Di Pietra et al. (2019) also perform an evaluation of UWB systems for indoor applications. The work compares several commercial UWB systems available to consumers and their viability in ranging and pose estimation. The sensors are treated as black box systems and the proprietary algorithms for each system was used. The results documented in this paper shows useful steps to do a primary evaluation of multiple anchor configurations in a given space.

2.2.2 Pozyx Localisation

In contrast to the raw readings obtained in the previous work, the Pozyx system has been used in several localisation systems, both indoors and outdoors. Experiments done by DeStefano et al.

(2019) use the Pozyx system in multiple scenarios for the purpose of education. The setup is simple and the two dimensional positions, x and y , form the basis of graphs that can be used to determine average velocities from linear interpolation of the a position versus time graph. Figures 2.4 and 2.5 show both how the physical setup looked and the some of the data collected. Although the UWB positioning system has advantages over several other systems the researchers note that using the Pozyx system in this scenario is not ideal for several reasons. Due to the accuracy of the system ($\pm 10cm$) leads to large variance in instantaneous velocity when calculations are done on a point to point basis.

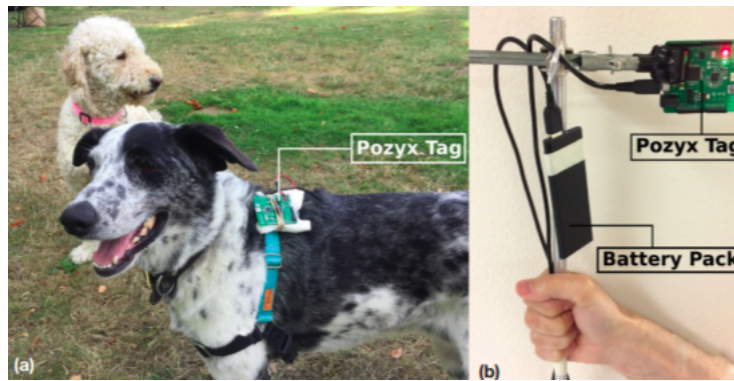


Figure 2.4: The experimental setups for both a dog and a student.

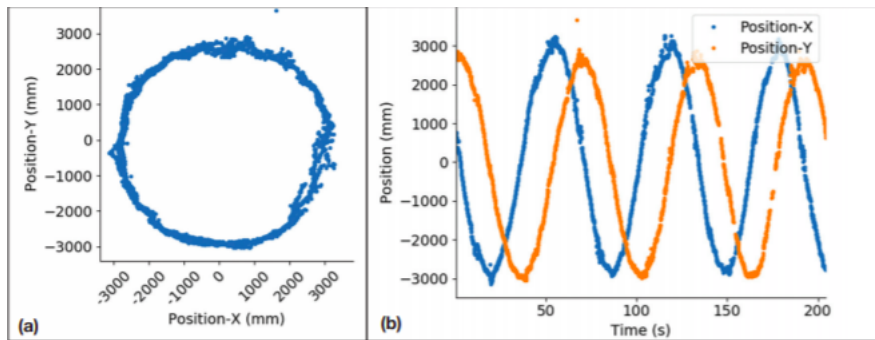


Figure 2.5: Data collected from a student walking in a circle.

Conceição et al. (2017) present a method for using the Pozyx in an outdoor environment. The systems is proposed to operate in two ways: 1.) Using raw range values from the Pozyx sensor and using an EKF externally for pose estimates. 2.) The pose estimates coming from the Pozyx sensor itself. A modified version of the EKF is described in the first scenario. An additional check is done for outliers. Outliers can be described as measurements that do not fit the pattern of the previous measurements. If an outlier is detected it is simply not considered in that time step and the previous calculated values are used instead. The test environment was an outdoor scenario with range error characterisation test which allowed for optimal anchor placement and a suitable testbed for implementing multiple positioning algorithms. A similar methodology would

be adapted for this work with focus on indoor limitations and the presence of dynamic obstacles (humans).

2.2.3 Pozyx - Arduino Implementation

Before continuing it should be noted that Ardupilot (2019) has addressed the idea of combining the Pozyx system with a Flight controller using the Ardupilot firmware. The implementation uses the Pozyx tag's compatibility with the Arduino UNO R3 or R2 pin layout. The Pozyx Arduino library is used to gather the relevant information from the Pozyx tag and then send it via serial to the FCU. This research aims to bridge this gap in the hardware and remove the need for the Arduino UNO for the indoor navigation. The major driving force of this is to minimize the amount of extra hardware that should be mounted on and indoor UAV.

