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Pattabiraman Venkatasubbu, Mukkesh Ganesh

Abstract: The production of cars has been steadily increasing in the past decade, with over 70 million passenger cars being produced in the year 2016. This has given rise to the used car market, which on its own has become a booming industry. The recent advent of online portals has facilitated the need for both the customer and the seller to be better informed about the trends and patterns that determine the value of a used car in the market. Using Machine Learning Algorithms such as Lasso Regression, Multiple Regression and Regression trees, we will try to develop a statistical model which will be able to predict the price of a used car, based on previous consumer data and a given set of features. We will also be comparing the prediction accuracy of these models to determine the optimal one.

Keywords: ANOVA, Lasso Regression, Regression Tree, Tukey's Test

I. INTRODUCTION

The used car market is an ever-rising industry, which has almost doubled its market value in the last few years. The emergence of online portals such as CarDheko, Quikr, Carwale, Cars24, and many others has facilitated the need for both the customer and the seller to be better informed about the trends and patterns that determine the value of the used car in the market. Machine Learning algorithms can be used to predict the retail value of a car, based on a certain set of features

Different websites have different algorithms to generate the retail price of the used cars, and hence there isn't a unified algorithm for determining the price. By training statistical models for predicting the prices, one can easily get a rough estimate of the price without actually entering the details into the desired website. The main objective of this paper is to use three different prediction models to predict the retail price of a used car and compare their levels of accuracy.

The data set used for the prediction models was created by Shonda Kuiper[1]. The data was collected from the 2005 Central Edition of the Kelly Blue Book and has 804 records of 2005 GM cars, whose retail prices have been calculated. The data set primarily comprises of categorical attributes along with two quantitative attributes.

The following are the variables used:

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Price: The calculated retail price of GM cars. The cars which were selected for this data set were all less than a year old and were considered to be in good condition.

Mileage: The total number of miles the car has been driven

Make: The manufacturer of the car **Model:** The specific models for each car

Trim: The type of car model **Type:** The car's body type

Cylinder: The number of cylinders present in the engine

Liter: The fuel capacity of the engine **Doors:** The number of doors in the car

cruise: A categorical variable (binary), which represents whether cruise control is present in the car (coded 1 if present) **sound:** A categorical variable (binary), that represents whether upgraded speakers are present in the car (coded 1 if present)

Leather: A categorical variable (binary), that represents whether the car has leather interiors (coded 1 if present)

Using these attributes, we will try to predict the price by using the Statistical Analysis System (SAS) for exploratory data analysis.

II. LITERATURE SURVEY

Overfitting and underfitting come into picture when we create our statistical models. The models might be too biased to the training data and might not perform well on the test data set. This is called overfitting. Likewise, the models might not take into consideration all the variance present in the population and perform poorly on a test data set. This is called underfitting. A perfect balance needs to be achieved between these two, which leads to the concept of Bias-Variance tradeoff. Pierre Geurts [2] has introduced and explained how bias-variance tradeoff is achieved in both regression and classification. The selection of variables/attribute plays a vital role in influencing both the bias and variance of the statistical model. Robert Tibshirani [3] proposed a new method called Lasso, which minimizes the residual sum of squares. This returns a subset of attributes which need to be included in multiple regression to get the minimal error rate. Similarly, decision trees suffer from overfitting if they are not pruned/shrunk. Trevor Hastie and Daryl Pregibon [4] have explained the concept of pruning in their research paper. Moreover, hypothesis testing using ANOVA is needed to verify whether the different groups of errors really differ from each other. This is explained by TK Kim and Tae Kyun in their paper [5]. A Post-Hoc test needs to be performed along with ANOVA if the number of groups exceeds two.

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Tukey's Test has been explored by Haynes W. in his research paper [6]. Using these techniques, we will create, train and test the effectiveness of our statistical models.

III. PROPOSED MODEL

A. Null Hypothesis

Even though the magnitude of overfitting has been reduced, Regression trees still suffer from overfitting even after Pruning. This leads to our following hypothesis.

Hypothesis: Multiple and Lasso Regressions are better at predicting price than the Regression Tree.

B. Training and Testing Data

The data is split into training(70% - 563 records) and testing(30% - 241 records) data sets through random sampling (seed was set to 2786).

C. Lasso Regression

Using Lasso regression on the training data set, we first select the subset of attributes which lead to optimal/least sum of squared error while predicting the price. It makes use of 10-fold cross-validation to "lasso" the optimal subset of attributes. It uses L1 regularization.

Table – 1: Lasso Regression Summary

	LAR Selection	n Summary					
Step	Effect Entered	Number Effects In	CV PRESS				
0	Intercept	1	5.47454E10				
-1	Cylinder_8	2	2.94477E10	26	Model Lacrosse	27	1079
2	Make_Cadil	3	2.54198E10	27	Model Vibe	28	1057
3	Type_Conve	4	1.70491E10	28	Trim SS Coupe 2D	29	991
4	Make_SAAB	5	1.0723E10	29	Trim SVM Hatchba	30	968
5	Liter	6	5716511688	30	Trim Sedan 4D	31	906
6	Model_XLR-V8	7	4455568638	31	Model Cavalier	32	900
7	Cruise_0	8	4462900633	32	Model AVEO	33	895
8	Mileage	9	3141496232	33	Trim CXS Sedan 4	34	886
9	Make_Chevr	10	3102016376	34	Model Sunfire	35	866
10	Model_Corvette	11	2636230790	35	Trim Custom Seda	36	849
11	Type_Wagon	12	2434477976	36	Trim SVM Sedan 4	37	842
12	Model_STS-V8	13	2241697550	37	Model Grand Am	38	834
13	Model_Park Ave	14	2022249850	38	Trim LS Coupe 2D	39	820
14	Model_9_5	15	2016211162	39	Trim LT Coupe 2D	40	809
15	Trim_SS Sedan 4D	16	1870278120	40	Trim GXP Sedan 4	41	785
16	Model_STS-V6	17	1767874656	41	Model_Century	42	780
17	Model_Grand Pr	18	1706384400	42	Model_L Series	43	7575
18	Model_CST-V	19	1594252419	43	Model_G6	44	734
19	Trim_Arc Sedan 4	20	1537014571	44	Trim_GTP Sedan 4	45	709
20	Trim_Arc Conv 2D	21	1432488055	45	Trim_Limited Sed	46	691
21	Trim_GT Coupe 2D	22	1357217957	46	Trim_AWD Sportwa	47	6879
22	Trim_Special Ed	23	1341923945	47	Trim_CXL Sedan 4	48	680
23	Model_9-2X AWD	24	1207730522	48	Trim_DTS Sedan 4	49	674
24	Model_Deville	25	1192390216	49	Leather_0	50	664
25	Model Malibu	26	1140423212	50	Trim_Arc Wagon 4	51	662

