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BRKSEC-3005

# Cryptographic Protocols and Algorithms

Frederic Detienne – Distinguished Engineer

# Cisco Spark

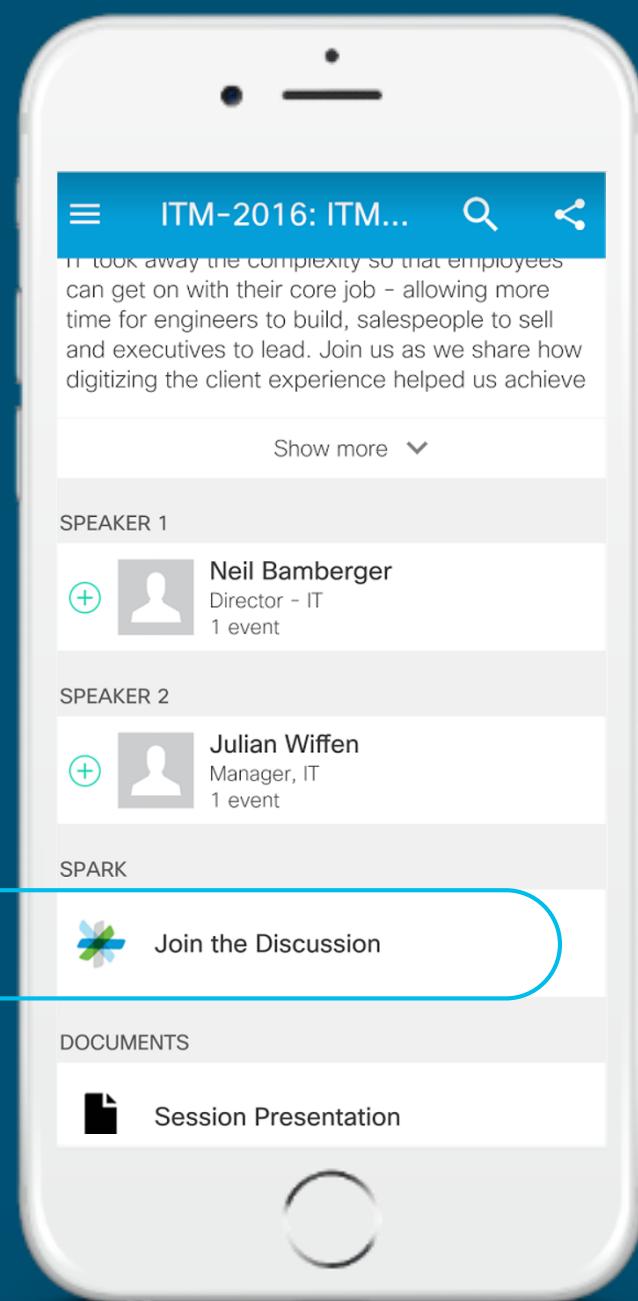


## Questions?

Use Cisco Spark to communicate with the speaker after the session

## How

1. Find this session in the Cisco Live Mobile App
2. Click “Join the Discussion”
3. Install Spark or go directly to the space
4. Enter messages/questions in the space



[cs.co/ciscolivebot#BRKSEC-3005](https://cs.co/ciscolivebot#BRKSEC-3005)

# My Professional Life

- Belgian
  - live in Aywaille
- Joined Cisco on January 1, 1997
  - fd@cisco.com
- Distinguished Engineer (TAC)
  - Web Content, AAA, Firewalls, VPNs, IPTV
  - Bit of everything (stuff nobody else wanted)
  - Made DMVPN, then FlexVPN
  - Focus on Serviceability



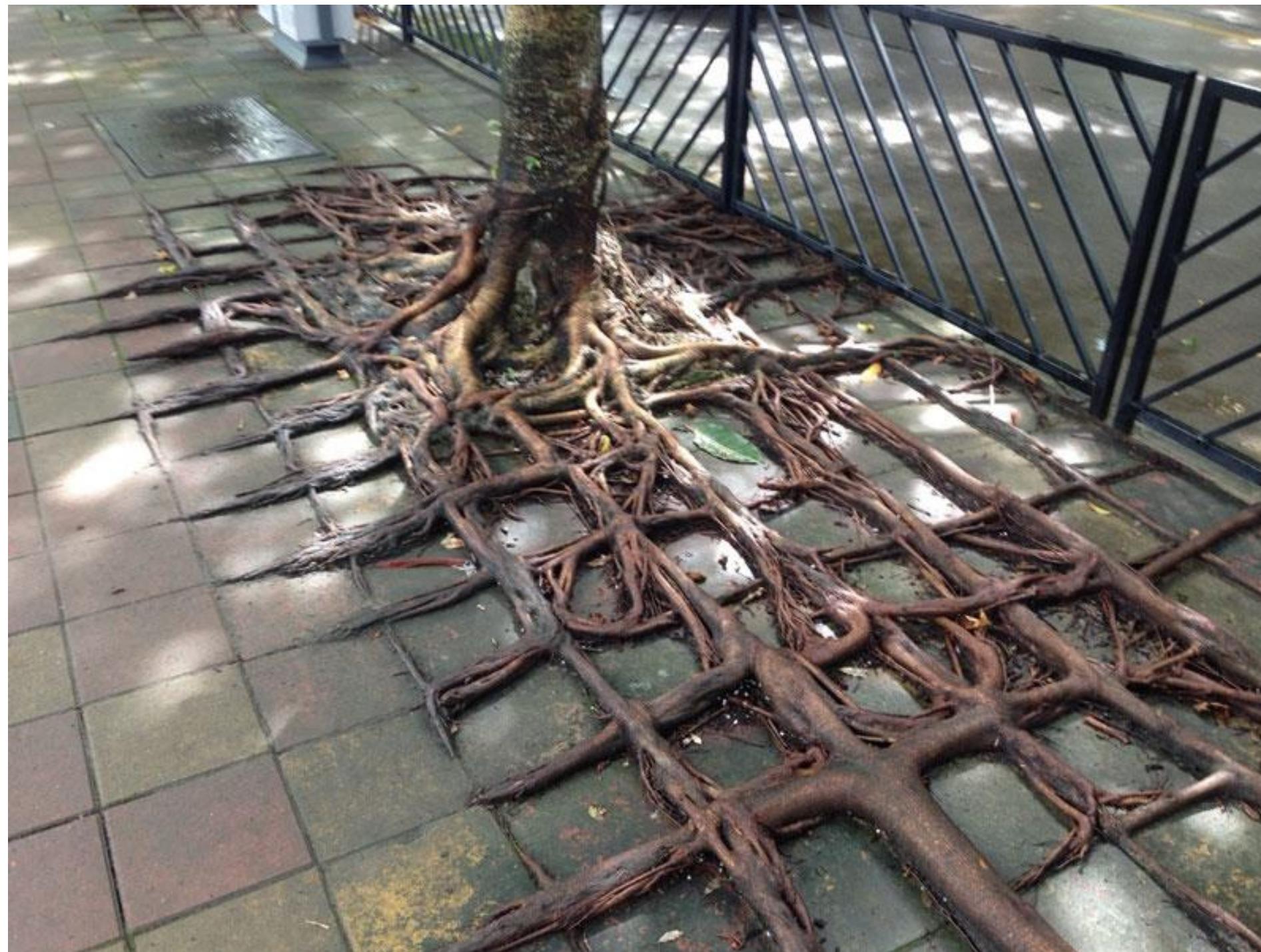
# Agenda

- A Brief Introduction
- Hash and HMAC's
- Symmetric Encryption
- MODP: Multiplicative Group of Integers Modulo P
- ECC: Elliptic Curve Cryptography
- Performances and Security
- Practical Applications; IKEv2, SSL and PKI
- Attacks, Weaknesses & Self-Inflicted Pain
- Conclusion and Recommendations



# Introduction

# The Tree of Math



What happened to that tree  
in front of math class ?

It grew squared roots



# Cryptographic Mechanisms



Encryption



Signatures



Data Authentication  
(HMAC)



