

## Practical No. 1

P41

## BASICS OF R-SOFTWARE

1. R is a software for statistical analysis of data computing.
  2. It is an effective data handling software.
  3. El outcomes storage is possible.
  4. It is capable of graphical display.
  5. It is a free software.
- Q.1] Solve the following:

$$1) > 4 + 6 + 8 \div 2 - 5$$

$$\rightarrow [1] 7.333333$$

$$2) > 2^2 + |-3| + \sqrt{45}$$

$$\rightarrow [1] 13.7082.$$

$$3) > 5^3 + 7 \times 5 \times 8 + 46 / 5.$$

$$\rightarrow [1] 3414.2.$$

$$4) \sqrt{4^2 + 5 \times 3 + 7 / 6}$$

$$\rightarrow [1] 5.6 \neq 1567$$

$$5) \text{round off } (46 \div 7 + 9 \times 8).$$

$$\rightarrow [1] 79.$$

Q.2] solve the following:

1)  $a = c(2, 3, 5, 7)^2$   
[1]  $\begin{matrix} 4 & 6 & 10 & 14 \end{matrix}$

2)  $b = c(2, 3, 5, 7) * c(2, 3, 5)$   
 $\begin{matrix} b \\ [1] & 4 & 9 & 10 & 21 \end{matrix}$

3)  $c = c(2, 3, 5, 7) * c(2, 3, 6, 4)$   
 $\begin{matrix} c \\ [1] & \text{Warning message.} & 4 & 9 & 30 & 28 \end{matrix}$

4)  $d = c(1, 6, 2, 3) * c(-2, -3, -4, -1)$   
 $\begin{matrix} d \\ [1] & -2 & -18 & -8 & -3 \end{matrix}$

5)  $e = c(2, 3, 5, 7)^2$   
 $\begin{matrix} e \\ [1] & 4 & 9 & 25 & 49 \end{matrix}$

6)  $f = c(4, 6, 8, 9, 4, 5) ^ c(1, 2, 3)$   
 $\begin{matrix} f \\ [1] & 4 & 36 & 512 & 9 & 16 & 125 \end{matrix}$

7)  $g = c(6, 2, 7, 5) / c(4, 5)$   
 $\begin{matrix} g \\ [1] & 1.50 & 0.40 & 1.75 & 1.00 \end{matrix}$

$$Q. 3] x = 20 \quad y = 30 \quad z = 2.$$

find i)  $x^2 + y^3 + z$ .  
ii)  $\sqrt{x^2 + y}$   
iii)  $x^2 + y^2$ .

P42

→ so i)  $x^2 + y^3 + z$ .  
[1] 27402.

ii)  $\sqrt{x^2 + y^2}$   
[1] 36.06551

iii)  $c = x^2 + y^2$ .  
c  
[1] 1300

4] find the matrix

> x = matrix (nrow = 4, ncol = 2, data = c(1, 2, 3, 4, 5, 6, 7, 8))

> x  
[, 1] [, 2]  
[1, ] 1 5  
[2, ] 2 6  
[3, ] 3 7  
[4, ] 4 8

5) find  $x+y$  and  $2x+3y$  when \*

$$x = \begin{bmatrix} 4 & -2 & 9 \\ -7 & 0 & 6 \\ 9 & -5 & 3 \end{bmatrix}$$

$$y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

$\rightarrow x = \text{matrix}(nrow = 3, ncol = 3, \text{data} = c(4, 7, 9, -2, 6, 7, 3))$ .

$[, 1] [, 2] [, 3]$

$$[1,] 4 -2 6$$

$$[2,] 7 0 7$$

$$[3,] 9 -5 3$$

$\rightarrow y = \text{matrix}(nrow = 3, ncol = 3, \text{data} = c(10, 12, 15, -5, -6, 7, 9, 5))$

$> a = x + y$

$> a$

$[, 1] [, 2] [, 3]$

$$[1,] 14 -7 13$$

$$[2,] 19 -4 16$$

$$[3,] 24 -11 8$$

$> b = 2x + 3y$

$b$

$[, 1] [, 2] [, 3]$

$$[1,] 38 -19 33$$

$$[2,] 50 -12 41$$

$$[3,] 63 -28 21$$

a) Marks      0 } Statistics      0 }  
               59, 20, 25, 24, 46, 56, 55, 45 } comp. sci student.  
               32, 36, 29, 35, 39      24, 22, 44, 52, 54, 40, 50,

>  $x = c(59, 20, 25, 24, 46, 56, 55, 45, 32, 36, 29, 35, 39)$   
> breaks = seq(20, 60, 5).  
> a = cut(x, breaks, right = FALSE).  
> b = table(a).  
> c = transform(b)  
> c.

	a	freq
1	[20, 25)	3
2	[25, 30)	3
3	[30, 35)	1
4	[35, 40)	3
5	[40, 45)	1
6	[45, 50)	3
7	[50, 55)	2
8	[55, 60)	4

R.W  
2.11

Practical NO: 2  
PROBABILITY DISTRIBUTION.

1) check whether the following are p.m.f.  
not.