51	Trim_DHS Sedan 4	52	618387221
52	Trim_GT Sportwag	53	612366627
53	Make_Satur	54	609667982
54	Trim_LS Sport Co	55	606909142
55	Model_Classic	56	604819404
56	Trim_SLE Sedan 4	57	601079687
57	Sound_0	58	598479882
58	Trim_GT Sedan 4D	59	597018312
59	Trim_Linear Conv	60	599172036
60	Trim_LT Sedan 4D	61	597976402
61	Trim_Coupe 2D	62	595494703
62	Trim_Conv 2D	63	587687756
63	Trim_LT MAXX Hba	64	586066103
64	Model_9_5 HO	65	585734528
65	Trim_MAXX Hback	66	585894705
66	Trim_LS Sedan 4D	67	586199168
67	Model_Monte Ca	68	582745854*
68	Trim_Quad Coupe	69	583208092
69	Trim_LT Hatchbac	70	583490938
70	Trim_LS Hatchbac	71	585911868
71	Trim_Aero Wagon	72	586112390
72	Trim_LS Sport Se	73	586892601
73	Trim_Aero Sedan	74	587208898
	* Optimal Value	of Criterion	

The LAR Selection summary returns the levels of attributes which need to be chosen to reduce the prediction error.

We can infer from the table-1 that the cross-validated predicted residual error sum of squares (CV PRESS) is the least for the 67 levels of the chosen attributes. Fig. 1 gives us a graphical representation of this. All the chosen 12 attributes, except doors, were lassoed.

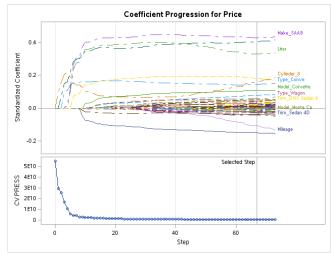


Fig. 1: The coefficients (estimates) of each parameter when other parameters are added is plotted. Also, the CV-Press of the selection process is plotted.

The error rate reaches the minimum value when the above-mentioned levels of the variables were selected for multiple regression. This is shown in Figure 2.

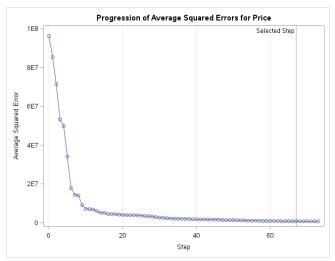


Fig. 2: The Average Square Error is also plotted against the number of levels of variables selected.

Since each level of the categorical variable is treated as a variable on its own (in multiple and Lasso regression), we get 67 estimates.

The prediction model works based on this generated equation:

$$Price = Intercept + P_1*E_1 + P_2*E_2 + \dots + P_{67}*E_{67}$$



Where P_1 - P_{67} are parameter values while E_1 - E_{67} are the parameter estimates. These parameter estimates are tabulated in Table 2.

Table – 2: Parameter Estimates of Lasso Regression

Parameter	Estim	ates		
arameter	DF	Estimate	Trim_Conv 2D	
ntercept	- 1	11930	Trim Coupe 2D	
Mileage	1	-0.180375		.
Model_9-2X AWD	1	-5262.702319	Trim_Custom Sed	a
Model_9_5	1	589.004468	Trim_DHS Sedan 4	ı
Model_9_5 HO	- 1	83.558352	Trim_DTS Sedan 4	
Model_AVEO	1	-925.178888	Trim GT Coupe 2D	,
Model_CST-V	1	2224.293026	Trim GT Sedan 4D	
lodel_Cavalier	1	-805.439239	_	-
lodel_Century	1	-450.383125	Trim_GT Sportwag	
Model_Classic	- 1	516.980697	Trim_GTP Sedan 4	
lodel_Corvette	1	6499.300407	Trim_GXP Sedan 4	
lodel_Deville	1	-6076.484632	Trim LS Coupe 2D	
lodel_G6	1	1524.839816		+
Model_Grand Am	1	-1417.822185	Trim_LS Sedan 4D	
lodel_Grand Pr	1	-1398.133632	Trim_LS Sport Co	
lodel_L Series	- 1	-695.355181	Trim_LT Coupe 2D	
lodel_Lacrosse	1	1040.680489	Trim_LT MAXX Hba	
Model_Malibu	1	-722.730821	Trim LT Sedan 4D	+
Model_Monte Ca	1	-3.299907	_	_
Model_Park Ave	1	4419.996622	Trim_Limited Sed	
Model_STS-V6	1	4615.191143	Trim_Linear Conv	
Model_STS-V8	1	3346.668189	Trim_MAXX Hback	
lodel_Sunfire	1	-1451.072301	Trim SLE Sedan 4	
lodel_Vibe	1	-450.775368		-
Model_XLR-V8	1	15127	Trim_SS Coupe 2D	
rim_AWD Sportwa	1	1105.577065	Trim_SS Sedan 4D	
rim_Arc Conv 2D	1	3609.398271	Trim_SVM Hatchba	
Trim_Arc Sedan 4	1	1967.547470	Trim SVM Sedan 4	
Trim_Arc Wagon 4	1	646.224125	_	
Trim_CXL Sedan 4	1	1167.499627	Trim_Sedan 4D	
Frim_CXS Sedan 4	1	2050.191555	Trim_Special Ed	