2.2.4 Summary

From a overview of work done with UWB technology and the Pozyx system we can see it is a well researched area in terms of evaluating the performance in static scenarios with not much obstacles. However, there seems to be a gap of these systems being tested and localised in households where dynamic obstacles can be present in the area. Furthermore, a major objective of this research would be to directly integrate the Pozyx system directly with a FCU and utilize the sensor fusion systems on board and evaluate the accuracy of the pose estimates. To that end, a similar approach taken by Di Pietra et al. (2019) would be used to first find an optimal anchor configuration and then evaluate it similar to how experiments were carried out by Conceição et al. (2017).

RESEARCH METHODOLOGY

From the literature there is a clear lack of results for localisation systems using the commercial Pozyx sensor network with drones in an household environment. To address the aims and objectives stated in 1.1, it is proposed that a lightweight on-board localisation be developed to check the feasibility of minimal hardware solution for an indoor drone. This would entail connecting a Pozyx tag directly to a FCU and integrate it with the pose localisation system existing already. To close the loop the pose information should be available in some format that can be used for autonomous control. Furthermore, the system should be tested in a practical environment, to this end, the Pozyx anchor network was setup in a kitchen. A kitchen represents one of the highest traffic areas in a household and it contains various materials that will make raw readings from a UWB system noisy and inaccurate. As a kitchen will contain both dynamic and static obstacles multiple anchor configurations must be tested in order to find optimal anchor positions in this given environment.

3.1 Anchor Configurations

Noting work from Di Pietra et al. (2019) and the setup procedures from Pozyx Labs (2018) it is important to have at least 4 anchors setup in non-planar orientations for the best positioning results. To determine a suitable anchor configuration in the given space a tag was placed at fixed known point in a given reference frame and the mounted locations of the 4 anchors were varied on each wall of the kitchen in order to prevent planar configurations and ambiguity when the tag calculates its position. Figure 3.1 shows a simplified layout and toybox configuration of the tag and anchors. Grey areas represent areas in the space that is impossible to traverse, red represents known obstacles that interfere and attenuate the UWB signal, blue represent

anchors, green the tag, cream is partially obstructed and the rest of the area is fully traversable. Before each run and data collection the tag was manually configured with the location of each of the anchors in the reference frame of the kitchen and recorded for at least 5 seconds. The tag was triggered to calculate the position repeatedly within the timeframe and the function call is blocking and takes $\approx 70ms$ so data was recorded at a frequency of $\approx 14.28Hz$. With a tag position of (1480,2330,980)mm, the following statistics were calculated using Matlab. In addition to the average error and standard deviation, kurtosis and skew metrics were added to show the number of outliers and symmetry of the recorded data. The error metrics are important to give an idea of how noisy the overall data is while kurtosis and skewness gives an indication if the noise follows a uniform distribution which would be beneficial ideal for state estimators. From table 3.1 we can see that configuration 12 gives acceptable error metrics and reasonable skew and kurtosis making it the best out of the configurations tested. To further support this Figure 3.2 shows several results obtained with several configurations and it can be seen that configuration 12 produced the best results.