i)	$x$	$P(x)$
	0	0.1
	1	0.2
	2	-0.5
	3	0.4
	4	0.3
	5	0.5

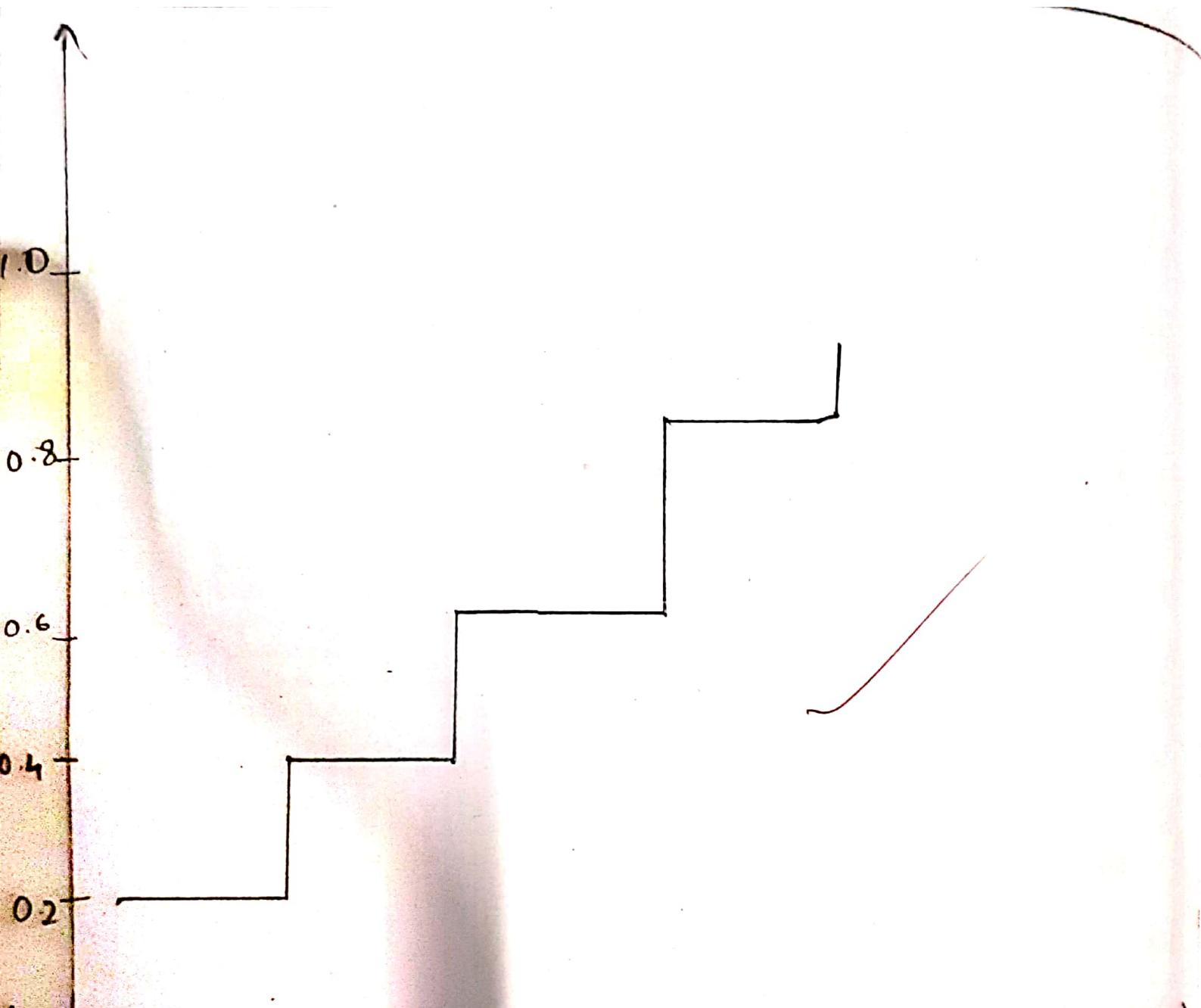
Since,  $p(2) = -0.5$ , can't be a probability function. In p.m.f  $P(x)$  is greater than 0 for all  $x$ .

ii)	$x$	1	2	3	4	5
	$P(x)$	0.2	0.2	0.3	0.2	0.2

It cannot be a p.m.f as ~~in~~ solution  $P(x) = 1$ .

iii)	$x$	10	20	30	40	50
	$P(x)$	0.2	0.2	0.35	0.15	0.1

Since it's sum is 1.  
 $\therefore$  It is p.m.f.



P45

(ii) Find C.D.F. for the following p.m.f  
Sketch the graph.

x	1	2	3	4	5
p(x)	0.2	0.2	0.35	0.15	0.1

$$\begin{aligned}
 F(x) &= 0 \\
 &= 0.2 \\
 &\approx 0.40 \\
 &= 0.75 \\
 &= 0.90 \\
 &= 1.00
 \end{aligned}$$

$$\begin{aligned}
 n &\leq 10 \\
 10 &\leq n \leq 20 \\
 20 &\leq n \leq 30 \\
 30 &\leq n \leq 40 \\
 40 &\leq n \leq 50 \\
 n &\geq 50
 \end{aligned}$$

x	1	2	3	4	5	6
p(x)	0.15	0.25	0.1	0.2	0.2	0.1

> Prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1).

> sum(Prob).

> cumsum(Prob).

x = c(1, 2, 3, 4, 5, 6).

Plot(x, xlab = "probability", ylab = "x", main = "probability distribution", cumsum(Prob))

Q1) check whether the following is p.d.f  
or not.

i)  $f(u) = 3 - 2u$ ;  $0 \leq u \leq 1$ .

$$= \int_0^1 f(u) du$$

$$= \int_0^1 (3 - 2u) du$$

$$= 3 \int_0^1 du - \int_0^1 2u du$$

$$= [3u - u^2]_0^1$$

$$= 2.$$

ii)  $f(u) = 3u^2$ ;  $0 \leq u \leq 1$ .

