

Academic Integrity Statement

I declare the following statements to be true:

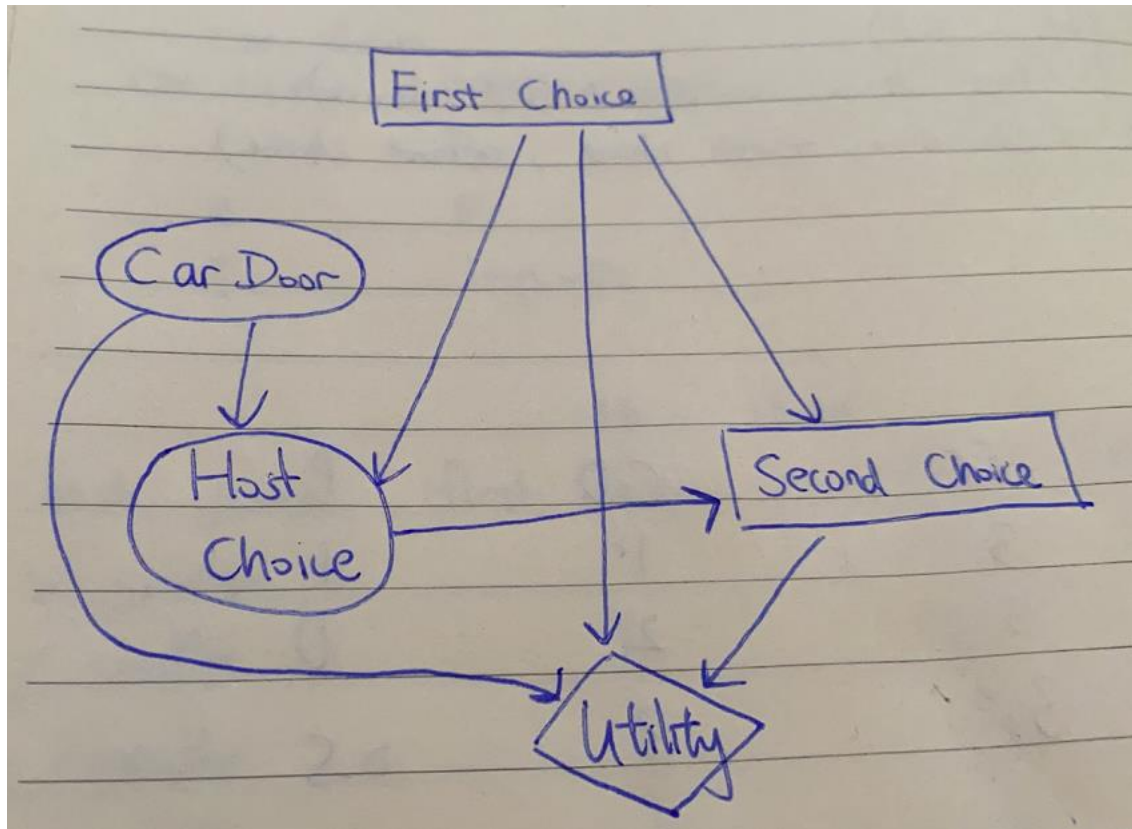
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- I have not shared and will not share any of my code with anyone at any point.
- I have not posted and will not post my code on any public or private forum or website.
- I have not discussed and will not discuss the contents of this assessment with anyone at any point.
- I have not posted and will not post the contents of this assessment and its solutions on any public or private forum or website.
- I will not search for assessment solutions online.
- I am aware that misconduct related to assessments can result in significant penalties, possibly including failure in the course and suspension (this is covered in Policy 71: <https://uwaterloo.ca/secretariat/policies-procedures-guidelines/policy-71>).

Failure to accept the integrity policy will result in your assignment not being graded.

