Homework #1

1. k-NN: Classification



X is three-dimensional. X belongs to one of four classes as follows:

- Class A: (7, 8, 200), (8, 9, 220), (6, 6, 180), (7.5, 8.5, 210), (6.5, 7, 190)
- Class B: (5, 5, 100), (5.5, 4.5, 120), (6, 5, 130), (5, 6, 110), (5.5, 5, 115)
- Class C: (2, 2, 50), (2.5, 2.5, 55), (1.5, 2, 45), (2, 2.5, 52), (3, 2, 58)
- Class D: (10, 3, 120), (12, 3.1, 110), (11, 2.9, 130), (14, 3, 120), (15, 2.6, 110)

A new sample X = (8,9,111) is given. Determine its class with k-NN

- a) Use k = 3 and L2 Distance
- b) Use k = 5 and L2 Distance
- c) Use weight-base k-NN. k = 3 and weight is $w(x) = \exp(-dist(x, x'))$
- d) Use weight-base k-NN. k = 5 and weight is $w(x) = \exp(-dist(x, x'))$
- e) Let X=(a,b,c). Which facor in (a, b, c) would predominantly affect the class determination?

2. k-NN: Regression



We want to predict the Price using Age, Horse_Power, Brand and MPG using k-NN. A new sample is (6, 200, 5, 30). Make a prediction on its Price

- a) k=3
- b) k=5
- c) Use weight-based k-NN. k=3, $w(x) = \exp(-dist(x, x'))$
- d) Use weight-based k-NN. k=5, $w(x) = \exp(-dist(x, x'))$

| id | Age | Horse_Power | Brand | MPG | Price |
|----|-----|-------------|-------|-----|--------|
| 1 | 2 | 200 | 4 | 27 | 30,000 |
| 2 | 5 | 150 | 3 | 35 | 20,000 |
| 3 | 3 | 180 | 4 | 25 | 25,000 |
| 4 | 1 | 230 | 2 | 10 | 21,000 |
| 5 | 5 | 180 | 5 | 40 | 38,000 |
| 6 | 4 | 210 | 3 | 30 | 31,000 |