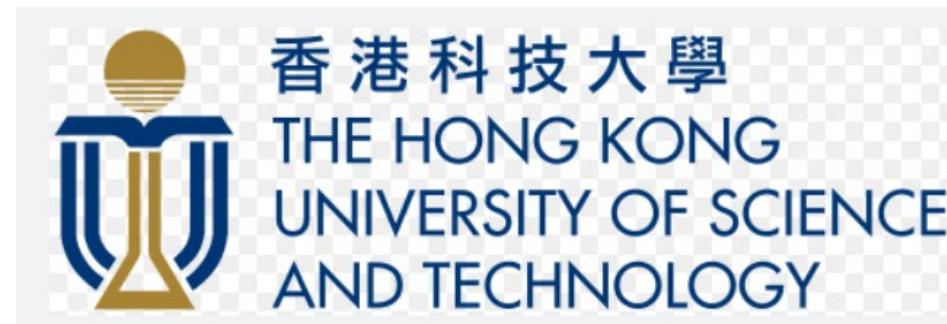




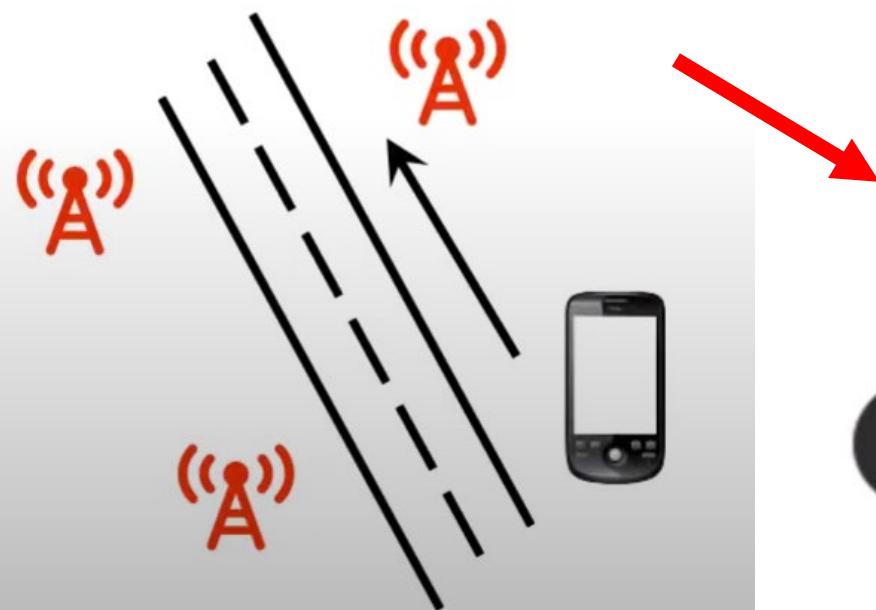
LHMM: A Learning Enhanced HMM Model for Cellular Trajectory Map Matching

Weijie Shi, Jiajie Xu*, Junhua Fang, Pingfu Chao, An Liu, and Xiaofang Zhou



Two Basic Concepts

Cellular Data



Cell tower

Carrier Server

User ID	Timestamp	Cell tower ID
A01	0802081032	37146
A01	0802081046	37149
A01	0802081068	37150
A01	0802081103	37153
A01	0802081148	37121
A01	0802081182	37154

.....

