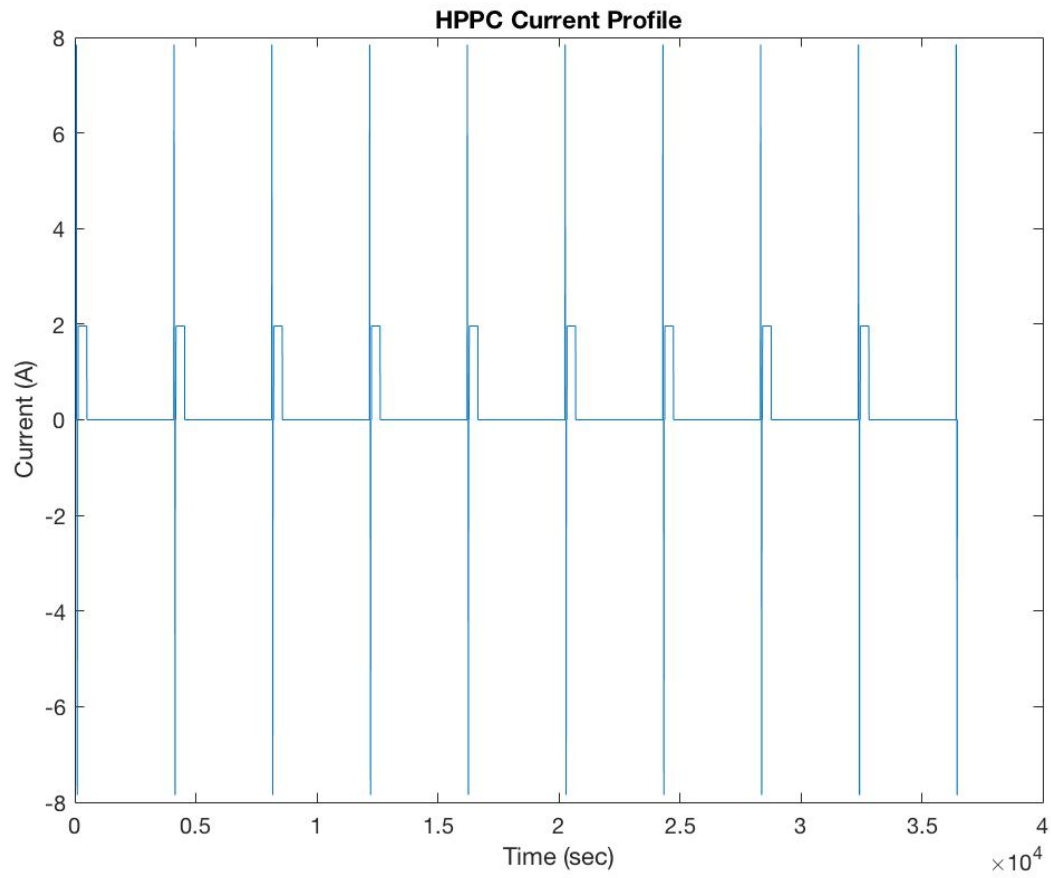
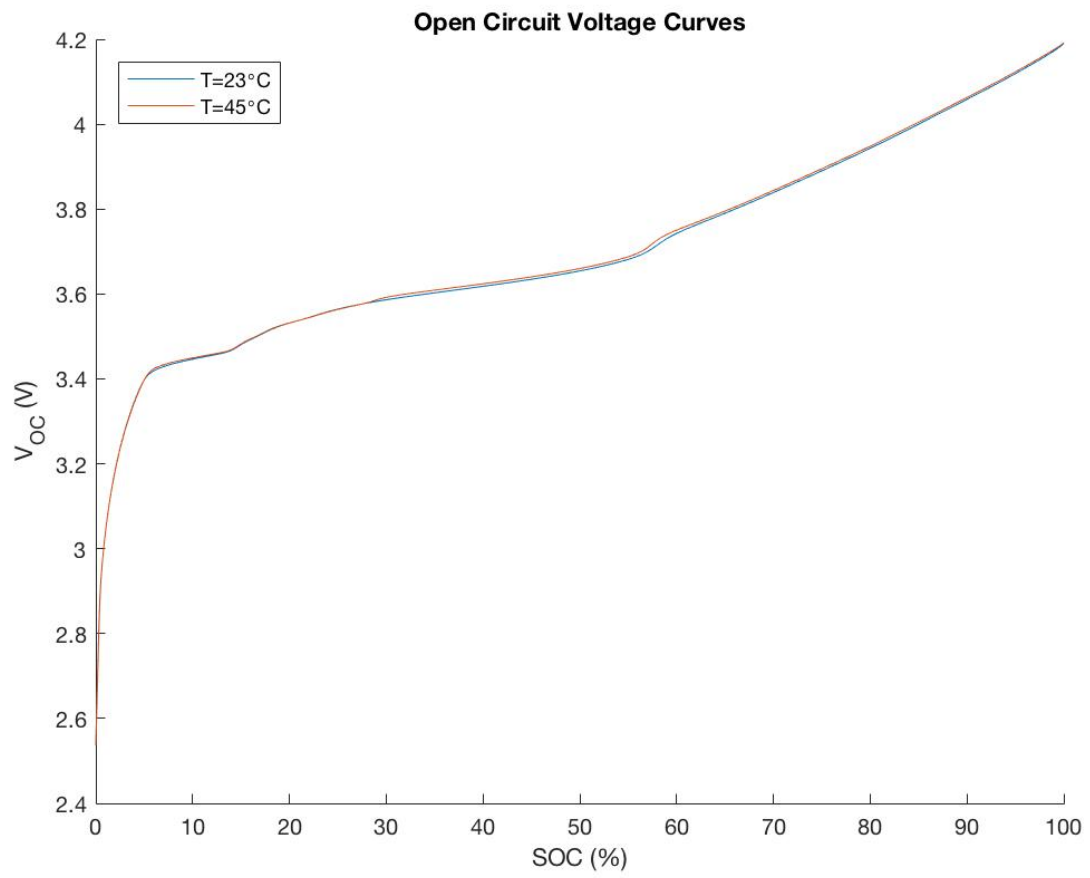