Random Number  
Generation



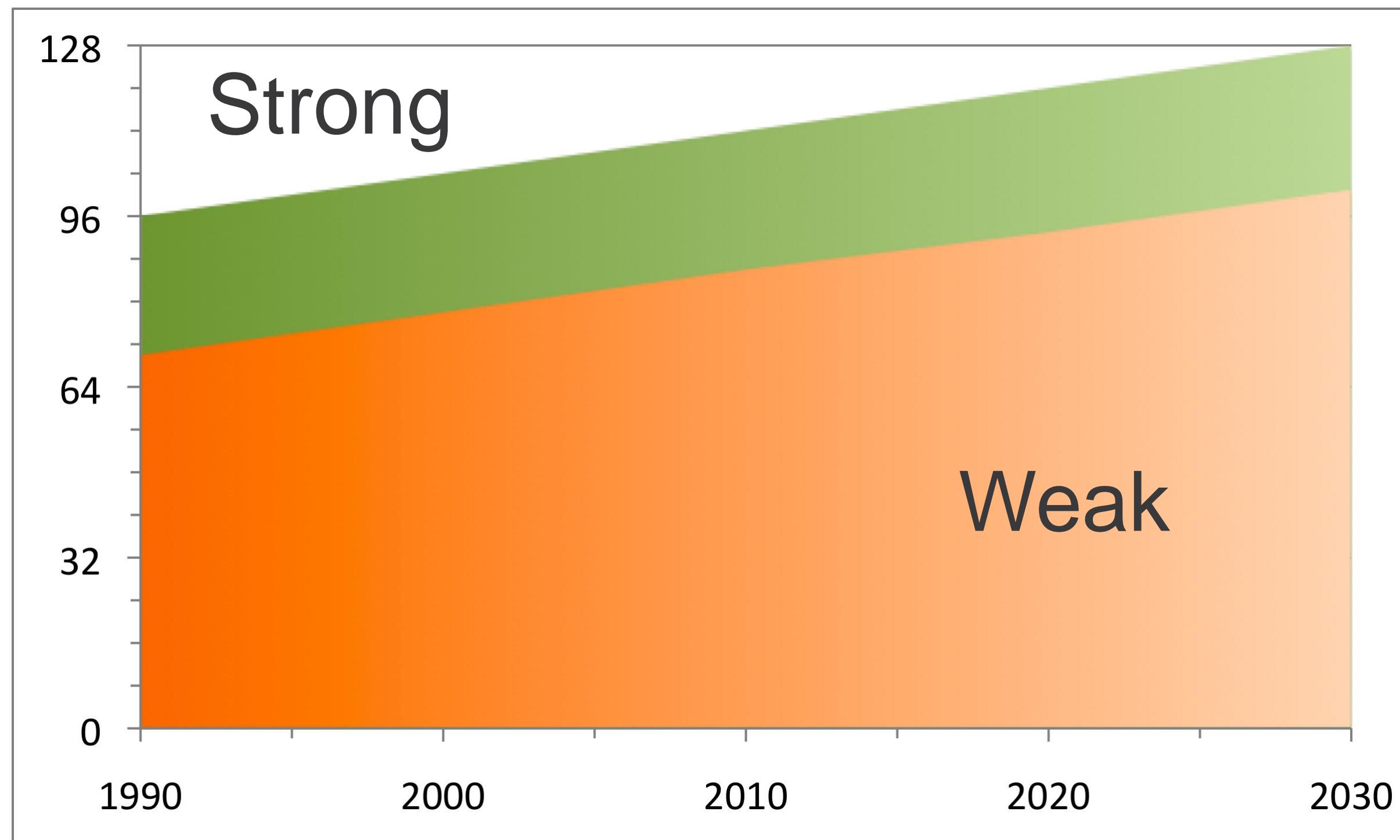
Key Establishment



Hashing



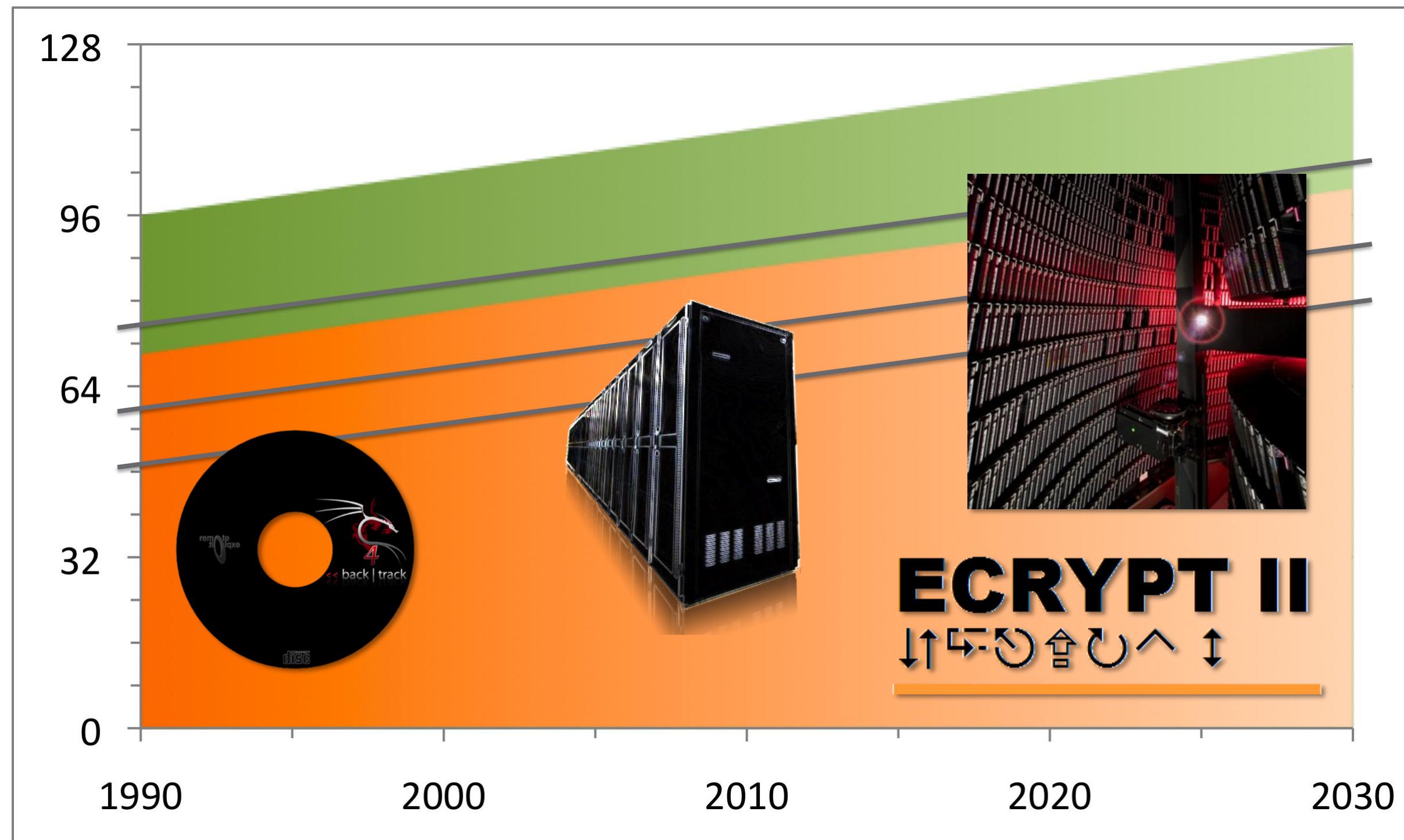
# Key Strength



Sources: Lenstra and Verheul, NIST

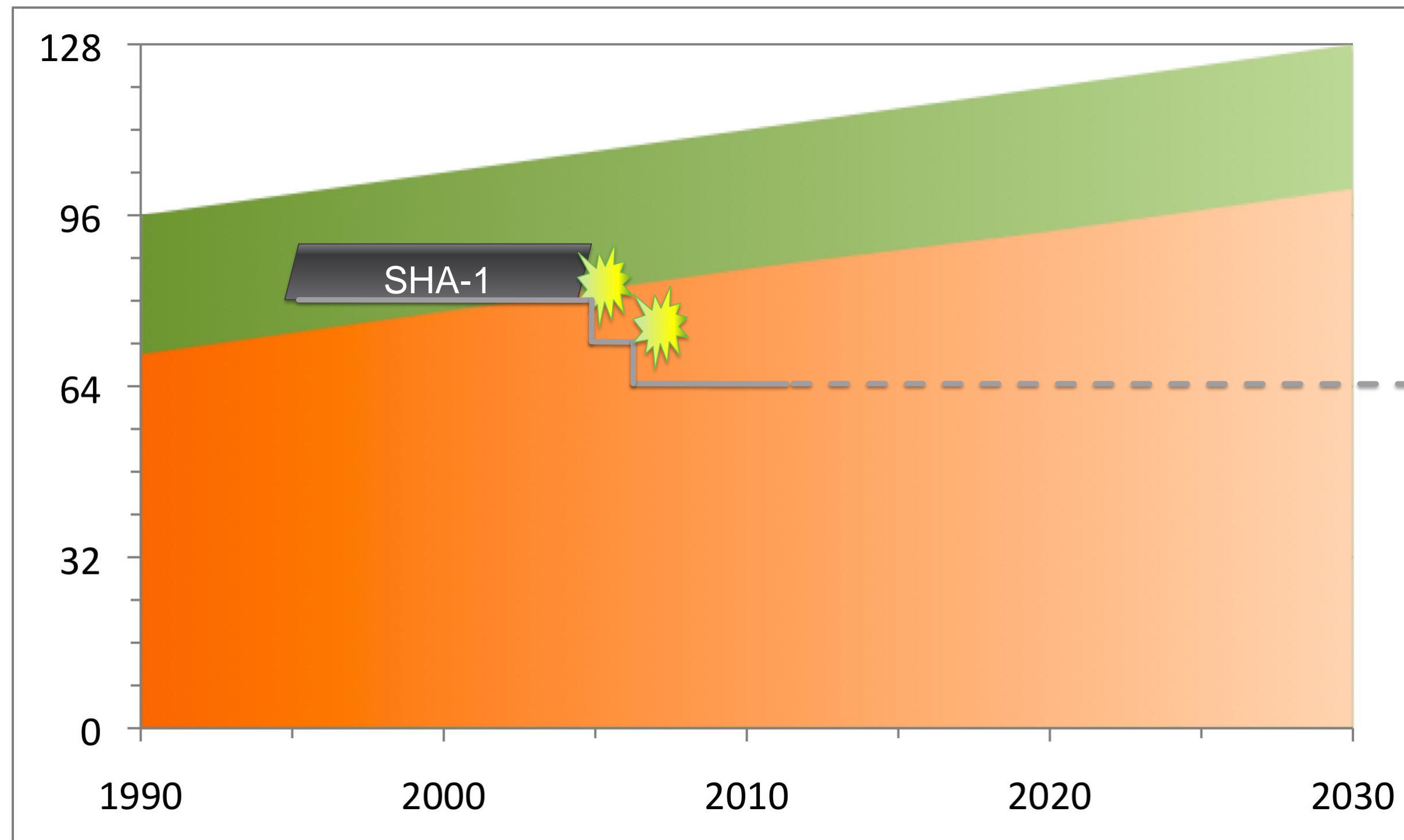


# Attacker Strength





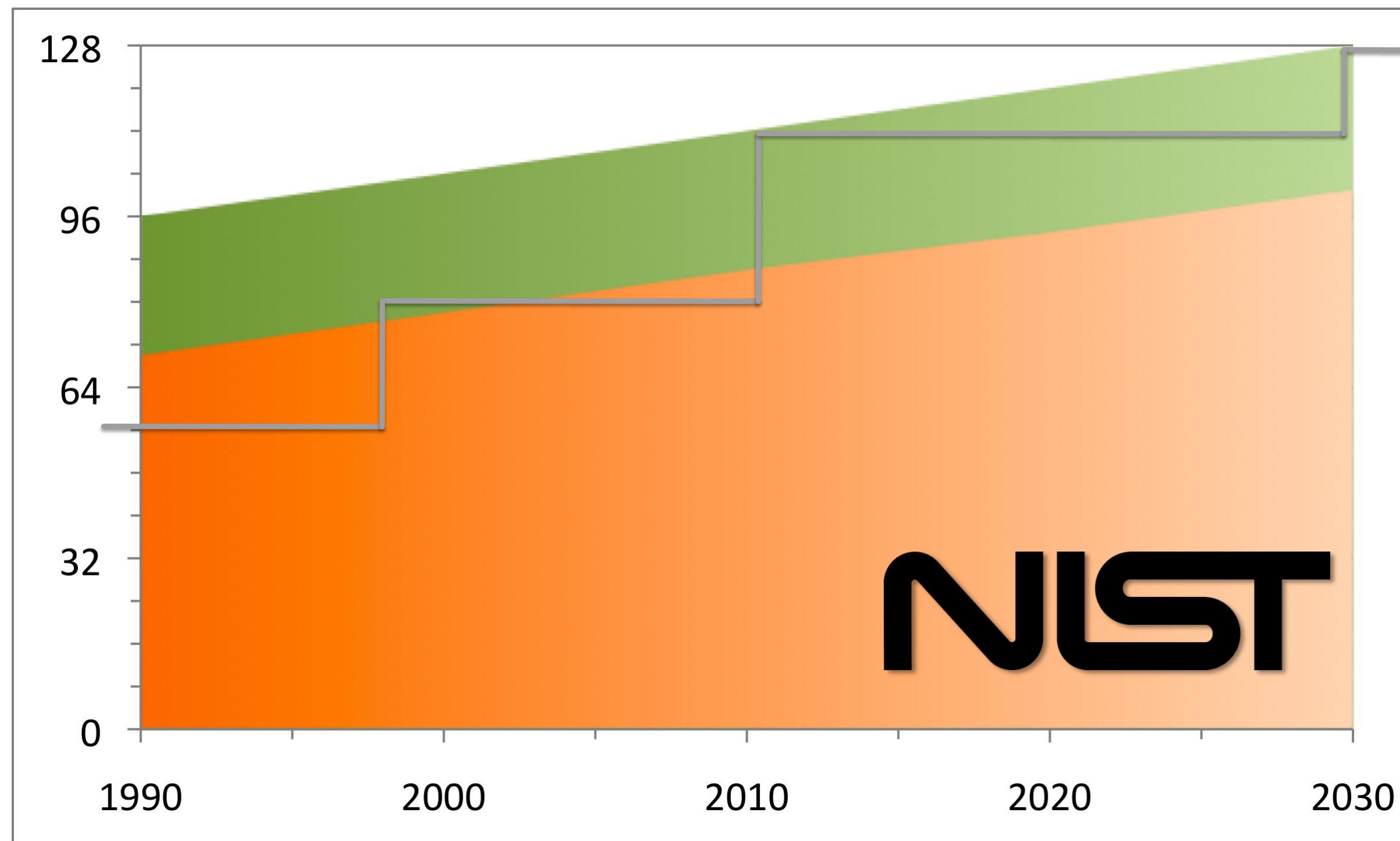
# Algorithms Never Get Stronger



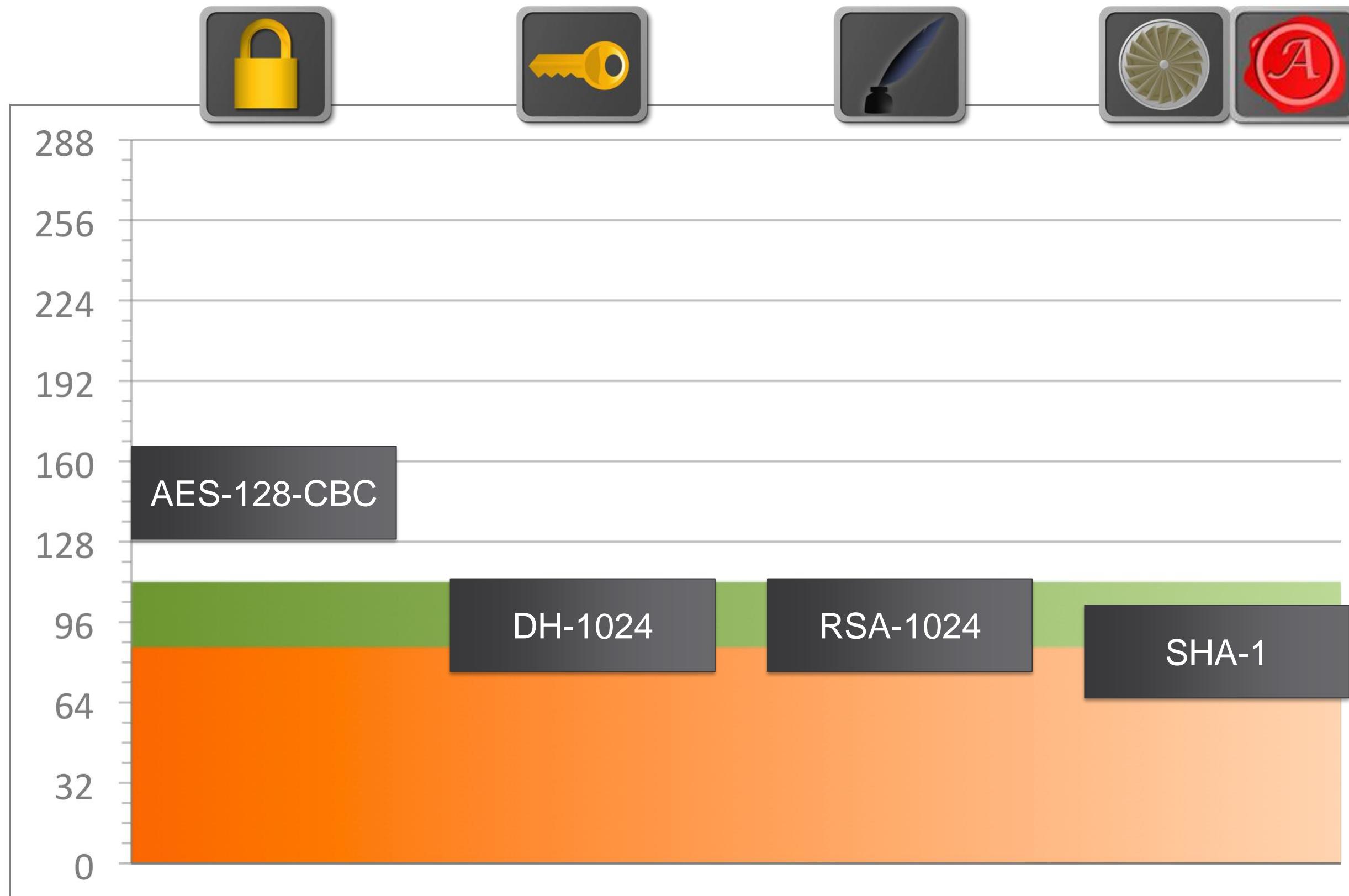
Sources: FIPS-180-1, Wang, Yin, Yu '05, Cochran '07



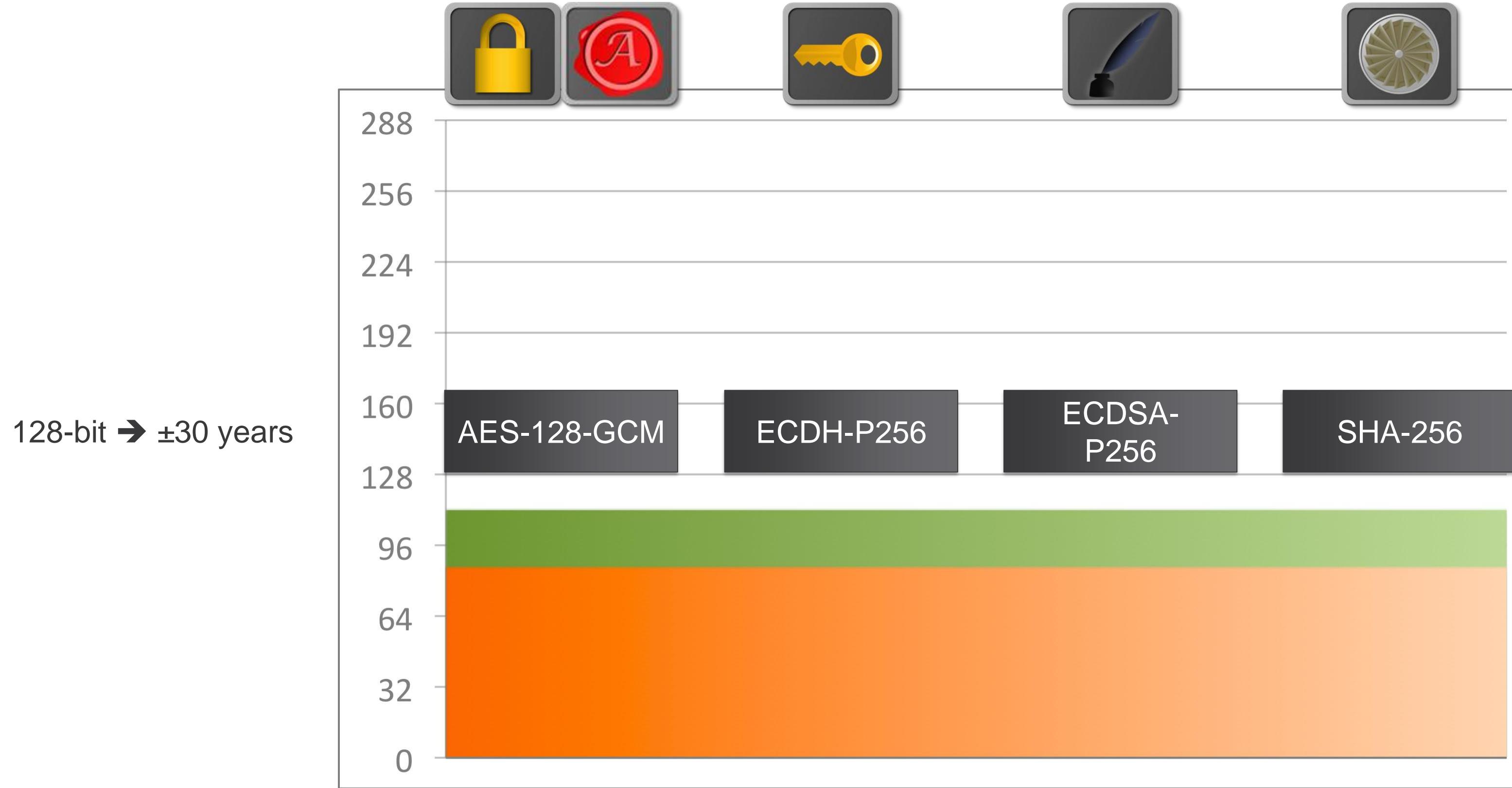
# Strength increases by steps



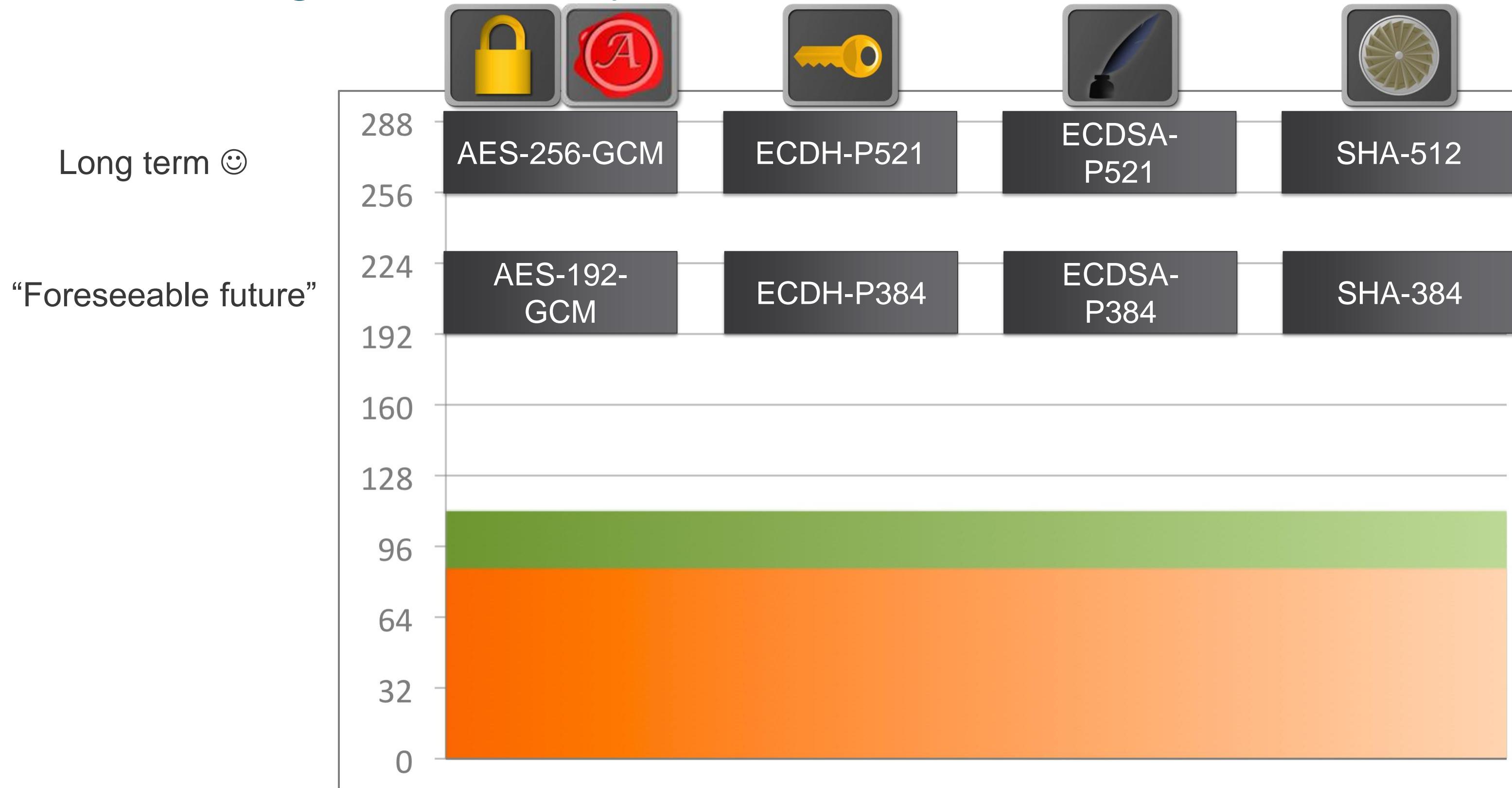
# Prevalent



# Next Generation Encryption



# NGE higher security levels



# Next Generation Encryption

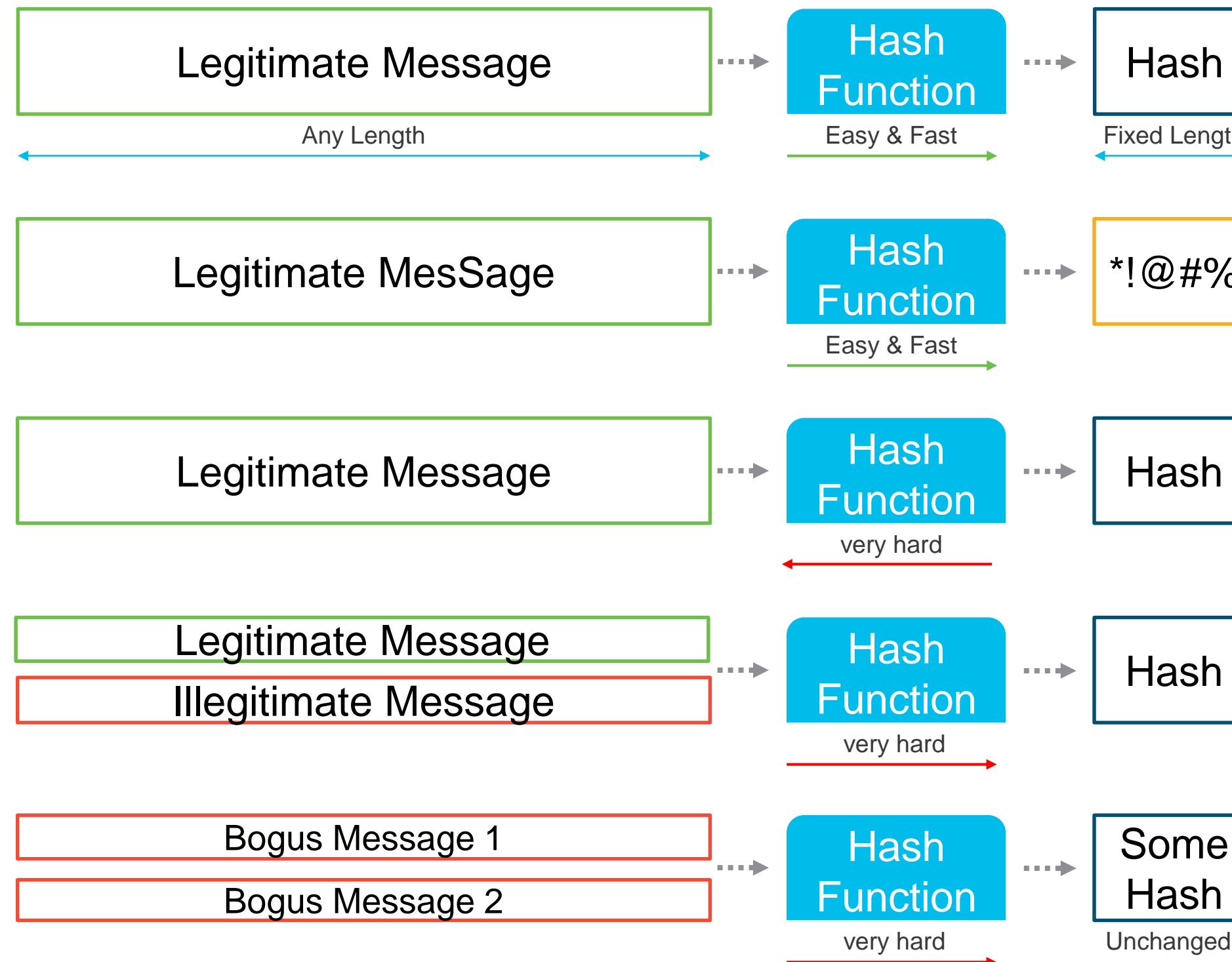
		Authenticated Encryption	AES-GCM
		Authentication	HMAC-SHA-2
		Key Establishment	ECDH
		Digital Signatures	ECDSA
		Hashing	SHA-2
		Entropy	SP800-90
		Protocols	TLSv1.2, IKEv2, IPsec, MACSec



# Hashes and HMAC's

## Focus on SHA-2

# What is a Cryptographic Hash Function



**Fixed length output**

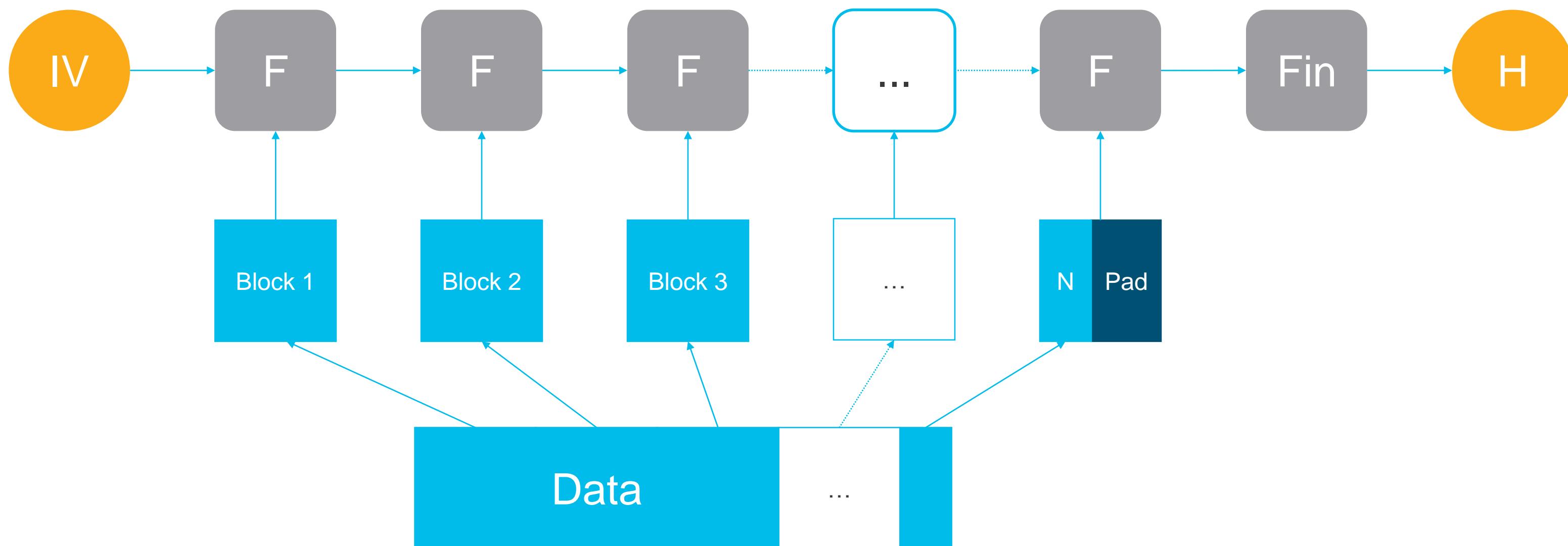
**Avalanche effect**  
(small change in message, big change in hash)