Two Basic Concepts

Cellular Trajectory Map-Matching



● GPS trajectory point

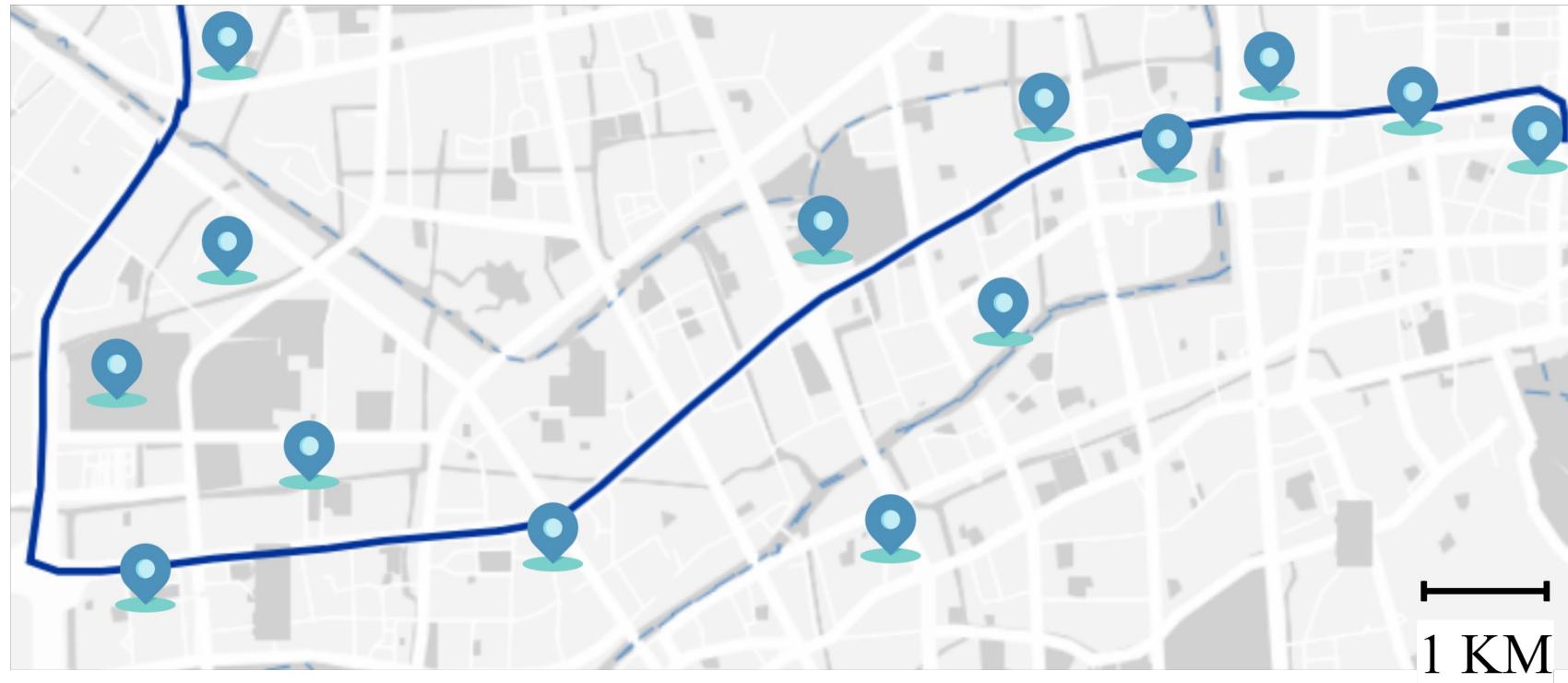


cellular trajectory point

traveled path

Two Basic Concepts

Cellular Trajectory Map-Matching



● GPS trajectory point

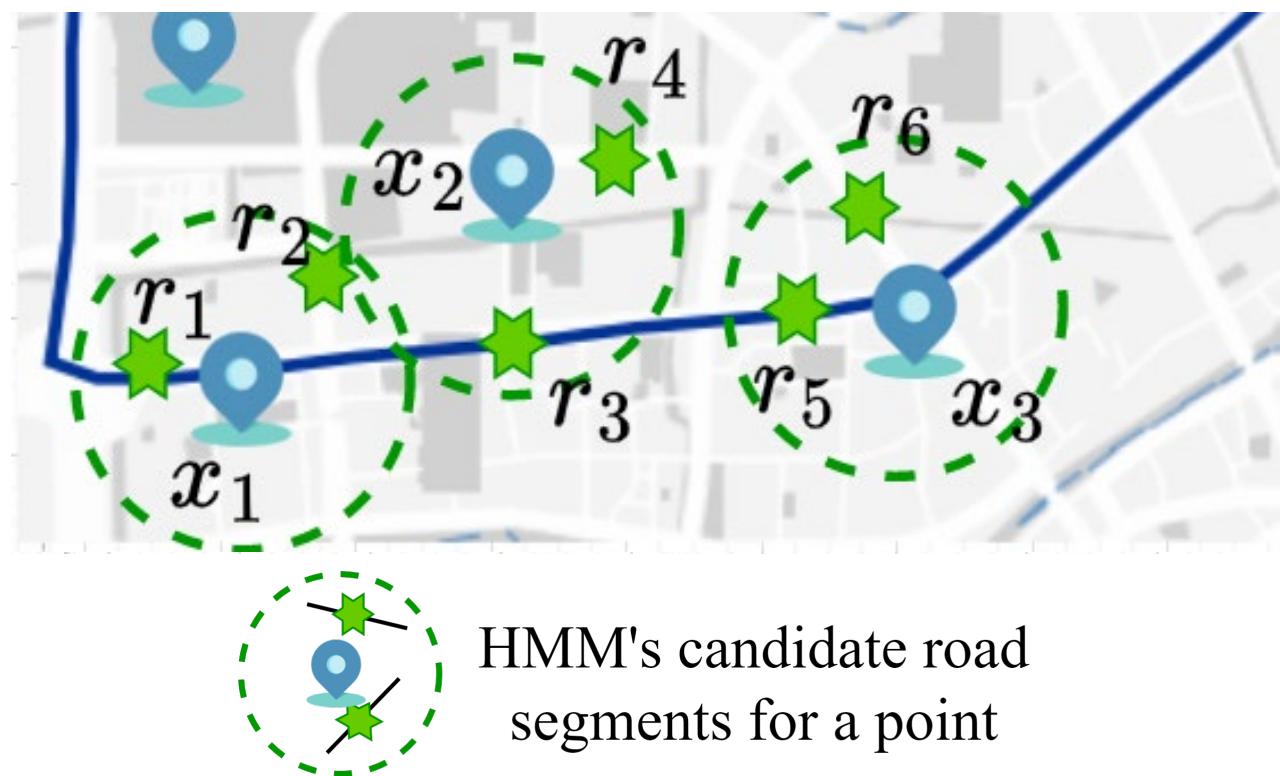


cellular trajectory point

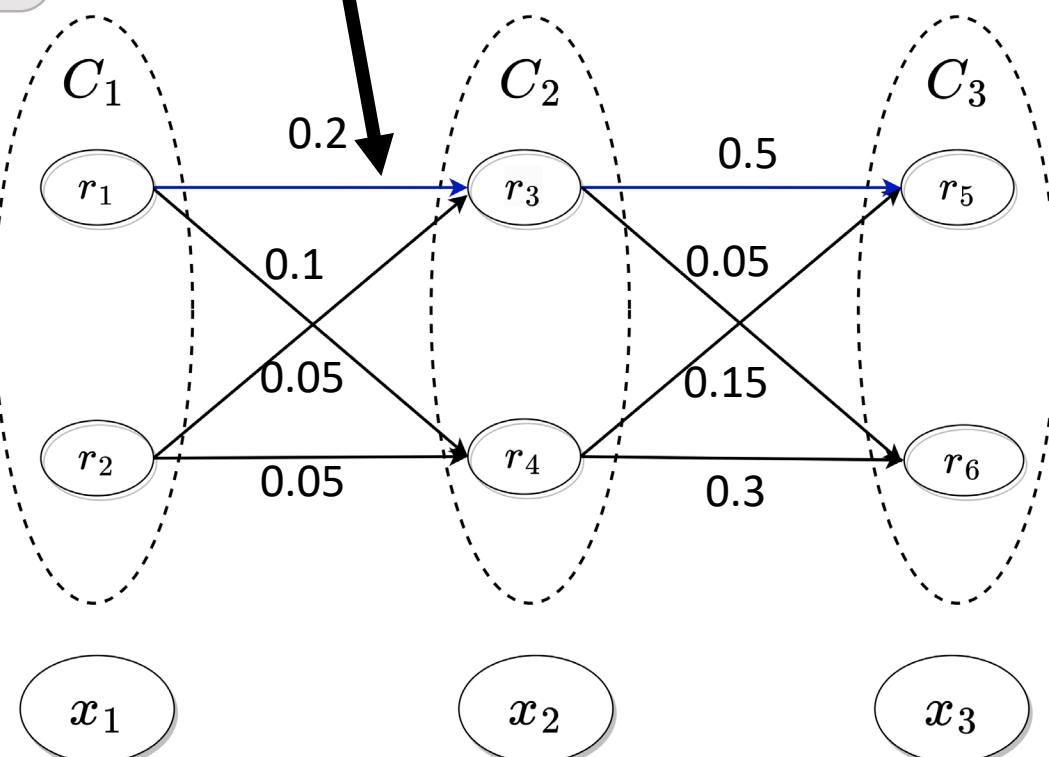
traveled path

Existing Methods

Hidden Markov Model (HMM)



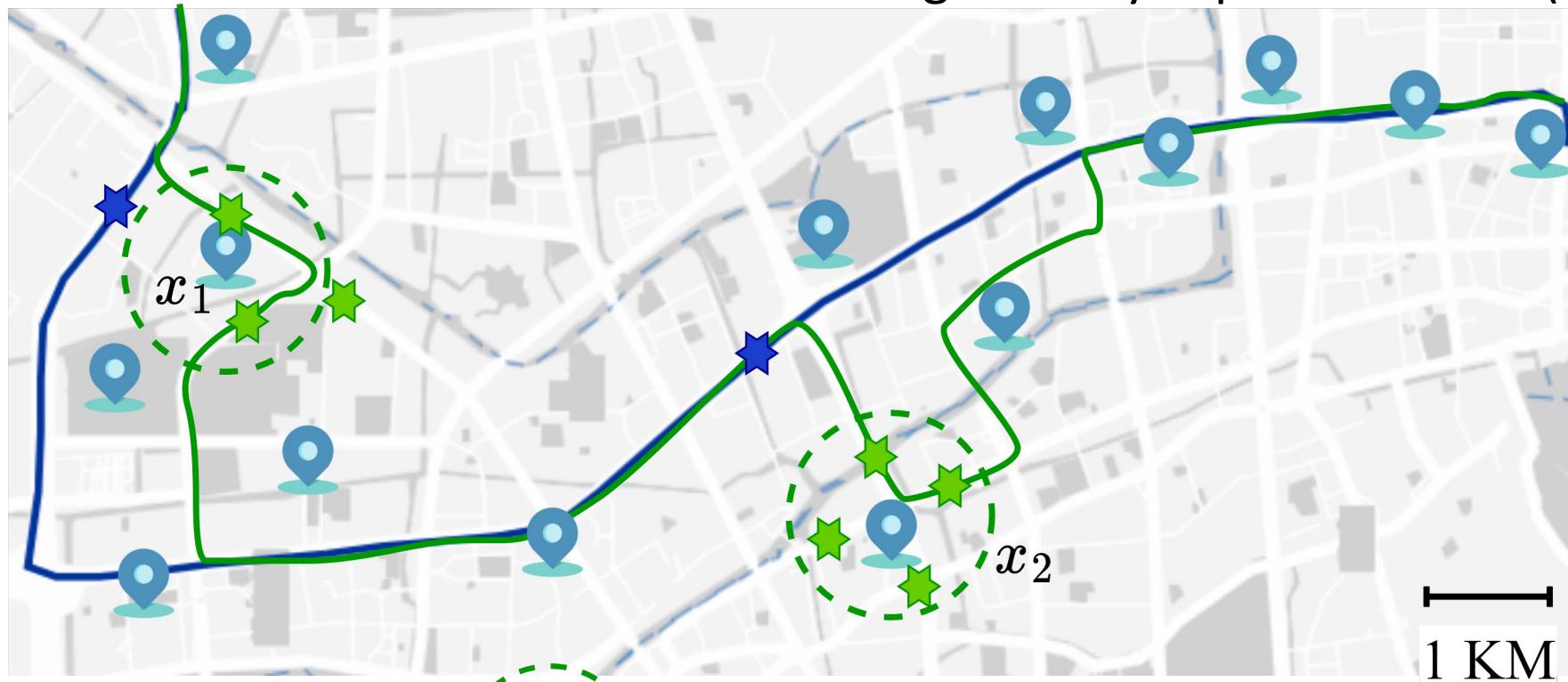
Observation Probability \times Transition Probability



Existing Methods

HMM's Drawback

The observation probability P_O and transition probability P_T are guided by explicit features (like distance)