**Problem 1.1)**

The capacity of the battery at 1C discharge was found to be 1.962 Ah. Based on this capacity, a 1C discharge current is 1.962 A and a 4C discharge current is 7.849 A. The sign convention for current in this problem is positive for discharge.



**Problem 1.2)**



**Problem 2a) Initial Parameter Guesses using Graphical Method**

<b>T = 23°C</b>			
<b>SOC</b>	<b>R0</b>	<b>R1</b>	<b>C1</b>
90%	0.03038	0.00654	1841.0
80%	0.03084	0.00761	1582.7
70%	0.03059	0.00740	1626.3
60%	0.03013	0.00638	1884.9
50%	0.02824	0.00485	2274.8
40%	0.02895	0.00490	2456.5
30%	0.02962	0.00495	2225.9
20%	0.03181	0.00557	1800.6

<b>T = 45°C</b>			
<b>SOC</b>	<b>R0</b>	<b>R1</b>	<b>C1</b>
90%	0.02318	0.00526	1909.8
80%	0.02344	0.00623	1610.4
70%	0.02364	0.00649	1856.9
60%	0.02364	0.00608	1983.4
50%	0.02221	0.00403	2486.4
40%	0.02221	0.00393	2554.8
30%	0.02262	0.00398	2521.8
20%	0.02349	0.00419	2399.9

**Problem 2b) Parameter Results from fminsearch**

<b>fminsearch Results: T=23°C</b>			
<b>SOC</b>	<b>R0</b>	<b>R1</b>	<b>C1</b>
90%	2.96E-02	1.17E-02	1.01E+03
80%	2.98E-02	1.52E-02	8.78E+02
70%	2.95E-02	1.77E-02	8.72E+02
60%	2.85E-02	1.64E-02	8.68E+02
50%	2.73E-02	9.35E-03	1.20E+03
40%	2.82E-02	1.10E-02	1.22E+03
30%	2.85E-02	1.08E-02	1.15E+03
20%	3.03E-02	9.63E-03	1.01E+03