By typing or writing my full legal name below, I confirm that I have read and understood the academic integrity statement above

Jennifer Shi

1 Decision Network for "Monty Hall" (28 marks)



Car Door	
Car Door	Prob(Car Door)
1	p_1
2	p_2
3	$1-p_1-p_2$

Host Choice			
Host Choice	First Choice	Car Door	Prob(Host Choice Car Door and First Choice)
Smaller	1	1	0.5
Bigger	1	1	0.5
Smaller	1	2	0
Bigger	1	2	1
Smaller	1	3	1
Bigger	1	3	0

Smaller	2	1	0
bigger	2	1	1
Smaller	2	2	0.5
Bigger	2	2	0.5
Smaller	2	3	1
Bigger	2	3	0
Smaller	3	1	0
Bigger	3	1	1
Smaller	3	2	1
bigger	3	2	0
Smaller	3	3	0.5
bigger	3	3	0.5

The utility function			
Car door	First choice	Second choice	U(car door, first choice, second choice)
1	1	stay	1
1	1	switch	0
1	2	stay	0
1	2	switch	1
1	3	stay	0
1	3	switch	1
2	1	stay	0
2	1	switch	1
2	2	stay	1
2	2	switch	0
2	3	stay	0
2	3	switch	1
3	1	stay	0
3	1	switch	1
3	2	stay	0
3	2	switch	1
3	3	stay	1
3	3	switch	0

2. $p_1 = 1/3$, $p_2=1/3$, $p_3=1/3$

f1(Car Door)	
Car Door	Val
1	1/3
2	1/3
3	1/3

f2(Host Choice, Car Door, First Choice)			
Host Choice	First Choice	Car Door	Val
Smaller	1	1	0.5
Bigger	1	1	0.5
Smaller	1	2	0
Bigger	1	2	1
Smaller	1	3	1
Bigger	1	3	0
Smaller	2	1	0
bigger	2	1	1
Smaller	2	2	0.5
Bigger	2	2	0.5
Smaller	2	3	1
Bigger	2	3	0
Smaller	3	1	0
Bigger	3	1	1
Smaller	3	2	1
bigger	3	2	0
Smaller	3	3	0.5
bigger	3	3	0.5

f3(Car Door, First Choice, Second Choice)			
Car door	First choice	Second choice	Val
1	1	stay	1
1	1	switch	0
1	2	stay	0
1	2	switch	1
1	3	stay	0
1	3	switch	1
2	1	stay	0
2	1	switch	1
2	2	stay	1
2	2	switch	0
2	3	stay	0
2	3	switch	1
3	1	stay	0
3	1	switch	1
3	2	stay	0
3	2	switch	1
3	3	stay	1
3	3	switch	0

Factor list: f1,f2,f3

Multiply f1 by f2 to get f4 (host choice, car door, first choice)

Factor list: f3,f4

F4(host choice,car door, first choice)			
Host Choice	Car Door	First Choice	Val
Smaller	1	1	1/6
Bigger	1	1	1/6
Smaller	2	1	0
Bigger	2	1	1/3
Smaller	3	1	1/3
Bigger	3	1	0
Smaller	1	2	0
bigger	1	2	1/3
Smaller	2	2	1/6
Bigger	2	2	1/6
Smaller	3	2	1/3
Bigger	3	2	0
Smaller	1	3	0
Bigger	1	3	1/3
Smaller	2	3	1/3
bigger	2	3	0
Smaller	3	3	1/6
bigger	3	3	1/6

Multiply f4 by f3 to get f5(host choice, car door, first choice, second choice)