**Pre-image resistance**  
(message can not be found from hash)

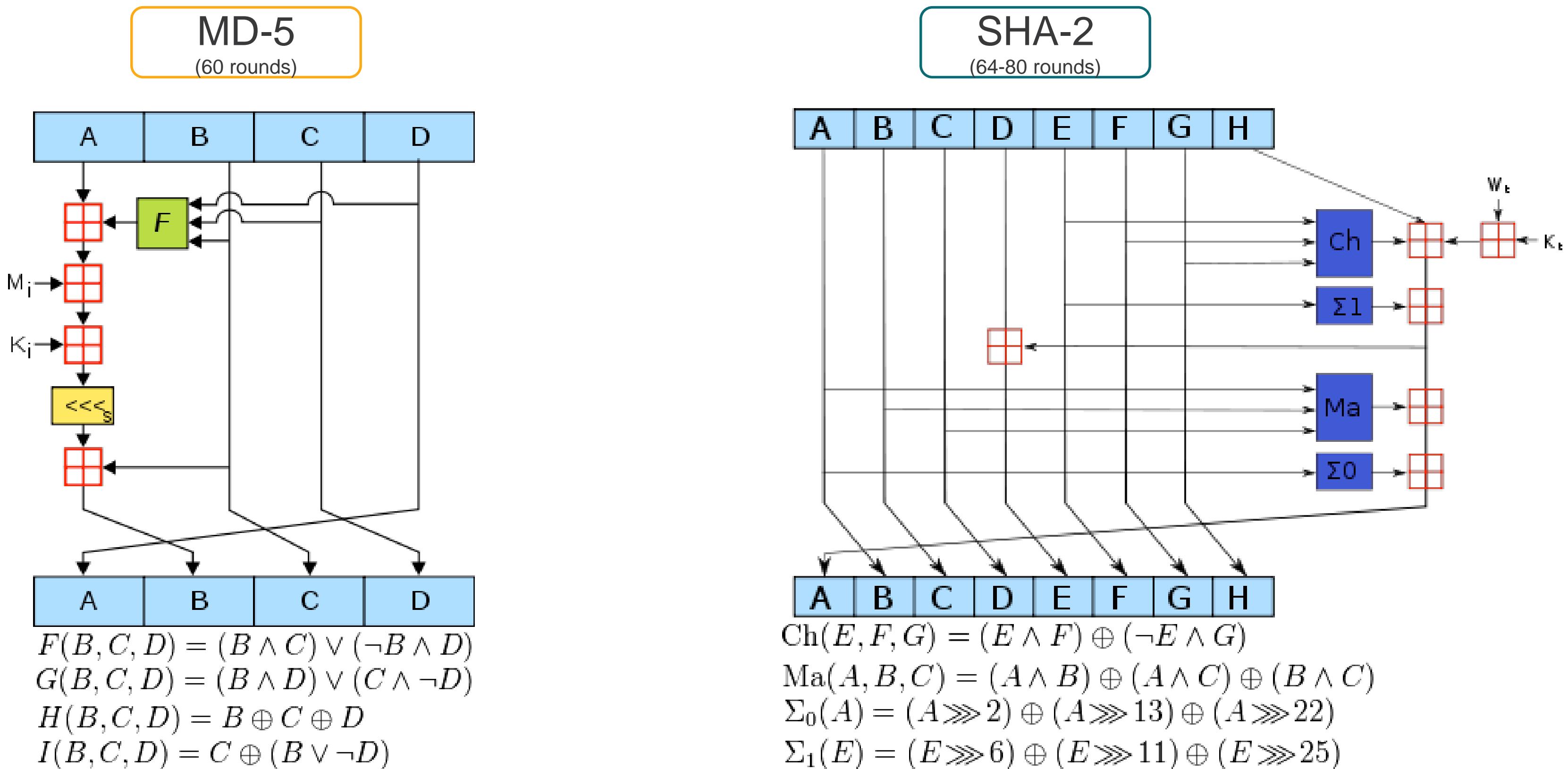
**Second pre-image resistance**  
(legitimate message and hash are imposed; find new message)

**Collision resistance**  
(attacker gets to select message 1 and 2 as long as they hash equally)

# The Merkle–Damgård Construction



# MD-5 vs SHA-2 – Hash Functions



# Rough Hash Algorithms Comparison

Algorithm/variant	Output size	Max msg size	Collisions found
MD-5	128	$2^{64}-1$	yes
SHA-1	160	$2^{64}-1$	yes (hard)
SHA-2	SHA-256	256	$2^{64}-1$
	SHA-384	512	$2^{128}-1$
	SHA-512	512	$2^{128}-1$

Note the increasing output size !

IPsec truncates output to 128, 192 or 256 bits (16, 24 or 32 bytes).

Not IKE

Algorithm ID	Block Size	Output Length	Trunc. Length	Key Length	Algorithm Type
HMAC-SHA-256-128	512	256	128	256	auth/integ
HMAC-SHA-384-192	1024	384	192	384	auth/integ
HMAC-SHA-512-256	1024	512	256	512	auth/integ
PRF-HMAC-SHA-256	512	256	(none)	var	PRF
PRF-HMAC-SHA-384	1024	384	(none)	var	PRF
PRF-HMAC-SHA-512	1024	512	(none)	var	PRF

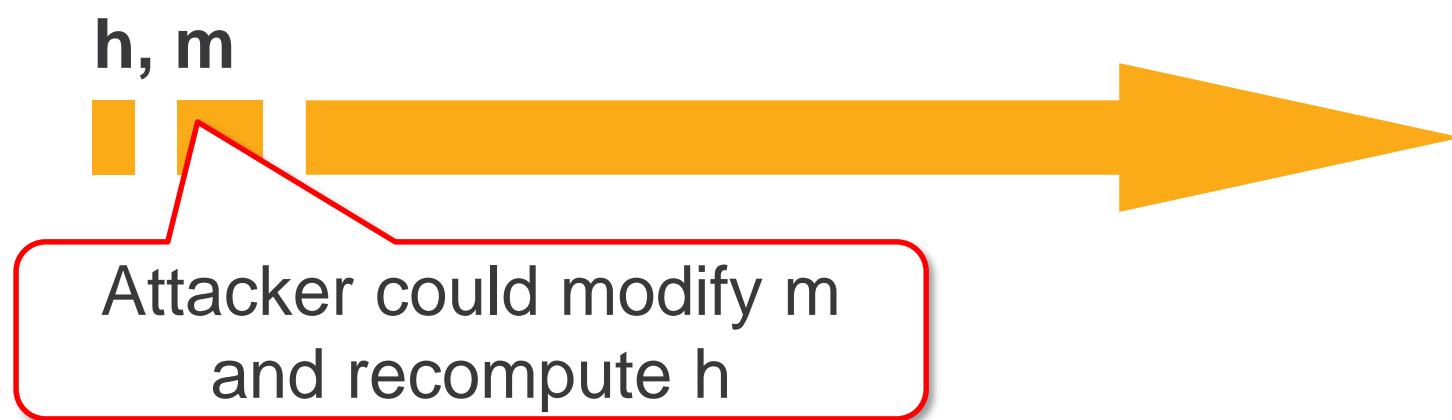
# Using a Hash or an HMAC

## Alice

Must send a message  $m$

**Goal: data does not get corrupted in transit**

Computes  $h = \text{HASH}(m)$



## Bob

Computes  $h' = \text{HASH}(m)$

Checks  $h' = h$

If yes  $\rightarrow$  message is valid

If no  $\rightarrow$  message was damaged

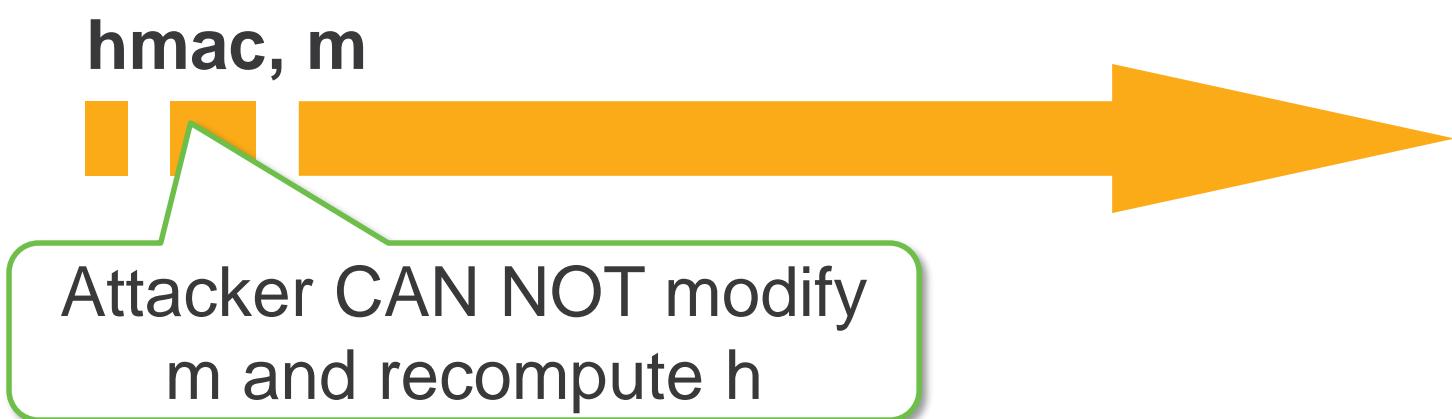
Collision Resistance

Share pre-shared key  $k$  with Bob

Must send a message  $m$

**Goal: Bob assured data comes from Alice**

Computes  $\text{hmac} = \text{HASH}(m|k)$



Share pre-shared key  $k$  with Alice

Computes  $h' = \text{HASH}(m|k)$

Checks  $h' = h$

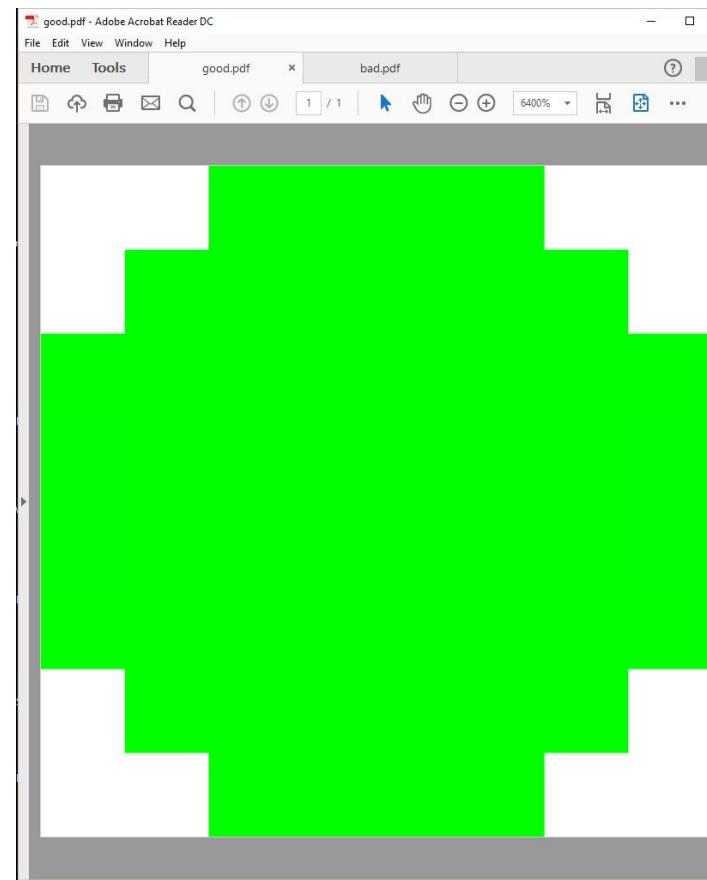
If yes  $\rightarrow$  message is valid

If no  $\rightarrow$  message was damaged

Unforgeability

# SHA-1 Collisions with SHAttered

good.pdf

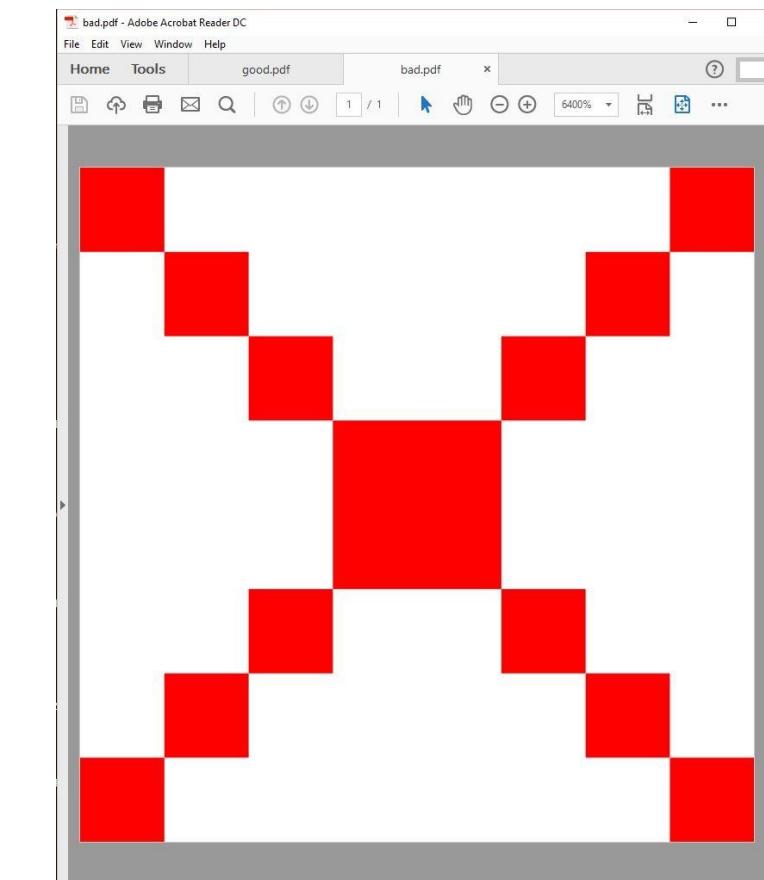


This attack required over 9,223,372,036,854,775,808 SHA1 computations.

This took the equivalent processing power as 6,500 years of single-CPU computations and 110 years of single-GPU computations.

-SHAttered.io

bad.pdf



SHA-1 checksum:

d00bbe65d80f6d53d5c15da7c6b4f0a655c5a86a

SHA-1 checksum:

d00bbe65d80f6d53d5c15da7c6b4f0a655c5a86a

# Applied hashing: Blockchain & bitcoin & ...

# Blockchain

## Block # 1 (genesis block)

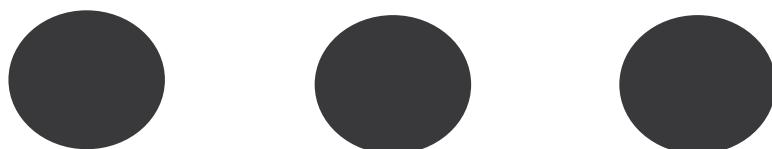
Timestamp  
Payload  
Nonce  
hashPrevBlock = None

## Block # 2

Timestamp  
Payload  
Nonce  
hashPrevBlock = H(#1)

## Block # 3

Timestamp  
Payload  
Nonce  
hashPrevBlock = H(#2)



```
class Block(object):  
    def __init__(self, hashPrevBlock, payload):  
        self.hashPrevBlock = hashPrevBlock  
        self.payload = payload  
        self.timestamp = datetime.now()  
        self.Nonce = self.mine()
```

```
def hash(self, Nonce=None):
```

```
def mine(self):
```

```
class BlockChain(object):  
    def __init__(self, size):
```

```
def verify(self):
```

# Mining

```
def mine(self):
    # let's calculate hash until we have "0000" at the beginning
    for nonce in range(1, 10000000):
        attempt = self.hash(nonce)

        if attempt.startswith("0000"): # Mathematical challenge (find hash that starts with x-number of 0's
            logger.debug("We found matching hash and we are setting it as Nonce: " + attempt)
            self.Nonce = attempt
            return self.Nonce

    logger.error("We couldn't find nonce satisfying 0's condition")
    exit(1)
```



Purpose of mining is to reach a secure, tamper-resistant consensus

Reward: Transaction fee + Reward (initially 50BTC, nowadays 12.5)

# Symmetric Encryption Algorithms: One Time Pad & AES

# One Time Pad

- A Pad is a **truly random** sequence of numbers
- Pad is used as encryption and decryption key through **modular addition**
- The Pad must be **as long as the message**
- The Pad must be used **ONLY ONCE**
- If used properly, this is the **strongest possible** encryption scheme



M	1	0	0	1	1	0	1	1	1	1	...
Pad	0	1	1	0	0	0	1	0	1	1	...
Cypher	1	1	1	1	1	0	0	1	0	...	

A One Time Pad (here using XOR)

# One Time Pad - example

	H	E	L	L	O	message
	7	4	11	11	14	
+	23	12	2	10	11	key
=	30	16	13	21	25	$m + k$
mod 26	4	16	13	21	25	$(m+k) \text{ mod } 26$
	<b>E</b>	<b>Q</b>	<b>N</b>	<b>V</b>	<b>Z</b>	<b>ciphertext</b>

	E	Q	N	V	Z	ciphertext
	4	16	13	21	25	
-	23	12	2	10	11	key
=	-19	4	11	11	14	$c - k$
mod 26	7	4	11	11	14	$(c-k) \text{ mod } 26$
	<b>H</b>	<b>E</b>	<b>L</b>	<b>L</b>	<b>O</b>	<b>message</b>



# Issue 1 – Key Length

	H	E	L	L	O	message
	7	4	11	11	14	
+	23	12	2	10	11	key
=	30	16	13	21	25	$m + k$
mod 26	4	16	13	21	25	$(m+k) \text{ mod } 26$
	E	Q	N	V	Z	ciphertext

Key must have the same size as message... Key exchange is a problem!

Use high quality Deterministic Random Bit Generator (DRBG)

Select Carefully... ☺

# Issue 2 – Key Re-use & Known Plain Text Attack

	H	E	L	L	O	message
	7	4	11	11	14	
+	23	12	2	10	11	key
=	30	16	13	21	25	$m + k$
mod 26	4	16	13	21	25	$(m+k) \text{ mod } 26$
	E	Q	N	V	Z	ciphertext
	H	E	L	L	O	known message
	4	16	13	21	25	ciphertext
-	7	4	11	11	14	known message
=	-3	12	2	10	11	$c - m$
mod 26	4	12	2	10	11	$(c - m) \text{ mod } 26$
=	KEY					

Assumption #1: Attacker knows some plain text (e.g. injection, guess,...)