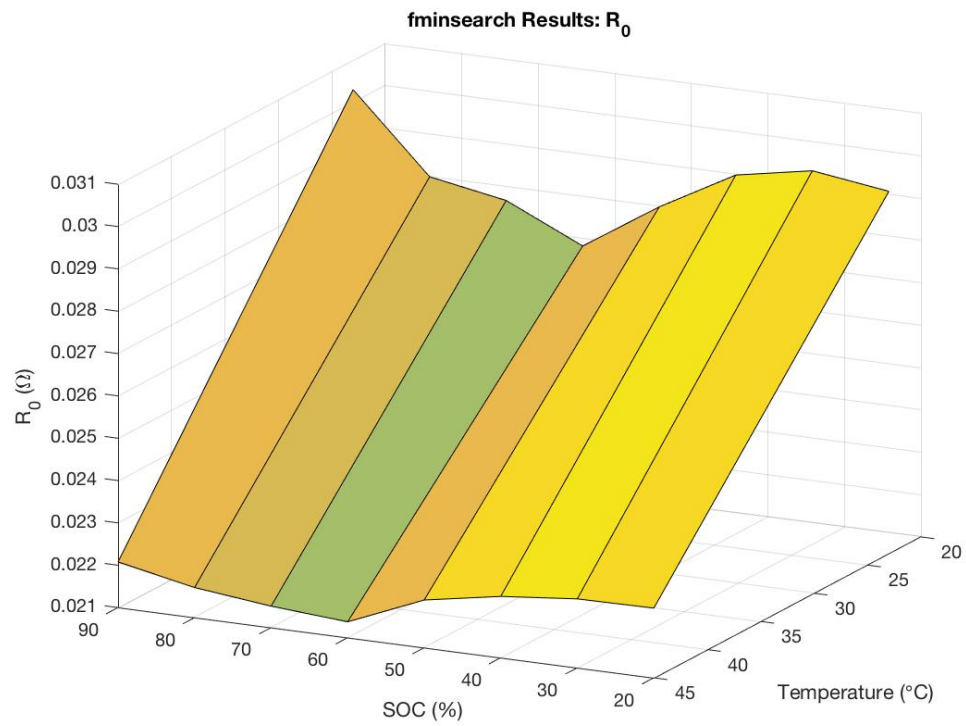
<b>fminsearch Results: T=45°C</b>			
<b>SOC</b>	<b>R0</b>	<b>R1</b>	<b>C1</b>
90%	2.26E-02	8.19E-03	1.24E+03
80%	2.26E-02	9.82E-03	1.07E+03
70%	2.24E-02	1.10E-02	1.00E+03
60%	2.21E-02	1.15E-02	9.93E+02
50%	2.14E-02	6.58E-03	1.43E+03
40%	2.15E-02	7.67E-03	1.49E+03
30%	2.17E-02	6.54E-03	1.44E+03
20%	2.21E-02	5.54E-03	1.30E+03