HMM-based model matching result



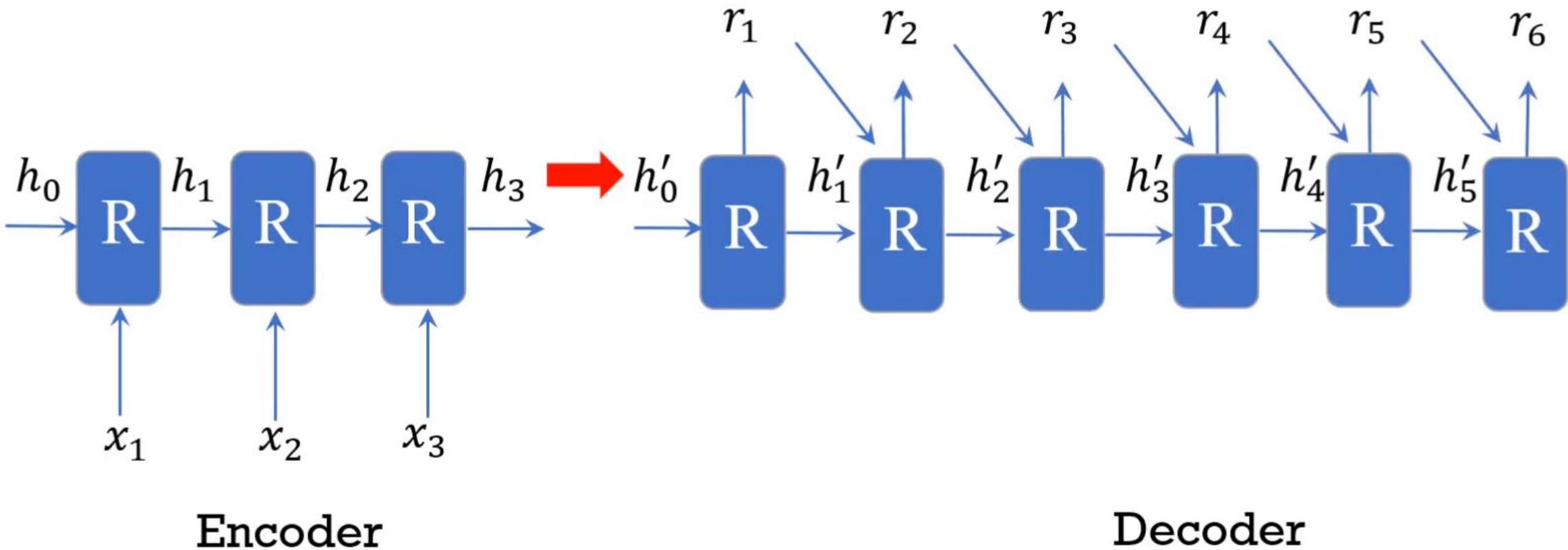
HMM's candidate road segments for a point



traveled road segment

Existing Methods

Sequence to Sequence Model (Seq2Seq)