Assumption #2: Attacker can wiretap ciphertext

Conclusion: Attacker can compute the key easily

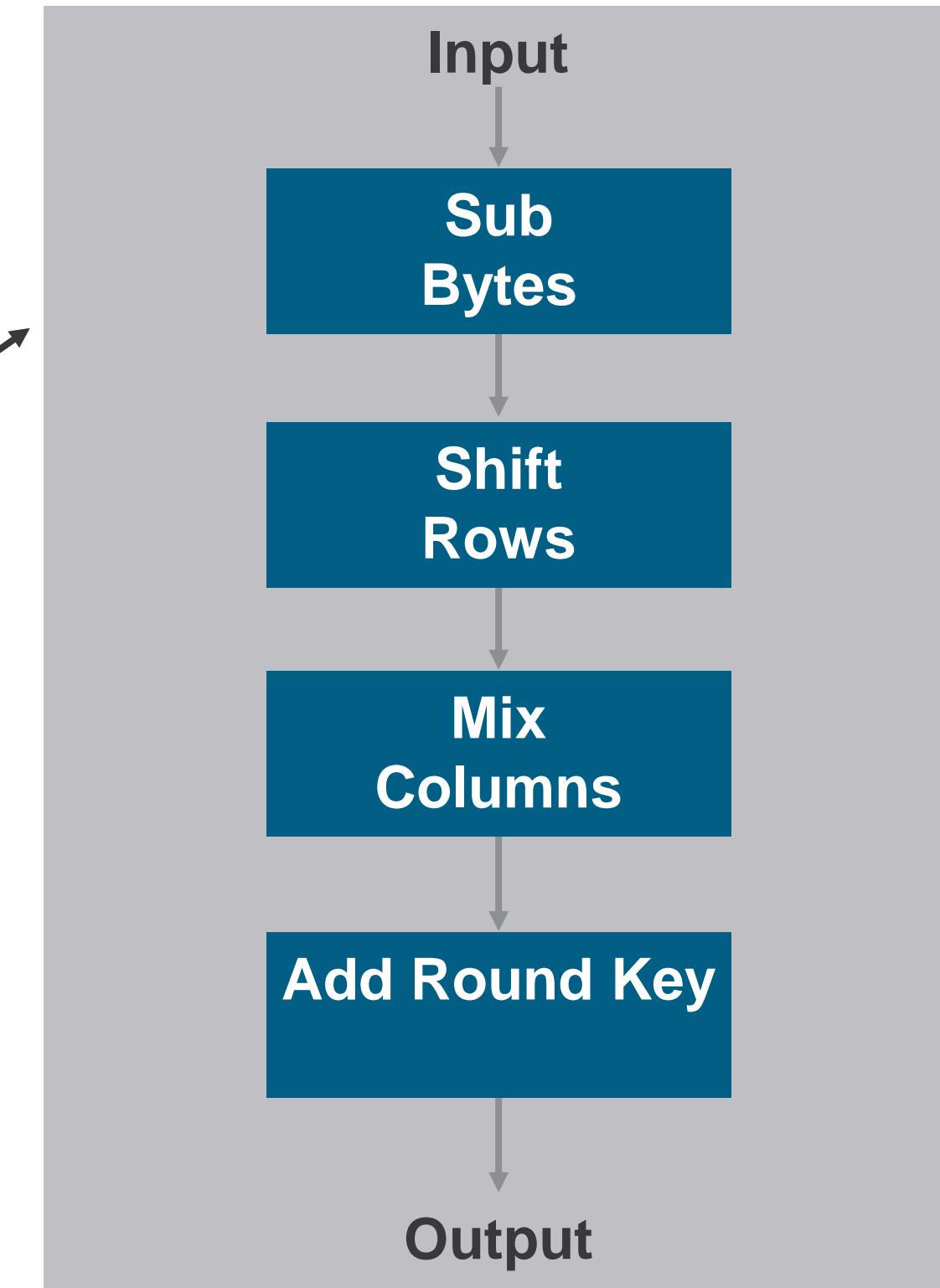
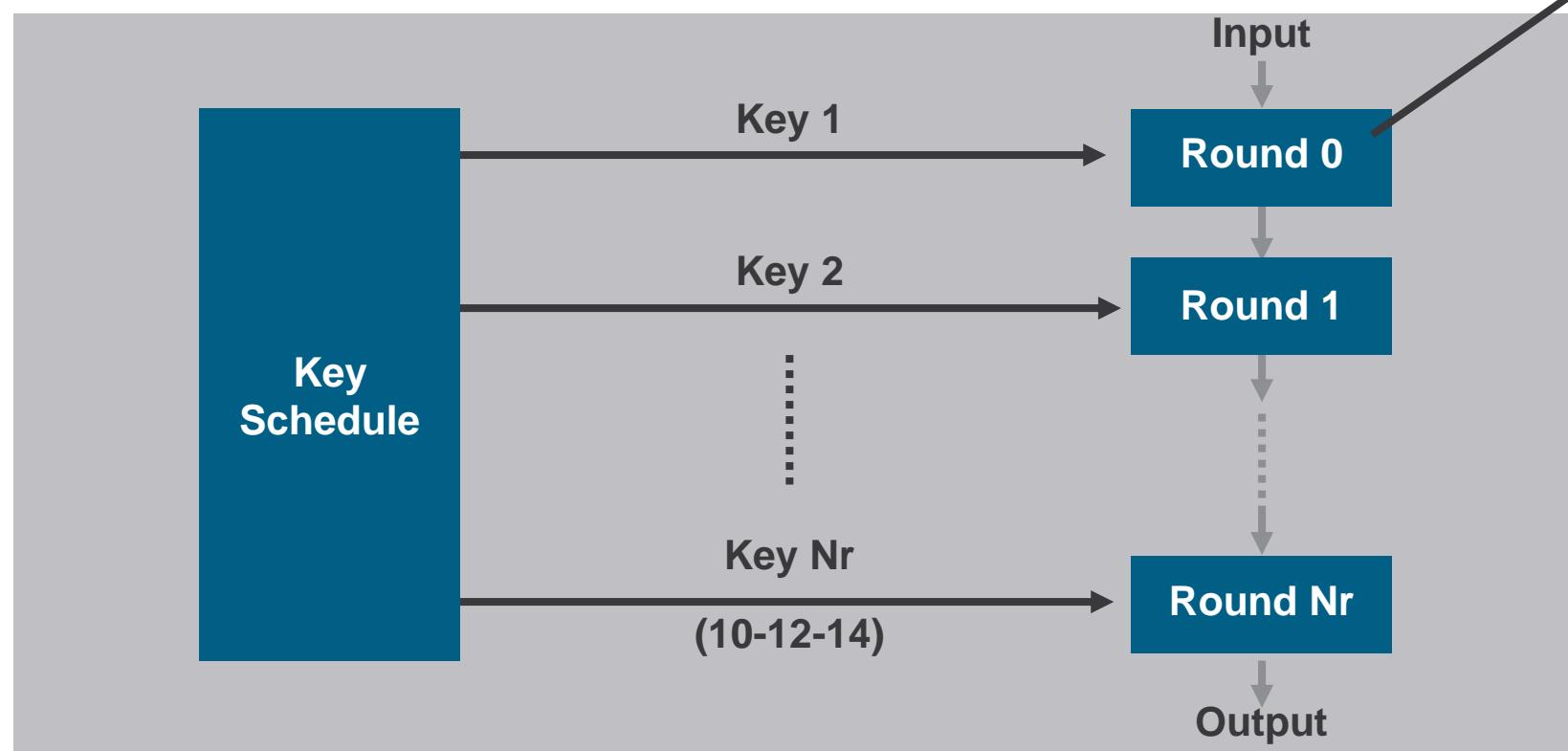
→ DO NOT REUSE KEY !!

# AES – The Advanced Encryption Standard

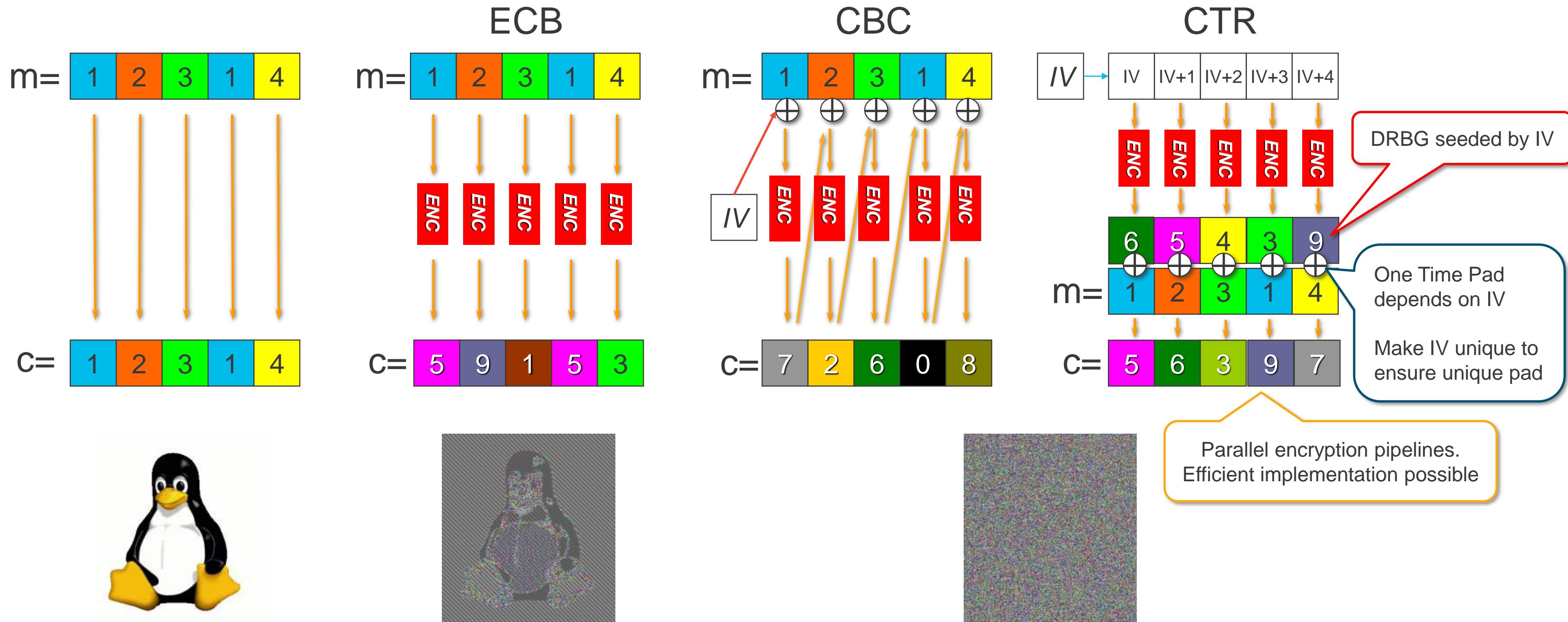
- The block size is large (128 bits standardized)
- The key size is large (128, 192 or 256 bits)
- AES operates on full bytes (faster on general purpose CPU's)
- National Institute of Standards and Technology:
  - “A machine that cracks 56 bits DES in 1 seconds takes 149 trillions years to crack 128-bits AES”
- Summary:
  - AES is faster and more secure than DES or 3-DES
  - AES is easier to implement than DES on tight hardware
  - **IS THIS TRUE ?**

# AES: Individual Rounds

Note: Last Round Is Slightly Different from the Rest of the Rounds (no Mix Columns)



# Block Cipher Mode of Operation (ECB, CBC, counter)



Penguin source: Wikipedia

# AES GCM

One Time Pad  
Algorithm

$GF(2^{128})$   
Polynomial  $x^{128}+x^7+x^2+x+1$   
 $GHASH(H, A, C) = X_{m+n+1}$   
u,v bits in  $A_m, P_n$

$$X_i = \begin{cases} 0 & \text{for } i = 0 \\ (X_{i-1} \oplus A_i) \cdot H & \text{for } i = 1, \dots, m-1 \\ (X_{m-1} \oplus (A_m^* \| 0^{128-v})) \cdot H & \text{for } i = m \\ (X_{i-1} \oplus C_{i-m}) \cdot H & \text{for } i = m+1, \dots, m+n-1 \\ (X_{m+n-1} \oplus (C_n^* \| 0^{128-u})) \cdot H & \text{for } i = m+n \\ (X_{m+n} \oplus (\text{len}(A) \| \text{len}(C))) \cdot H & \text{for } i = m+n+1 \end{cases}$$

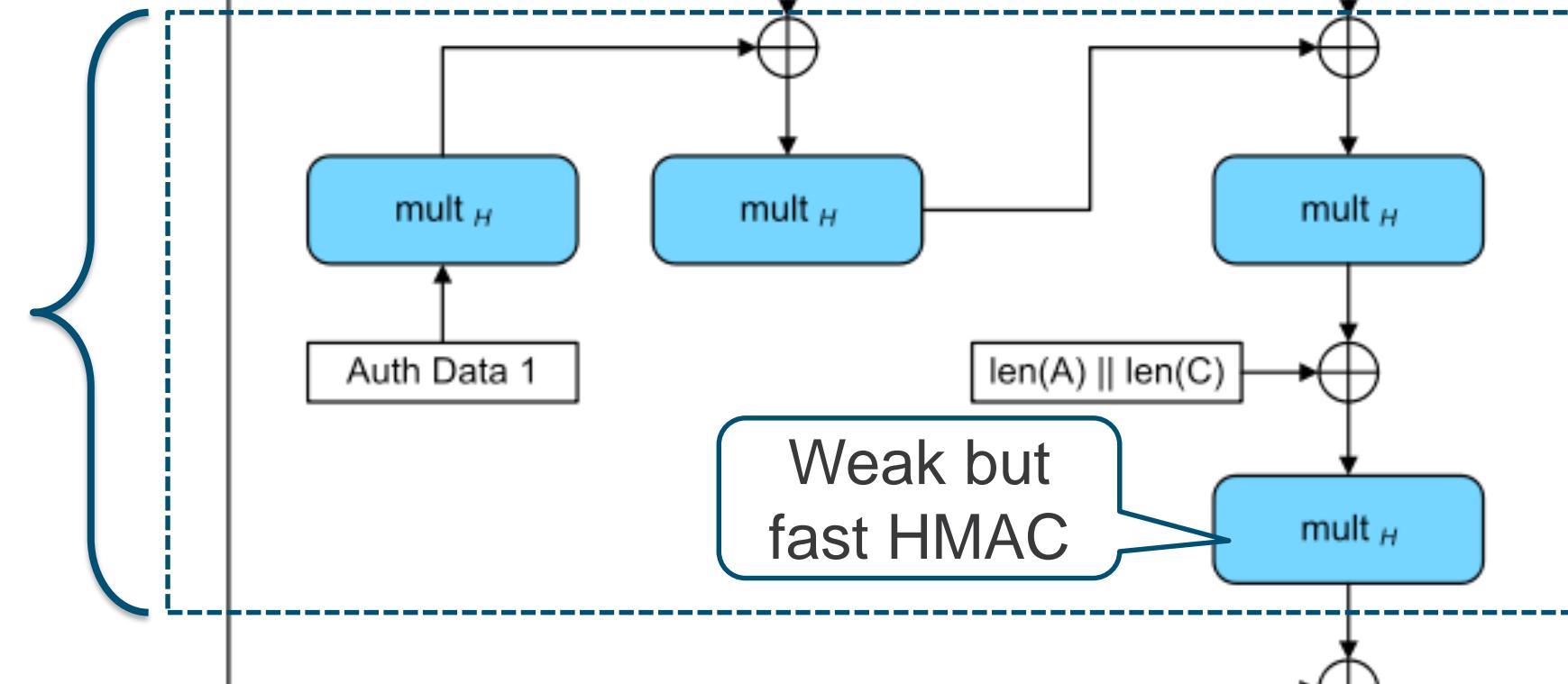
AES GCM in summary

- AES is more secure than 3DES
- AES-CTR CAN be much faster (implementation...)
- GMAC consumes less than SHA-2 (or even SHA-1)

Fed from Initialization  
Vector

AES Based PRNG  
generate pad...  
Secure CTR DRBG

One Time Pad...  
Parallelization possible



Weak but  
fast HMAC

Encrypted HMAC → Very strong !  
ICV can be 8, 12 or 16 bytes

# MODP

# Multiplicative Group of Integers Modulo P

Nummer	Meldestelle	Begleitungen	Streitkräfte-Kommunikations-Schlüssel Nr. 649												Ablaufzeitraum											
			zu den Befehlsmitteln				zu den Sämtlichen				zu den Sämtlichen															
649	31	I	V	II	14	06	14	SI	Q1	DV	KU	FO	WT	RV	JH	12	LQ	wry	dry	xzb	rig					
649	30	IV		III	II	06	26	02	IS	E9	M1	RX	DT	U2	JQ	AO	C9	ST	kti	acv	zil	wsa				
649	29	III		II	1	12	24	03	XH	AK	PF	OO	DJ	AT	CV	IO	ER	GS	LW	PS	PN	EU				
649	28	II		III	V	08	56	16	DI	CN	DX	PV	OK	FV	A1	DK	OT	MQ	KU	DX	L7	O2				
649	27	II		I	IV	13	03	07	LT	EQ	HS	UW	DY	IN	BV	OR	AM	LO	PF	HT	ER	UN				
649	26	I	IV	V		17	22	19	VZ	AL	BT	KD	CD	E1	32	DU	F5	EP	xle	gbo	uvv	rzn				
649	25	IV	III	I		08	25	12	GR	PV	AD	IT	PK	HJ	L2	NS	EQ	CW	out	uhq	new	uit				
649	24	V		I	IV		05	16	14	TY	AS	OK	KY	JN	DR	HX	GL	GT	SU	kpl	swl	yci	tla			
649	23	IV		II	I	24	12	04	QV	PK	AK	ED	SD	QJ	ME	SK	GN	LT	ebn	ewm	udf	tie				
649	22	II		IV	V	08	09	21	IU	AS	BV	OL	P2	ES	IM	RX	LW	AT	QO	DO	WZ	CN				
649	21	I	V	II	13	05	19	PT	OK	KE	CH	RU	EL	PY	OS	EL	DM	AV	CE	TV	HK	jpc	acc	mve	wee	
649	20	III	IV	V		24	01	15	MR	XH	BQ	TW	DF	NO	QI	AU	SY	JL	OK	DE	TW	qjd	ref	new	yah	
649	19	V		III	I	17	25	22	QX	PR	PH	VI	DL	CM	AE	22	J5	Q1	idt	fpr	jwg	tia				
649	18	IV		II	V	15	23	20	EJ	OF	IV	AQ	XW	TX	WT	PS	LD	BD	iss	shw	vej	rzn				
649	17	I	IV	V		25	10	08	TR	K1	LS	EM	OV	OT	QX	AF	JF	BU	psa	hal	rog	ysi				
649	16	V		II		08	16	13	HM	JO	D1	NN	SY	X5	OS	PU	FQ	CT	tdp	dhb	ckb	uiv				
649	15	II	IV	I		01	01	07	DS	NY	ME	OK	LX	AJ	SQ	CO	IP	NT	tdw	hij	soh	wve				
649	14	IV	I	V		15	11	05	OM	JR	X5	IT	EL	PG	A1	DT	CQ	NV	int	mcx	ijv	ztk				
649	13	I	III	II		13	20	03	LY	PO	XH	BR	IQ	JG	AV	SK	KT	CX	sgt	dts	gjo	rrq				
649	12	V		II	IV		18	10	07	PM	BL	D9	XW	SD	AT	IT	DO	IL	PW	tdy	rkf	ijw	xti			
649	11	II	IV	III		02	26	15	KN	UF	HS	PW	YM	DO	IS	QT	DL	JY	ses	rjy	wei	wsb				
649	10	III	V	IV		23	21	01	LM	1X	MS	QD	IV	FT	DO	VZ	PF	XN	tdc	sbs	vbn	rxo				
649	9	V		I	III		16	04	03	QT	BS	LS	K7	AT	10	DN	HD	HW	JZ	edj	eyr	wby	tih			
649	8	IV		II	V	13	19	25	P1	EQ	ST	CO	ED	AM	EL	TX	DO	XP	yix	dma	ake	tii				
649	7	I	IV	II		09	01	29	UX	1S	HS	BR	QQ	CP	PE	JT	MV	AN	ian	dpb	tsj	wai				
649	6	III	I	V		11	18	14	DQ	GU	SN	MP	HR	A2	CE	PO	JL	VY	lju	edr	lys	wad				
649	5	V		II		23	02	29	IL	AP	EU	HO	HV	CL	OK	B1	PU	HS	PL	EW	XY	lju	shy	vey	ujb	
649	4	II	IV	V		04	21	03	QT	WS	RV	OM	AC	BL	OS	KK	QN	OP	SD	DM	JW	TK	tsb	shy	vey	wak
649	3	V		I		10	11	06	BF	NR	DX	CS	XR	MF	CH	DP	EX	DE	IV	AV	OJ	lo	apd	ieu	wak	
649	2	IV	V			16	14	07	BN	XU	EO	PI	KQ	CP	OS	JW	A3	VR	aqd	bdy	tsr	xid				
649	1	II	I			22	12	10	DP	BN	H2	CX	GY	ER	AP	UT	SW	JD	xgi	edf	gig	wav				

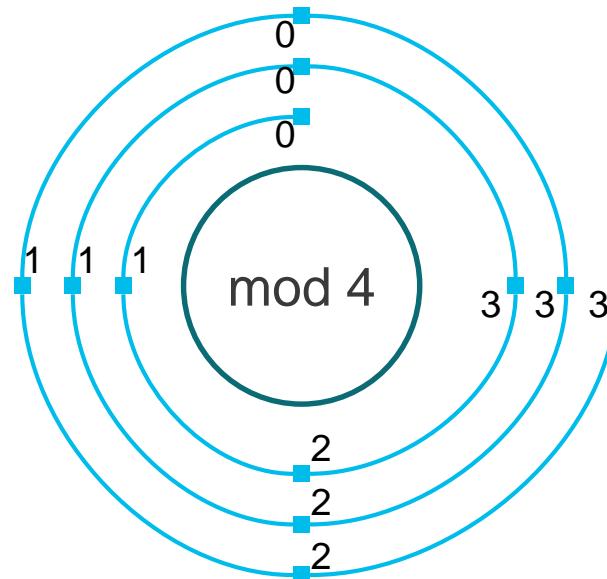
# RSA

- Rivest, Shamir, Adleman (1977)
  - Patented but expired => no more royalty
  - Public key cryptosystem
- Variable key length (usually 512-2048 bits)
- Based on the (current) difficulty of factoring very large numbers

# Modular Arithmetic

- Modulo is like a clock

0 1 2 3 4 5 6 7 8 9 10 11...



