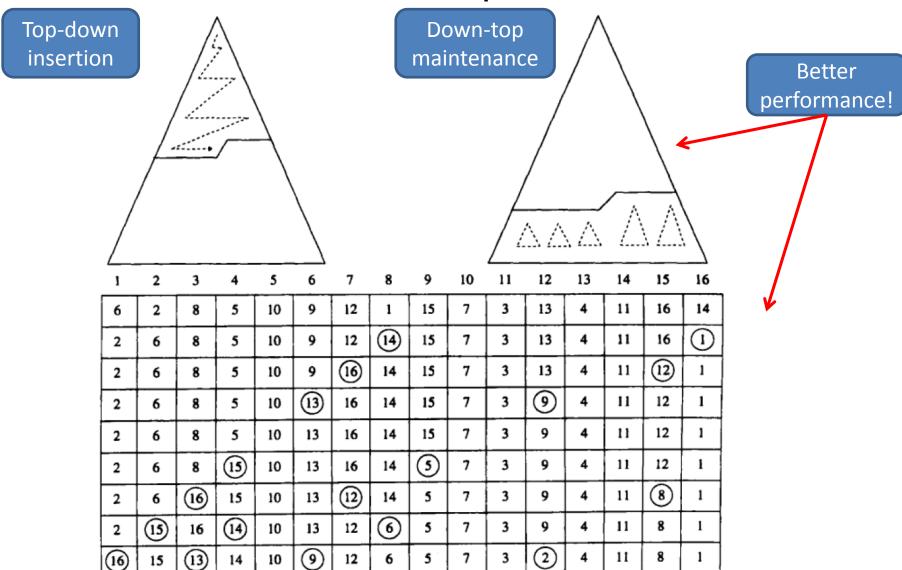
heap sort

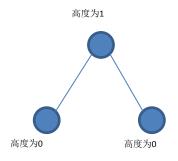
```
算法 Heapsort (X, n)
输入: X(下标从1至n的数组)
输出: X (排序后的数组 )
begin
  Build_Heap (X); {见下文}
  for i := n downto 2 do

swap (A[1], A[i]); O(n \lg n)
     Rearrange Heap (i-1)
     {基本等同于图 4.7 中的程序 Remove_Max_from_Heap}
end
```

图 6.13 算法 Heapsort

Two ways to build heap substantial different performance!

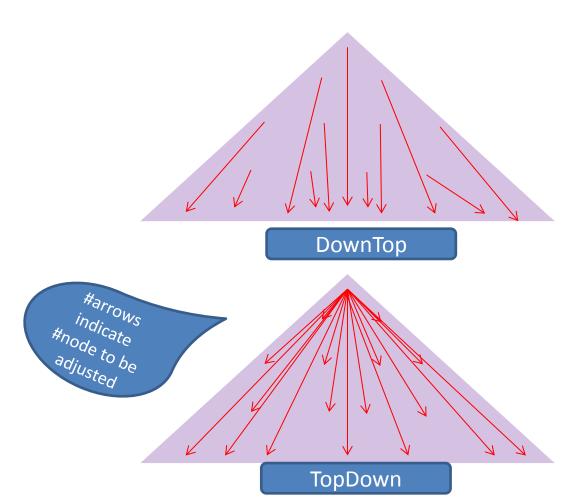




What if Top-down

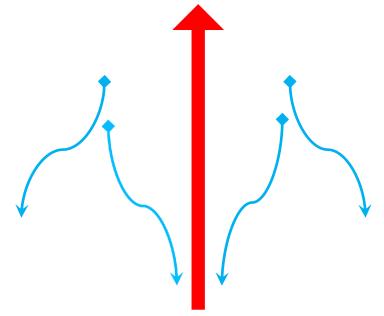
- 6
- 62
- 826
- 8562
- 108625
- 0 0 0 0

Swap次数超过自底而上法! Performance speed up ~ approx 50%.



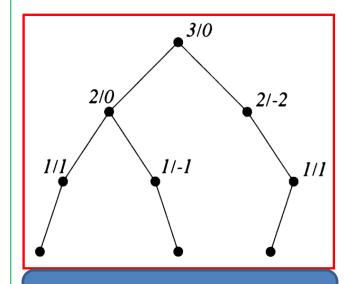
Down-top maintenance

- 隐式建立完全二叉树,将每个节点看做一个子堆的堆头.
- 倒序逐个处理元素, 对其代表的子堆, 做自上而下的维护.



Some Properties of Trees

- Level The level of a node is defined by 1 + the number of connections between the node and the root.
- Height of tree –The height of a tree is the number of edges on the longest downward path between the root and a leaf.
- Height of node –The height of a node is the number of edges on the longest downward path between that node and a leaf.
- Depth –The depth of a node is the number of edges from the node to the tree's root node.



本textbook可以此图为范例!

GPU parallel sorting

 http://http.developer.nvidia.com/GPUGems3/ gpugems3_ch39.html

 https://research.nvidia.com/sites/default/files/ /publications/nvr-2008-003.pdf

http://en.wikipedia.org/wiki/NVIDIA_GPU

Max & Min

- Non-divide-and-conquer method is worse.
- Best complexity: 3n/2. (step=3: 5n/3, step=4: 6n/4)

[So each time taking a **pair** out is the best.]