$$= \int_0^1 f(u) du$$

$$= \int_0^1 3u^2 du$$

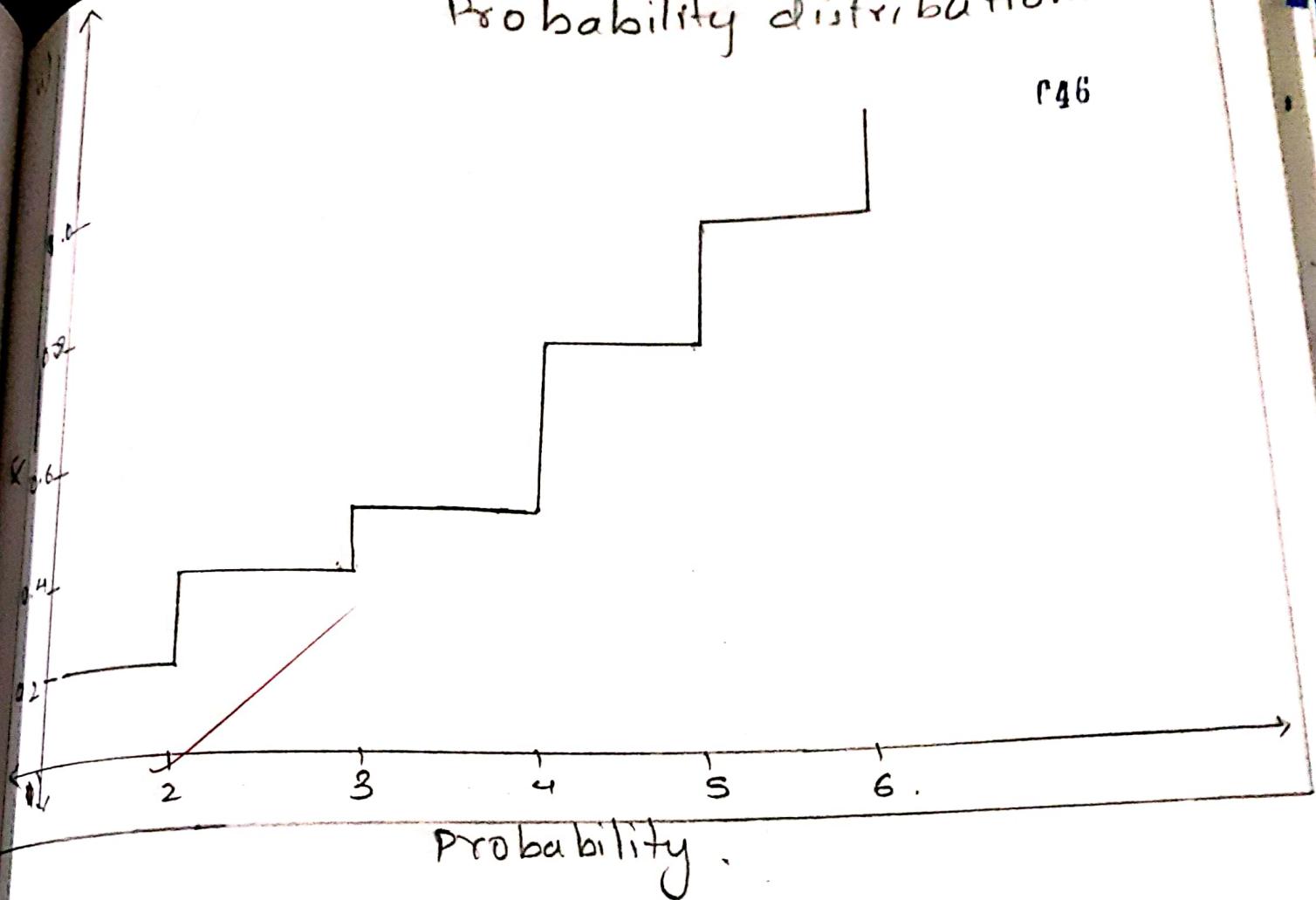
$$= \left[ \frac{3u^3}{3} \right]_0^1$$

$$= [1 - 0]$$

$$= 1.$$

# Probability distribution.

p46



### PRACTICAL - 3.

PA7

i) find the probability of exactly 10 in 100 trial with  $P = 0.01$ .

Suppose there are 12 MCQ. Suppose each Question has 5 opt out of which 1 is correct.  
find the probability of having  
 i) exactly 4 correct answer  
 ii) atmost 4 correct answer.  
 iii) More than 5 correct answer.

ii) Find the complete distribution when  $n=5$  &  $p=0.1$ .

~~i)  $n=12, p=0.25$ , find the following probability~~

- $P(x=5)$
- $P(x \leq 5)$ .
- $P(x > 7)$ .
- $P(5 \leq x \leq 7)$ .

The probability of a Salesman making a sell to a customer is 0.15. find a probability of

- no sells out of 10 customer.
- more than 3 sells out of 20.

Answer:

1)  $\text{dbinom}(10, 100, 0.1)$ .  
[1] 0.1318653.

2)  $\text{dbinom}(4, 12, 0.2)$ .  
[1] 0.1328756.

3) i)  $\text{dbinom}(4, 12, 0.2)$ .  
[1] 0.9274445.

iii)  $\text{Pbinom}(5, 12, 0.2)$ .  
[1] 0.01940528

3).  $\text{dbinom}(0.5, 5, 0.1)$ .  
[1] 0.590499      0.32805  
      0.00810      0.00045

0.07290  
0.00001

4)  $\text{dbinom}(5, 12, 0.25)$ .  
[1] 0.1032414.

$\text{Pbinom}(5, 12, 0.25)$ .  
[1] 0.9455978.

$1 - \text{Pbinom}(7, 12, 0.25)$ .  
[1] 0.00278151.

[1] 0.04014945

P48

> dbinom(0, 10, 0.15)

[1] 0.1968744

i) > 1 - Pbinom(3, 20, 0.15)