### Problem 2c) Parameter Results from Genetic Algorithm

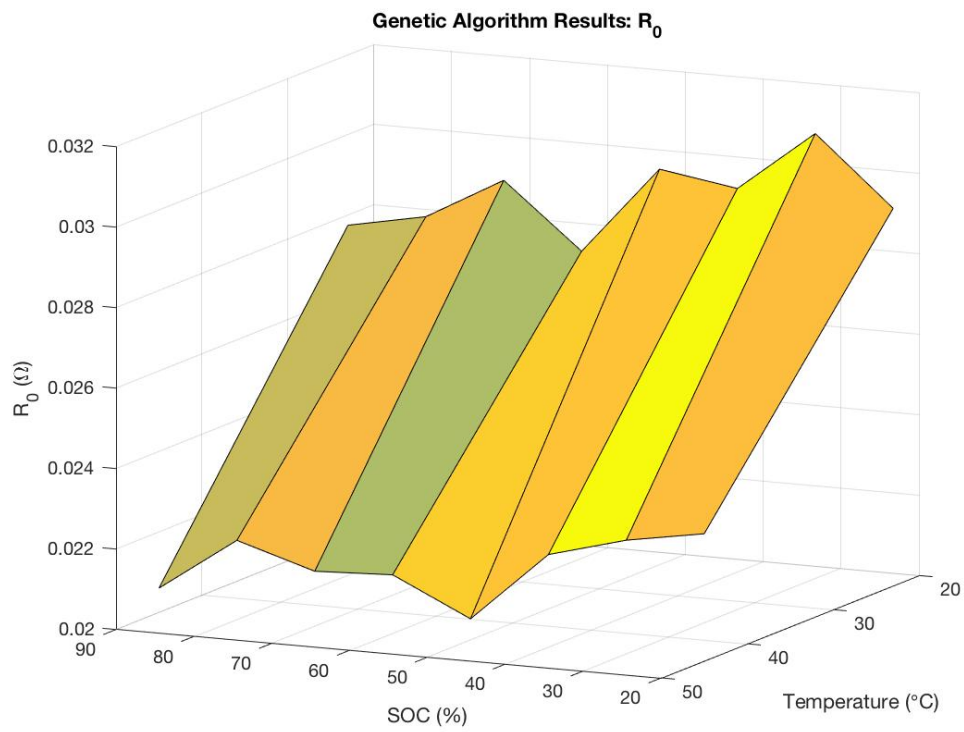
Genetic Algorithm Results: T=23°C			
SOC	R0	R1	C1
90%	2.94E-02	1.20E-02	9.42E+02
80%	3.11E-02	1.06E-02	1.14E+03
70%	2.95E-02	1.75E-02	8.78E+02
60%	2.98E-02	1.52E-02	9.81E+02
50%	2.76E-02	9.04E-03	1.33E+03
40%	2.92E-02	8.71E-03	1.50E+03
30%	2.81E-02	1.11E-02	1.03E+03
20%	2.78E-02	9.92E-03	5.90E+02

Genetic Algorithm Results: T=45°C			
SOC	R0	R1	C1
90%	2.32E-02	7.21E-03	1.43E+03
80%	2.28E-02	1.02E-02	1.13E+03
70%	2.23E-02	1.16E-02	9.67E+02
60%	2.05E-02	1.27E-02	7.87E+02
50%	2.15E-02	6.35E-03	1.33E+03
40%	2.14E-02	7.79E-03	1.40E+03
30%	2.20E-02	8.97E-03	1.58E+03
20%	2.06E-02	7.10E-03	7.75E+02

