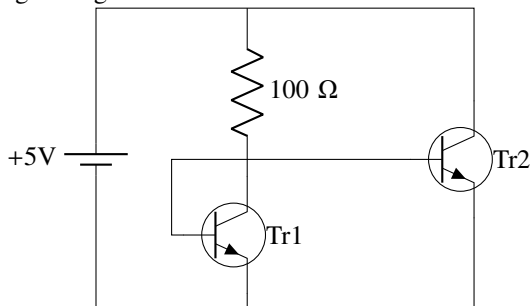


- 1) The isospin and the strangeness of Ω^- baryon are
- a) 1, -3 b) 0, -3 c) 1, 3 d) 0, 3
- 2) The lifetime of an atomic state is 1 nanosecond. The natural line width of the spectral line in the emission spectrum of this state is of the order of
- a) 10^{-10} eV c) 10^{-6} eV
b) 10^{-9} eV d) 10^{-4} eV
- 3) The degeneracy of an excited state of nitrogen atom having electronic configuration $1s^2 2s^2 2p^2 3d^1$ is
- a) 6 b) 10 c) 15 d) 150
- 4) The far infrared rotational absorption spectrum of a diatomic molecule shows equidistant lines with spacing 20 cm^{-1} . The position of the first Stokes line in the rotational Raman spectrum of this molecule is
- a) 20 cm^{-1} b) 40 cm^{-1} c) 60 cm^{-1} d) 120 cm^{-1}
- 5) A metal with body centered cubic (bcc) structure shows the first (i.e. smallest angle) diffraction peak at a Bragg angle of $\theta = 30^\circ$. The wavelength of X-ray used is 2.1 \AA . The volume of the primitive unit cell of the metal is
- a) $26.2 (\text{\AA})^3$ b) $13.1 (\text{\AA})^3$ c) $9.3 (\text{\AA})^3$ d) $4.6 (\text{\AA})^3$
- 6) In the following circuit, Tr1 and Tr2 are identical transistors having $V_{BE} = 0.7 \text{ V}$. The current passing through the transistor Tr2 is



a) 57 mA

b) 50 mA

c) 48 mA

d) 43 mA

7) The following Boolean expression

$$Y = A \cdot \bar{B} \cdot \bar{C} \cdot \bar{D} + \bar{A} \cdot B \cdot \bar{C} \cdot D + \bar{A} \cdot \bar{B} \cdot \bar{C} \cdot D + \bar{A} \cdot \bar{B} \cdot C \cdot D + \bar{A} \cdot B \cdot C \cdot D + A \cdot \bar{B} \cdot \bar{C} \cdot D$$

can be simplified to

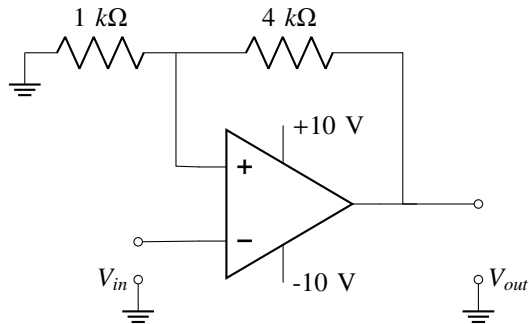
a) $\bar{A} \cdot \bar{B} \cdot C + A \cdot \bar{D}$

c) $A \cdot \bar{B} \cdot \bar{C} + \bar{A} \cdot D$

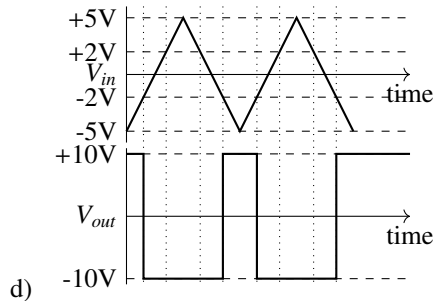
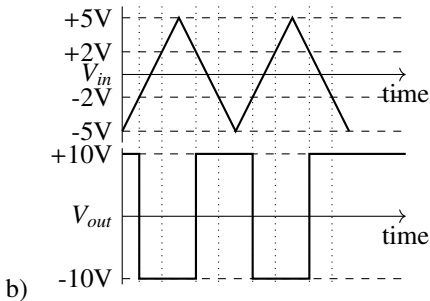
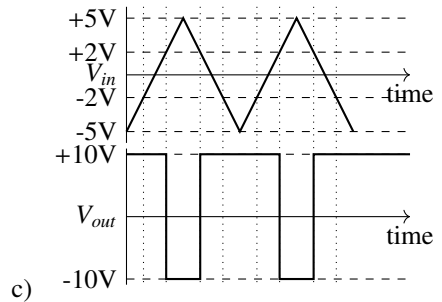
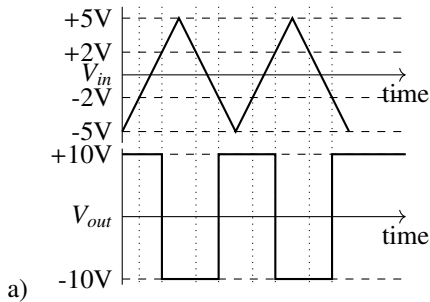
b) $\bar{A} \cdot B \cdot \bar{C} + A \cdot \bar{D}$

d) $A \cdot \bar{B} \cdot C + \bar{A} \cdot D$

8) Consider the following circuit.



Which of the following correctly represents the output V_{out} corresponding to the input V_{in} ?



Common Data for Questions 48 and 49:

Consider a function $f(z) = \frac{z \sin z}{(z-\pi)^2}$ of a complex variable z .

- 9) Which of the following statements is **TRUE** for the function $f(z)$?
- a) $f(z)$ is analytic everywhere in the complex plane
 - b) $f(z)$ has a zero at $z = \pi$
 - c) $f(z)$ has a pole of order 2 at $z = \pi$
 - d) $f(z)$ has a simple pole at $z = \pi$
- 10) Consider a counterclockwise circular contour $|z| = 1$ about the origin. The integral $\oint f(z) dz$ over this contour is
- a) $-\pi$
 - b) zero
 - c) $i\pi$
 - d) $2i\pi$

Common Data for Questions 50 and 51:

The tight binding energy dispersion ($E - k$) relation for electrons in a one-dimensional array of atoms having lattice constant a and total length L is

$$E = E_0 - \beta - 2\gamma \cos(ka),$$

where E_0 , β , and γ are constants and k is the wave-vector.

- 11) The density of states of electrons (including spin degeneracy) in the band is given by
- a) $\frac{L}{\pi\gamma a \sin(ka)}$
 - b) $\frac{L}{2\pi\gamma a \sin(ka)}$
 - c) $\frac{L}{2\pi\gamma a \cos(ka)}$
 - d) $\frac{L}{\pi\gamma a \cos(ka)}$
- 12) The effective mass of electrons in the band is given by
- a) $\frac{\hbar^2}{\gamma a^2 \cos(ka)}$
 - b) $\frac{\hbar^2}{2\gamma a^2 \cos(ka)}$
 - c) $\frac{\hbar^2}{\gamma a^2 \sin(ka)}$
 - d) $\frac{\hbar^2}{2\gamma a^2 \sin(ka)}$