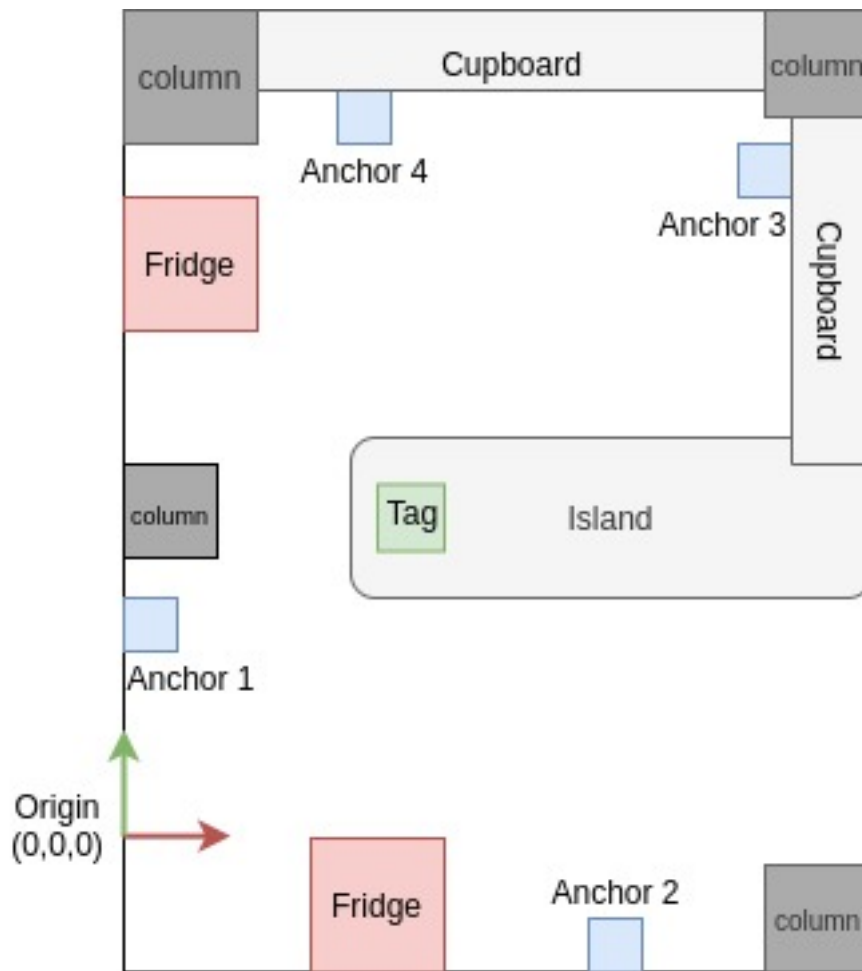


Figure 3.1: Birds eye view of the test environment.