Make_Cadil	1	13886
Make_Chevr	1	-784.202071
Make_SAAB	1	12048
Make_Satur	1	-218.047931
Type_Conve	1	5780.790292
Type_Wagon	1	2014.086276
Cylinder_8	1	4725.325637
Liter	1	2899.110914
Cruise_1	1	52.281909
Sound_0	1	-173.157633
Leather_1	1	221.835813

The parameter estimates of the 67 levels are tabulated here Since Lasso regression heavily relies on the training set to find the best fit levels of attributes, it might miss out on some levels of categorical variables which do not show much association in the training dataset, due to random sampling. This might cause our model to be slightly (maybe even statistically insignificant) underfit, since in-group variance might have been overlooked. Hence, an iterative process is needed to determine the mean error rate.

D. Multiple Regression

A general linear model, which models price to the set of selected attributes is trained (on the training data set). The results are tabulated in Table 3. The variables which were selected in Lasso Regression are used here. However here, all the levels of the variables are taken into consideration.

Table – 3: Multiple Regression Summary

				Dependent	Varial	ale: Pric	e				
_			-							alue	
Source		-	DF		Sum of Squares						Pr >
Model			73	5384591					91	0.75	<.000
Error Corrected Total		_	489 3960				808	09897			
Corrected	lota	al c	562	5424195	2121						
		R-Sq		Coeff Var	D	t MSE	п	rice M			
		0.99				9.9431	P	2116			
		0.88	2098	4.251910	08	9.8431		2110	0.09		
Sour	200	DE		Type I SS	Mon	n Squar		E V-	lue	Pr	. =
Milea		-	1	754087627		5408762			1.09	<.00	
Mode	_	31		1879845703		7353695			3.36	<.00	
Trim	-	38		1201526121	-	3161910			9.04	<.00	
Make		-						-			-
Туре			5	0					÷		
Cylin			,	0			÷				
Liter)	0							
Cruis	se	1	1	28758		2875	8	(0.04	0.85	06
Sour	nd	1	1	5915030		591503	0	7	7.30	0.00	71
Leat	her	1	1	4709008		470900	8		5.81	0.01	63
Sou	rce	D	F	Type III SS	Mear	Square		F Va	lue	Pr>	F
Mile	age		1	1159816853	115	981685	3	1432	.05	<.000	01
Mod	lel		8	493298602	6	166232	5	76	.14	<.000	01
Trim	1	3	1	608810398	1	9639048	5	24	.25	<.000	01
Mak	e		0	0					-		
Тур	9		0	0					-		
Cyli	nder		0	0					-		
Lite	r		0	0							
Crui	ise		1	49015		49018	5	0	.06	0.80	58
Sou	nd		1	5487410		5487410)	6	.78	0.00	95
Leat	ther		1	4709008		4709008	3	5	.81	0.016	83

The result of the GLM procedure with P-value and R² values are tabulated along with the type 1 and type 3 error rates.

From this model, we can see that the variable Price and the selected variables are highly correlated since the R-Square (coefficient of determination) value is around 0.9927. This implies that these variables account for about 99.27% of the variance in the Price.

Moreover, both Type 1 and Type 3 SS tables show us that all the variables are significantly correlated with Price (P values <0.05), except Cruise control, which is confounded when the other variables are held at their mean.

Similar to the GLM Select procedure, this procedure also returns a set of parameter estimates, for numerical variables and every level of the categorical variables.

$$Price = Intercept + P_1 * E_1 + P_2 * E_2 + \dots + P_n * E_n$$
 (2)

Where P_1 - P_n are parameter values while E_1 - E_n are the parameter estimates. These parameter estimates are tabulated in Table 4.