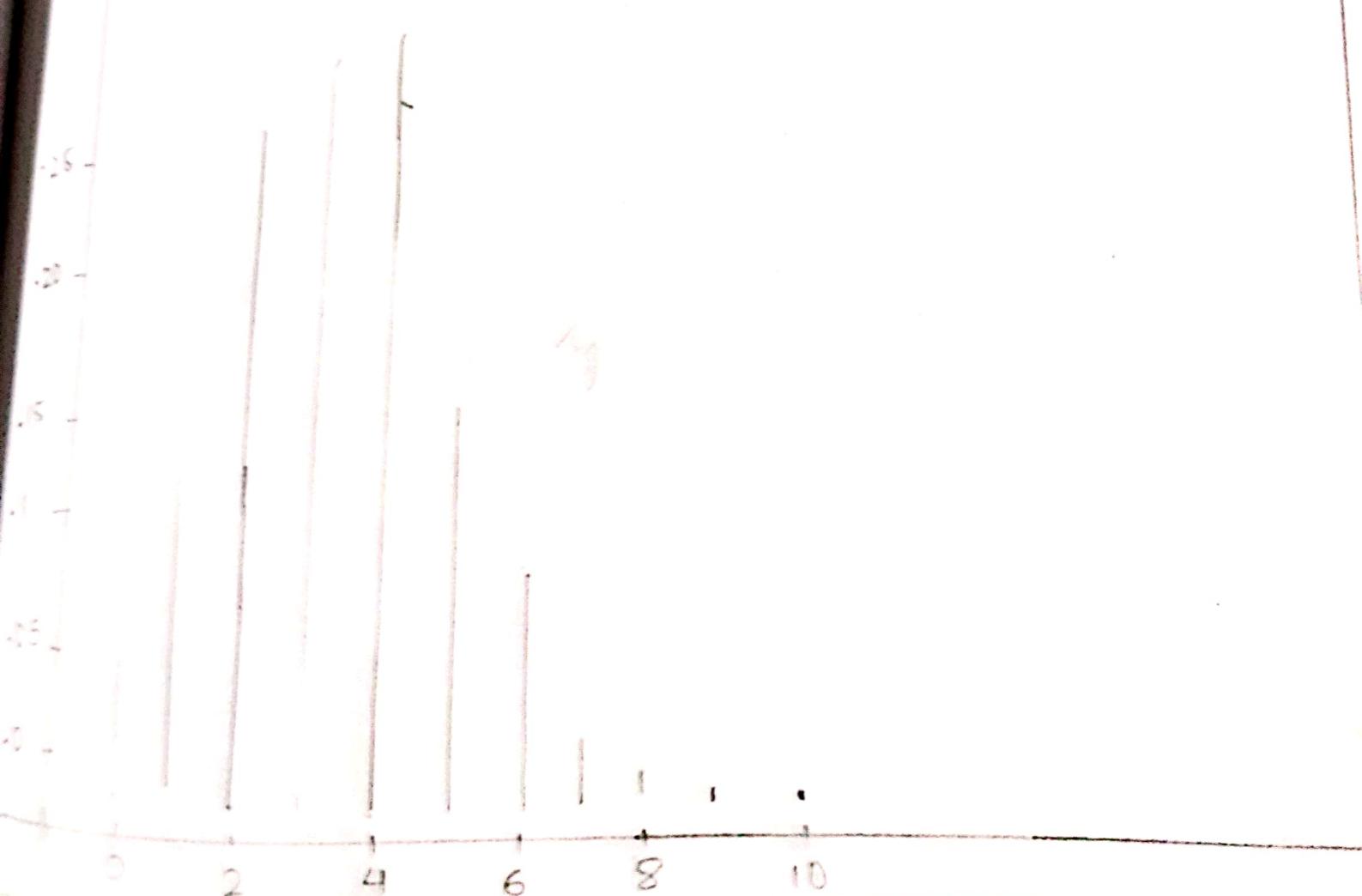
[1] 0.3522748

A salesman has a 20% probability of making a selling to a customer what a minimum no. Out of 30 customers with 88% probability. Sells then can make

> qbinom(0.88, 30, 0.2)

[1] 9.

x follows binomial distributions with n=10 p=0.3  
plot a graph of pmf & c.d.f.



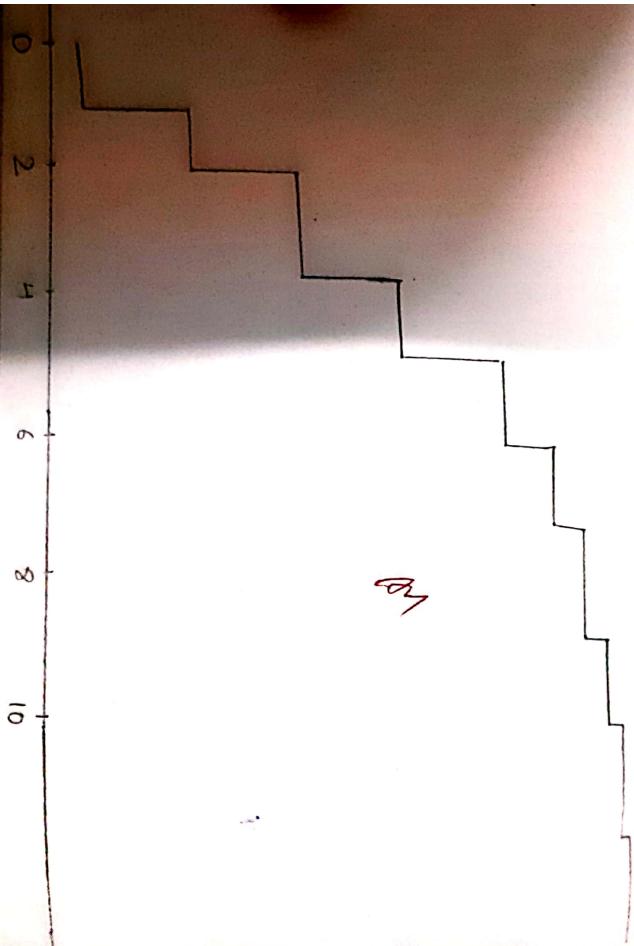
```
> p = 0.3  
> x = np.array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10])  
> prob = np.zeros((x, n, p))  
> cumprob = np.zeros((x, n, p))  
> d = data = frame[["x", "probability"]]  
> point(d)
```

[1]

```
x values. probability  
0 0.0282075249  
1 0.1210608216  
2 0.233444405  
3 0.2668249320
```

```
plot(x, prob, "h").  
plot(x, cumprob, "s")
```

h



## PRACTICAL - 4.

049

### Normal Distribution.

$$\begin{aligned}
 p(x = u) &= dnorm(x, u, \sigma) \\
 p(x < u) &= pnorm(x, u, \sigma) \\
 p(x > u) &= 1 - pnorm(x, u, \sigma)
 \end{aligned}$$

To generate random from a normal distribution in (standard random no). The  $rnorm(n, u, \sigma)$ .

i) A random variable  $x$  follows normal distribution with mean =  $u = 12$  & standard deviation =  $\sigma = 3$ . find

$$\begin{aligned}
 \text{i)} \quad &P(x \leq 15) \\
 \text{ii)} \quad &P(10 \leq x \leq 13) \\
 \text{iii)} \quad &P(x \geq 14).
 \end{aligned}$$

iv) Generate 5 observation. (random numbers).

$\rightarrow p1 = rnorm(15, 12, 3)$ .

$\rightarrow p1$

[1] 0.8413444 #.