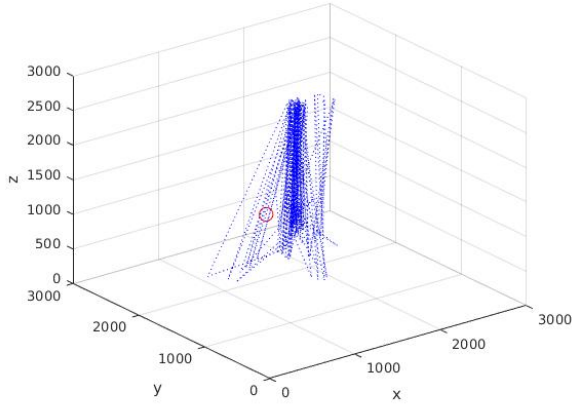
3.1. ANCHOR CONFIGURATIONS

Config #	Anchor positions (mm)	Avg. Error	Std. Deviation $\begin{pmatrix} x, \\ y, \\ z \end{pmatrix}$	Kurtosis	Skewness
1	$\begin{pmatrix} (0,0,1115), \\ (3680,-405,1550), \\ (3655,4080,1906), \\ (270,4465,2090) \end{pmatrix}$	342.5906	$\begin{pmatrix} 183.1707, \\ 205.3426, \\ 972.6239 \end{pmatrix}$	$\begin{pmatrix} 2.349, \\ 1.5967, \\ 1.415 \end{pmatrix}$	$\begin{pmatrix} -0.4083, \\ -0.3522, \\ 0.4551 \end{pmatrix}$
2	$\begin{pmatrix} (0,665,1115), \\ (2995,-405,1889), \\ (3655,4080,1906), \\ (270,4465,2090) \end{pmatrix}$	173.5938	$\begin{pmatrix} 43.2345, \\ 45.6897, \\ 133.8616 \end{pmatrix}$	$\begin{pmatrix} 21.8923, \\ 10.1765, \\ 119.1344 \end{pmatrix}$	$\begin{pmatrix} -2.8672, \\ -0.3453, \\ 8.9025 \end{pmatrix}$
3	$\begin{pmatrix} (0,665,1115), \\ (2995,-405,1889), \\ (3655,4080,1906), \\ (1526,4559,837) \end{pmatrix}$	203.8502	$\begin{pmatrix} 128.4693, \\ 118.3216, \\ 209.1637 \end{pmatrix}$	$\begin{pmatrix} 14.2955, \\ 11.2045, \\ 2.9124 \end{pmatrix}$	$\begin{pmatrix} -2.579, \\ -0.3920, \\ 0.4055 \end{pmatrix}$
4	$\begin{pmatrix} (0,665,1115), \\ (2995,-405,1889), \\ (3655,4080,1906), \\ (1070,5170,491) \end{pmatrix}$	85.8562	$\begin{pmatrix} 40.2197, \\ 40.6081, \\ 66.2120 \end{pmatrix}$	$\begin{pmatrix} 6.7558, \\ 7.5180, \\ 3.4722 \end{pmatrix}$	$\begin{pmatrix} -0.4260, \\ -0.5344, \\ -0.1242 \end{pmatrix}$
5	$\begin{pmatrix} (0,665,1115), \\ (2995,-405,1889), \\ (3960,3368,2304), \\ (1070,5170,491) \end{pmatrix}$	64.8616	$\begin{pmatrix} 65.3883, \\ 53.8458, \\ 78.5751 \end{pmatrix}$	$\begin{pmatrix} 13.3707, \\ 13.2178, \\ 11.0111 \end{pmatrix}$	$\begin{pmatrix} -0.6016, \\ 0.3745, \\ 0.0461 \end{pmatrix}$
6	$\begin{pmatrix} (0,665,1115), \\ (2737,-410,1913), \\ (3655,3598,1668), \\ (1187,4760,590) \end{pmatrix}$	189.933	$\begin{pmatrix} 40.8435, \\ 32.6482, \\ 58.5618 \end{pmatrix}$	$\begin{pmatrix} 11.8957, \\ 11.8924, \\ 11.092 \end{pmatrix}$	$\begin{pmatrix} 0.7516, \\ -0.0100, \\ -0.1322 \end{pmatrix}$
7	$\begin{pmatrix} (0,665,1115), \\ (2737,-410,1913), \\ (3655,4529,1777), \\ (1187,4760,590) \end{pmatrix}$	100.6929	$\begin{pmatrix} 75.8269, \\ 72.0940, \\ 41.9398 \end{pmatrix}$	$\begin{pmatrix} 26.0285, \\ 17.4295, \\ 7.2328 \end{pmatrix}$	$\begin{pmatrix} -3.1681, \\ -0.8384, \\ -0.7151 \end{pmatrix}$
8	$\begin{pmatrix} (0,645,1214), \\ (2737,-410,1913), \\ (3651,4120,1853), \\ (1066,4760,491) \end{pmatrix}$	138.1276	$\begin{pmatrix} 26.2243, \\ 21.8750, \\ 70.6189 \end{pmatrix}$	$\begin{pmatrix} 4.6048, \\ 52.2374, \\ 50.9467 \end{pmatrix}$	$\begin{pmatrix} -0.4858, \\ 5.0752, \\ 5.1757 \end{pmatrix}$

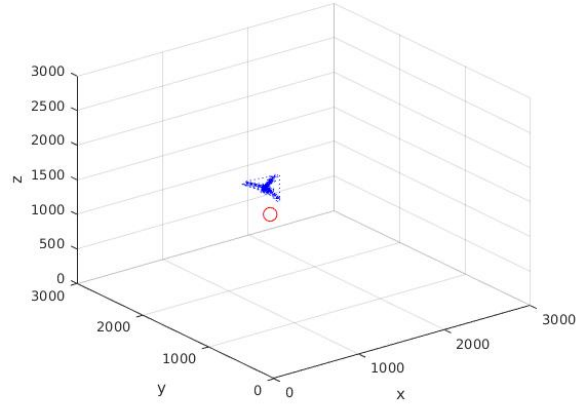
9	$\begin{pmatrix} (0, 645, 1214), \\ (2737, -410, 1913), \\ (3970, 3063, 2320), \\ (1066, 4760, 491) \end{pmatrix}$	258.296	$\begin{pmatrix} 165.7105, \\ 95.081, \\ 475.0623 \end{pmatrix}$	$\begin{pmatrix} 2.2833, \\ 1.7939, \\ 2.3406 \end{pmatrix}$	$\begin{pmatrix} -0.6982, \\ 0.2746, \\ 0.7517 \end{pmatrix}$
10	$\begin{pmatrix} (0, 645, 1214), \\ (2737, -410, 1913), \\ (3651, 3550, 1810), \\ (1066, 4760, 491) \end{pmatrix}$	235.348	$\begin{pmatrix} 116.1306, \\ 89.9868, \\ 420.8322 \end{pmatrix}$	$\begin{pmatrix} 3.6670, \\ 4.7058, \\ 3.8066 \end{pmatrix}$	$\begin{pmatrix} 1.5079, \\ -1.7613, \\ -1.5615 \end{pmatrix}$
11	$\begin{pmatrix} (0, 645, 1214), \\ (2737, -410, 1913), \\ (3651, 3550, 1810), \\ (1591, 4450, 1775) \end{pmatrix}$	223.4468	$\begin{pmatrix} 120.9674, \\ 79.8602, \\ 409.8192 \end{pmatrix}$	$\begin{pmatrix} 3.389, \\ 4.6663, \\ 3.1988 \end{pmatrix}$	$\begin{pmatrix} 1.1099, \\ -1.5397, \\ -1.2038 \end{pmatrix}$
12	$\begin{pmatrix} (0, 645, 1214), \\ (2737, -410, 1913), \\ (3651, 4120, 1853), \\ (1591, 4450, 1775) \end{pmatrix}$	111.8493	$\begin{pmatrix} 27.568, \\ 17.7124, \\ 64.4278 \end{pmatrix}$	$\begin{pmatrix} 4.8522, \\ 7.4335, \\ 6.2489 \end{pmatrix}$	$\begin{pmatrix} -0.0239, \\ -0.8535, \\ 3.7132 \end{pmatrix}$