- $b^x \text{ mod } n = r$  also written as  $b^x \equiv r \pmod{n}$ 
  - b is the base
  - x is the exponent
  - n is the modulus
  - r is the remainder
- Knowing b, x & n, it is **very easy to compute r**
- Knowing x, r & n, it is **very difficult to compute  $b = \sqrt[x]{r} \pmod{n}$**  aka the RSA problem
- Knowing b, r & n, it is **very difficult to compute  $x = \log_b(r) \pmod{n}$**  aka the discrete log problem

unless there are trapdoors

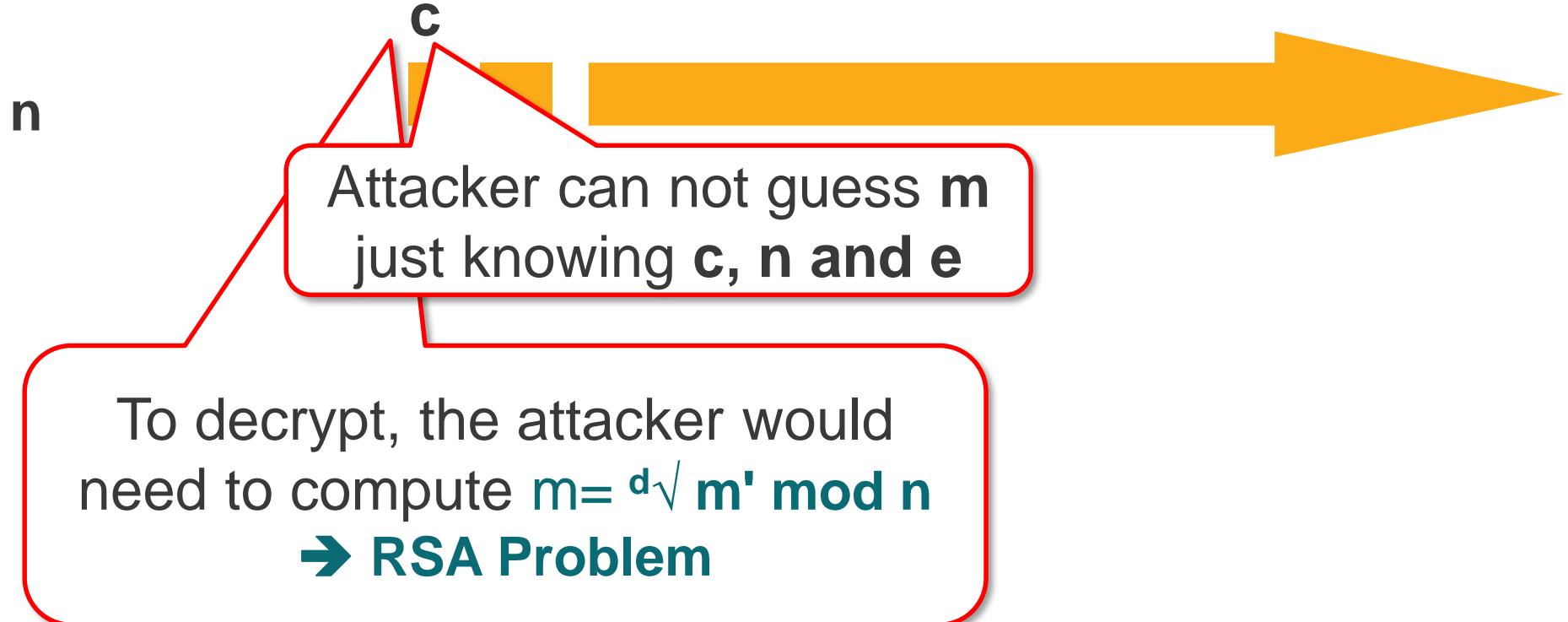
# Encryption with Modular Arithmetic

## Alice

Must send a private message  $m$

Takes  $n$  &  $e$  from Bob  
(we assume  $m < n$ )

Computes  $c = m^e \text{ mod } n$



## Bob

Selects three numbers  $n$ ,  $d$  &  $e$   
 $n$  &  $e$  are **public**,  $d$  is **secret**  
 $e, d$  are chosen such as  $ed \equiv 1 \pmod{n}$

Computes  $m' = c^d \text{ mod } n$

$$\begin{aligned} m' &= c^d \text{ mod } n \\ &= (m^e)^d \text{ mod } n \\ &= m^{ed} \text{ mod } n \\ &= m^1 \text{ mod } n \\ &= m \end{aligned}$$

- Bob has reversed the operation !!
- Bob knows  $d$  but nobody else...
- We have an encryption scheme

# Signature with Modular Arithmetic

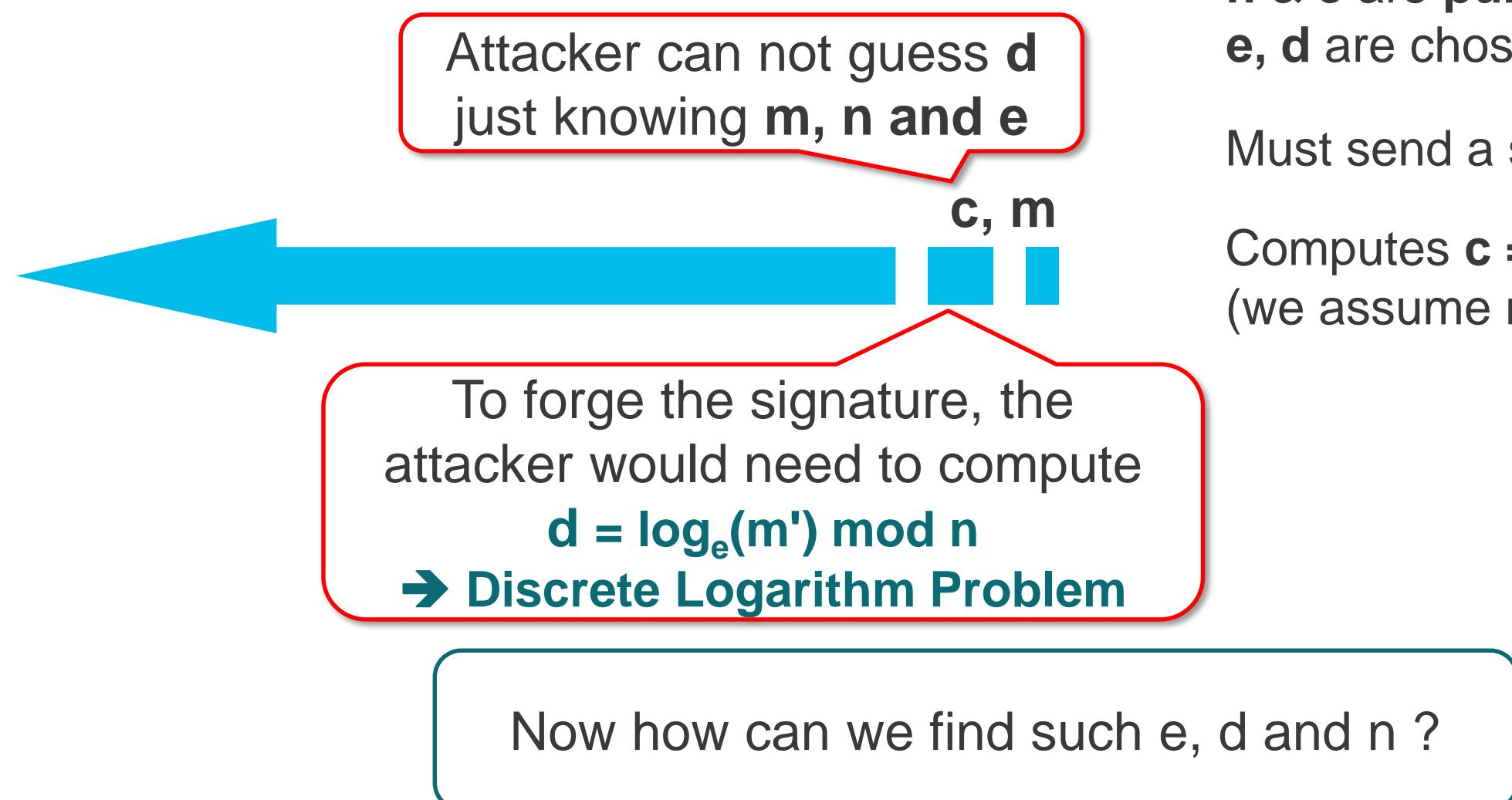
Alice

Takes  $n$  &  $e$  from Bob

Computes  $m' = c^e \text{ mod } n$

$$\begin{aligned}m' &= c^e \text{ mod } n \\&= (m^d)^e \text{ mod } n \\&= m^{de} \text{ mod } n \\&= m^1 \text{ mod } n \\&= m \text{ mod } n \\&= m\end{aligned}$$

→ Bob must have sent the  $c, m$



Bob

Selects three numbers  $n$ ,  $d$  &  $e$

$n$  &  $e$  are **public**,  $d$  is **secret**

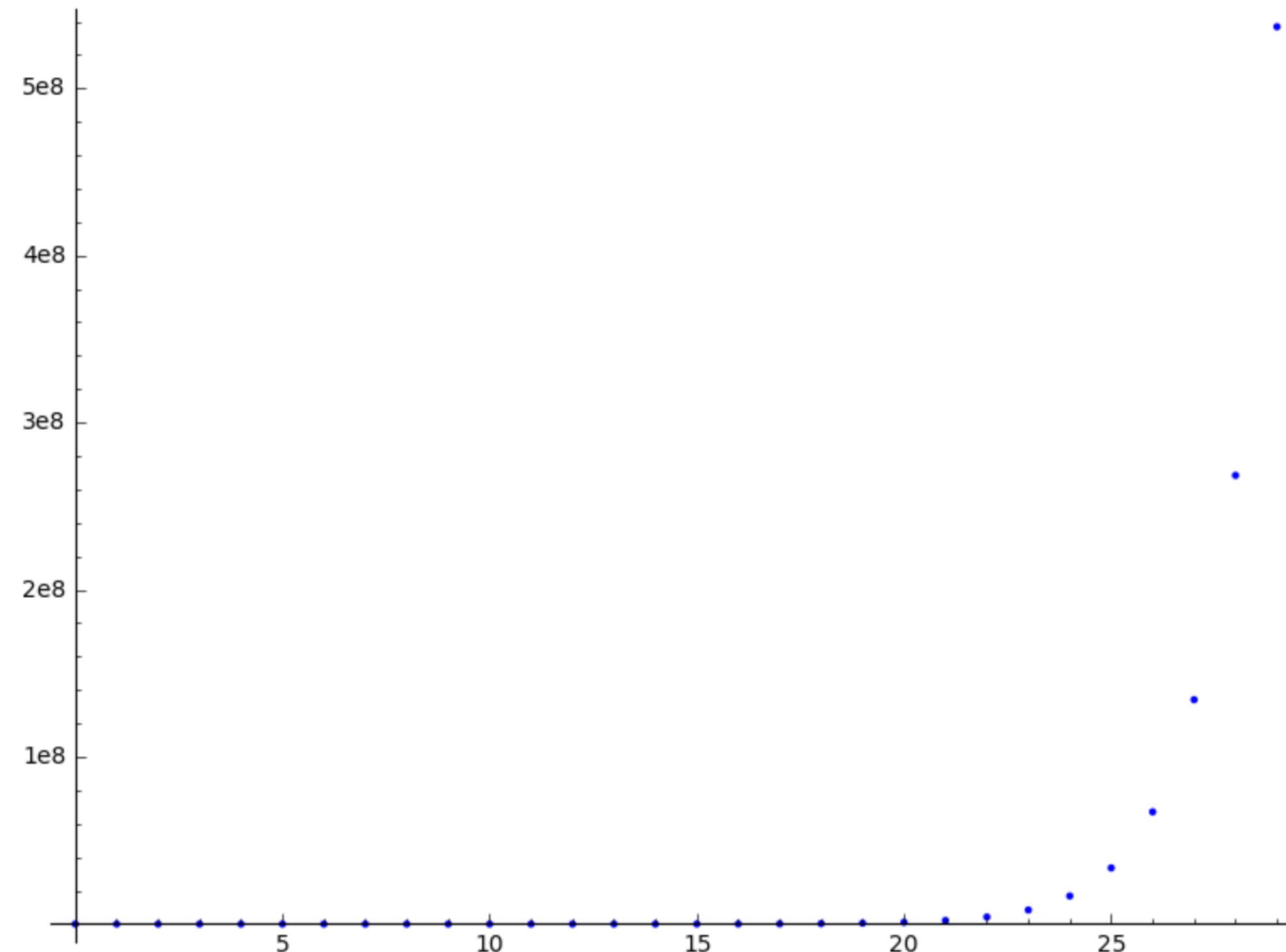
$e$ ,  $d$  are chosen such as  $ed \equiv 1 \pmod{n}$

Must send a signed message  $m$

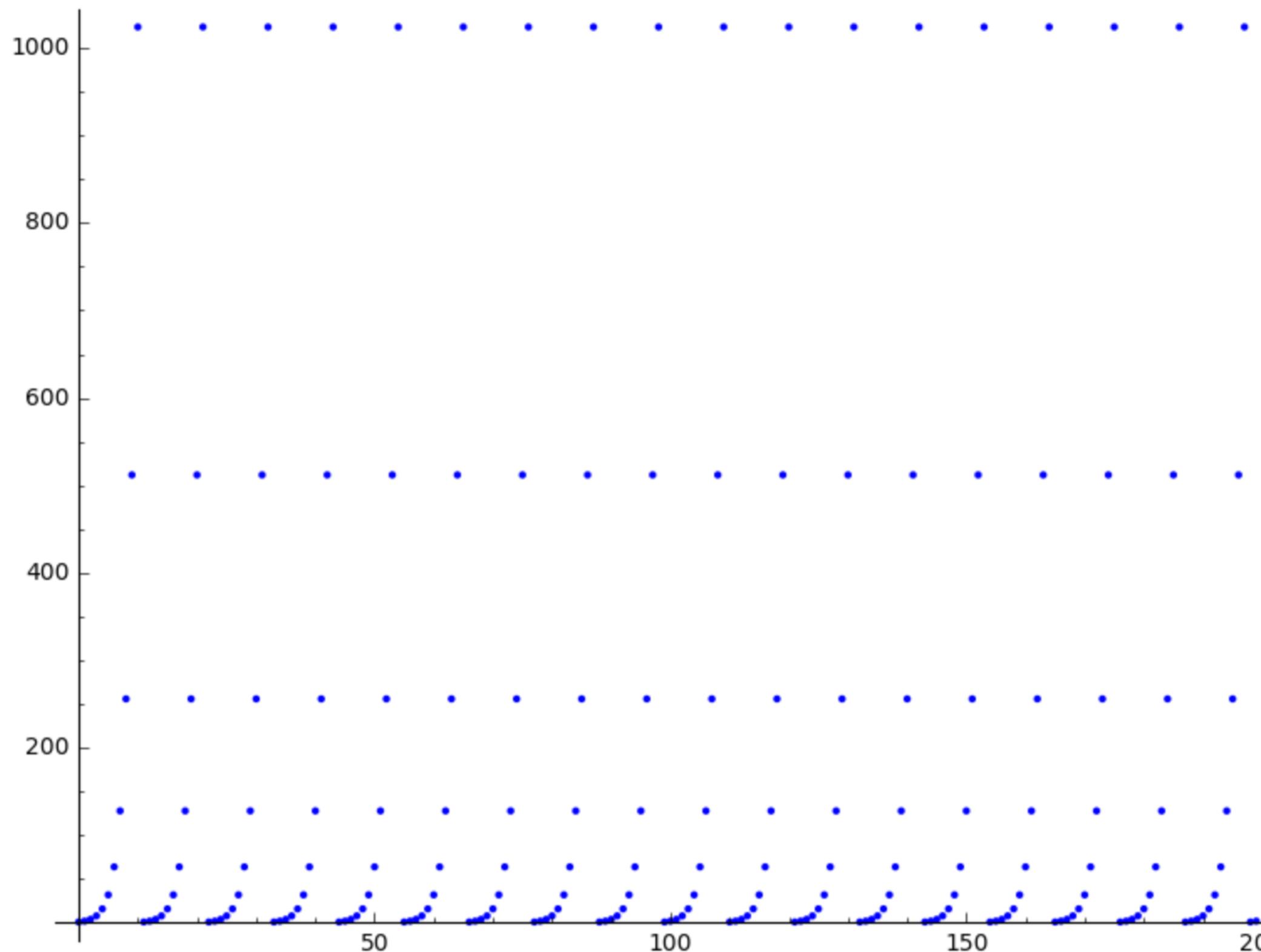
Computes  $c = m^d \text{ mod } n$

(we assume  $m < n$ )