Existing Methods

Seq2Seq's Drawback

Facing severe error propagation

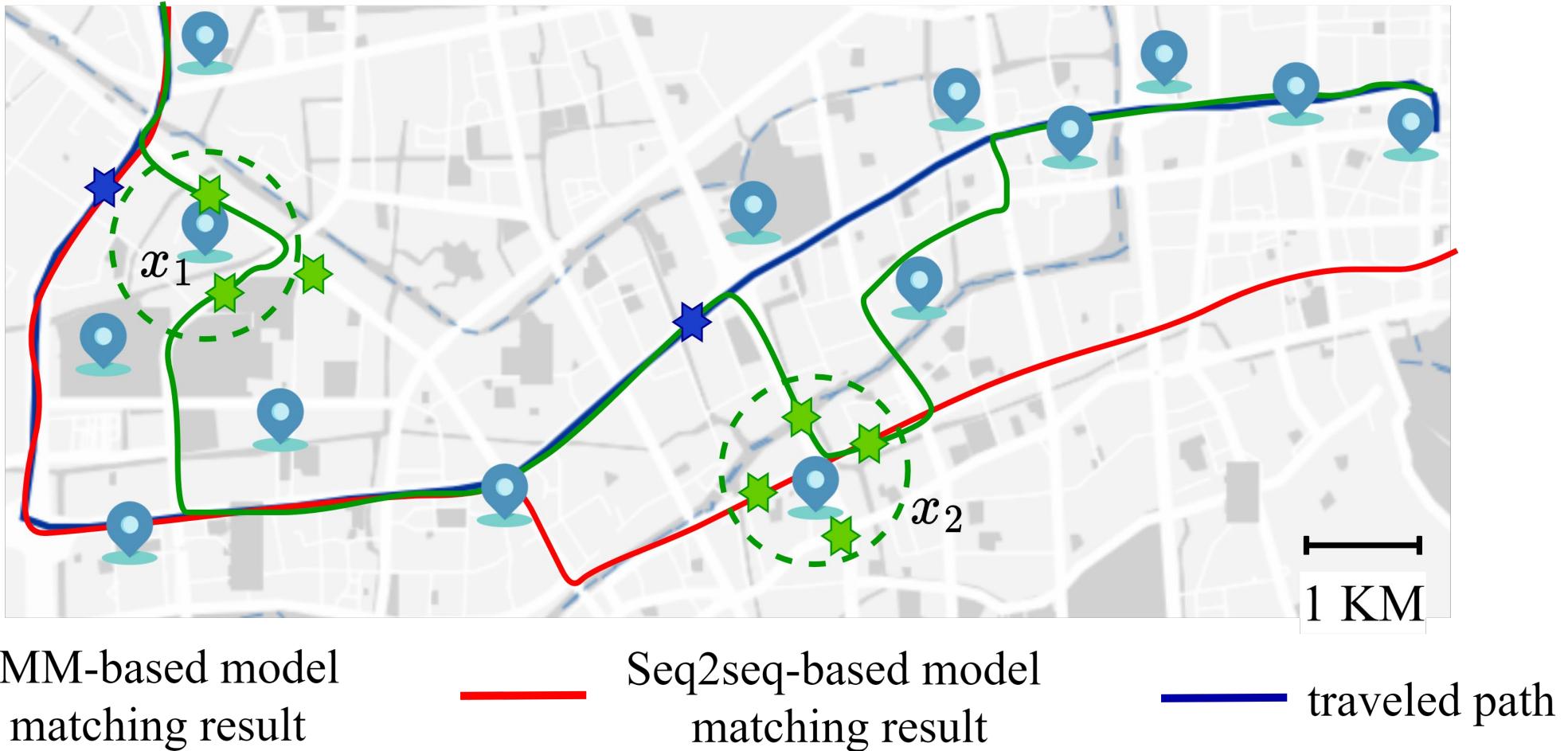


Seq2seq-based model
matching result

traveled path

Existing Methods

Advantages of HMM and Seq2Seq



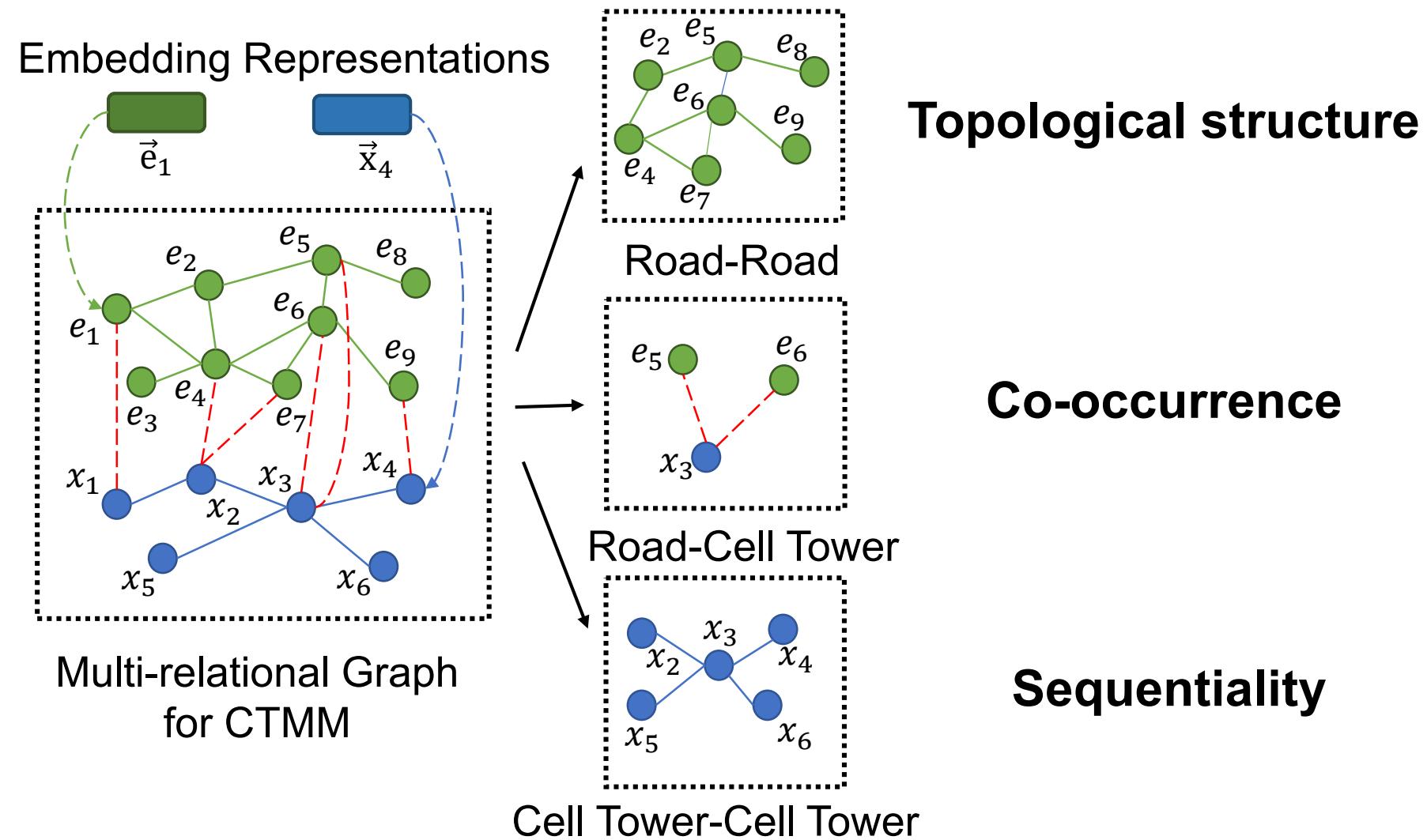
Learning Enhanced Hidden Markov Model

Learning Enhanced Hidden Markov Model

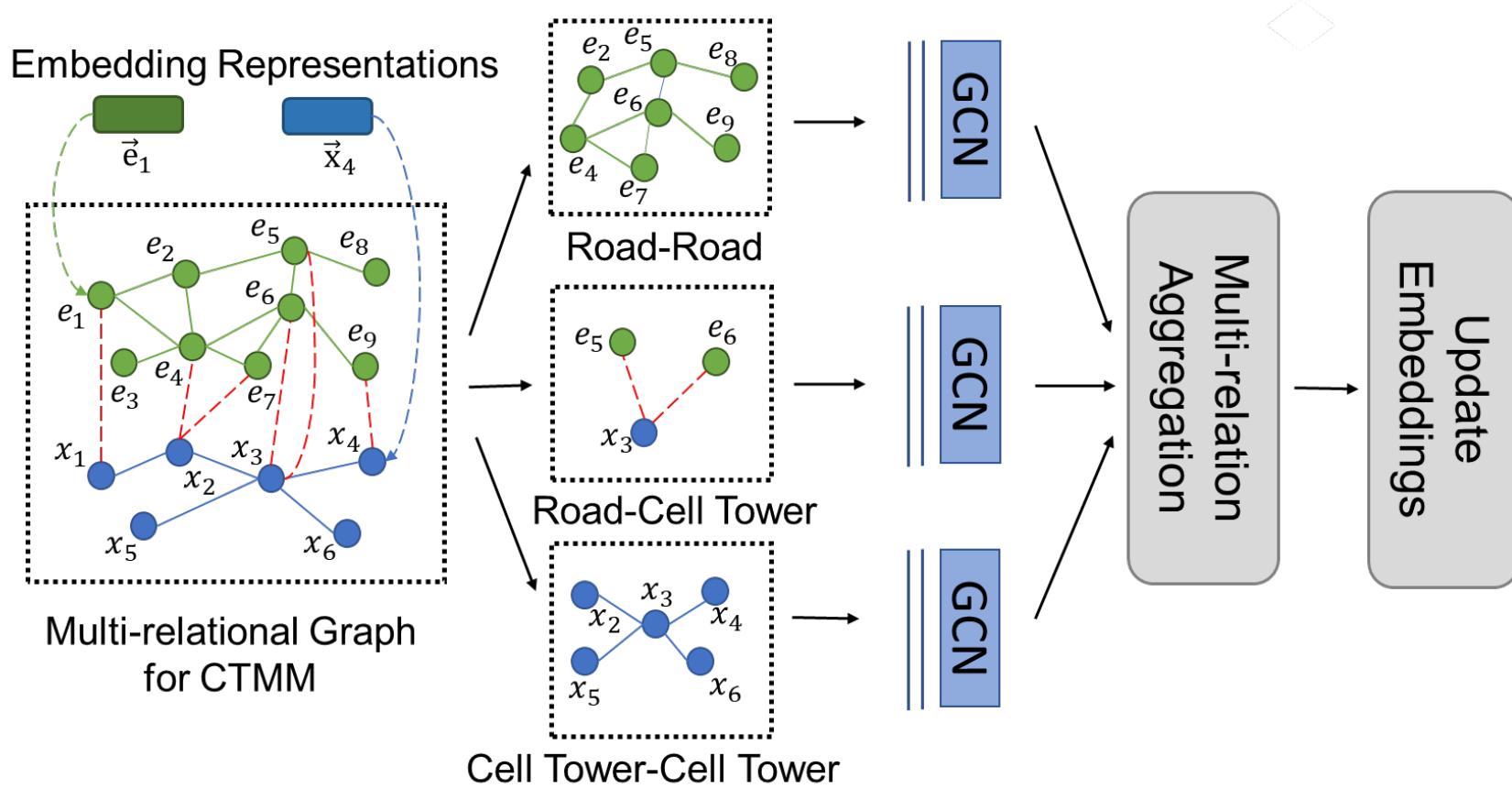
Aim to using **Neural Network** instead of hand-designed heuristic
to learn **Observation Probability P_O** and **Transition Probability P_T**

Challenge 1 – Multi-relation Representation Learning

How to effectively capture these relations and embedded them into a shared space?



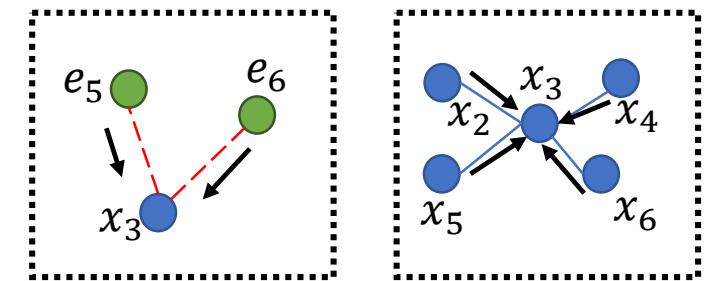
Solution 1 – Multi-relation Representation Learning



Step1: Initialize

$$\begin{array}{c} [0,0,1,0,0,0,\dots] \\ \downarrow \\ x_3 \\ [0.052,0.712,0.52,\dots] \end{array}$$

Step2: Message passing



$$z_i^{rel} = \frac{1}{|\mathcal{N}_i^{rel}|} \sum_{v_j \in \mathcal{N}_i^{rel}} W_{rel}^{(l)} h_j^{(l)}$$

Step3: jointly aggregate the message
And update the

$$h_i^{(l+1)} = \sigma \left(\sum_{rel \in \mathcal{R}} W_{agg} z_i^{rel} + W_0^{(l)} h_i^{(l)} \right)$$