Table 3.1: Statistics of the data recorded for each configuration.

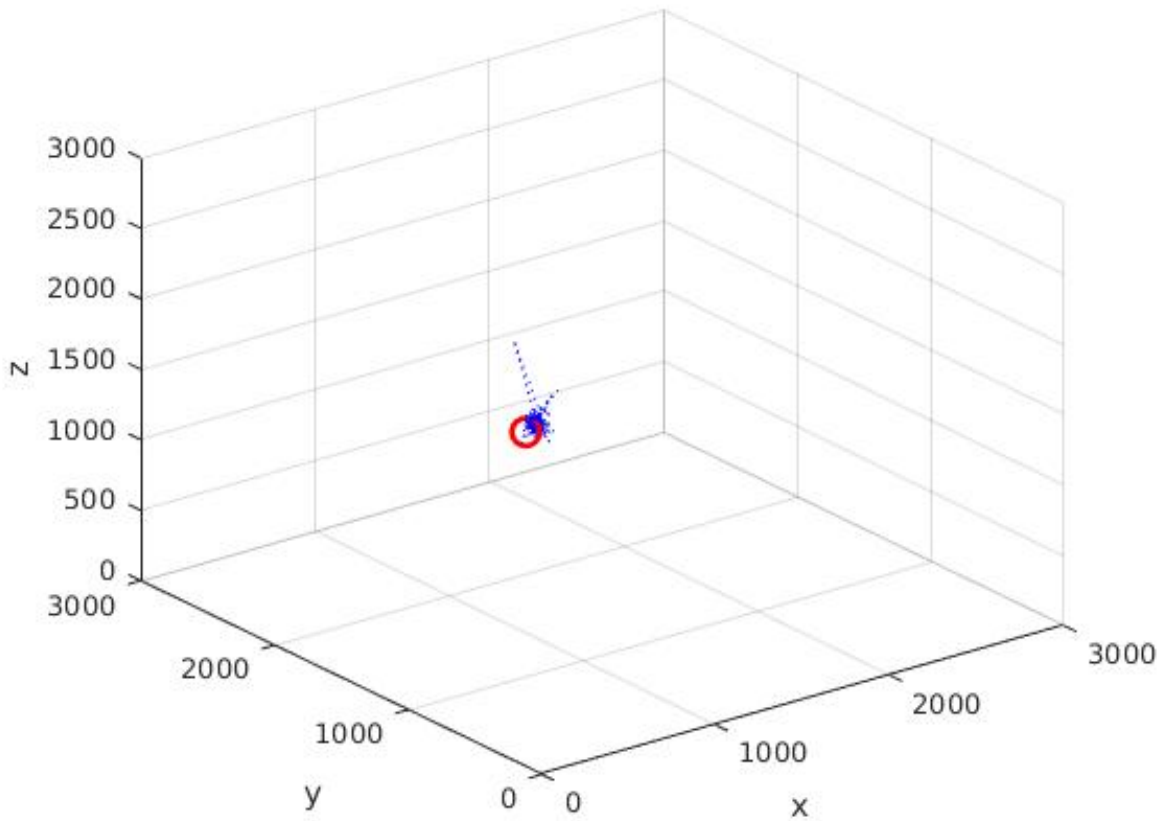
Intro to the basic concept, highlight Pietra's paper and how I am using that to phrase and determine the best location Show pics, diagrams and initial table of results?