$\rightarrow cat("P(x \leq 15) = ", p1)$ .

$p(x \leq 15) = 0.8413444$ .

$\rightarrow p2 = rnorm(13, 12, 3) - pnorm(10, 12, 3)$ .

$\rightarrow p2$ .

[1] 0.2524925

$\rightarrow rnorm(5, 12, 3)$ .

[1] 11.253625 7.628228 10.848236 5.045339 13.

Q19

2)  $X$  follows normal distribution with  $\mu = 10$  and  $\sigma^2 = 2$ .  
i) find  $P(X > 12)$ .  
ii)  $P(5 \leq X \leq 12)$ .  
iii) generate 10 observations.  
iv) find  $k$ , such that  $P(X < k) = 0.4$ .

$\rightarrow p_1 = \text{pnorm}(7, 10, 2)$ .

,  
 $p_1$ .

[1] 0.0668042.

$\rightarrow p_2 = \text{pnorm}(12, 10, 2) - \text{pnorm}(5, 10, 2)$ .

,  
 $p_2$ .

[1] 0.9351351.

$\rightarrow p_3 = 1 - \text{pnorm}(12, 10, 2)$ .

,  
 $p_3$ .

[1] 0.1526553.

$\rightarrow \text{pnorm}(10, 10, 2)$ .

[1] 9.021622 11.981599 9.079404 8.882845  
9.017746 13.423563 11.354241 10.159904

12.324565 11.582792.

✓

$\rightarrow qnorm(0.4, 10, 2)$ .

[1] 9.493306.

5 Random no. for normal distribution  
means,  $\sigma = 4$ , find sample mean, median, SD &  
print it.

050

> norm(5, 15, 4).

[1] 14.29548 16.45344 14.20567 19.43212 11.34906

[2] mean(x).

[3] 15.30922.

0.9  
> me = median(x).

[4] 14.29548.

[5] n=5

> variance = ((n-1)\*var(x))/n.

> variance.

[2] 6.967641.

> sd = sqrt(variance).

> sd.

[1] 2.639629.

> cat("sample mean is =", am).

Sample mean is = 15.30922.

> cat("sample median is =", me).

Sample median = 14.29548.

> cat("sample sd =", sd).

Sample sd = 2.639629.

X follows normal

find  $P(X \leq 40)$

$P(40 \leq X \leq 55)$

if  $P(25 \leq X \leq 35) = P(X \leq k) = 0.6$

(i) find k such that  $P(X \leq k) = 0.6$

21. given  $(85, 10, 30, 10)$

$P_1$

[1]  $0.82113447$

$P_2 = 1 - Pnorm(35, 30, 10)$

$P_2 = 0.3688345$

$P_3 = Pnorm(35, 30, 10) - Pnorm(25, 30, 10)$

$P_3 = 0.5929249$

$Pnorm(0, 6, 30, 10)$

[1]  $32.53349$

Standard normal graph.

plot Standard normal graph

> x = seq(-3, 3, by = 0.1)

> y = dnorm(x)

> plot(x, y, xlab = "x val", ylab = "probability",

main = "Standard normal graph")

✓  
2.1.20

## PRACTICAL - 5

NORMAL & t-test.

- 1) Test the hypothesis  $H_0: \mu = 15$ ,  $H_1: \mu \neq 15$ .  
 Random sample of size 400 is drawn. It is calculated that the S.D is 3. Test the hypothesis at 5% level of significance.

$$\text{formula: } z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}}$$

$$\mu_0 = \mu \quad n_{\mu} = \bar{n}$$

$$\sigma_d = \sigma \quad n = n.$$

$$\rightarrow z = \frac{\bar{x} - \mu_0}{\sigma_d / \sqrt{n}}$$

$$z = (m_x - m_0) / (s_d / (\sqrt{n}))$$

$$[1] - 6.66667.$$

pvalue =  $2 * (1 - \text{pnorm}(\text{abs}(z)))$   
 pvalue.  
 [1] 2.616796e-11.

Since, p-value is ~~less~~ than 0.05, we ~~accept~~ it.  $H_0: \mu = 15$ .

1) We + the hypothesis.  $H_0: \mu = 10$ ,  $H_1: \mu \neq 10$ . Random sample of size 400 is drawn with sample mean  $S.D = 2.25$ . Test the hypothesis at 5% level of significance.

$\mu$

$\neq 15$

$\epsilon 1$

$n$

$\approx 10$

$m_0 = 10$

$m_n = 10.2$

$s_d = 2.25$

$n = 400$

$$z = (m_n - m_0) / (s_d / (\sqrt{n}))$$
$$z = (10.2 - 10) / (2.25 / (\sqrt{400}))$$
$$z = 1.77778$$

$$[1] p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$
$$[1] 0.07544636$$

Since, the pval is more than 0.05  
we accept  $H_0: \mu = 10$ .

3) Test the Hypothesis  $H_0: \text{proportion of smokers in college is } 0.2$ .  
A sample is collected & the sample proportion is calculated = 0.125. Test the hypothesis at 5% level of significance. (sample size = 400).

$$\rightarrow P = 0.2, P = 0.125, n = 400, Q = 1 - P.$$
$$z = (P - P) / (\sqrt{P * Q / n})$$

$$[1] z = -3.75$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$[1] 0.000168346$$

So we reject  $H_0: \text{proportion} = 0.2$ .