Challenge 2 – Learning for Observation Probability

For P_0 : there are too roads with high relevance with the point x_2



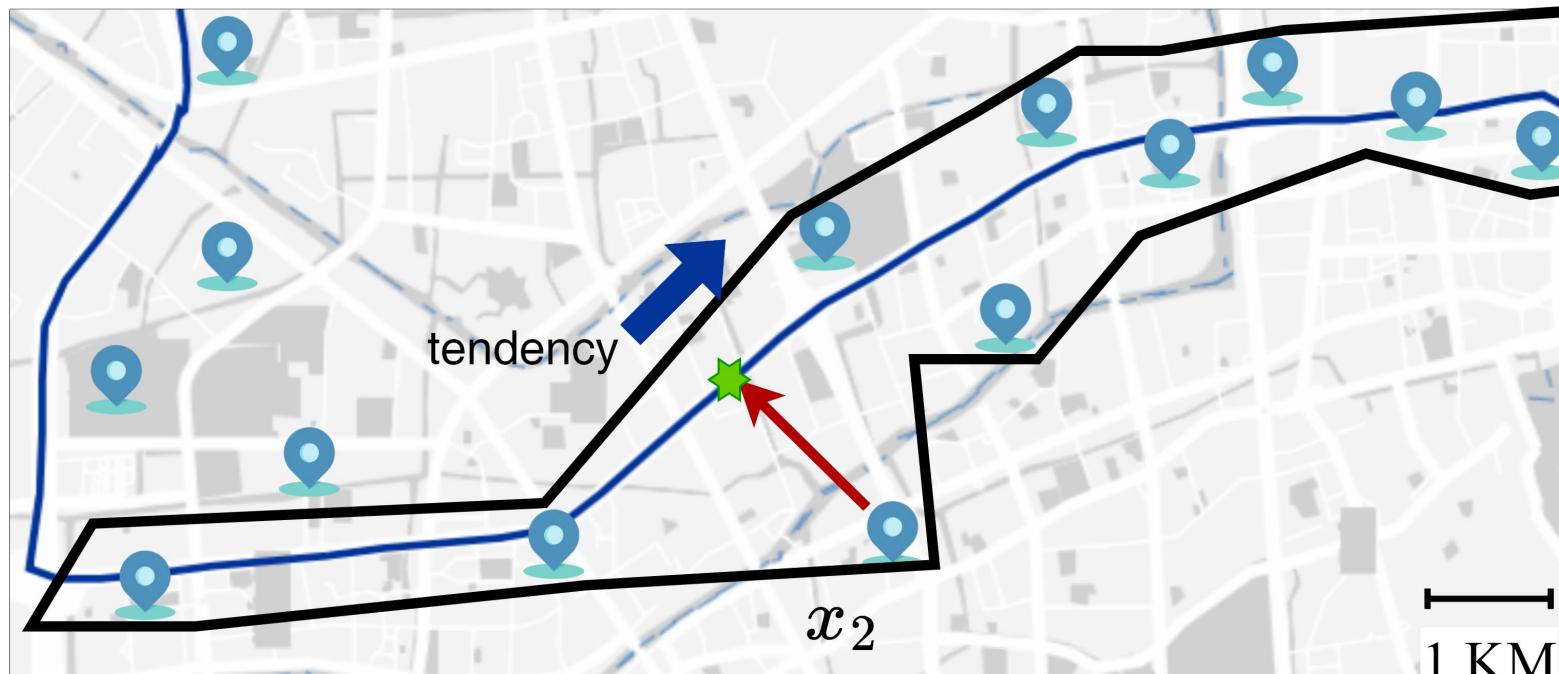
cellular trajectory point



traveled path

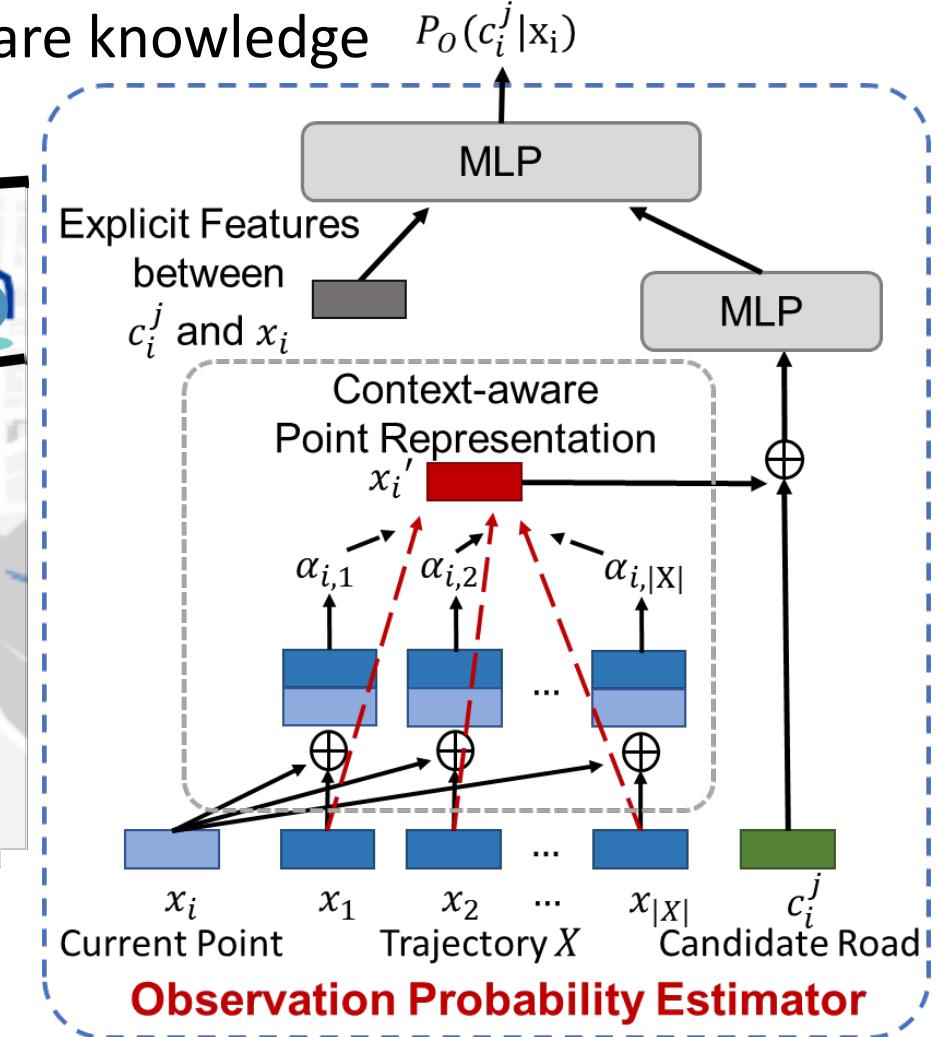
Solution 2 – Learning for Observation Probability

For P_O : capture the implicit point-road with context-aware knowledge



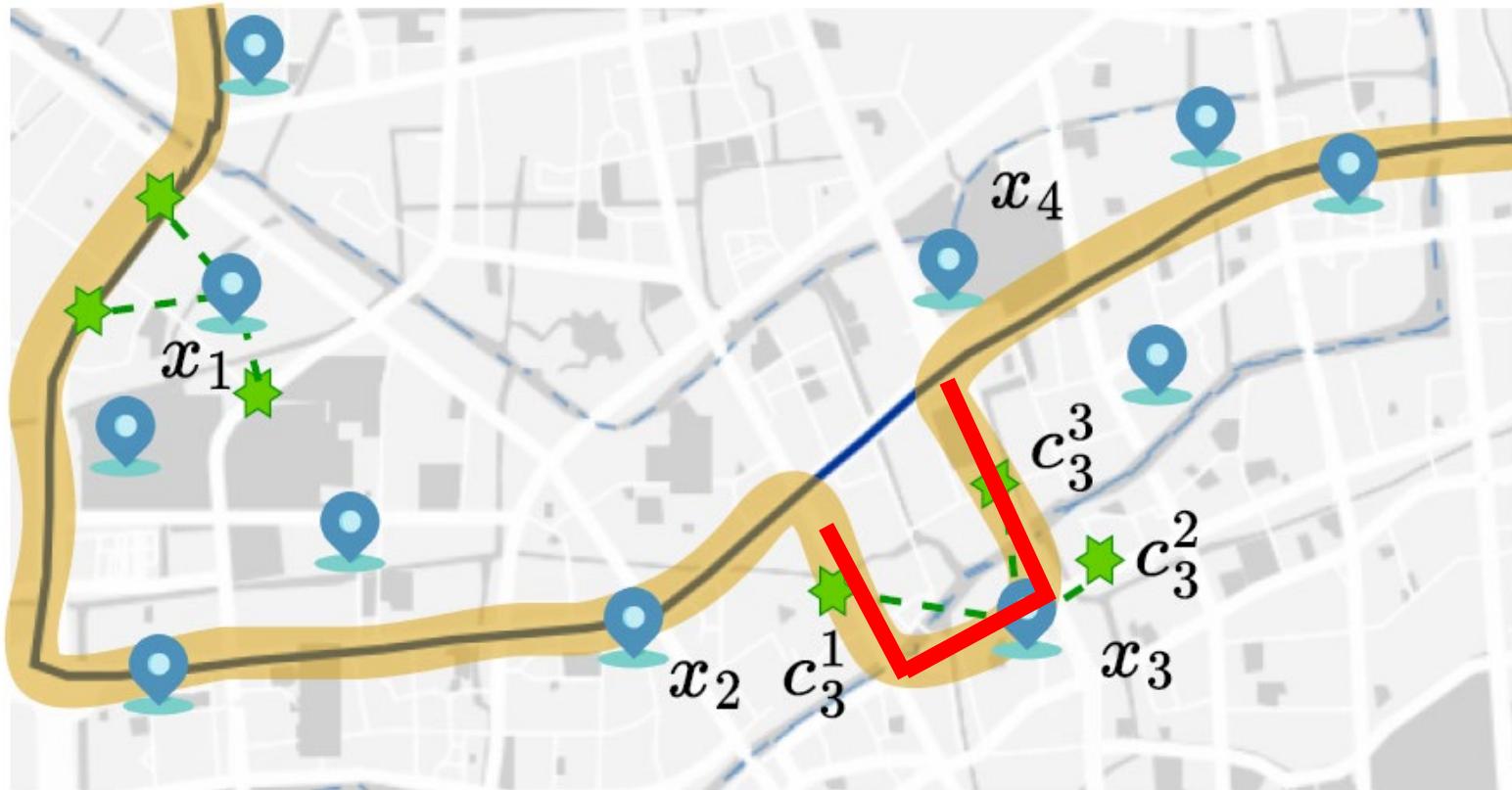
cellular trajectory point

traveled path



Challenge 3 – Learning for Transition Probability

For P_T : how to test the detour of the moving path?