K-th Min

问题 已知序列 $S=x_1, x_2, \dots, x_n$ 以及整数 k, $1 \le k \le n$, 试查找 S 中第 k 小的数。

```
算法 Selection (X, n, k)
输入: X(下标从 1 至 n 的数组 ) 和 k(某个整数 )
输出: S ( 第 k 小的数; 数组 X 也做过变动 )
begin
                                                                   pivot
   if (k < 1) or (k > n) then print "error"
   else
      S := Select(1, n, k)
end
procedure Select (Left, Right, k);
begin
                            错误! Select= X[Left]
   if Left = Right then
      Select := Left
                                                             Selection
   else
                                                       常用于查找中数,
      Partition (X, Left, Right); {见图 6.9}
                                                           why?Pivot is
      Let Middle be the output of Partition;
                                                     approaching the middle
      if Middle – Left + 1 \ge k then
         Select (Left, Middle, k)
      else
         Select (Middle +1, Right, k - (Middle - Left + 1))
end
```

图 6.16 算法 Selection

Majority

令 E 是整数序列 x_1, x_2, \dots, x_n 。 E 中 x 的重数(multiplicity)是 x 在 E 中出现的次数。如果某个数 z 的重数大于 n/2,则它就是 E 中的众数(majority)。

- 众数必是中数; 若不是,则众数不存在.
- 如果Selection(n/2)返回的中数不是众数,则 众数不存在!

```
中数法:
Majority(X,n)
{
    int m = Selection(X, n, n/2);
    return CheckMajority(m);
}
```

[观察]众数保留:

若 $x_i \neq x_j$,且两个数都被删除,那么原来集合中的众数现在仍为新集合中的众数。

voting: 算法 Majority (X, n) **输入**: X (有n 个正数的数组) **输出:** *Majority* (X中的众数; 若不存在, 则输出-1) begin C := X[1];M := 1: $\{ \text{首次扫描: 删去除 } C \text{ 以外的所有选票} \}$ for i := 2 to n do if M = 0 then Works for dominant voting C := X[i]; (e.g. win over 60% votes) M := 1else if C = X[i] then M := M + 1else M := M - 1: $\{$ 第二次扫描:检验 C 是否为众数 $\}$ if M = 0 then Majority := -1else Count := 0:for i := 1 to n do if X[i] = C then Count := Count + 1; if Count > n/2 then Majority := C

else Majority := -1

end

Compression!

Synonyms: source coding, bit-rate reducing

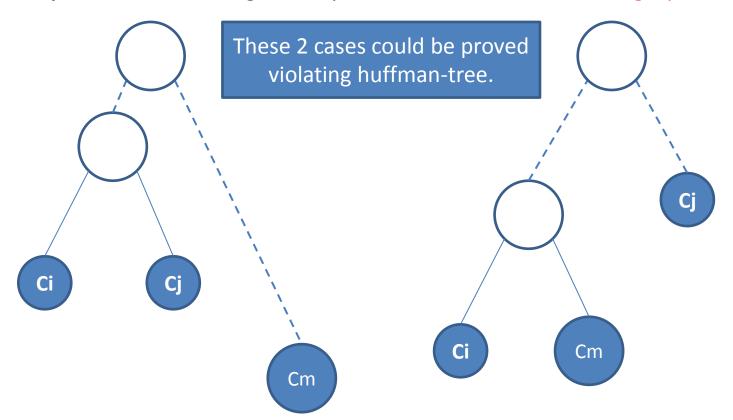
- Huffman-encoding for text bit-streaming
 - -lossless data compression
 - -variable length encoding.

Huffman Tree(optimal B-tree)

- Degree(vi) = 2 or 0;
- With lowest sum-weighted-path-length.

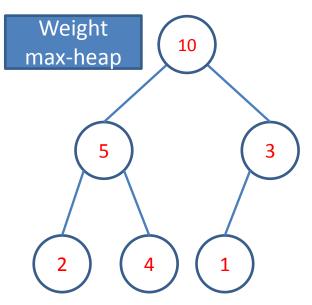
property:

If ci, cj has the lowest weights, they are at the lowest level, sharing a parent node.



Huffman-encoding

```
算法 Huffman_Encoding (S, f)
输入:S(字符串)和f(字频数组)
输出: T(S)的霍夫曼树)
begin
   insert all characters into a heap H according to their frequencies;
   while H is not empty do
      if H contains only one character X then
         make X the root of T
      else
         pick two characters X and Y with lowest frequencies
            and delete them from H;
         replace X and Y with a new character Z whose frequency is
            the sum of the frequencies of X and Y:
         insert Z to H:
         make X and Y children of Z in T {Z 仍没有父节点}
```



end

算法 Huffman_Encoding

以正常方式minHeap建立编码树的流程图在书上106页红色图片

下一页是maxHeap的,推出的元素顺序 没有错,但是这maxHeap压根没帮上忙!