## 2d) fminsearch Surface Plot



## 2e) Genetic Algorithm Surface Plot



### Problem 2f) Comparison of Methods

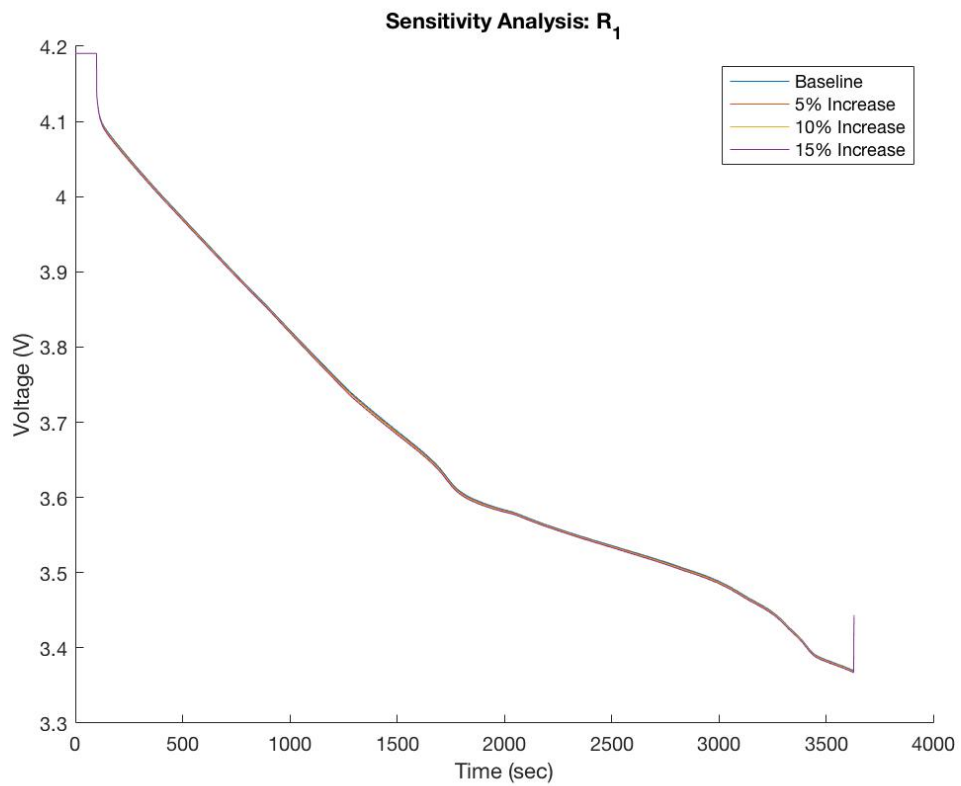
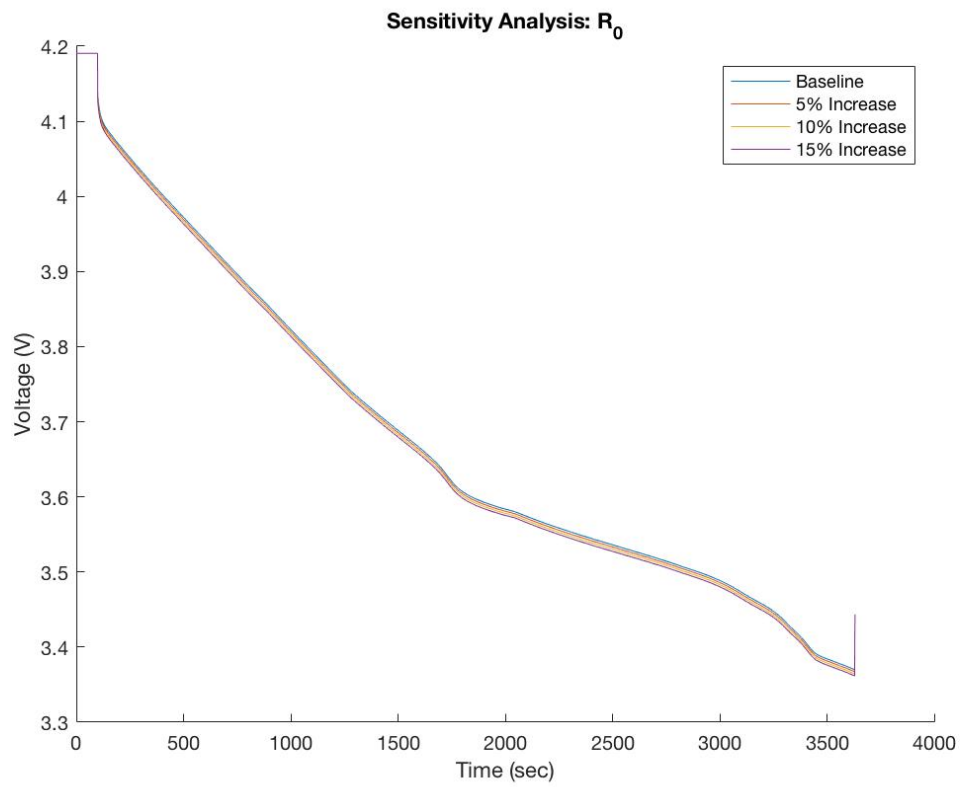
The main advantage of the fminsearch method compared to the genetic algorithm is that it is less computationally intensive and therefore is significantly faster to run. Because fminsearch is given a location to start the optimization at, the algorithm may get stuck at a local minimum near this start point. This may be an advantage if one is confident that the answer is in the vicinity of the start point, but it could be a disadvantage if the goal is to minimize the error as much as possible. The genetic algorithm, on the other hand, generates candidates within the entire space within the specified constraints. This makes it less likely to get stuck in a local minimum, but it requires more computational resources.