Factor list: f5

	F5(host choice, First Choice, Car Door, Second Choice)			
Host choice	First Choice	Car Door	Second choice	Val
Smaller	1	1	stay	1/6
Bigger	1	1	stay	1/6
Smaller	1	1	switch	0
Bigger	1	1	switch	0
Smaller	1	2	stay	0
Bigger	1	2	stay	0
Smaller	1	2	switch	0
Bigger	1	2	switch	1/3
Smaller	1	3	stay	0
Bigger	1	3	stay	0
Smaller	1	3	switch	1/3
Bigger	1	3	switch	0
Smaller	2	1	stay	0
Bigger	2	1	stay	0
Smaller	2	1	switch	0
bigger	2	1	switch	1/3
smaller	2	2	stay	1/6
bigger	2	2	stay	1/6
smaller	2	2	switch	0
Bigger	2	2	switch	0
Smaller	2	3	stay	0
Bigger	2	3	stay	0
Smaller	2	3	switch	1/3
Bigger	2	3	switch	0
Smaller	3	1	stay	0
Bigger	3	1	stay	0
Smaller	3	1	switch	0
Bigger	3	1	switch	1/3
Smaller	3	2	stay	0
Bigger	3	2	stay	0
Smaller	3	2	switch	1/3
Bigger	3	2	switch	0
Smaller	3	3	stay	1/6
Bigger	3	3	stay	1/6
Smaller	3	3	switch	0
bigger	3	3	switch	0

Sum out Car door from f5 to get f6(host choice, first choice, second choice)

Factor list: f6

F6(host choice, first choice, second choice)			
Host choice	first choice	Second choice	val
Smaller	1	Stay	1/6
Bigger	1	Stay	1/6
Smaller	1	Switch	1/3
Bigger	1	Switch	1/3
Smaller	2	Stay	1/6
Bigger	2	Stay	1/6
Smaller	2	Switch	1/3
Bigger	2	Switch	1/3
Smaller	3	Stay	1/6
Bigger	3	Stay	1/6
Smaller	3	Switch	1/3
Bigger	3	Switch	1/3

From f6, determine the optimal policy for second choice

Optimal policy for second choice		
Host choice	first choice	Second choice
Smaller	1	Switch
Bigger	1	Switch
Smaller	2	Switch
Bigger	2	Switch
Smaller	3	Switch
Bigger	3	Switch

F7 is being created after determining the optimal policy:

F7(host choice, first choice)		
Host choice	first choice	val
Smaller	1	1/3
Bigger	1	1/3
Smaller	2	1/3
Bigger	2	1/3
Smaller	3	1/3
Bigger	3	1/3

Factor list: f8

F8(first choice)	
first choice	val
1	2/3
2	2/3
3	2/3

Optimal policy for the first choice: choose anything

Expected Utility of the optimal choice = 2/3

3. $p_1 = 0.8$, $p_2=0.1$, $p_3=0.1$

f1(Car Door)	
Car Door	Val
1	0.8
2	0.1
3	0.1

f2(Host Choice, Car Door, First Choice)			
Host Choice	First Choice	Car Door	Val
Smaller	1	1	0.5
Bigger	1	1	0.5
Smaller	1	2	0
Bigger	1	2	1
Smaller	1	3	1
Bigger	1	3	0
Smaller	2	1	0
bigger	2	1	1
Smaller	2	2	0.5
Bigger	2	2	0.5
Smaller	2	3	1
Bigger	2	3	0
Smaller	3	1	0
Bigger	3	1	1
Smaller	3	2	1
bigger	3	2	0
Smaller	3	3	0.5
bigger	3	3	0.5

f3(Car Door, First Choice, Second Choice)			
Car door	First choice	Second choice	Val
1	1	stay	1
1	1	switch	0
1	2	stay	0
1	2	switch	1
1	3	stay	0
1	3	switch	1
2	1	stay	0
2	1	switch	1
2	2	stay	1
2	2	switch	0
2	3	stay	0
2	3	switch	1
3	1	stay	0
3	1	switch	1
3	2	stay	0
3	2	switch	1
3	3	stay	1
3	3	switch	0

Factor list: f1,f2,f3

Multiply f1 by f2 to get f4 (host choice, car door, first choice)

Factor list: f3,f4

F4(host choice,car door, first choice)			
Host Choice	Car Door	First Choice	Val
Smaller	1	1	0.4
Bigger	1	1	0.4
Smaller	2	1	0
Bigger	2	1	0.1
Smaller	3	1	0.1
Bigger	3	1	0
Smaller	1	2	0
bigger	1	2	0.8
Smaller	2	2	0.05
Bigger	2	2	0.05
Smaller	3	2	0.1
Bigger	3	2	0
Smaller	1	3	0
Bigger	1	3	0.8
Smaller	2	3	0.1
bigger	2	3	0
Smaller	3	3	0.05
bigger	3	3	0.05