Table - 4: Parameter Estimates of Multiple Regression

							Model XLR-V8	0.00000	В			
Parameter	Estimate		Standard Error	t Value	Pr	> Iti	Trim AWD Sportwa	1403.35298	В	452.3758837	3.1	10 0
Intercept	65357.71411	В	338.7093195	194.11		0001	Trim Aero Conv 2	3585.16498	В	675.2493313	5.0	31 <
Mileage	-0.18481	-	0.0048835	-37.84		0001	Trim Aero Sedan	-2691.07765	В	699.8088760	-3.8	85 0
Model 9-2X AWD	-37289.38111	В	614.1831122	-80.71		0001	Trim Aero Wagon	-933.73144	В	842.0462909	-1.1	11 0
Model 9 3	-35296.16123	В	469.8443603	-75.12	<.0	0001	Trim Arc Conv 2D	7337.82741	В	675.2118877	10.8	87 <
Model 9 3 HO	-32915.53020	В	679.1892212	-48.46	<(0001	Trim Arc Sedan 4	-77.88681	В	486.3534827	-0.1	16 0
Model 9 5	-31623.78449	В	451 4985553	-70.04		0001	Trim Arc Wagon 4	782.26079	В	465.9823406	1.6	88 0
Model 9 5 HO	-31278.61804	В	832,3506337	-37.58	<.0	0001	Trim CX Sedan 4D	-2965.34780	В	520.8103869	-5.6	89 <
Model AVEO	-49587.15748	В	642.7200237	-77 15		0001	Trim CXL Sedan 4	-1497.34465	В	486.7958180	-3.0	0 80
Model Bonnevil	40001.10140	В	516 0028160	-79.43		0001	Trim CXS Sedan 4	0.00000	В			
Model CST-V	-14670.76189	В	655.6385810	-22.38	-14	0001	Trim Conv 2D	2855.00108	В	721.6337577	3.6	96 <
Model CTS	-30226.42345	В	675.2713617	-44.78		0001	Trim Coupe 2D	-1748.94887	В	550.1784098	-3.1	18 0
Model C15 Model Cavalier	-30220.42340 -47498.91131	В	597.1873761	-79.54		0001	Trim Custom Seda	-2942 25814	В	514 5423072	-5	72 4
Model Cavaller Model Century	-47498.91131 -43887.65908	В	631.6972266	-79.54		0001	Trim DHS Sedan 4	2841.44331	В	664.8961601	4.3	27 <
Model Century Model Classic	-43887.85908 -45946.33568	В	640.1245680	-71.78		0001	Trim DTS Sedan 4	3245.63577	В	715.4464014	4.5	
					-14		Trim GT Coupe 2D	646.26328	В	741.8700293	0.8	
Model Cobalt	-46712.35251	В	601.7780460	-77.62		0001	Trim GT Sedan 4D	-1103.50589	В	582.1038905	-1.6	
Model Corvette	-23521.01278	В	712.5300847	-33.01		0001	Trim GT Sportwag	1146.16407	В	452.1955261	2.6	
Model Deville	-27020.10490	В	641.3631111	-42.13		0001						
Model G6	-40353.56209	В	617.1102709	-85.39	<.0	0001	Trim GTP Sedan 4	1520.55283	В	637.3977100	2.3	
Model GTO	-30411.49383	В	703.3165454	-43.24		0001	Trim GXP Sedan 4	2741.49838	В	571.6131934	4.8	80 4
Model Grand Am	-47085.11233	В	741.4080127	-83.51	<.0	0001	Trim Hardtop Con	0.00000	В			
Model Grand Pr	-42817.18963	В	631.4756193	-67.80	<.0	0001	Trim L300 Sedan	0.00000	В			
Model Impala	-41984.28591	В	603.5127505	-69.57	<.0	0001	Trim LS Coupe 2D	-1123.59900	В	550.1303565	-2.0	04 (
Model Ion	-46263.26174	В	591.6424302	-78.19	<.0	0001	Trim LS Hatchbac	-394.70742	В	662.8277300	-0.6	30 C
Model L Series	-45407.97249	В	445.6985809	-101.88	<.0	0001	Trim LS MAXX Hba	-567.22900	В	591.6751026	-0.6	96 0
Model Lacrosse	-38667.66403	В	490.2095435	-78.88	<.0	0001	Trim LS Sedan 4D	-776.01024	В	501.0271130	-1.5	55 0
Model Lesabre	-40075.18228	В	515.4683788	-77.75		0001	Trim LS Sport Co	-1698.76844	В	624.1889147	-2.7	72 (
Model Malibu	-43894 77849	В	602 2931867	-72.88	<.(0001	Trim LS Sport Se	-809.05535	В	595.6347212	-1.3	36 0
Model Monte Ca	-43068.25281	В	726.1099800	-59.31	<1	0001	Trim LT Coupe 2D	2205.98930	В	714.1313029	3.0	00 0
Model Park Ave	-38722.89073	В	454.5671398	-80.79		0001	Trim LT Hatchbac	-369.88643	В	651,4177480	-0.5	57 0
Model STS-V6	-23088 20298	В	654 5603270	-35.27		0001	Trim LT MAXX Hba	-81.94184	В	652.9516792	-0.1	13 0
Model STS-V8	-18770.29802	В	629.8807982	-28.62		0001	Trim LT Sedan 4D	-392.22303	В	530.2088091	-0.7	74 0
Model Sunfire	-47084.57035	В	703.9717325	-86.88		0001	Trim Limited Sed	0.00000	В			-
Model Suntire Model Vibe	-47004.57035 -48316.43680	В	703.9717325 462.4063161	-100.80		0001	Trim Linear Conv	6494.06989	В	529.8423161	12.2	26 4
		-		-100.16	<.0	0001	Train Emear Conv	0464.00808	-	528.0425101	14.4	
Trim Linear Seda	0.00000											
Trim Linear Wago	0.00000											
Trim MAXX Hback	-822.49178	E	630.455878	7 -1.	30	0.1926						
Trim Quad Coupe	-441.93382	E	539.909913	4 -0.	82	0.4135						
Trim SE Sedan 4D	-1158.51424	E	545.471041	8 -2.	12	0.0342						
Trim SLE Sedan 4	0.00000	E	3									
Trim SS Coupe 2D	3822.12984	Е	723.650404	6 5.								
Trim SS Sedan 4D	4498.32818	Е			01	<.0001						
Trim SVM Hatchba	-2542.37138		630.393622	3 7.	.01	<.0001						
Trim SVM Sedan 4) E										
			8 620.597127	4 -4.	14	<.0001						
Trim Sedan 4D	-1586.36866	3 E	620.597127 636.979803	'4 -4. 18 -2.	14	<.0001 <.0001 0.0131						
	-1586.36866 -1854.33717) E	8 620.597127 8 636.979803 8 438.194708	'4 -4. 18 -2.	14	<.0001						
Trim Special Ed	-1586.36866 -1854.33717 0.00000	E	3 620.597127 3 636.979803 3 438.194708	74 -4. 18 -2. 11 -4.	.14 .10 .49 .23	<.0001 <.0001 0.0131						
Trim Special Ed Trim Sportwagon	-1586.36866 -1854.33717 0.00000 0.00000) E	3 620.597127 3 636.979803 3 438.194708 3	74 -4. 18 -2. 11 -4.	14 10 49 23	<.0001 <.0001 0.0131 <.0001						
Trim Special Ed Trim Sportwagon Make Buick	-1586.36866 -1854.33717 0.00000 0.00000) E	8 620.597127 3 636.979803 3 438.194708 3 3	'4 -4. 18 -2. 11 -4.	.14 .10 .49 .23	<.0001 <.0001 0.0131 <.0001						
Trim Special Ed Trim Sportwagon Make Buick Make Cadil	-1586.36860 -1854.33717 0.00000 0.00000 0.00000) E	8 620.597127 8 636.979803 3 438.194708 3 3	74 -4. 18 -2. 11 -4.	14 10 49 23	<.0001 <.0001 0.0131 <.0001	Liter 1.8	0.00000	В			
Trim Special Ed Trim Sportwagon Make Buick Make Cadil Make Chevr	-1586.36860 -1854.33717 0.00000 0.00000 0.00000 0.00000) E	3 620.597127 3 636.979803 3 438.194708 3 3 3 3 3 3 3 3 3	'4 -4. 18 -2. 11 -4.	.14 .10 .49 .23	<.0001 <.0001 0.0131 <.0001	Liter 2.2	0.00000	В			
Trim Special Ed Trim Sportwagon Make Buiok Make Cadil Make Chevr Make Ponti	-1586.36860 -1854.33717 0.00000 0.00000 0.00000) E	3 620.597127 3 636.979803 3 438.194708 3 3 3 3 3 3 3 3 3	'4 -4. 18 -2. 11 -4.	.14 .10 .49 .23	<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3	0.00000	B B			
Trim Special Ed Trim Sportwagon Make Buiok Make Cadil Make Chevr Make Ponti	-1586.36860 -1854.33717 0.00000 0.00000 0.00000 0.00000) E	3 620.597127 3 636.979803 3 438.194708 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	'4 -4. 18 -2. 11 -4.	.14 .10 .49 .23	<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5	0.00000 0.00000 0.00000	B B			
Trim Special Ed Trim Sportwagon Make Buiok Make Cadil Make Chevr Make Ponti Make SAAB	-1586.39886 -1854.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000		3 620.597127 3 636.979803 3 438.194708 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	74 -4. 18 -2. 101 -4.	14 10 49 23	<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.8	0.00000 0.00000 0.00000 0.00000	B B B	-		