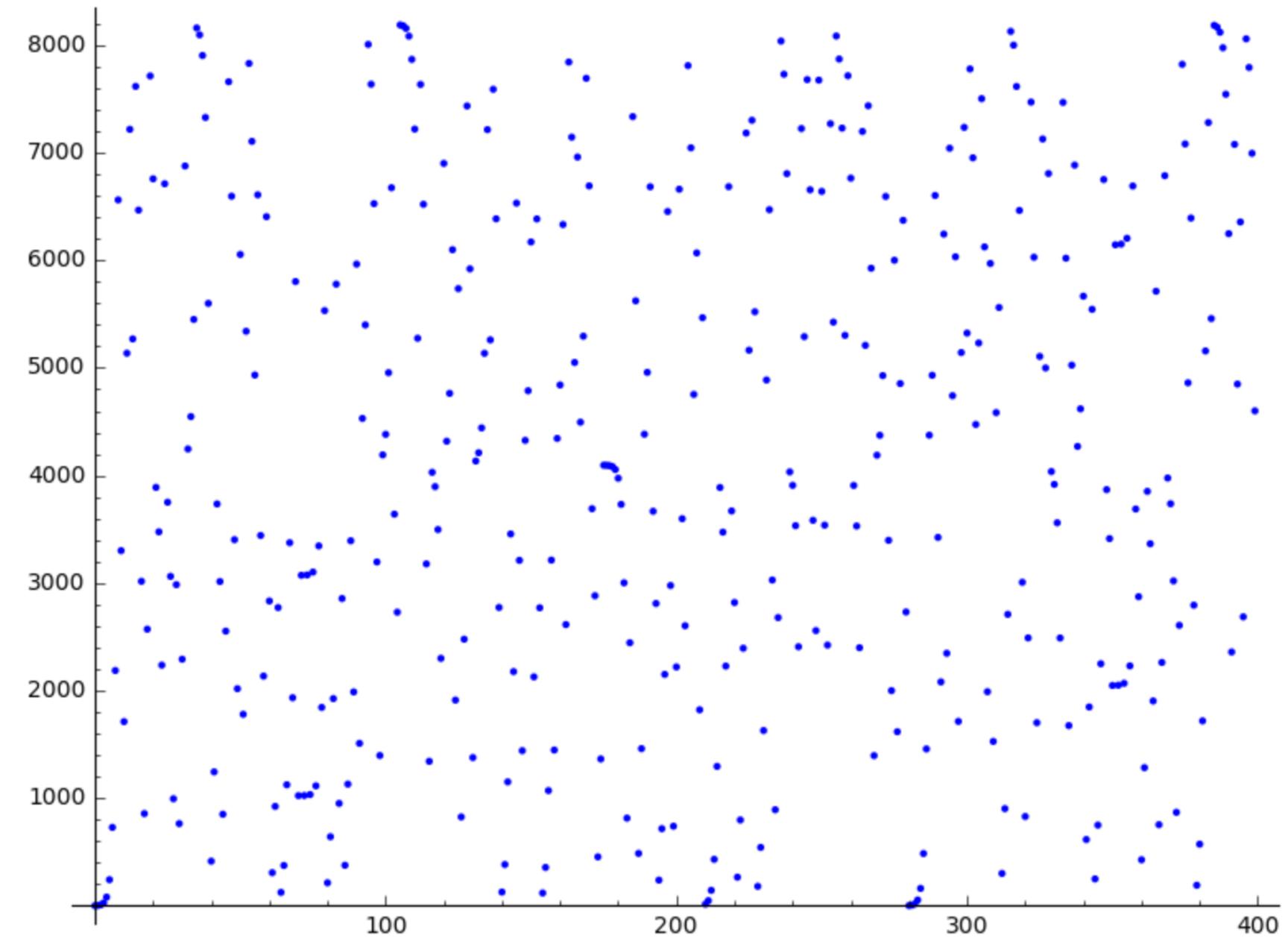
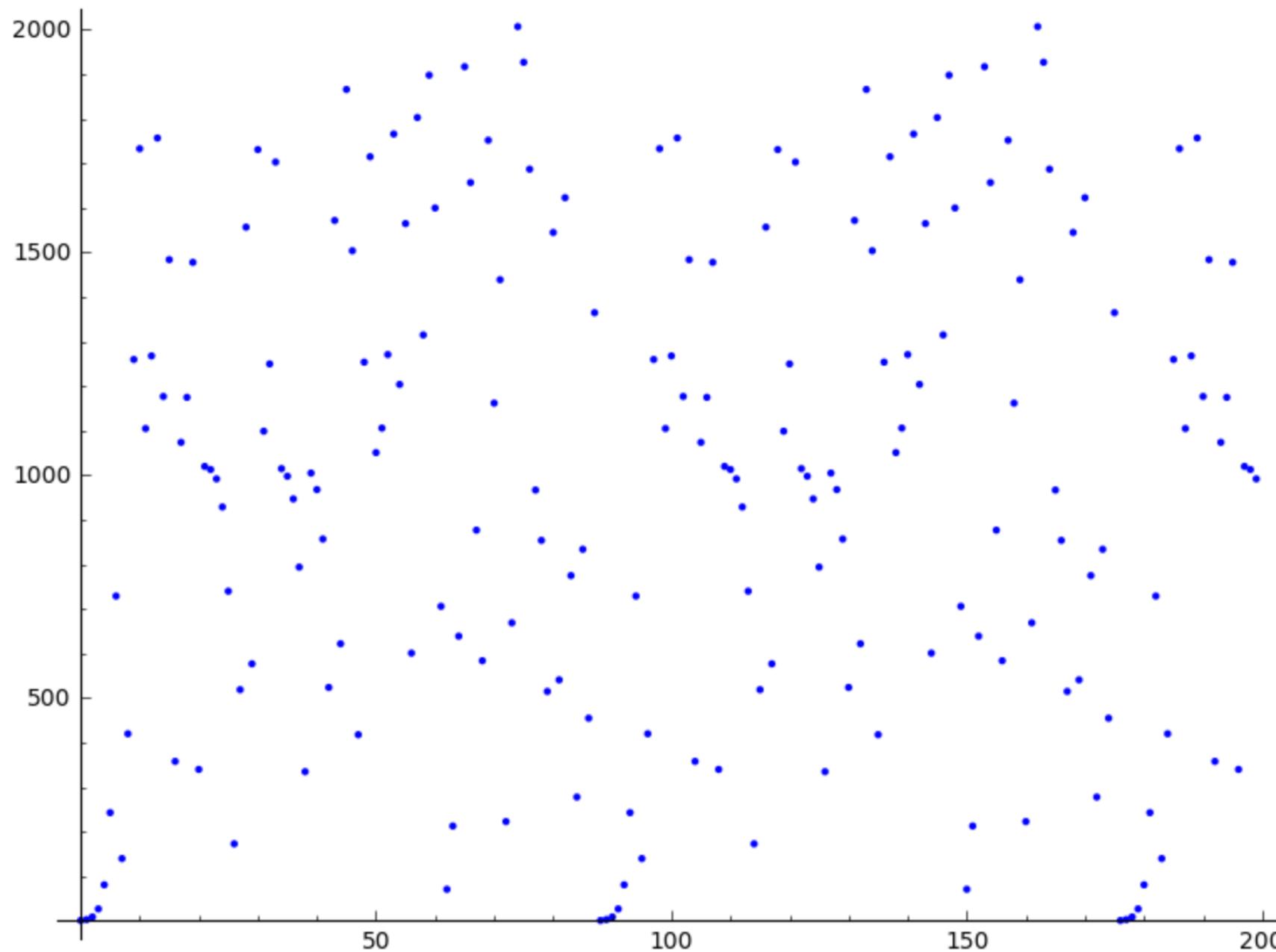
# Regular Exponentiation – Use Dichotomy to Reverse



# MODP Exponentiation – dichotomy is broken

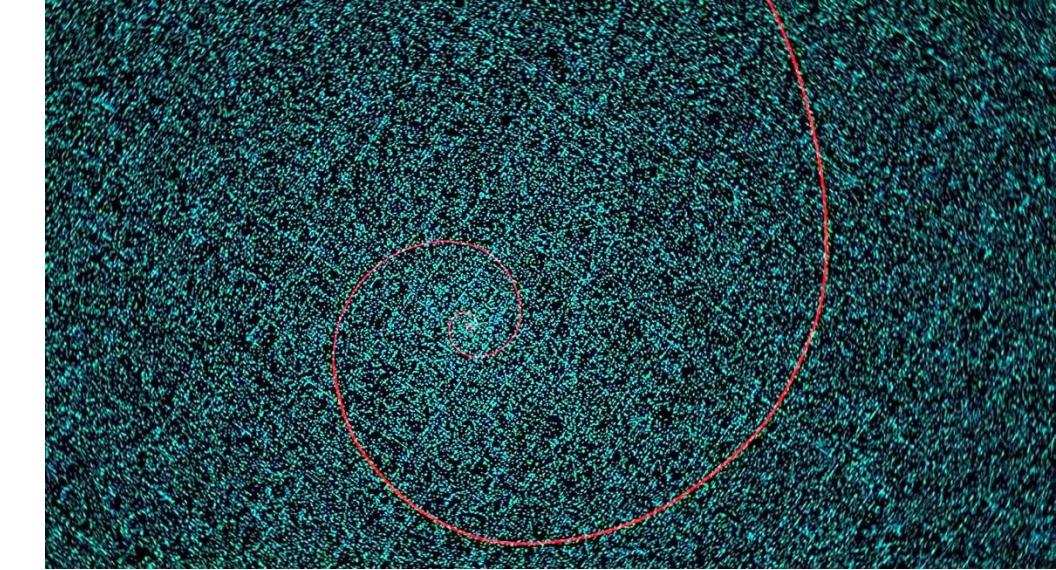


# Where Quantum Computers Come In



# About Prime Numbers

- A number is prime if it can be divided by one or itself
- A number is composite if it can be divided by 2 or more prime numbers
  - **Factorization is a hard problem.** Best algorithm yields  $O\left(\exp\left(\left(\frac{64}{9}b\right)^{\frac{1}{3}}(\log b)^{\frac{2}{3}}\right)\right)$ .
- Fundamental Theorem of Arithmetic: a given number has a single factorization
- Euclid's theorems: there are **infinitely many primes**
  - prime density (ratio of primes per composite up to x) is  $1/\ln(x)$
  - density drops off rapidly in the beginning but very slowly after a few powers of 10
  - $\pi(x) = x/\ln(x)$  : number of primes  $< x$
- Euler's  $\varphi(n)$  function or **Euler's totient**
  - # of integers in  $[1,n]$  that are relatively prime to n:  $|k \in [2,n] \mid \text{GCD}(k,n) = 1|$ ,  $\{1\}$ 
    - 2 numbers are coprime if they share no factor other than 1.
  - Property:  **$n_1, n_2, \text{GCD}(n_1,n_2)=1 \rightarrow \varphi(n_1*n_2)=\varphi(n_1)*\varphi(n_2)$**  – Totient is multiplicative
  - **if x is prime  $\rightarrow \varphi(n) = n-1$**  since  $1\dots n-1$  coprime with n and n divisible by itself
- Euler's theorem:  **$m^{\varphi(n)} \equiv 1 \pmod{n}$  if m and n are co-prime.**



picture: Khan Academy

# RSA keys – finding $e, d, n \mid m^{ed} \equiv m \pmod{n}$

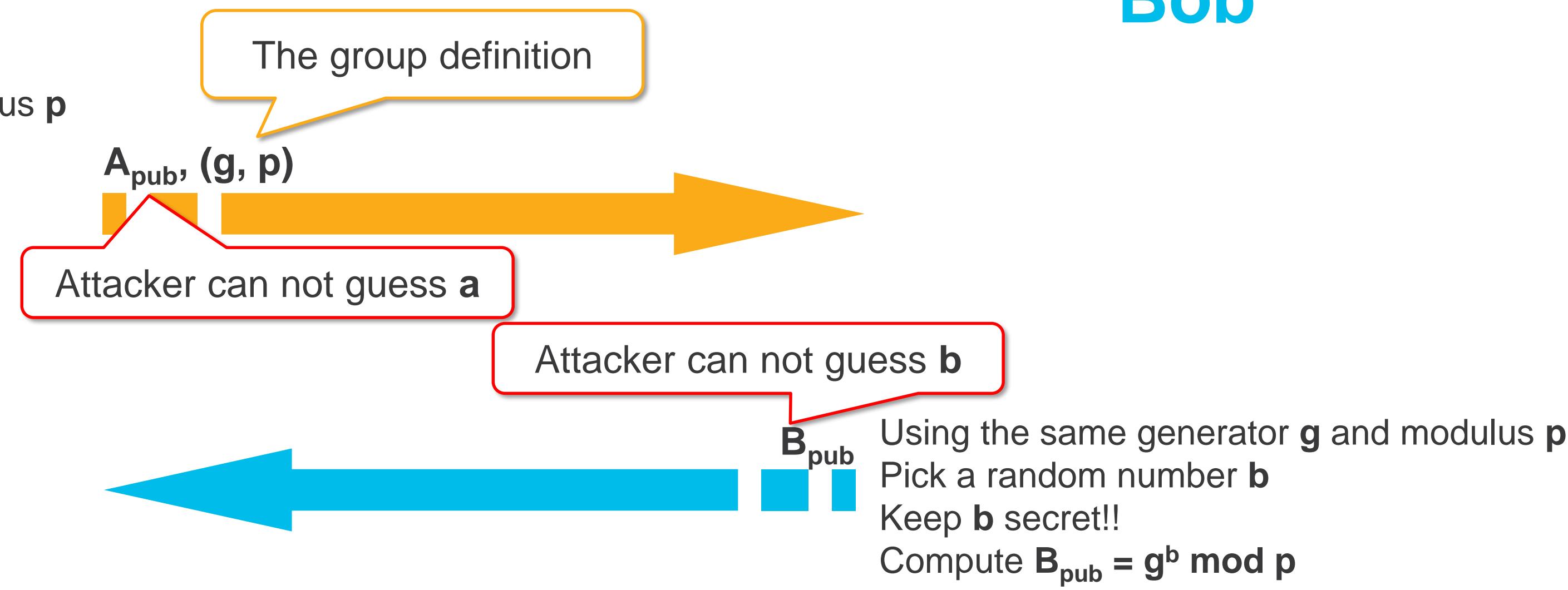
- Choose two distinct prime numbers  $p, q$  and hide them forever!
- $n = p \cdot q \rightarrow n$  is hard to factor if  $p$  &  $q$  are very large
- $\phi(n) = n - (p+q-1)$ 
  - $p$  &  $q$  are prime  $\rightarrow \phi(p)=p-1 \quad \phi(q)=q-1$
  - $\phi(n) = \phi(pq) = \phi(p) \phi(q) = (p-1)(q-1) = n - (p+q-1)$
- Final steps Euler theorem...
  - $1^k = 1 \rightarrow (m^{\phi(n)})^k \equiv 1^k \pmod{n} \rightarrow m^{k\phi(n)} \equiv 1 \pmod{n}$
  - $1m = m \rightarrow m \cdot m^{k\phi(n)} \equiv m \pmod{n} \rightarrow m^{k\phi(n)+1} \equiv m \pmod{n}$
  - we look for  $e, d, n$  such that  $m^{ed} \equiv m^{k\phi(n)+1} \equiv m \pmod{n} \rightarrow ed = k \phi(n) + 1$
- $\rightarrow d = \frac{k \phi(n)+1}{e} = \frac{k (n - (p+q-1)) + 1}{e}$
- Select  $e$ , small integer and  $k$  such that  $\text{GCD}(d, \phi(n)) = 1$  (i.e.  $d$  &  $\phi(n)$  are co-prime)
  - $e$  is usually 3 or 65537
  - adjust  $k$  to make  $d$  an integer

m – arbitrary message  
n – the modulus  
e – the public key  
d – the private key

# DH –Diffie-Hellman

## Alice

Select a generator **g** and a modulus **p**  
Pick a random number **a**  
Keep **a** secret!!  
Compute  $A_{\text{pub}} = g^a \text{ mod } p$



$$\text{Secret}_{\text{Init}} = (B_{\text{pub}})^a \text{ mod } p$$

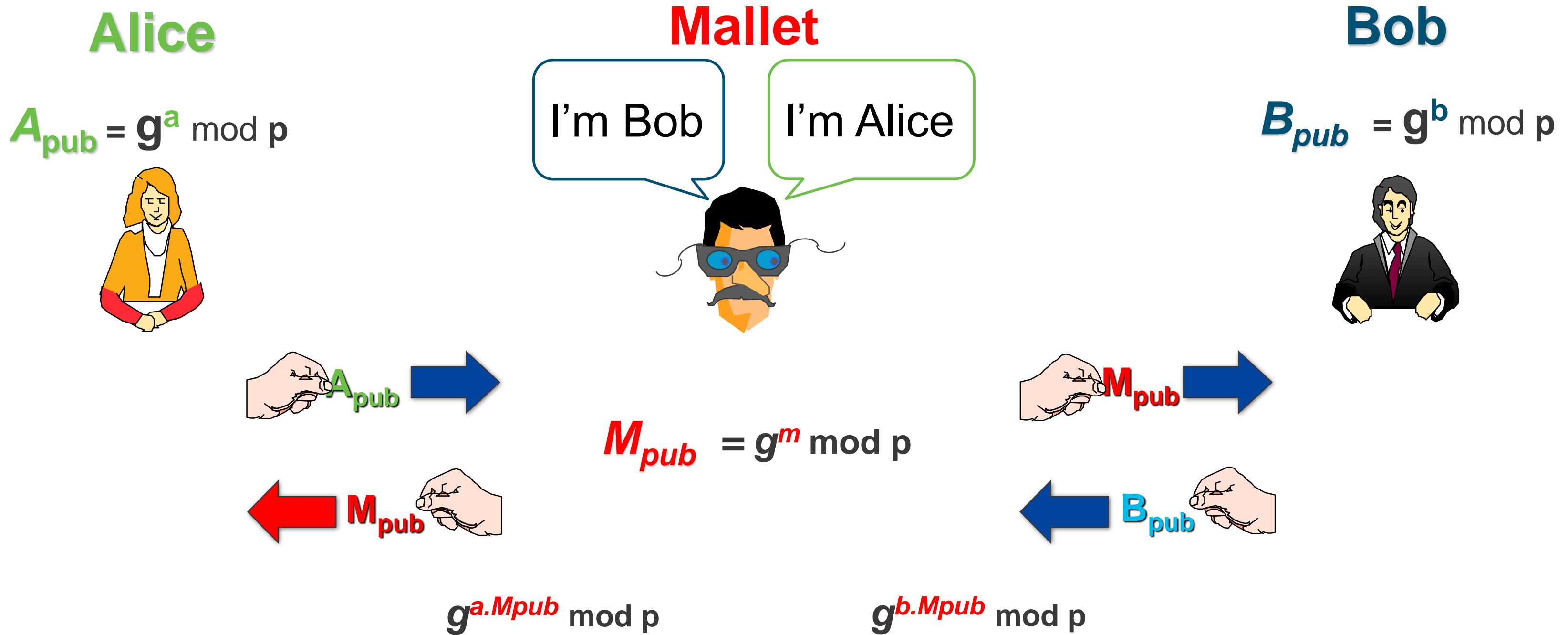


$$\text{Secret} = g^{a.b} \text{ mod } p$$



$$\text{Secret}_{\text{Resp}} = (A_{\text{pub}})^b \text{ mod } p$$

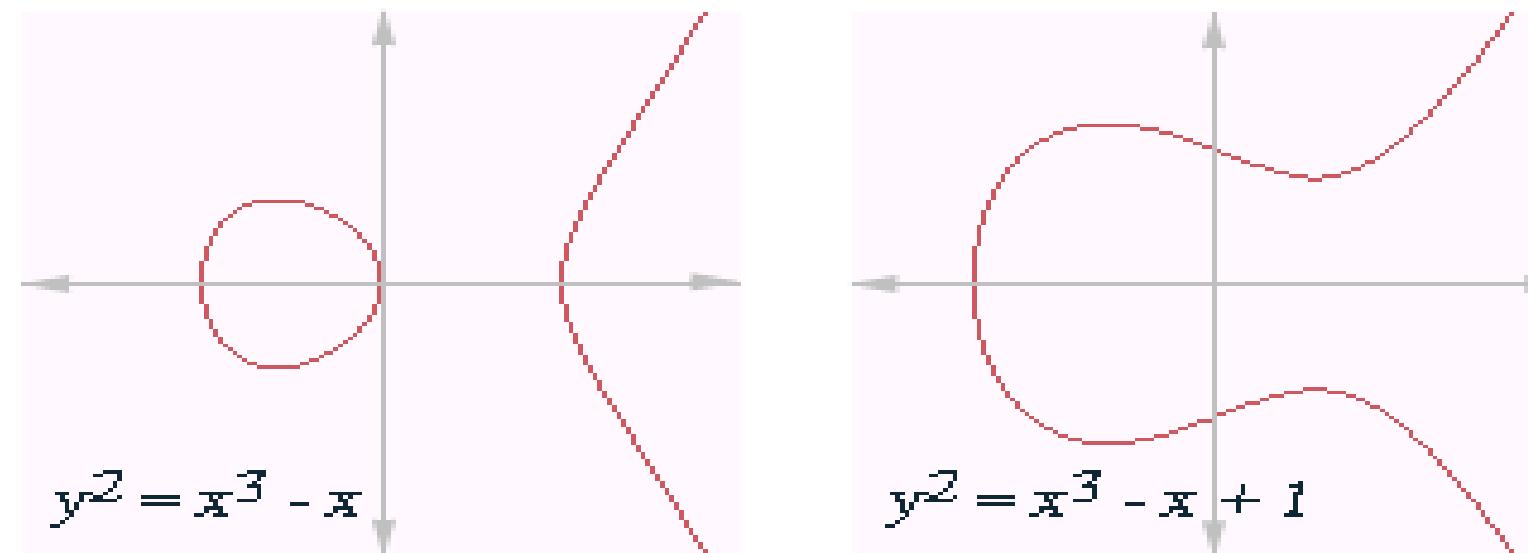
# DH is sensitive to a Man-in-the-Middle Attack



