

Homework 1

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1.

a. 53_{10}

$$53 / 8 = 6 \dots 5 \quad 5$$

$$6 / 8 = 0 \dots 6 \quad 65$$

0 done

$$\text{So } 53_{10} = 65_8$$

b. FA_{16}

$$FA_{16} = 1111(F) \ 1010(A) = 1111 \ 1010_2$$

$$1111 \ 0_2 = 011(3) \ 111(7) \ 010(2) = 372_8$$

2.

a. 19_{10}

$$19 / 2 = 9 \dots 1 \ 1$$

$$9 / 2 = 4 \dots 1 \ 11$$

$$4 / 2 = 2 \dots 0 \ 011$$

$$2 / 2 = 1 \dots 0 \ 0011$$

$$1 / 2 = 0 \dots 1 \ 10011$$

0 done

$$\text{So } 19_{10} = 10011_2 = 00010011_2 \text{ (2's comp)}$$

b. -13_{10}

$$13 / 2 = 6 \dots 1 \ 1$$

$$6 / 2 \dots 3 \quad 01$$

$$3 / 2 = 1 \dots 1 \ 101$$

$$1 / 2 = 0 \dots 1 \ 1101$$

0 done

$$\text{So } 13_{10} = 1101_2 = 00001101_2$$

$$-13_{10} = 11110010_2 \text{ (1's comp)} = 11110011_2 \text{ (2's comp)}$$

c. -23_{10}

$$23 / 2 = 11 \dots 1 \ 1$$

$$11 / 2 = 5 \dots 1 \ 11$$

$$5 / 2 = 2 \dots 1 \ 111$$

$$2 / 2 = 1 \dots 0 \ 0111$$

$$1 / 2 = 0 \dots 1 \ 10111$$

0 done

$$\text{So } 23_{10} = 10111_2$$

$$-23_{10} = 11101000_2 \text{ (1's comp)} = 11101001_2 \text{ (2's comp)}$$

d. ED_{16}

$$ED_{16} = 1110(E) \ 1101(D) = 11101101_2 \text{ (2's comp)}$$

$$11101101_2 - 1 = 11101100_2 \text{ (1's comp)}$$

$$11101100_2 \text{ (1's comp)} = -00010011_2 = -19_{10}$$

3.

a. $0xABCD \text{ OR } 0x9876$

$$ABCD_{16} = 1010(A) \ 1011(B) \ 1100(C) \ 1101(D) = 1010 \ 1011 \ 1100 \ 1101_2$$

$$9876_{16} = 1001(9) \ 1000(8) \ 0111(7) \ 0110(6) = 1001 \ 1000 \ 0111 \ 0110_2$$

$$1010 \ 1011 \ 1100 \ 1101_2$$

OR

$$1001 \ 1000 \ 0111 \ 0110_2$$

$$= 1011 \ 1011 \ 1111 \ 1111_2$$

$$= BBFF_{16}$$

$$= 0xBBFF$$

b. $0xFEED \text{ AND } (\text{NOT}(0xBEEF))$

$$FEED_{16} = 1111(F) \ 1110(E) \ 1110(E) \ 1101(D) = 1111 \ 1110 \ 1110 \ 1101_2$$

$$BEEF_{16} = 1011(B) \ 1110(E) \ 1110(E) \ 1111(F) = 1011 \ 1110 \ 1110 \ 1111_2$$

$$\text{Not}(0xBEEF) = 0100 \ 0001 \ 0001 \ 0000_2$$

$$1111 \ 1110 \ 1110 \ 1101_2$$

AND

$$0100 \ 0001 \ 0001 \ 0000_2$$

$$= 0100 \ 0000 \ 0000 \ 0000$$

$$= 4000_{16}$$

$$= 0x4000$$

4.

a. $01000010 \ 01100101 \ 01110011 \ 01110100 \ 00100000 \ 01101111 \ 01100110$

$$01000010_2 \ 01100101_2 \ 01110011_2 \ 01110100_2 \ 00100000_2 \ 01101111_2 \ 01100110_2$$

= 66₁₀ 101₁₀ 115₁₀ 116₁₀ 111₁₀ 51₁₀

By ASCII table

= B e s t o 3

b. 01001100 01110101 01100011 01101011 00100001
01001100₂ 01110101₂ 01100011₂ 01101011₂ 00100001₂

= 76₁₀ 117₁₀ 99₁₀ 107₁₀ 33₁₀

By ASCII table

= L u c k !

5.

a. 5 bits

14 / 2 = 7.....0 0

7 / 2 = 3.....1 10

3 / 2 = 1.....1 110

1 / 2 = 0.....1 1110

0 done

14₁₀ = 01110

-14₁₀ = 10010 (2's comp)

b. 6 bits

14₁₀ = 001110

-14₁₀ = 110010 (2's comp)

c. 7 bits

14₁₀ = 0001110

-14₁₀ = 1110010 (2's comp)

From the experiments, I found two's complement is easier to store ints, when you need to extend the width of the register the value is being stored in. With two's complement, storing a less bit number in a high bit register is a matter of repeating its most significant bit. On the other hand, if we just simply flip the first bit, we would need to clear the existing bit, which is an extra operation in addition to padding.

6. Code is attached

Test:

```
Enter 2 positive integers for calculation:
2 10
Please choose an operation from (+ or -)+
2+10 = 12
2's comp: 00000000000000000000000000001100
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```
Enter 2 positive integers for calculation:
4 50
Please choose an operation from (+ or -)-
4-50 = -46
2's comp: 11111111111111111111111111010010
```

```
Enter 2 positive integers for calculation:
2 2
Please choose an operation from (+ or -)-
2-2 = 0
2's comp: 00000000000000000000000000000000
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