(a) Plot of Config 1



(b) Plot of Config 2



(c) Plot of Config 12

Figure 3.2: Sample plots of several anchor configurations.



APPENDIX A

Two Way Ranging (TWR)

TWR is a ranging method that utilises TOF and delays during transmission of a packet in order to determine the range between a tag and anchor. Figure A.1 provides a simple illustration of how this works. The distance for an individual tag and an anchor can be obtained by:

$$d = c \cdot \frac{(TT2 - TT1) - (TA2 - TA1)}{2}$$

This is repeated for each anchor and then the position of the tag can be determined via trilateration. Geometrically, the position of the tag can be described as the point intersection of all the circles with distance, d , from the tag. This can be seen in Figure A.2.

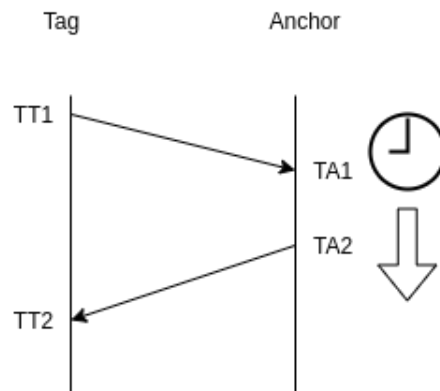


Figure A.1: Packet transfer in TWR.

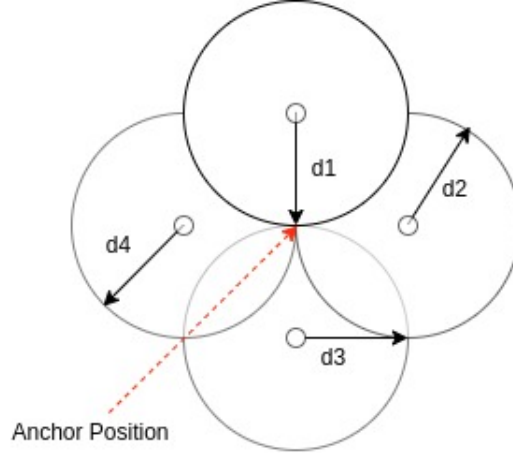


Figure A.2: 4 Anchor and 1 Tag trilateration in 2D.

Sensor Fusion

From the previous section we have described the basic principle of operation of the Pozyx system. With a tag we are able to at least determine a rough estimate of the position of a tag in a given reference frame. Additionally, the tag has an Inertial Measurement Unit (IMU), consisting of an Accelerometer, Gyroscope and Magnetometer, and an Altimeter. These are used in one of the operational modes of the Pozyx system in order to improve accuracy. The idea of sensor fusion is to combine multiple sources of data in order to get a fairly accurate estimate of the pose of the system. The measurements from the tag can be combined with the sensors onward a FCU in order to achieve this. The de-facto sensor fusion technique is called the Extended Kalman Filter (EKF). Chadaporn et al. (2014) present a useful description and example of how the EKF works. Algorithmically, the EKF is a recursive process using predictions based on the dynamics of the vehicles and updating the estimate based on these predictions and measurements from various sources. The major requirement for the EKF is that the process model and the measurement model are differentiable. The steps for the EKF are as follows:

1. Provide an initial estimate for the state, \hat{x}_k^+ , and the prediction error, P_k^+ .
2. Compute the Kalman gain, $K_k = P_k^+ H_k^T (H_k P_k^+ H_k^T + R)^{-1}$
3. Update the estimate with measurement z_k , $\hat{x}_k = \hat{x}_k^+ + K_k (z_k - h(\hat{x}_k^+))$
4. Update the prediction error, $P_k = (I - K_k H_k) P_k^+$
5. Project the state ahead, $\hat{x}_{k+1}^+ = f(\hat{x}_k, u_k, w)$
6. Project the Prediction error ahead, $P_{k+1}^+ = A_k P_k A_k^T + Q_k$
7. Repeat from step 2.

Where K is the Kalman gain, R is the Measurement Noise Covariance Matrix, Q is the Process Noise Covariance matrix.

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