4) Last year farmer lost 25-30% of their crop  
 Random Sample of 60 fields are collected &  
 it is found that 9 fields crops are insect poll.  
 Test the hypo at 1% level of significance.

$$\rightarrow H_0 : p = 0.2, H_1 : \mu p > 0.2$$

$$H_1 : p = 9\% = 0.09$$

$$P = 0.2, P = -0.09, n = 60, Q = 1 - P.$$

$$\rightarrow p = 0.2, P = 0.15$$

$$Z = (p - P) / (\sqrt{P(1-P)/n})$$

$$[2] \approx 0.9682458$$

$$p\text{value} = 2^{*}(1 - \text{pnorm}(\text{abs}(z)))$$

pvalue

$$[2] 0.3329216$$

5) Test the hypo  $H_0 : \mu = 12.5$  from the following  
 Sample at 5%. Level of sig:

$$\rightarrow x = c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94, 11.89, 12.16, 12.04)$$

$$n = \text{length}(x)$$

$$[2] 10$$

$$mx = \text{length}(x)$$

$$mx$$

$$[2] 12.07$$

$$\text{variance} = (n-1) * \text{var}(x)/n$$

$$\text{Variance}$$

$$[2] 0.019521$$

$$sd = \text{sqrt}(\text{variance})$$

$$sd \\ [2] 0.1397176.$$

$$mo = 12.5$$

$$t = (mx - mo) / (sd / (\text{sqrt}(n)))$$

$$[1] -8.894909$$

$$\text{pvalue} = 2 * (\text{l-pnorm}(\text{abs}(\frac{t}{2})))$$

$$[2] 0$$

since the value is less than 0.5, value rejected

AN  
16.1.20

## PRACTICAL - 6.

## LARGE SAMPLE TEST.

[Q.1] Let the population mean (The amt spent customer in a restaurant) is 250. Sample of 100 customer Selected. The Mean is calculated as 275 as the Standard Deviation is 30. Test the hypothesis of Standard population is 250 or not at 5% level of significance.

$$\rightarrow m_x = 275, m_0 = 250 \quad SD = 30 \quad n = 100$$

$$z = (m_x - m_0) / (SD / \sqrt{n})$$

$$[1] 2.333333.$$

$$p_v = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

[2] 0.

Since the p value is less than 0.05  
 $\therefore$  we reject  $H_0$ .

random sample of 1k student it was found  
that blue pen Test the hypothesis  
at 1 level of significance.

$$n = 1000$$

$$P = \frac{450}{1000} = 0.45$$

$$P = 0.8 \quad Q = 1 - P$$

$$Z = (P - p) / (\sqrt{p * q / n})$$

$$[2] = -3.952847$$

$$PV = 2^* (1 - \text{norm}(\text{abs}(z)))$$

$$[2] \neq .72268 \approx 0.5.$$

Since the value of  $P$

is less than 0.05.  
 $\therefore$  we reject  $H_0: P = 0.8$ .

- 3) Two random Sample of size 1000 & 2000 are drawn from 2 population with the same S.D. 2.5. The Sample means are 67.5 & 68. respectively. Test the hypothesis  $H_0: \mu_1 = \mu_2$  against  $H_a: \mu_1 \neq \mu_2$  at 5% O.S.

$$n_1 = 1000$$

$$n_2 = 2000$$

$$m_{\mu_1} = 67.5$$

$$m_{\mu_2} = 68$$

$$Sd_1 = 2.5$$

$$Sd_2 = 2.5$$

$$\therefore = (m_{\mu_1} - m_{\mu_2}) / \sqrt{(Sd_1^2/n_1) + (Sd_2^2/n_2)}$$

$$\therefore = 5.163078$$

$$P_V = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$[2] 2.417564e-07.$$

Accept. Reject.

Q) A study of noise level in two hospital that given below test the claim that the two hospitals have same level of noise at 1% L.D.S.

	Hos. A	Hos. B
SD	24	34
Mean	61.2	59.5
S.D.	7.9	7.5

$$n_1 = 84$$

$$\dots$$

$$n_2 = 34$$

$$\dots$$

$$m_{x_1} = 61.2$$

$$\dots$$

$$m_{x_2} = 59.4$$

$$\dots$$

$$Sd_1 = 7.9$$

$$\dots$$

$$Sd_2 = 7.5$$

$$z = (m_{x_1} - m_{x_2}) / \sqrt{(Sd_1^2/n_1) + (Sd_2^2/n_2)}$$

$$z = 1.162529.$$

$$P_V = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$[2] 7.0 \cdot 2450211.$$

Accept.

On a sample of 600 students 400 use blue ink in another college from a sample of 900 students in a third college. Test the hypothesis that the proportion of students using blue ink in 2 colleges are equal or not at 1% I.O.S.

$$H_0 : p_1 = p_2, \quad H_1 : p_1 \neq p_2.$$

$$n_1 = 600 \\ n_2 = 900$$

$$p_1 = 400/600 = 0.666 \dots \\ p_2 = 450/900 = 0.5 \\ p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2) \\ q = 1 - p.$$

$$\therefore z = (p_1 - p_2) / \sqrt{p * q / (1/n_1 + 1/n_2)} \\ [1] \quad 6.381834.$$

$$p_v = 2 * (1 - \text{pnorm}(\text{abs}(z))) \\ [1] \quad 1.753222e-10.$$

$\therefore$  we reject  $H_0 : p_1 = p_2$ .

---

$$\text{Ans} \quad P_1 = P_2 \quad \Leftrightarrow \quad d_1 = P_1 + P_2$$

$$c) \quad n_1 = 200 \quad n_2 = 200 \quad p_2 = 30/200.$$

$$p_1 = 44/200$$

$$q = 1 - p$$

$$\frac{p_1}{p_2} = \frac{9}{11} \quad 0.815$$

$$z^2 = (p_1 - p_2) / \sqrt{p_1 * p_2 * (1/n_1 + 1/n_2)}$$

$$[z] \quad 1.862741$$

$$p_{\text{v}} = 2^* (1 - \text{norm}(\text{abs}(z)))$$

$$[p_{\text{v}}] \quad 0.04142888$$

∴ Accept.

~~AM 3.01.10~~

PRACTICE - 4

Small Sample Test

156

The marks are 10 students are given by 10 hypotheses that the sample comes from population with avg marks 66.

$$\text{H}_0: \mu = 66 \\ \text{H}_1: \mu < 66$$

One Sample t-test.

Data :  $x = [68, 61, 67, 66, 65, 69, 70, 70, 71, 72]$ ,  $\bar{x} = 65.65141$ ,  $s = 0.14829$ .  
Alternative hypothesis : true mean is not equal to 66. 95 percent confidence interval:

sample estimates :

mean of  $x$

$$65.65141$$

Since, the p-value is smaller.  $\therefore$  we reject the significance of at 5%.

b)  $\alpha = 0.05$   
S.E.(p-value  $\approx 0.005$ )  $\Rightarrow$  can't accept  $H_0$  "else can't suggest rejection".