Trim Special Ed Trim Sportwagon Make Buiok Make Cadil Make Chevr Make Ponti Make SAAB Make Satur	-1586,38866 -1854,33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	3 E E E E E E E E E E E E E E E E E E E	3 620.597127 3 636.978803 3 438.194708 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	74 -4. 188 -2. 11 -4.		<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.8 Liter 3.1	0.00000 0.00000 0.00000 0.00000 0.00000	B B B B	-		
Trim Special Ed Trim Sportwagon Make Buick Make Cadil Make Chevr Make Ponti Make SAAB Make Satur Type Conve	-1586.38804 -1854.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	3 E E E E E E E E E E E E E E E E E E E	3 620.597127 3 636.97803 3 438.194708 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	74 -4. 188 -2. 111 -4.	.14 .10 .49 .23	<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.8 Liter 3.1 Liter 3.4	0.00000 0.00000 0.00000 0.00000 0.00000	B B B B			
Trim Special Ed Trim Sportwagon Make Buiok Make Cadil Make Chevr Make Ponti Make SAAB Make Satur Type Conve	-1586.38864 -1894.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	3 E E E E E E E E E E E E E E E E E E E	3 020.597127 3 636.979803 3 438.194708 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	14 -4. 18 -2. 11 -4.	14 10 49 23	<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.8 Liter 3.1 Liter 3.4 Liter 3.5	0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	B B B B B			
Trim Special Ed Trim Sportwagon Make Buiok Make Cadil Make Chevr Make Ponti Make SAAB Make SAAB Myee Conve Type Conve Type Coupe	-1586.36806 -1854.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	3 E E C C C C C C C C C C C C C C C C C	3 020.597127 0 036.878803 3 438.194708 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	14 -4. 18 -2. 11 -4.	14 10 49 23	<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.8 Liter 3.1 Liter 3.4 Liter 3.6	0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	B B B B B			
Trim Special Ed Trim Sportwagon Make Buick Make Cadil Make Chevr Make Ponti Make SAAB Make Satur Type Conve Type Cupe Type Hatch Type Sedan	-1586.36866 -1854.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000) E E E E E E E E E E	020.597127 030.676803 3 438.194708 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	14 -4. 18 -2. 11 -4.		<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.5 Liter 3.1 Liter 3.4 Liter 3.5 Liter 3.6 Liter 3.6	0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	B B B B B B			
Trim Special Ed Trim Sportwagon Make Bulick Make Cadil Make Chevr Make Ponti Make SAAB Make SAAB Make SAU Type Conve Type Coupe Type Hatch Type Wagon	-1586.38866 -1854.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	3 E E E E E E E E E E E E E E E E E E E	020.507127 030.679803 0438.194708 03 03 03 03 03 03 03 03 03 03 03 03 03	14 -4. 18 -2. 11 -4.	14 10 49 23	<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.8 Liter 3.1 Liter 3.4 Liter 3.5 Liter 3.6 Liter 3.6 Liter 3.8 Liter 4.6	0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	B B B B B B B B B			
Trim Special Ed Trim Sportwagon Make Bulick Make Cadil Make Chevr Make Ponti Make SAAB Make SAAB Type Coupe Type Coupe Type Hatch Type Wagon Cylinder 4	-1598.38864 -1884.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	3 E E E E E E E E E E E E E E E E E E E	020.597127 030.979803 3 438.194708 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	14 -4. 18 -2. 11 -4.		<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.8 Liter 3.1 Liter 3.4 Liter 3.5 Liter 3.6 Liter 3.6 Liter 3.6 Liter 3.6 Liter 3.8 Liter 4.6 Liter 5.7	0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	B B B B B B B B B			
Trim Special Ed Trim Sportwagon Make Buick Make Cadil Make Chevr Make Ponti Make Satur Type Conve Type Coupe Type Goupe Type Sedan Type Sedan Type Sedan Cylinder 4 Cylinder 6	-1598.36866 -1884.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	3 E E E E E E E E E E E E E E E E E E E	020.507127 020.50	14 -4. 18 -2. 11 -4.		<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.5 Liter 2.8 Liter 3.1 Liter 3.1 Liter 3.6 Liter 3.6 Liter 3.8 Liter 4.6 Liter 5.7 Cruiso 0	0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	B B B B B B B B B B B B B B B B B B B			0.80
Trim Special Ed Trim Sportwagon Make Cadil Make Cadil Make Cadil Make Chevr Make Ponti Make SAAB Make SAAB Make SAB Make Satur Type Coupe Type Coupe Type Coupe Type Wagon Cylinder 4 Cylinder 8	-1586.38866 -1884.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	3 E E E E E E E E E E E E E E E E E E E	0 0 0 0 0 7 1 2 7 3 0 0 0 0 7 1 0 7 0 0 0 0 7 1 0 0 0 0 0 0	14 -4. 18 -2. 11 -4.		<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.5 Liter 2.8 Liter 3.1 Liter 3.4 Liter 3.5 Liter 3.5 Liter 4.6 Liter 5.7 Cruise 0 Cruise 1	0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	B B B B B B B B B B B		-0.25	0.80
Make Buick Make Cadil Make Chevr Make Ponti Make SAAB Make Satur Type Conve Type Conve Type Sedan Type Wagon Cylinder 4 Cylinder 6	-1598.36866 -1884.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	3 E E E E E E E E E E E E E E E E E E E	0 0 0 0 0 7 1 2 7 3 0 0 0 0 7 1 0 7 0 0 0 0 7 1 0 0 0 0 0 0	14 -4. 18 -2. 11 -4.	.14	<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.5 Liter 2.8 Liter 3.4 Liter 3.4 Liter 3.6 Liter 3.6 Liter 3.6 Liter 3.6 Liter 3.8 Liter 3.8 Liter 3.8 Sound 0	0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	B B B B B B B B B B B	123.3212068		0.808
Trim Special Ed Trim Sportwagon Make Bulok Make Cadil Make Cadil Make Chevr Make Ponti Make Satur Type Conve Type Conve Type Coupe Type Hatch Type Sedan Type Wagon Cylinder 4 Cylinder 6 Cylinder 8 Liter 2	-1586.38866 -1884.33717 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	3 E E E E E E E E E E E E E E E E E E E	020 597127 020 597127 030 670603 438 104708 3 3 3 3 3 3 3 3 3 3 3 3 3	-4 -4. -4 -4. -8 -2. -1 -4. 	14 10 49 23	<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.5 Liter 2.8 Liter 3.1 Liter 3.4 Liter 3.5 Liter 3.5 Liter 4.6 Liter 5.7 Cruise 0 Cruise 1	0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	B B B B B B B B B B B		-0.25	
Trim Special Ed Trim Sportwagon Make Cadil Make Cadil Make Cadil Make Chevr Make Ponti Make SAAB Make SAAB Make SAB Make Satur Type Coupe Type Coupe Type Coupe Type Wagon Cylinder 4 Cylinder 8	-1598.30306 -1894.33717 0.00000	S E S S S S S S S S	020.597127 030.677693 030.67	-4444444444.		<.0001 <.0001 0.0131 <.0001	Liter 2.2 Liter 2.3 Liter 2.5 Liter 2.5 Liter 2.8 Liter 3.4 Liter 3.4 Liter 3.6 Liter 3.6 Liter 3.6 Liter 3.6 Liter 3.8 Liter 3.8 Liter 3.8 Sound 0	0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	B B B B B B B B B B B		-0.25	