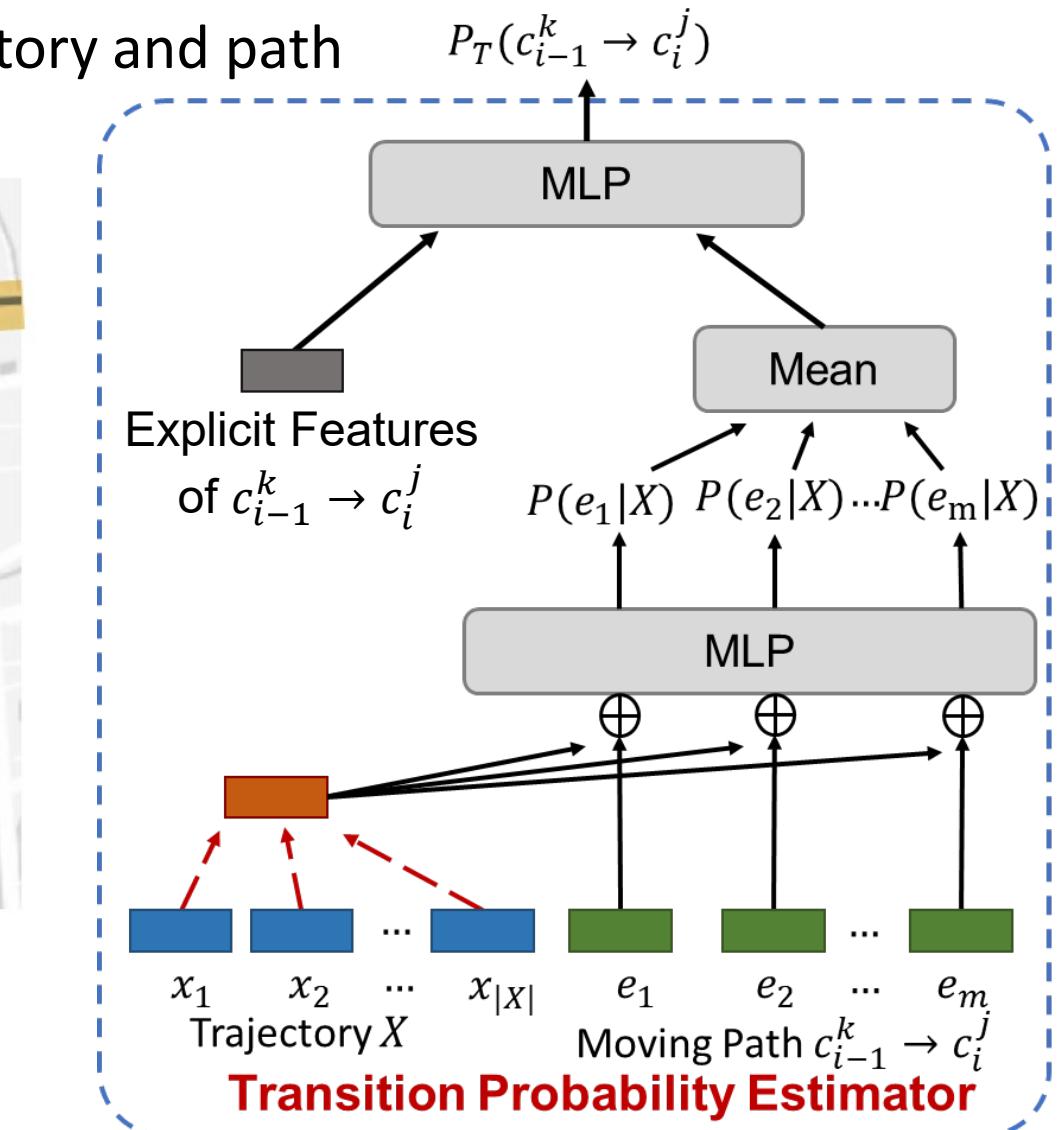
matching result

Solution 3 – Learning for Transition Probability

For P_T : capture the implicit features between trajectory and path

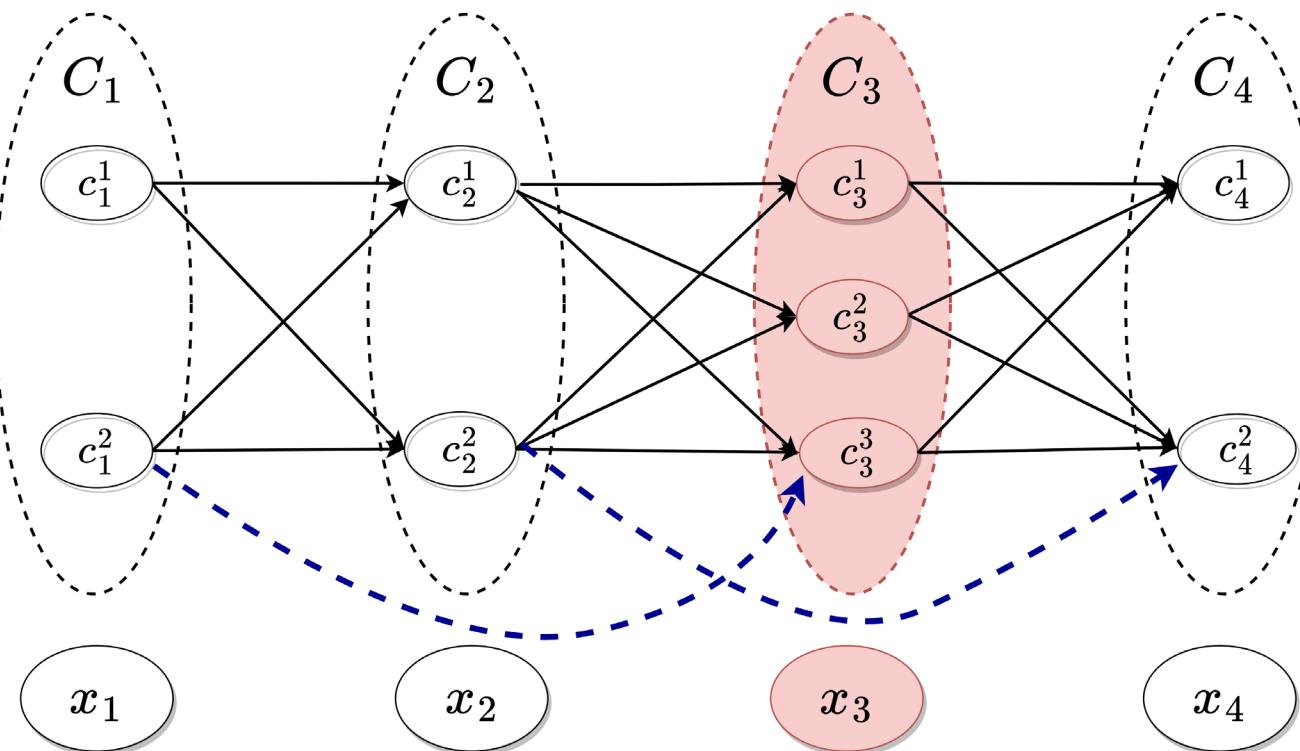
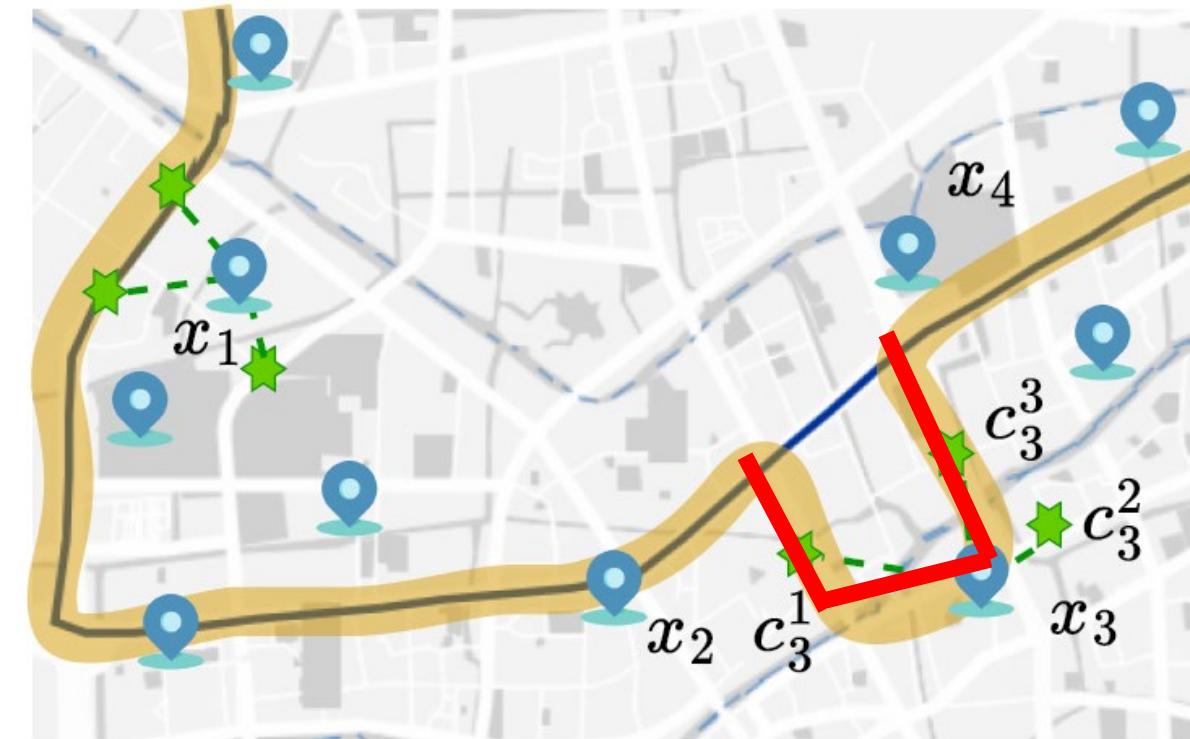