Multiply f4 by f3 to get f5(host choice, car door, first choice, second choice)

Factor list: f5

F5(host choice, First Choice, Car Door, Second Choice)				
Host choice	First Choice	Car Door	Second choice	Val
Smaller	1	1	stay	0.4
Bigger	1	1	stay	0.4
Smaller	1	1	switch	0
Bigger	1	1	switch	0
Smaller	1	2	stay	0
Bigger	1	2	stay	0
Smaller	1	2	switch	0
Bigger	1	2	switch	0.1
Smaller	1	3	stay	0
Bigger	1	3	stay	0
Smaller	1	3	switch	0.1
Bigger	1	3	switch	0
Smaller	2	1	stay	0
Bigger	2	1	stay	0
Smaller	2	1	switch	0
bigger	2	1	switch	0.8
smaller	2	2	stay	0.05
bigger	2	2	stay	0.05
smaller	2	2	switch	0
Bigger	2	2	switch	0
Smaller	2	3	stay	0
Bigger	2	3	stay	0
Smaller	2	3	switch	0.1
Bigger	2	3	switch	0
Smaller	3	1	stay	0
Bigger	3	1	stay	0
Smaller	3	1	switch	0
Bigger	3	1	switch	0.8
Smaller	3	2	stay	0
Bigger	3	2	stay	0
Smaller	3	2	switch	0.1
Bigger	3	2	switch	0
Smaller	3	3	stay	0.05
Bigger	3	3	stay	0.05
Smaller	3	3	switch	0
bigger	3	3	switch	0

Sum out Car door from f5 to get f6(host choice, first choice, second choice)

Factor list: f6

F6(host choice, first choice, second choice)			
Host choice	first choice	Second choice	val

Smaller	1	Stay	0.4
Bigger	1	Stay	0.4
Smaller	1	Switch	0.1
Bigger	1	Switch	0.1
Smaller	2	Stay	0.05
Bigger	2	Stay	0.05
Smaller	2	Switch	0.1
Bigger	2	Switch	0.8
Smaller	3	Stay	0.05
Bigger	3	Stay	0.05
Smaller	3	Switch	0.1
Bigger	3	Switch	0.8

From f6, determine the optimal policy for second choice

Optimal policy for second choice		
Host choice	first choice	Second choice
Smaller	1	Stay
Bigger	1	Stay
Smaller	2	Switch
Bigger	2	Switch
Smaller	3	Switch
Bigger	3	Switch

F7 is being created after determining the optimal policy:

F7(host choice, first choice)		
Host choice	first choice	val
Smaller	1	0.4
Bigger	1	0.4
Smaller	2	0.1
Bigger	2	0.8
Smaller	3	0.1
Bigger	3	0.8

Factor list: f8

F8(first choice)	
first choice	val
1	0.9
2	0.9
3	0.9

Optimal policy for the first choice: choose 2 or 3

Expected Utility of the optimal choice = 0.9

2 Reinforcement Learning (36 marks)

1. The long term utility values for grid lecture:
- ```
[[0.705548 0.654131 0.6098 0.469813]
 [0.760959 0. 0.66902 -1.]
 [0.811043 0.867702 0.917319 1.]]
```

2. The optimal policy for grid lecture:
- ```
['down ' 'left ' 'left ' 'left ']
['down ' 'X      ' 'down ' '-1    ']
['right' 'right' 'right' '1      ']
```

3. The long term utility values for grid a4:
- ```
[[-0.133841 0.010468 0.200468 0.383342]
 [-0.267863 -0.22003 0. 0.571973]
 [-0.435932 -1. 1. 0.780025]]
```

4. The optimal policy for grid a4:
- ```
['right' 'right' 'right' 'down ']
['up     ' 'up     ' 'X      ' 'down ']
['up     ' '-1     ' '1      ' 'left ']
```