The parameter estimates of the 11 selected variables are tabulated here.

The QQ plot for the residual of the price (the difference between the observed and predicted values) and the histogram of the distribution of residuals show us that it approximately follows a normal distribution, with some outliers being present.

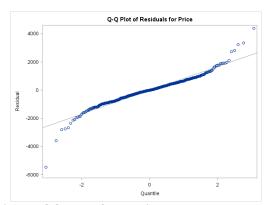


Fig. 3: The QQ-Plot of the residuals are plotted to check for normal distribution

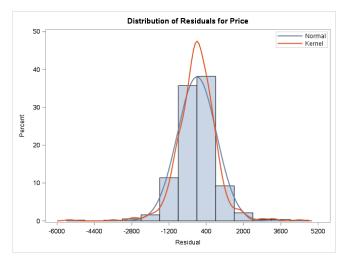


Figure 4: The distribution of residuals is plotted to check for normal distribution.

The studentized residual plot shows us the presence of around 28 outliers in this training data set.

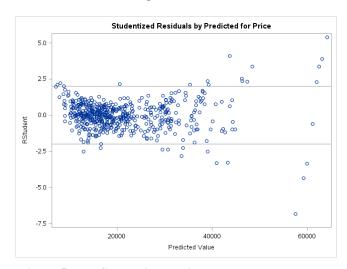


Figure 5: The Studentized residuals are plotted to check for outliers.

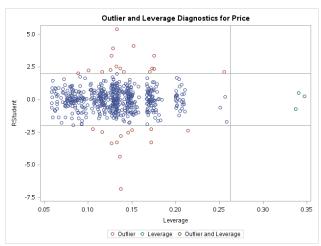


Figure 6: The studentized leverage and outlier plot is used to find whether there are any outliers which heavily influence the prediction model.



The leverage and outlier plots show that these outliers do not hold any leverage. Hence, their absence from the data set doesn't affect the model significantly.

E. Regression Tree

A regression tree which models price to the selected subset of attributes is created (by using the training data set) by calling the HPSPLIT Procedure. The results are tabulated in table 5.