matching result



Challenge 4 – Improved Lattice Graph

how to remedy the detour of the moving path?

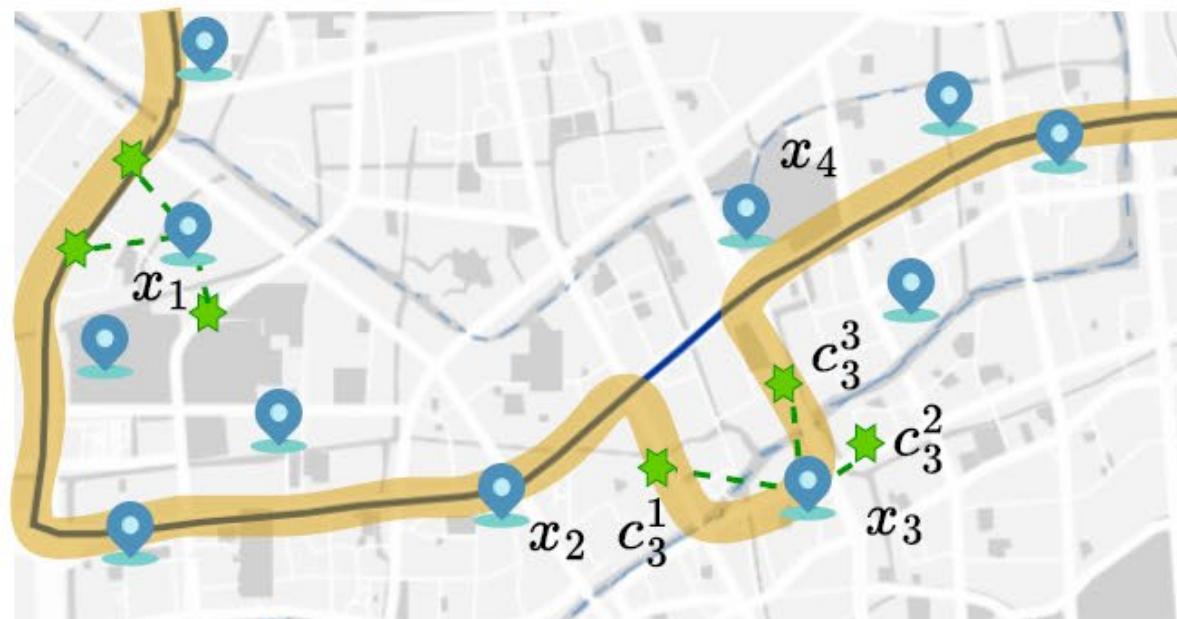


matching result

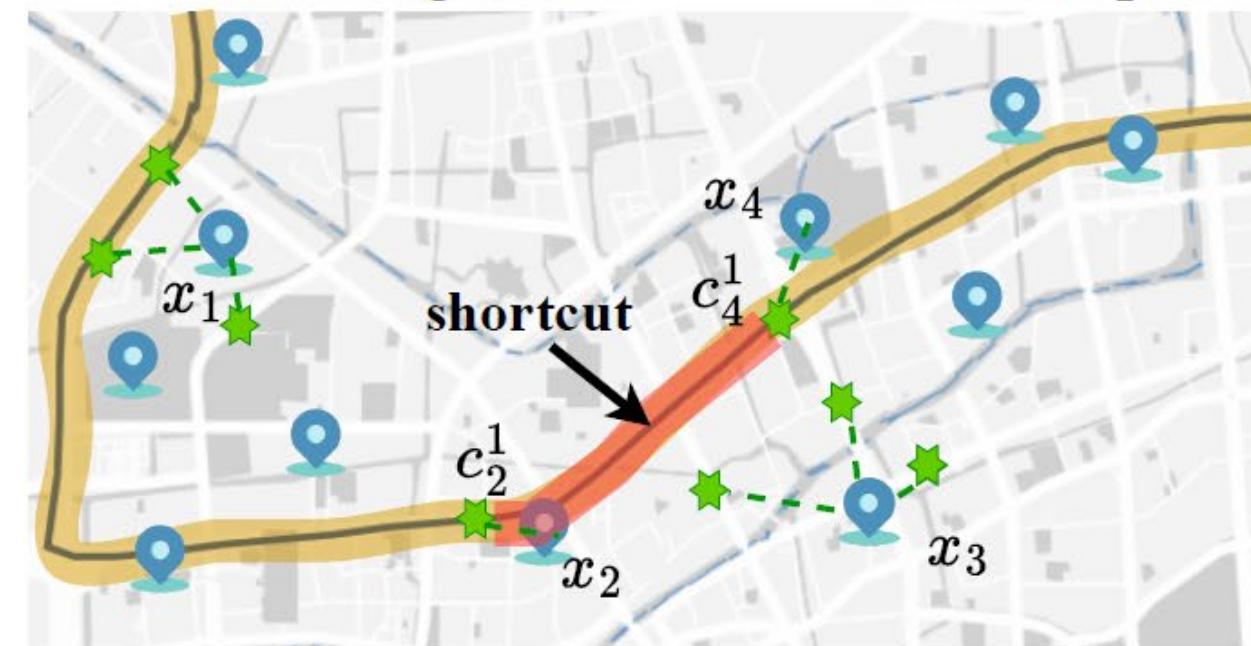
Solution 4 – Improved Lattice Graph

using shortcuts to provide chances to skip the unqualified candidate set

📍 cellular trajectory point ⚪ candidate road



█ matching result — traveled path



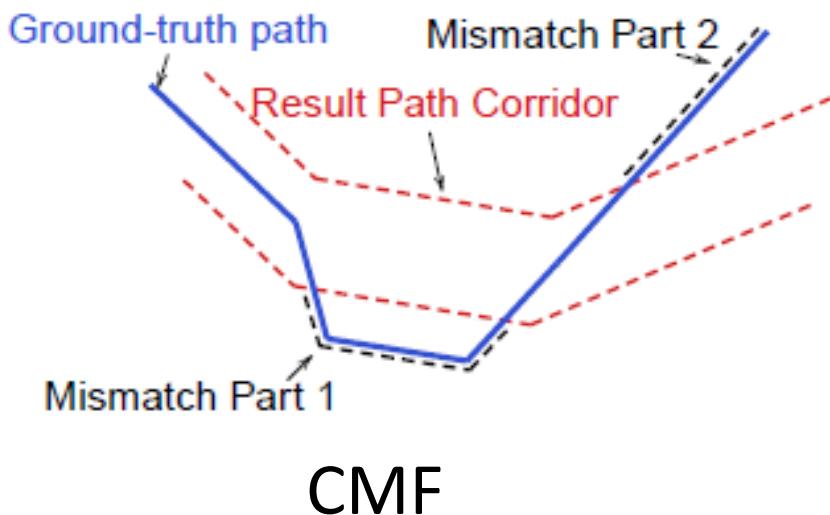
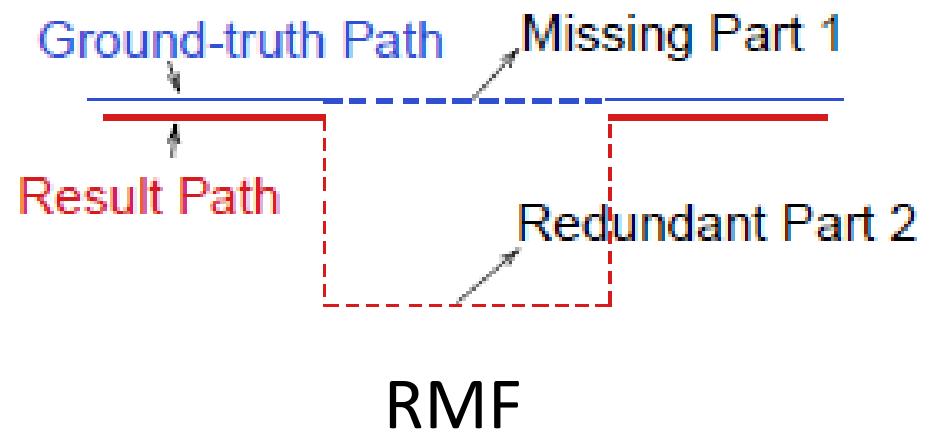
Experiment - Dataset

category	Hangzhou	Xiamen
road segments	92,913	64,828
intersections	67,330	37,591
all cellular trajectory points	3.61 million	1.18 million
all GPS trajectory points	9.73 million	4.98 million
cellular trajectory points per trajectory	34	40
GPS trajectory points per trajectory	81	88
average cellular sampling interval (s)	67	42
maximum cellular sampling interval (s)	247	185
average cellular sampling distance (m)	730	650
median cellular sampling distance (m)	493	455

DATASET CHARACTERISTIC

Experiment - Evaluation criteria

- Precision and Recall
- Route Mismatch Fraction (RMF)
- Corridor Mismatch Fraction (CMF)

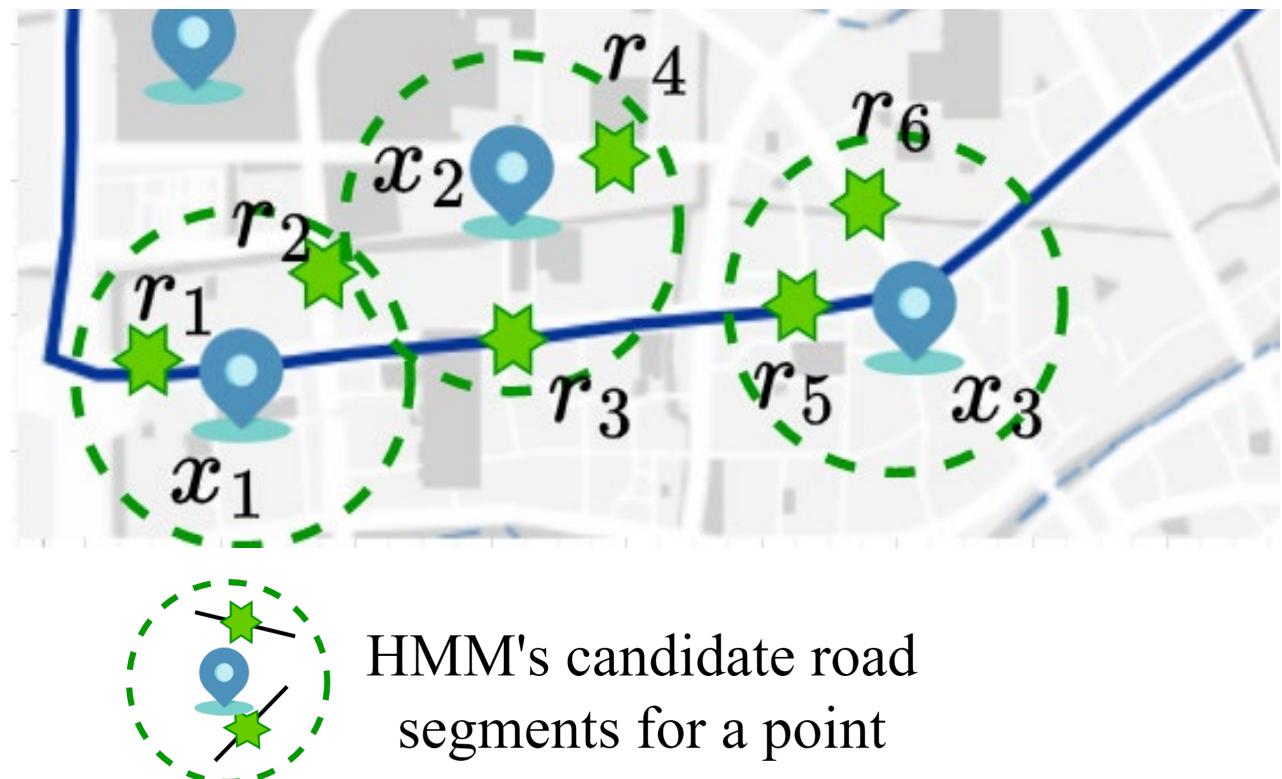


$$RMF = \frac{\sum \text{length of mismatched road segments}}{\text{length of the ground-truth path}}$$

$$CMF = \frac{\sum \text{corridor uncovered length}}{\text{length of the ground-truth path}}$$

Experiment - Evaluation criteria

- Precision and Recall
- Route Mismatch Fraction (RMF)
- Corridor Mismatch Fraction (CMF)
- Hitting Ratio (HR)
- Average inference Time (Avg Time)



Experiment – Overall Performance

HMM based methods

Dataset Metric	Precision	Recall	Hangzhou			Xiamen		
			RMF	CMF50	Avg Time (s)	Precision	Recall	RMF
Methods designed for GPS trajectory map-matching								
STM [8]	0.388	0.476	1.237	0.225	0.040	0.411	0.498	1.050