# ECC

# Elliptic Curve Cryptography

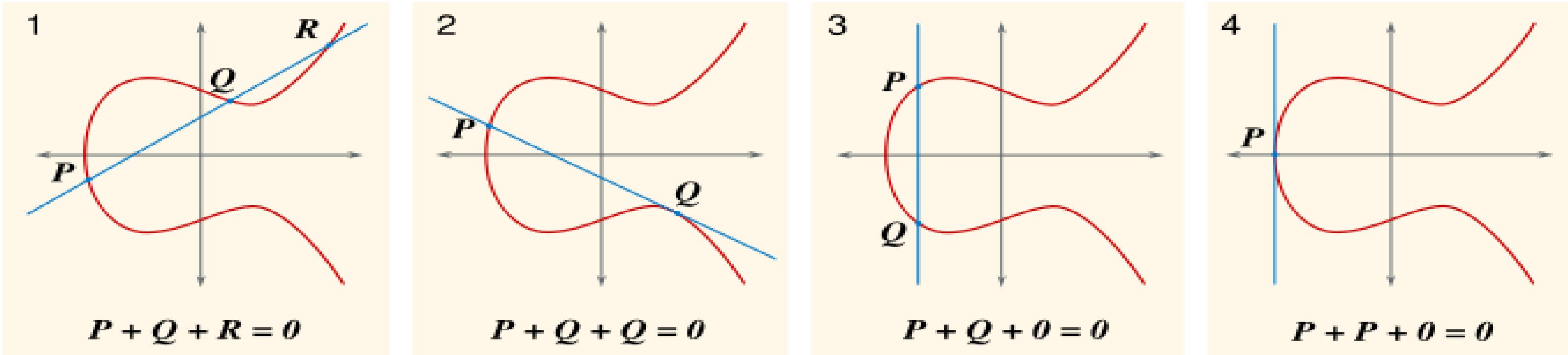
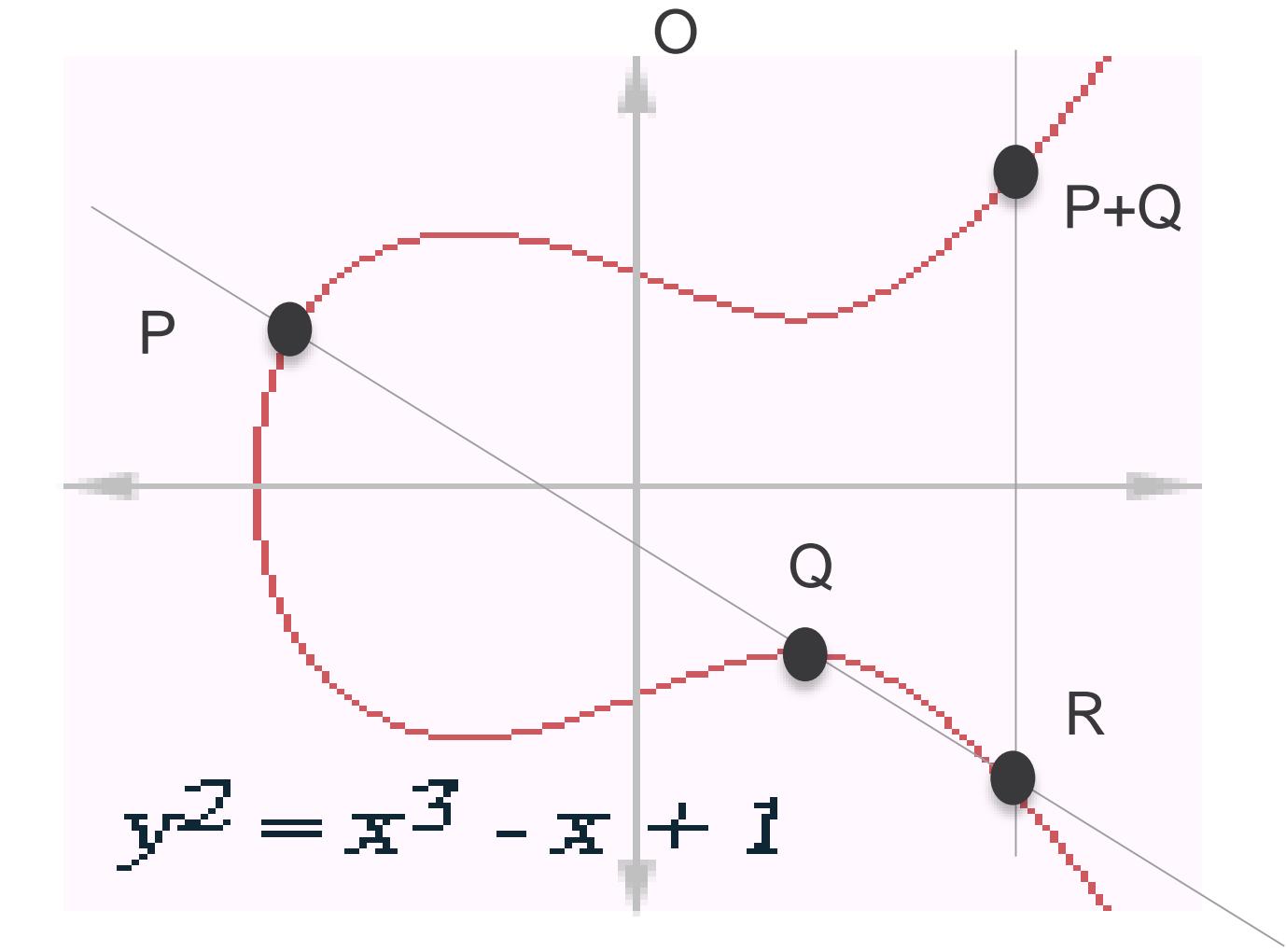
# What is an elliptic curve ?



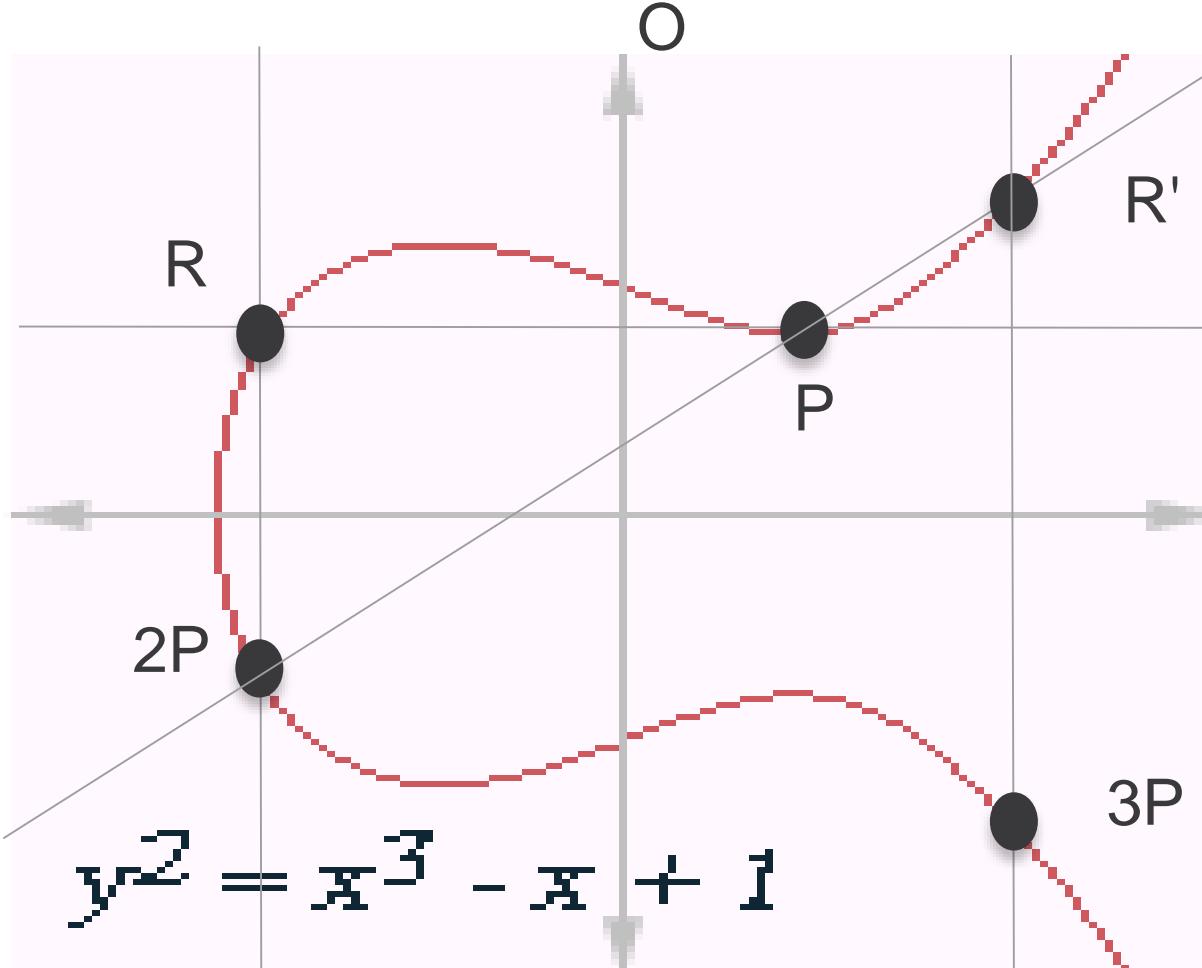
- A curve of general equation  $y^2=x^3+ax+b$ 
  - It MUST be a smooth curve
  - Its discriminant MUST BE NON ZERO:  $D = 4A^3 + 27B^2$
- **The Elliptic Curve is the set of points**
  - that satisfy the equation of the curve (ie. that “belong” to the curve)
  - Plus special **point at infinity** that we call O (the letter O)

# Elliptic Curve Addition

- Let P and Q be two points on the curve
- A line (P,Q) cuts the curve at a third point R
  - If the line is parallel to the Y axis, this point is O
  - If the line is tangent to the curve, the tangent point is counted twice
- The group operator + is defined such as  
 $P+Q+R = O$ ; O is the identity
- The reflected point from R is P+Q



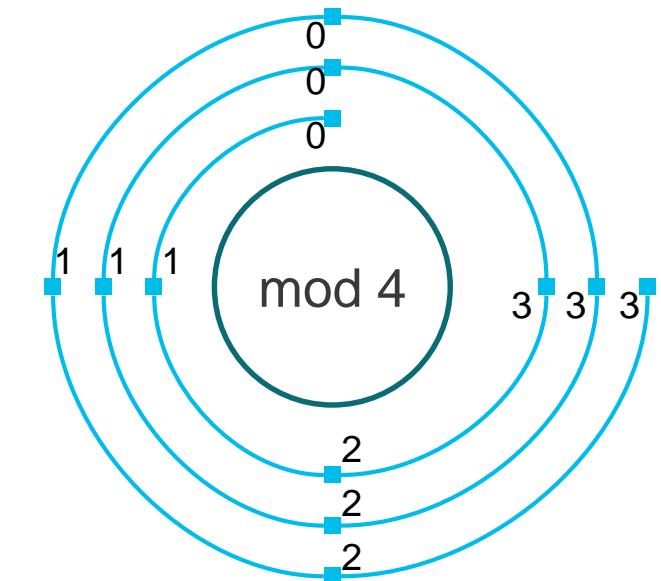
# The scalar multiplication $n \cdot P$



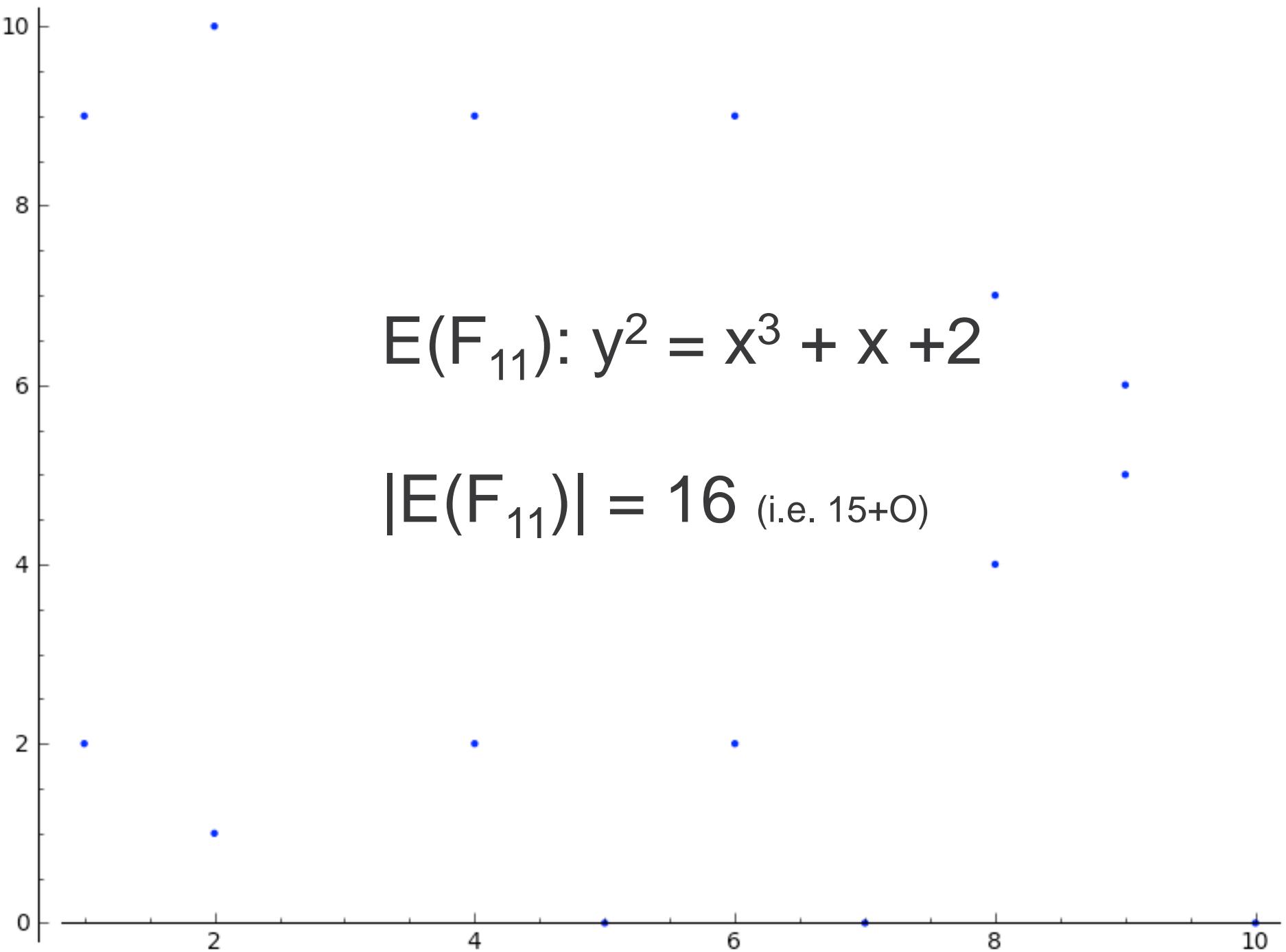
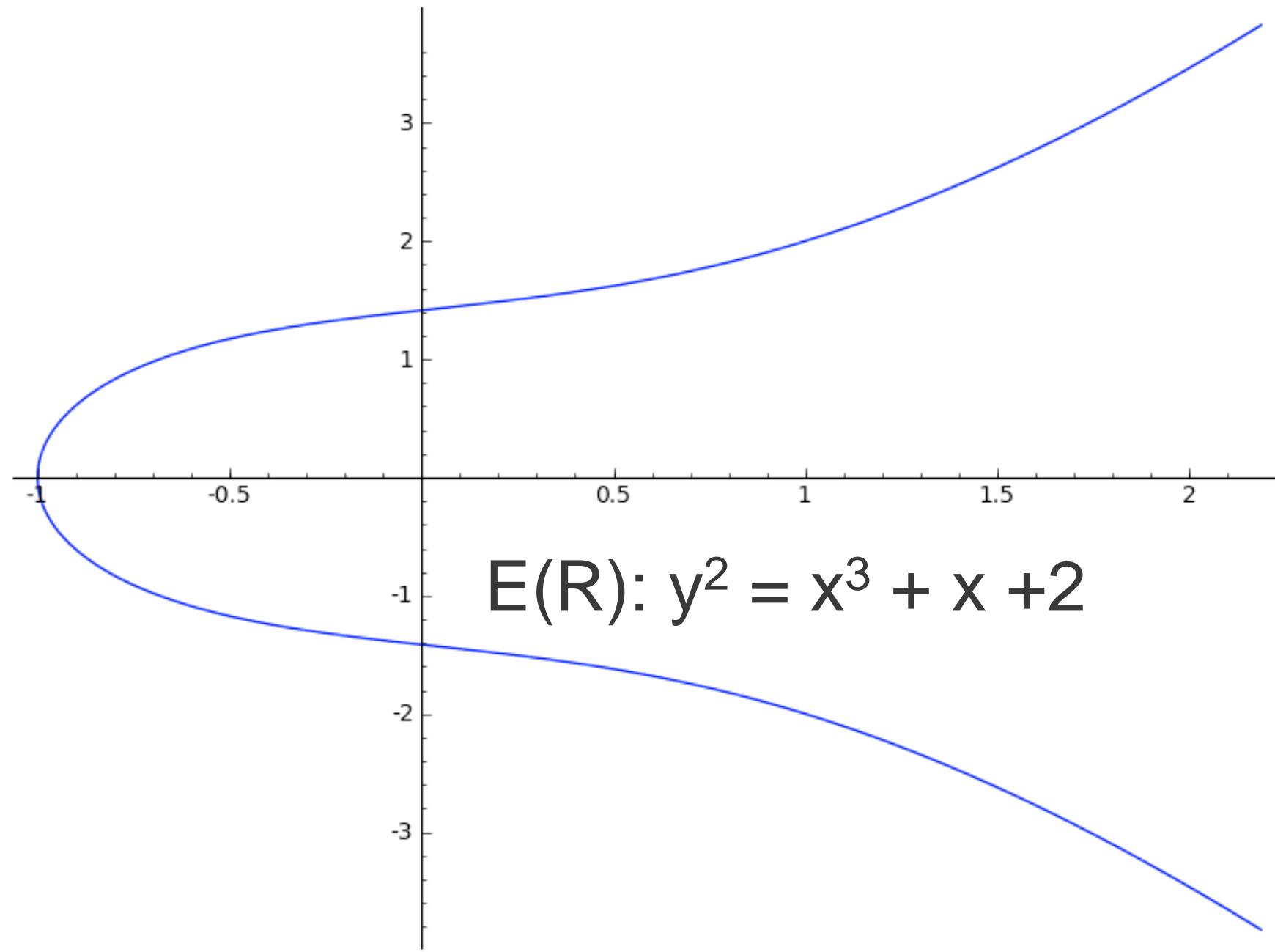
- Let's start with  $P+P = 2 \cdot P$
- For drawing  $(P,P)$ 
  - draw a tangent to the curve  $\rightarrow R$
  - $(O,R)$  cuts in  $P+P=2P$
- This is a scalar multiplication
  - One can derive  $3P = 2P+P$ ,  $4P = 3P+P$ , ...,  $nP = (n-1)P+P$