Table - 5: HPSPLIT Procedure summary

		rmance In			
	Execution N			-Machine	
	Number of	Threads	2		
	Data /	Access In	formati	on	
	Data	Engine	Role	Path	
	WORK.MEX1	V9	Input	On Client	
	Mo	odel Infon	mation		
Spl	it Criterion Used	I		Vari	ano
Pru	ning Method			Cost-Compl	exit
Suk	tree Evaluation	Criterion		Cost-Compl	exit
Nur	mber of Branche	5			
	ximum Tree Dep	th Reques	sted		1
Max		th Achiev	ed		1
	ximum Tree Dep	ui Acillev			
Max	ximum Tree Dep e Depth	ui Aciliev			1
Ma: Tre					-
Max Tre	e Depth	Before Pro	uning		34
Max Tre Nur	e Depth mber of Leaves I	Before Pro	uning		34
Max Tre Nur	e Depth mber of Leaves I	Before Pru	uning	ad 563	10 34- 152

The HPSPLIT Procedure uses Variance for split criteria and Cost-Complexity for Pruning. The number of leaves before and after pruning is also shown.

This tree, before pruning, had 344 leaf nodes. Upon using the cost complexity algorithm for pruning, the number of leaves got reduced to 152. The process of pruning is visually represented in figure 7.

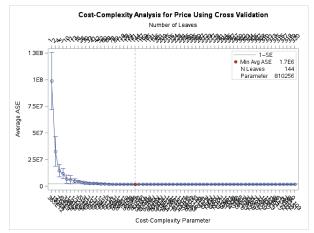


Figure 7: The Average Square Rate is plotted against the number of leaves and cost-complexity parameter to find the minimum ASE.

Here, the minimum average square error is 1.7E6, and that model is selected. The following tree (Fig 8) was produced,

which has reduced overfitting. The zoomed-in regression tree (Fig 9) is generated alongside the actual regression tree.

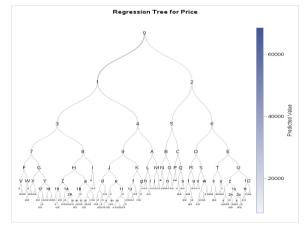


Figure 8: The Regression tree is graphically represented.

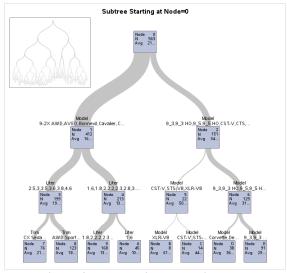


Figure 9: Zoomed in Regression tree.

The order of importance of the variables is also tabulated (table 6). From it, we can infer that the model of the car is most associated with price and that the presence/absence of upgraded sound systems is least associated with price.

Table – 6: HPSPLIT Attribute Importance

Leave	N s	ASE		RSS
15	2 12	1859	6	8606340
	Variable I	mport	ance	
	Tra	aining		
Variable	Relative	Impo	rtance	Count
Model	1.0000	:	215640	25
Liter	0.3080	6	6418.3	5
Trim	0.1855	4	0004.7	31
Mileage	0.1839	3	9651.1	80
Туре	0.0410		8849.2	3
Leather	0.0106		2296.2	3
Make	0.0076		1629.4	2
Sound	0.0073		1575.6	2



F. Prediction on test data

The 3 trained models were used to predict the price of the test data, which contained 241 records. The Observed vs Predicted graphs were plotted for all the three models.

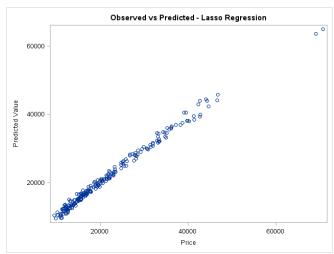


Figure 10: Observed vs Predicted Price – Lasso Regression.

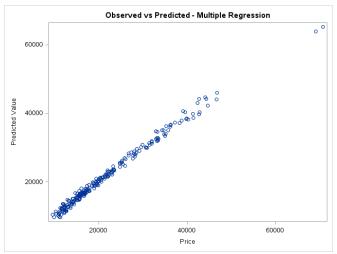


Figure 11: Observed vs Predicted Price – Multiple Regression.

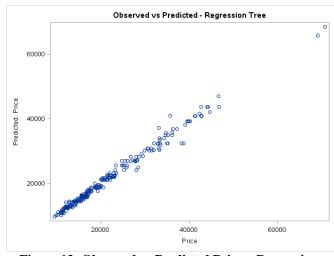


Figure 12: Observed vs Predicted Price – Regression Tree.

The error rates for these models were calculated by using the following formula:

$$Mean (\sum (|(observed - predicted)|/observed) * 100)$$
 (3)

The results are tabulated below.

Table - 7: Model Error Rates

Model	Error Rate
Lasso Regression	3.581%
Multiple Regression	3.468%
Regression Tree	3.512%

Looking at our models, we see that error rate in multiple regression (3.468%) is smaller than the error rate in Regression tree (3.512%) which is lesser than the error rate in Lasso Regression (3.581%).

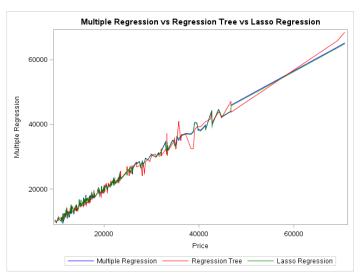


Figure 13: A color-coded line graph comparing the price predictions of the different models with the actual value

However, from this, we can't conclude that our hypothesis holds good since the error rates were found only on one variation of the training and testing data set. By iterating this process[8](with the selection of different records by varying the seed of the random sampling procedure), we will get a set of error rates of lasso regression, multiple regression and regression tree, for the same variation of the data set.