IVMM [10]	0.409	0.518	1.125	0.188	0.101	0.428	0.529	0.936
IEM [32]	0.430	0.522	1.024	0.178	0.045	0.451	0.537	0.889
DeepMM [37]	0.446	0.544	0.881	0.172	0.951	0.478	0.568	0.785
MCM [34]	0.449	0.552	0.893	0.169	0.033	0.479	0.572	0.780
TransformerMM [38]	0.455	0.552	0.838	0.170	1.667	0.483	0.577	0.769
Methods designed for CTMM								
CLSTERS [41]	0.443	0.551	0.922	0.173	0.043	0.470	0.563	0.805
SNet [12]	0.446	0.555	0.891	0.169	0.034	0.475	0.565	0.792
THMM [42]	0.461	0.562	0.815	0.165	0.041	0.486	0.583	0.767
DMM [15]	0.467	0.566	0.784	0.163	0.853	0.489	0.594	0.755
Our method								
LHMM	0.516	0.613	0.670	0.126	0.032	0.547	0.667	0.641
Improved	10.49%	8.30%	14.54%	22.69%	3.03%	11.86%	12.28%	8.79%
								15.09%
								5.12%

Seq2Seq based methods

Experiment – Ablation Results

Dataset	Variant	Precision	CMF50	HR
Hangzhou	LHMM	0.516	0.126	0.953
	LHMM-E	0.457	0.142	0.931
	LHMM-H	0.489	0.136	0.942
	LHMM-O	0.428	0.178	0.920
	LHMM-T	0.472	0.155	0.926
	LHMM-S	0.484	0.140	0.937
	STM	0.388	0.225	0.874
	STM+S	0.405	0.189	0.911
Xiamen	LHMM	0.545	0.125	0.965
	LHMM-E	0.494	0.144	0.938
	LHMM-H	0.517	0.142	0.942
	LHMM-O	0.462	0.158	0.931
	LHMM-T	0.524	0.135	0.952
	LHMM-S	0.516	0.139	0.944
	STM	0.411	0.198	0.882
	STM+S	0.432	0.170	0.915

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Summary

- we have developed a learning-enhanced HMM map-matching approach for cellular trajectories.
- A representation learning component is designed to fully capture multi-relational information tailored for the CTMM task.
- A learned observation probability captures the implicit context-aware correlation between roads and points for better positioning denoising, and a learned transition probability models the hidden relevance between moving paths and trajectories.
- These two probabilities then guide the path-finding process on an improved candidate graph.