### Problem 2g)

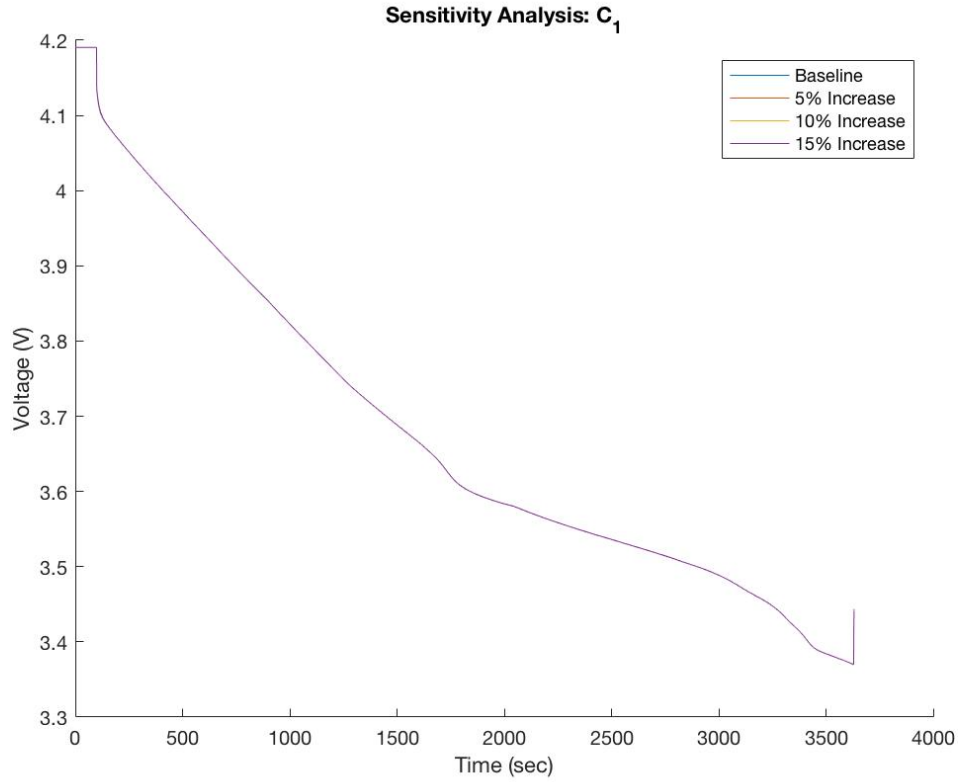
Overall RMS Error		
	fminsearch	ga
<b>T=23°C</b>	0.327%	0.335%
<b>T=45°C</b>	0.203%	0.198%

The genetic algorithm performed better than the fminsearch for both 23°C and 45°C, although they were quite close. There was a much more significant difference between the 23°C case and the 45°C case than there was between the two search methods.

## 2h) Sensitivity Analysis (conducted on Genetic Algorithm results for $T=23^{\circ}\text{C}$ )







## 2i) Sensitivity Analysis Comments

Because this sensitivity analysis uses a constant current input, the expression for the voltage drop across the  $R_1C_1$  branch of the circuit can be solved easily, yielding the expression:

$$V_1 = R_1 I + k e^{-\frac{1}{R_1 C_1} t}$$

where  $k$  is an integration constant. Therefore, the value of  $C_1$  only affects transient behavior in the system because of the exponential decay function. Since  $R_1 C_1 \approx 10$  sec, changing  $C_1$  will have very little impact on the system after a short amount of time. As  $t$  gets large, the voltage of the battery becomes:

$$V_{batt} = V_{OC} - I(R_0 + R_1)$$

Since  $R_0$  is 2-3 times larger than  $R_1$ , the system is much more sensitive to a percentage change in  $R_0$  than it is to the same percentage change in  $R_1$ .

## Model Validation

The overall RMS error obtained for the US06 model validation was 0.165%. The range of SOC achieved throughout the trial is incredibly narrow. This suggests that the BMS of the vehicle is working to constrain the SOC, and this car is likely a HEV. It is certainly not a BEV, because the SOC would have to vary much more than is observed in order to cover any meaningful distance. It is possible that the car was a PHEV, since these vehicles do allow for SOC depletion until a certain point, at which point SOC is constrained, but the car started at a modest SOC.