8) Two groups of student scored the following marks, reject the hypothesis that no significant difference between the two groups.  
 $X = 18, 22, 21, 17, 20, 14, 23, 20, 21$   
 $Group-II = 16, 20, 14, 21, 20, 18, 13, 15, 17, 21$

$\Rightarrow H_0$ : There is no diff between two groups

$$X = c(18, 22, 21, 17, 20, 14, 23, 20, 22, 21)$$
$$Y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$$
$$t.test(x, y)$$

# two sample t-test.

data:  $X \sim Y$ ,  
 $t = 2.2573$ ,  $df = 16.346$ ,  $p\text{-value} = 0.037$   
alternative hypothesis: true diff ~~between~~ in means is not equal to 0.  
95 percent confidence interval:  
0.1628205 5.0341795

sample estimates:

mean of  $X$  mean of  $Y$ ,

rejctd.

16) The sales data of 6 shops before and after an special campaign given below.

before data: 53, 28, 31, 48, 50, 42  
after : 58, 29, 30, 55, 56, 45

Test the hypo that the campaign is effective.

H<sub>0</sub>: There is no significant diff of sales before and after the campaign

$x = c(53, 28, 31, 48, 50, 42)$

$y = c(58, 29, 30, 55, 56, 45)$

$t.test(x, y, paired = T, alternative = "greater")$ .

paired t-test.

data: x & y.  
 $t = -2.4815$ ,  $df = 5$ , p-value = 0.9806.

alternative hypo: true diff in means is greater than 0 as percent confidence interval:

-6.035547 In R

Sample estimates:  
mean of the diff

-3.5.

Accepted.

Q39.

Two medicines are applied to two groups of patient respectively

$$g_1 : 10, 12, 13, 11, 14$$
$$g_2 : 8, 9, 12, 14, 15, 10, 9$$

Q8 there any sig diff between two medicines

$H_0$ : there is no signi. diff.

$$\lambda = C\{10, 12, 13, 11, 14\}$$

$$x = \gamma(8, 9, 12, 14, 15, 10, 9)$$

t-test ( $x, y$ )

Sample t-test

$$t = 0.80384 \quad df = 9.7994, p\text{-value} = 0.441$$

95 percent confidence interval:

$$-1.781171 \quad 3.481171$$

mean of  $x$        $\bar{x}$   
                        12

mean of  $y$   
                        11

Since, the  $p$ -value is greater than 0.05 therefore accept H<sub>0</sub> of significance.

The following are the weights before & after  
the diet program. Is the diet program effective? 658

before: 120, 125, 115, 130, 128, 119

after: 100 <sup>then</sup> ~~114, 95, 90~~ <sup>no</sup> <sup>sig</sup> <sup>diff.</sup> 115, 99

$x = c(120, 125, 115, 130, 128, 119)$   
 $y = c(100, 114, 95, 90, 115, 99)$

data: x & y

$t = 4.9293$ ,  $df = 5$ , p-value = 0.997  
- Inf 29.11493.

Mean of the differences

20.66667.

Since, the p-value is greater than 0.05.  
 $\therefore$  accept 5% of significance

~~114, 95  
6.2, 90~~

Practical - 8

Large & Small sample test

$$① H_0: \mu = 65 \quad H_1: \mu \neq 65$$

$$n = 100$$

$$m_x = 52$$

$$m_0 = 65$$

$$S_d = 7$$

$$z_{cal} = (m_x - m_0) / (S_d / (\sqrt{n}))$$

$$z_{cal}$$

$$[1] 4.285714$$

$$Pvalue = 2 * (1 - pnorm(abs(z_{cal})))$$

$$Pvalue$$

$$[1] 1.22153e-05$$

We reject.

$$2) P = 350/700 \quad H_0: P = \frac{1}{2}, ?$$

$$n = 700 \quad P = 0.5$$

$$\therefore q = 1 - P$$

$$z = (P - p) / (\sqrt{p * q / n})$$

$$[1] 0$$

$$PV = 2 * (1 - pnorm(abs(z)))$$

$$[1] 1$$

Accept the pvalue at  $H_0: p = \frac{1}{2}$ .

$$n_1 = 1000$$

$$n_2 = 1500$$

$$p_1 = 0.02$$

$$p_2 = 0.01$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$p$$

$$[1] 0.014$$

$$q = 1 - p$$

$$z = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$z$$

$$[1] 0.003474737$$

$$pv = 2 * (1 - pnorm(abs(z)))$$

$$pv$$

$$[1] 0.03702364$$

/

we reject

$$\text{H}_0: \mu = 100$$

$$mx = 99$$

$$sd = 8$$

$$mo = 100$$

$$n = 400$$

$$z = (mx - mo) / (sd / (\sqrt{n}))$$

$$z$$

$$[1] -2.5$$

$$pv = 2 * (1 - pnorm(abs(z)))$$

$$pv$$

$$[1] 0.01241933$$

we reject

t-test(x) { 68, 69, 69, 71, 71, 72 }

One Sample t-test  
t = 4.91, df = 5, p-value = 5.500,  
alternative hypothesis: true mean of x is not equal to 64.66479  
mean of x = 68.14286

we reject  $H_0$

7).

$H_0$

$$n = 100$$

$$m_\theta = 1200$$

$$m_x = 1150$$

$$z = (m_x - m_\theta) / (\text{sd} / (\sqrt{n}))$$

$$z = -4$$

$$pv = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$(1) \text{pv} = 6.334248e-05$$

we reject.

$$H_0: \sigma_1 = \sigma_2$$

$x = [66, 67, 75, 76, 82, 84, 88, 90, 92]$  (60)  
 $y = [64, 66, 74, 78, 82, 87, 92, 93, 95, 97]$ .  
 $\text{var.test}(x, y)$ .

F test to compare two variances.

0.70686, numdf = 8, denomdf = 10, p-value = 0.6359  
95 percent confidence interval:  
0.1833662 3.036093.

sample estimates:

ratio of variances  
0.7068567.

we accept  $H_0$

$$H_0: P_1 = P_2$$

$$n_1 = 200$$

$$n_2 = 300$$

$$p_1 = 44/200$$

$$p_2 = 56/300$$

$$P = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$q = 1 - P$$

2.

$$[1] 0.9128709$$

$$PV = (2 * (1 - pnorm(\text{abs}(z))))$$

$$PV$$

$$[1] 0.3613104$$

P

0.2.