G. Iterative ANOVA based comparison of models

Using One-way Analysis Of Variance (ANOVA) we need to verify whether the error rates of these models differ significantly from each other.

The process was run 35 times, and the error rates for lasso regression, multiple regression, and regression tree were noted (Table 8) along with the respective seeds of splitting for reproducibility.



Table – 8: Seed – Error Matrix

	Total rows: 35	Total columns: 4	H -	← Rows 1-35 → →
	Seed	multiple	tree	lasso
	2786	3.46839529	3.51176948	3.58138216
	1589	3.6757781	3.5680421	3.57764978
	100	3.67042	4.14094084	4.01717736
	1458	3.49021115	3.24932075	3.48042261
	2607	3.25016677	3.91970384	3.28921334
	8457	3.61699478	4.40631117	3.71202329
	5841	3.44307372	3.67629277	3.6288628
	6985	3.68199985	3.77225492	3.64147977
ĺ	4185	3.51752289	3.58014847	3.45390467
	1208	3.58700681	4.02278469	3.48855108
	7408	3.55941912	3.48832635	3.56545587
	7985	3.38059236	3.7056248	3.33113402
	27	3.32998887	3.41531015	3.24091976
	3451	3.64931838	3.89251644	3.71782049
	8	3.6142105	4.21475854	3.71334439
	587	3 0037316	3 65458366	3 10518136

This table contains the error rates of the three models for 35 different variations of training and test data.

The data were recoded to perform ANOVA.

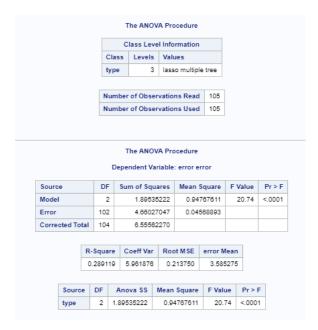
Table - 9: Recoded Error Data

	error	type		
58	4.0627354	tree		
59	3.94371457	tree		
60	3.85089763	tree		
61	3.591572	tree		
62	3.63890433	tree		
63	3.58138216	lasso		
64	3.57764978	lasso		
65	4.01717736	lasso		
66	3.48042261	lasso		
67	3.28921334	lasso		
68	3.71202329	lasso		
69	3.6288628	lasso		
70	3.64147977	lasso		
71	3.45390467	lasso		
72	3.48855108	lasso		
73	3.56545587	lasso		

This table contains the recoded error rates.

The ANOVA procedure was carried out, and the results were tabulated in table 10.

Table - 10: ANOVA Summary



With the P-value being lesser than 0.05, we can confirm that the error rates are significantly different from each other. Their distribution is also plotted (Fig 14).

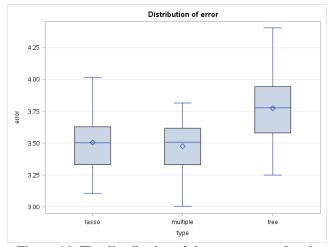


Figure 14: The distribution of the error rates of each model type is represented using box plots.

Table - 11: Mean Error Rates

Level of type		error	
	N	Mean	Std Dev
lasso	35	3.50528606	0.19866047
multiple	35	3.47601284	0.18966152
tree	35	3.77452740	0.24825250

The mean error rates of the models (Table 11) might be misleading, since we can't be sure about which groups/models have significantly different means from the other. This is due to the existence of more than 2 groups/levels. One-Way ANOVA can only find out whether there exists any significant difference between any of the groups. To get a clearer picture, we need to perform a post-hoc test to find the groups which have significantly different means.

We are performing a Tukey's test (Tukey's Honest Significant Difference Test) to find out the groups which are actually different from each other.

The test compares all possible pairs of means and checks for statistically significant differences between them. Since the sample size for all the groups is the same, we do not use the Tukey-Kramer Method[7], and use the standard version of the algorithm.

Table – 12: Tukey's Test Summary

Alpha	0.05
Error Degrees of Freedom	102
Error Mean Square	0.045689
Critical Value of Studentized Range	3.36358
Minimum Significant Difference	0.1215



From table 12 we can get the critical value of the studentized range and the minimum significant difference. The result is plotted graphically (Fig 15).

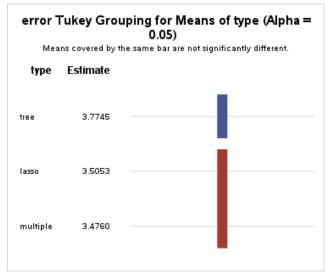


Figure 15: The result of Tukey's Test is plotted in such a way that the means which are covered by the same bar are not significantly different.

From Fig. 15, we can infer that the mean error rates of lasso regression models and multiple regression models are not significantly different, but the mean error rate of regression trees are higher and significantly different from the other two.

IV. CONCLUSION AND FUTURE ENHANCEMENT

The prediction error rate of all the models was well under the accepted 5% of error. But, on further analysis, the mean error of the regression tree model was found to be more than the mean error rate of the multiple regression and lasso regression models. Even though for some seeds the regression tree has better accuracy, its error rates are higher for the rest. This has been confirmed by performing an ANOVA. Also, the post-hoc test revealed that the error rates in multiple regression models and lasso regression models aren't significantly different from each other. To get even more accurate models, we can also choose more advanced machine learning algorithms such as random forests, an ensemble learning algorithm which creates multiple decision/regression trees, which brings down overfitting massively or Boosting, which tries to bias the overall model by weighing in the favor of good performers. More data from newer websites and different countries can also be scraped and this data can be used to retrain these models to check for reproducibility.

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Pattabiraman Venkatasubbu obtained his Ph.D. from Bharathiar University, India. He has a total Professional experience of 19 years working in various prestigious institutions. He is currently a Professor at Vellore Institute of Technology, Chennai Campus, India. He has authored several books in the field of Computer Science. He is a

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