We ~~reject~~ accept  $H_0$

$\rightarrow H_0$ : Condition of home & child are independent.

$$x = \{70, 80, 35, 50, 20, 45\}$$

$$m = 3$$

$$n = 2$$

$y = \text{matrix}(x, \text{nrow} = m, \text{ncol} = n)$

$y$	[,1]	[,2]
[1,]	70	50
[2,]	80	20
[3,]	35	45

$PV = \text{chisq.test}(y)$ .

$PV$

Pearson's chi-squared test.

data: y.

$\chi^2 = 25.646$ , df = 2, pvalue =  $2.698e-06$

$\therefore H_0$  is rejected, as since  $pV$  is less than 0.05.

Test the hypothesis that disease and vaccination are independent or not.

Vaccine.

Disease	Affected	Not Affected
Affected	70	46
Not Affected	35	37

$H_0$ : Condition of disease and vaccination are independent.

$$\chi^2 = \sum (O - E)^2 / E$$

$$m = 2$$

$$n = 2$$

$y = \text{matrix}(x, \text{ncol} = m, \text{ncol} = n)$ .

$y$

	[1, 1]	[1, 2]
[1, ]	70	46
[2, ]	35	37

$PV = \text{chisq.test}(y)$

$PV$

$\chi^2 = 2.0275$ ,  $df = 1$ ,  $PV = 0.1545$

$H_0$  is Accepted, Since,  $PV$  is more than 0.05.

3) Perform a ANOVA for the following data

Type	Observations
A	50, 52.
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

→ H<sub>0</sub>: The means are equal for A, B, C, D

$$x_1 = c(50, 52)$$

$$x_2 = c(53, 55, 53)$$

$$x_3 = c(60, 58, 57, 56)$$

$$x_4 = c(52, 54, 54, 55)$$

d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))  
names(d)

[1] "values" "ind".

> oneway.test(values ~ ind, data = d, var.equal = T)

one-way analysis of means  
data: values ~ ind

F = 11.735, num df = 3, denom df = 9, p-value =

> anova = aov(values ~ ind, data = d)  
Summary(anova)

ind individuals	Df	sum Sq	Mean Sq	F value	P(F).
	3	71.06	23.688	11.73	0.00183**
	9	18.17	2.019		0.62

Signif codes : 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' '.

The following data gives the life of the tire of 4 brands

TYPE	LIFE
A	20, 23, 18, 17, 18, 22, 24
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 14, 16

H0: The average life of A, B, C, D are equal.

$$x_1 = c(20, 23, 18, 17, 18, 22, 24)$$

$$x_2 = c(19, 15, 17, 20, 16, 17)$$

$$x_3 = c(21, 19, 22, 17, 20)$$

$$x_4 = c(15, 14, 16, 18, 14, 16)$$

d = stack(list(values ~ ind, b1 = x1, b2 = x2, b3 = x3, b4 = x4))  
names(d).

> oneway.test(values ~ ind, data = d, var.equal = T)  
One-way analysis of means.

data:

$F = 6.8445$ , num df = 3, denom df = 20,  
P-value = 0.002349.

> anova = aov(values ~ ind, data = d)  
summary(anova).

# stats

40

45

42

45

37

36

49

59

20

27

# maths

60

48

47

20

25

27

57

58

25

27

PRACTICAL - 10

063

NON-PARAMETRIC TEST.

following are the amounts of Sulphur oxide emitted by an industry in 20 days. Sign test to test the hypothesis that the population medium is 21.5 at 5% LOS

17 15 20 29 19 18 22 25 27 9 24 20 17  
6 24 14 15 23 24 26

$$H_0: \text{population medium is } 21.5$$

$$x = \{17, 15, 20, \dots, 26\}$$

$$m_e = 21.5$$

$$S_p = \text{length}(x(x > m_e))$$

$$S_n = \text{length}(x(x < m_e))$$

$$n = S_p + S_n$$

$$\begin{bmatrix} n \\ 1 \end{bmatrix} 20$$

$$Pv = \text{pbnom}(S_p, n, 0.5)$$

$$Pv$$

$$\begin{bmatrix} 1 \end{bmatrix} 0.4119015$$

Accepted.

2) give the alternative is  
following is a data of 10 observations  
apply sign test to test the hypothesis  
that the population medium is 625 against the alternative it  
is more than 625.

612,

→  $H_0$  : population medium is 625.

$$x = c(612, 619, 631, 628, 643, 640, 655, 649, 673, 663)$$

$$m_e = 625$$

$$sp = \text{length}(x[x > m_e])$$

$$sn = \text{length}(x[x < m_e])$$

$$n = sp + sn$$

n

[1] 10.

$$pv = \text{pbinom}(sn, n, 0.5)$$

pv

[1] 0.0546875.

Accepted.

the following are the values of a sample from the population  
medium is 60. Hypothesis that it is more than 60 against the alternative  
63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39, 52, 69, 48, 66, 72, 63, 87, 69.  
 $H_0$ : population median is equal to 60  
 $H_1$ : population median is greater than 60

$x = c \dots \dots \dots$

wilcox.test(x, alter = "greater", mu = 60).

wilcoxon signed rank test with continuity correction.

data: x

v = 145, p-value = 0.02298

alternative hypothesis: true location is greater than 60.

since, pvalue is less than 0.05,  $\therefore$

we rejected.

is  $V_{12}$  less than the population median or less than 12.

→  $H_0$ : population median is less than 12.

$x = c(15, 17, 24, 25, 20, 21, 32, 28, 12, 24, 26)$ .

`wilcox.test(x, alternative = "less", mu = 12)`.

wilcoxon SRT with continuity  
data : x.

$V = 66$ , p-value = 0.9986.

alternative hypothesis: true location is less than 12.

Since pvalue is more than 0.05  
 $\therefore$  it is accepted.

5). The weights of students before or after they stopped smoking are given below. Using WSRT test that there is no significant change.