# Fast Forward – the finite fields $F_m$ & $F_{2^k}$

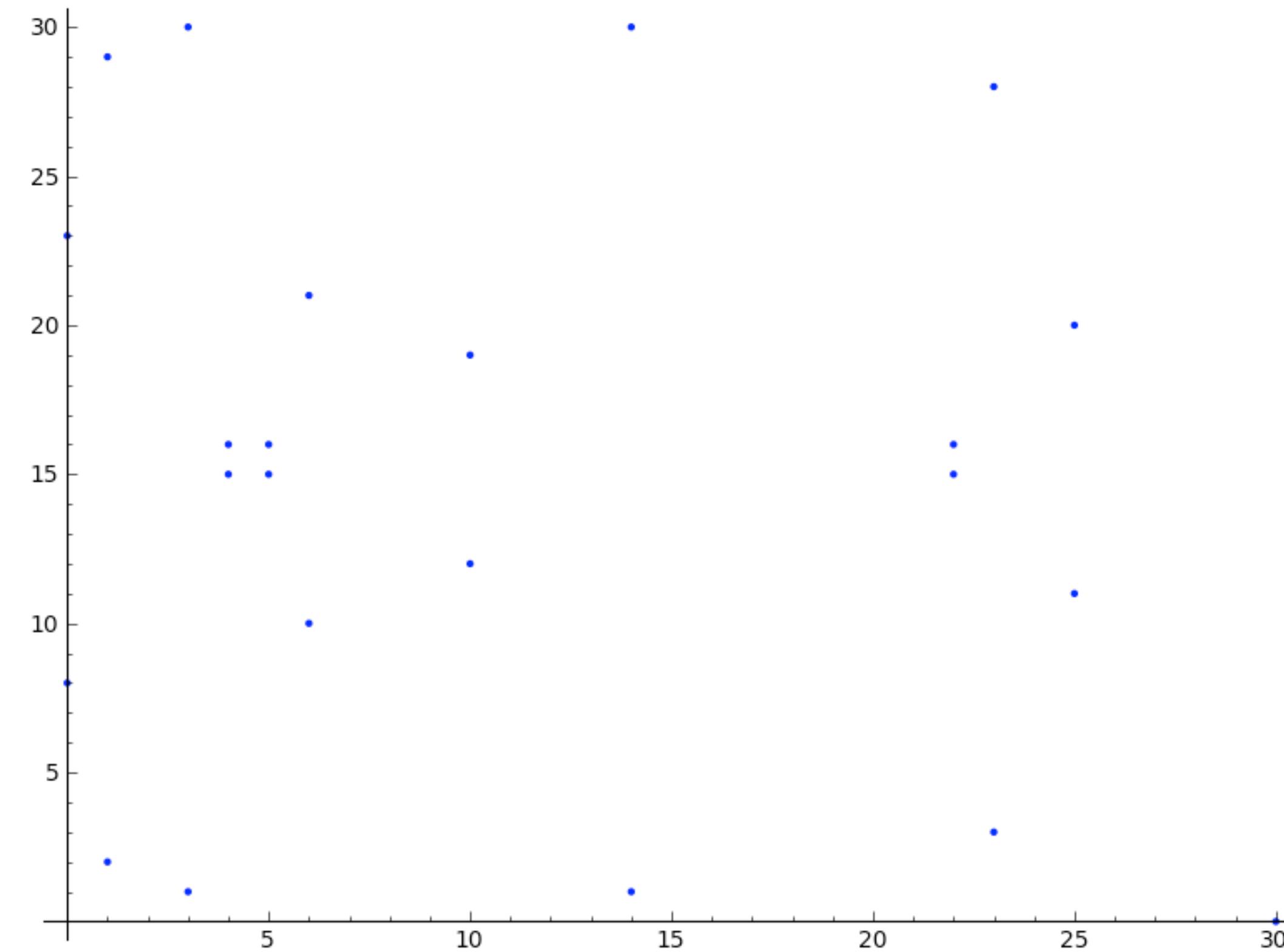
- Remember... modulo arithmetic
- Galois Field = Finite Field
- Let  $E$  be an elliptic curve defined over a finite field  $F_m$  (modulo  $m$ ):
  - $E(F_m) : \{\infty\} \cup \{(x,y) \text{ in } F_m \times F_m \mid y^2 = x^3 + ax + b, a, b \text{ in } F_m\}$
  - $E(F_m)$  is the set of points whose coordinates belong to  $F_m \times F_m$  and satisfy the equation + point at infinity
  - The set along group operations (+, x) seen before form an Abelian Group under multiplication → a field.
  - For cryptography,  $m$  should be a prime number
- It **seems (seemed ?)** more computationally efficient if  $m = 2^k - 1$  yielding the notation  $F_{2^k}$ 
  - Multiplication supposed to be more efficient → very important for ECDH and ECDS
  - In this case, the Koblitz curve is used:  $y^2 + xy = x^3 + ax^2 + 1$  where  $a=0$  or  $a=1$
  - For cryptography,  $k$  should be a prime number
  - $m$  should remain a prime – it would be called a Mersenne Prime
  - **There is debate about the actual security and efficiency of these curves!**
- The **order of a group  $G$**  is the **cardinality** of that group written  $\text{ord}(G)$  or  $|G|$ .
- The order of a **point  $P$  in a group  $G$**  is the value  $n$  such that  $n * P = O$  written  $\text{ord}(p)$  or  $|p|$



# Example Curve



# Example on $F_{31}$ – Complexity Increases

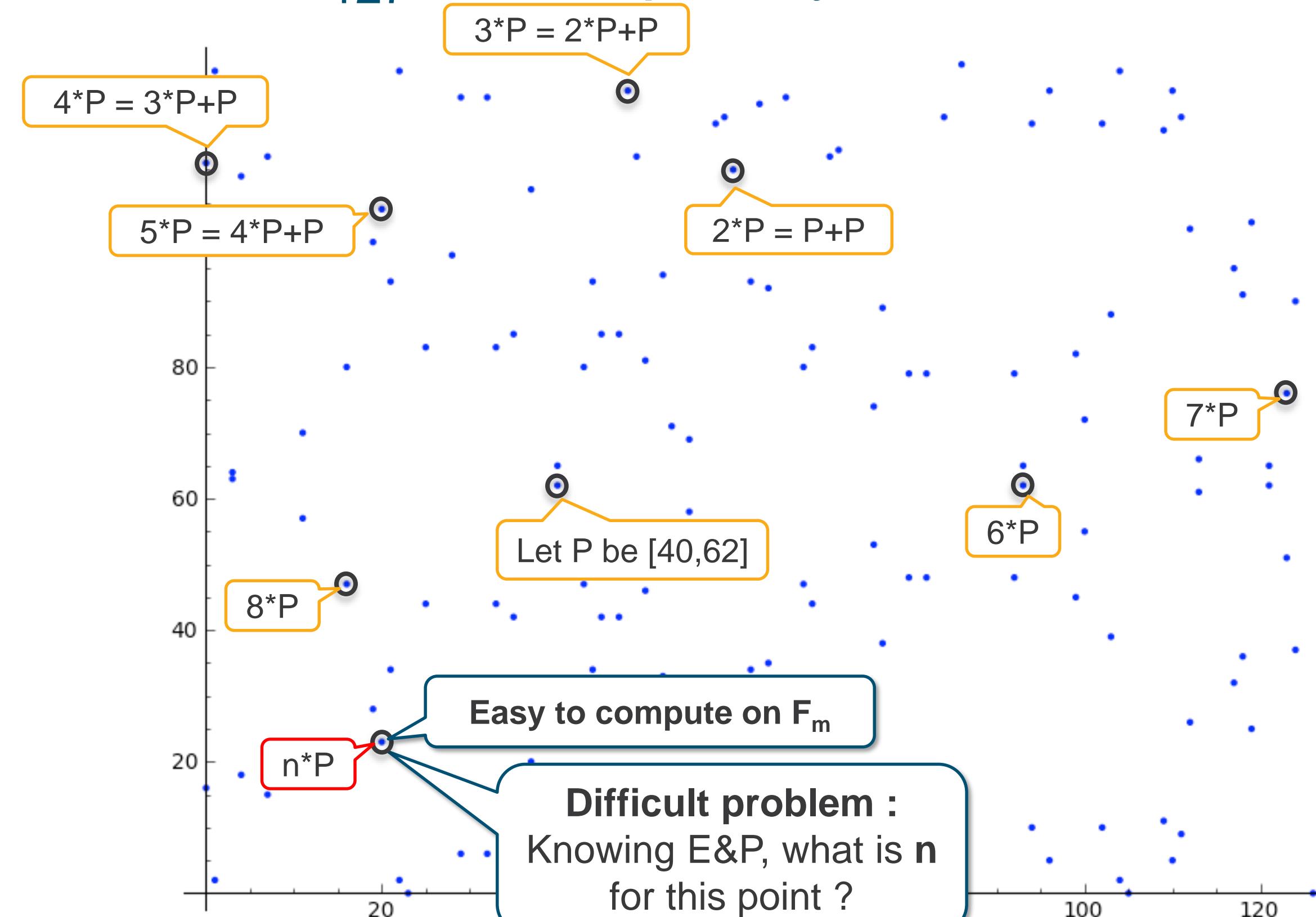


$$m = 2^5 - 1 = 31$$

$$E(F_{31}): y^2 = x^3 + x + 2$$

$$|E(F_{31})| = 24$$

# The same on $F_{127}$ – Complexity Further Increases



$$m = 2^7 - 1 = 127$$

$$E(F_{127}): y^2 = x^3 + x + 2$$

$$|E(F_{127})| = 136$$

# ECDH – Elliptic Curve Diffie-Hellman

Alice

Select a curve  $f$  and a point  $P$  on the curve  
Pick a random number  $a$   
Keep  $a$  secret!!  
Compute  $A_{\text{pub}} = a * P$

The curve definition  $f$   
and point  $P$

$A_{\text{pub}}, (P, f(x), m)$

Attacker can not guess  $a$

Bob

Using the same curve  $f$  and point  $P$   
Pick a random number  $b$   
Keep  $b$  secret!!  
Compute  $B_{\text{pub}} = b * P$

$\text{Secret}_{\text{Init}} = a * B_{\text{pub}}$



$\text{Secret} = a * b * P$



$\text{Secret}_{\text{Resp}} = b * A_{\text{pub}}$

P-256 from "NIST routines"

# Representation of Elliptic Curves

- Elliptic curve domain parameters
  - $(p, a, b, G, n, h)$  for a curve over a prime field  $F_p$
  - $(m, f(x), a, b, G, n, h)$  for a curve over a binary field  $F_{2^m}$
- Where
  - **p** is the prime modulus
  - **G** is the generator (base point) of the curve
  - **n** is the order of G. i.e **n\*G=O**
  - **a, b** are the coefficient of  $y^2 + xy = x^3 + ax + b \pmod{p}$
- Who defines elliptic curves ?
  - National Institute of Standards and Technology (NIST)
  - American National Standard Institute (ANSI)
  - Agence Nationale pour la Sécurité des Systèmes Informatiques(ANSSI)
  - Institute of Electrical and Electronics Engineers (IEEE)
  - Certicom
  - Brainpool ECC

## 4.3 Curve P-256

### 4.3.1 Parameters

The curve P-256 is given by the following parameters (see also [FIPS186-2]).  
The prime  $p_{256} = 2^{256} - 2^{224} + 2^{192} + 2^{96} - 1$ :

$p_{256} = 1157920892103562487626974469494075735300\backslash$   
 $86143415290314195533631308867097853951$

in hexadecimal form:

$p_{256} = \text{ffffffff } 00000001 \text{ 00000000 } 00000000 \text{ 00000000 }$   
 $\text{ffffffff } \text{ ffffffff}$

The parameter  $a = p_{256} - 3$ :

$a = 1157920892103562487626974469494075735300\backslash$   
 $86143415290314195533631308867097853948$

in hexadecimal form:

$a = \text{ffffffff } 00000001 \text{ 00000000 } 00000000 \text{ 00000000 }$   
 $\text{ffffffff } \text{ ffffffff}$

the parameter  $b$ :

$b = 4105836372515214212932612978004726840911\backslash$   
 $4441015993725554835256314039467401291$

in hexadecimal form:

$b = 5ac635d8 \text{ aa3a93e7 } b3ebbd55 \text{ 769886bc } 651d06b0 \text{ cc53b0f6 }$   
 $3bce3c3e \text{ 27d2604b}$

Base point G:

$x_G = 4843956129390645175905258525279791420276\backslash$   
 $2949526041747995844080717082404635286$

$y_G = 3613425095674979579858512791958788195661\backslash$   
 $1106672985015071877198253568414405109$

in hexadecimal form:

$x_G = 6b17d1f2 \text{ e12c4247 } f8bce6e5 \text{ 63a440f2 } 77037d81 \text{ 2deb33a0 }$   
 $f4a13945 \text{ d898c296}$

$y_G = 4fe342e2 \text{ fe1a7f9b } 8ee7eb4a \text{ 7c0f9e16 } 2bce3357 \text{ 6b315ece }$   
 $cbb64068 \text{ 37bf51f5}$

in hexadecimal form with X9.63 compression (lead byte 02 if  $y_G$  is even, 03 if  $y_G$  is odd):

$\bar{G} = 00000003 \text{ 6b17d1f2 } e12c4247 \text{ f8bce6e5 } 63a440f2 \text{ 77037d81 }$   
 $2deb33a0 \text{ f4a13945 } d898c296$

Order  $q$  of the point  $G$  (and of the elliptic curve group  $E$ ):

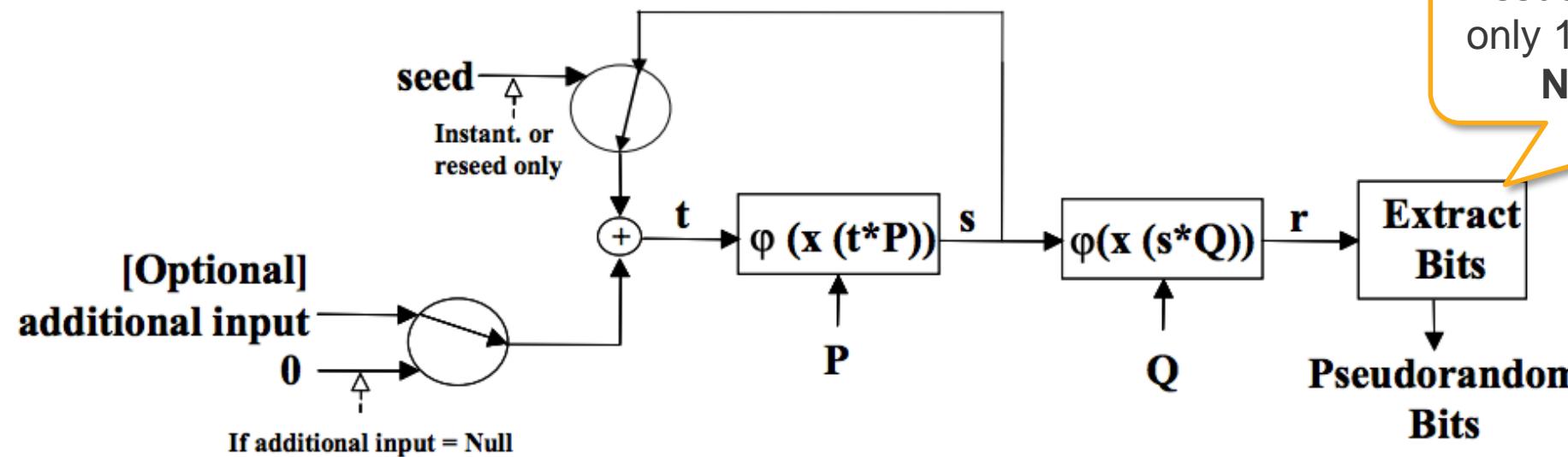
$q = 1157920892103562487626974469494075735299\backslash$   
 $96955224135760342422259061068512044369$

hexadecimal form:

$q = \text{ffffffff } 00000000 \text{ ffffffff } \text{ ffffffff }$   
 $bce6faad \text{ a7179e84 }$   
 $f3b9cac2 \text{ fc632551}$

# A back door'ed PRNG: Dual EC DRBG

source: NIST 800-90A



Issue #1: extract too many bits –  
only 16 bits to guess leads to  $s^*Q$ .  
Not a problem in itself...

## A.1.1 Curve P-256

```
p = 11579208921035624876269744694940757353008614\
      3415290314195533631308867097853951
n = 11579208921035624876269744694940757352999695\
      5224135760342422259061068512044369
b = 5ac635d8 aa3a93e7 b3ebbd55 769886bc 651d06b0 cc53b0f6 3bce3c3e
      27d2604b
Px = 6b17d1f2 e12c4247 f8bce6e5 63a440f2 77037d81 2deb33a0
      f4a13945 d898c296
Py = 4fe342e2 fela7f9b 8ee7eb4a 7c0f9e16 2bce3357 6b315ece
      cbb64068 37bf51f5
Qx = c97445f4 5cdef9f0 d3e05e1e 585fc297 235b82b5 be8ff3ef
      ca67c598 52018192
Qy = b28ef557 ba31dfcb dd21ac46 e2a91e3c 304f44cb 87058ada
      2cb81515 1e610046
```

Issue #2: NSA managed to make  
baked P&Q values a standard.  
The last nail in the coffin

if  $P=eQ$ , knowing  $sQ$  means  $sP=seQ \rightarrow$  once you know  $sQ$ , you  
know what is going to be the next  $sP$ : just compute  $e^*sQ$  !!

Then you know  $sQ$  effortlessly  $\rightarrow$  compute the next  $sP$  etc. forever!!

$P$  &  $Q$  are supposed to be truly random point but the NSA cheated  
the process and cooked  $P$  &  $Q$  to have a relationship  $P=eQ$ . Of  
course,  $e$  is super secret and very hard (impossible) to find.

By breaking the PRNG, the attacker can  
break all other crypto mechanisms. New  
asymmetric or symmetric keys, DH  
secrets, pre-master secrets, etc.

NSA did NOT break cryptography.  
NSA abused a PROCESS !!

# Performance and Security Comparisons

# Security Level of Symmetric Crypto Algorithms

Security Level	Work Factor	Algorithms
Weak	$O(2^{40})$	DES, MD5
Legacy	$O(2^{64})$	RC4, SHA1
Minimum	$O(2^{80})$	3DES, SEAL, SKIPJACK
Standard	$O(2^{128})$	AES-128, SHA-256, GHASH
High	$O(2^{192})$	AES-192, SHA-384, GHASH
Ultra	$O(2^{256})$	AES-256, SHA-512, GHASH

# Quantum Strength (for comparison)

Algorithm	Key Length	Classical Bit Strength	Quantum Bit Strength
RSA/DH 1024	1024 bits	80 bits	0 bits
RSA/DH 2048	2048 bits	112 bits	0 bits
ECC/ECDH 256	256 bits	128 bits	0 bits
ECC/ECDH 521	521 bits	256 bits	0 bits
AES 128	128 bits	128 bits	64 bits
AES 256	256 bits	256 bits	128 bits
SHA 256	256 bits	256 bits	128 bits

# ECDH Gains in Security

The Table Below Shows the Comparable Key Lengths Required in DH/RSA as Compared to ECC Based DH to Secure a Symmetric Key of a Given Length

Symmetric Key Length	ECC Key Length	DH/RSA Key Length
80	163	1024
112	233	2048
128	283	3072
192	409	7680
256	571	15360

Reference: draft-ietf-ipsec-ike-ecc-groups-05.txt with Further Reference Contained Therein

# IOS IKEv2 New Smart Defaults

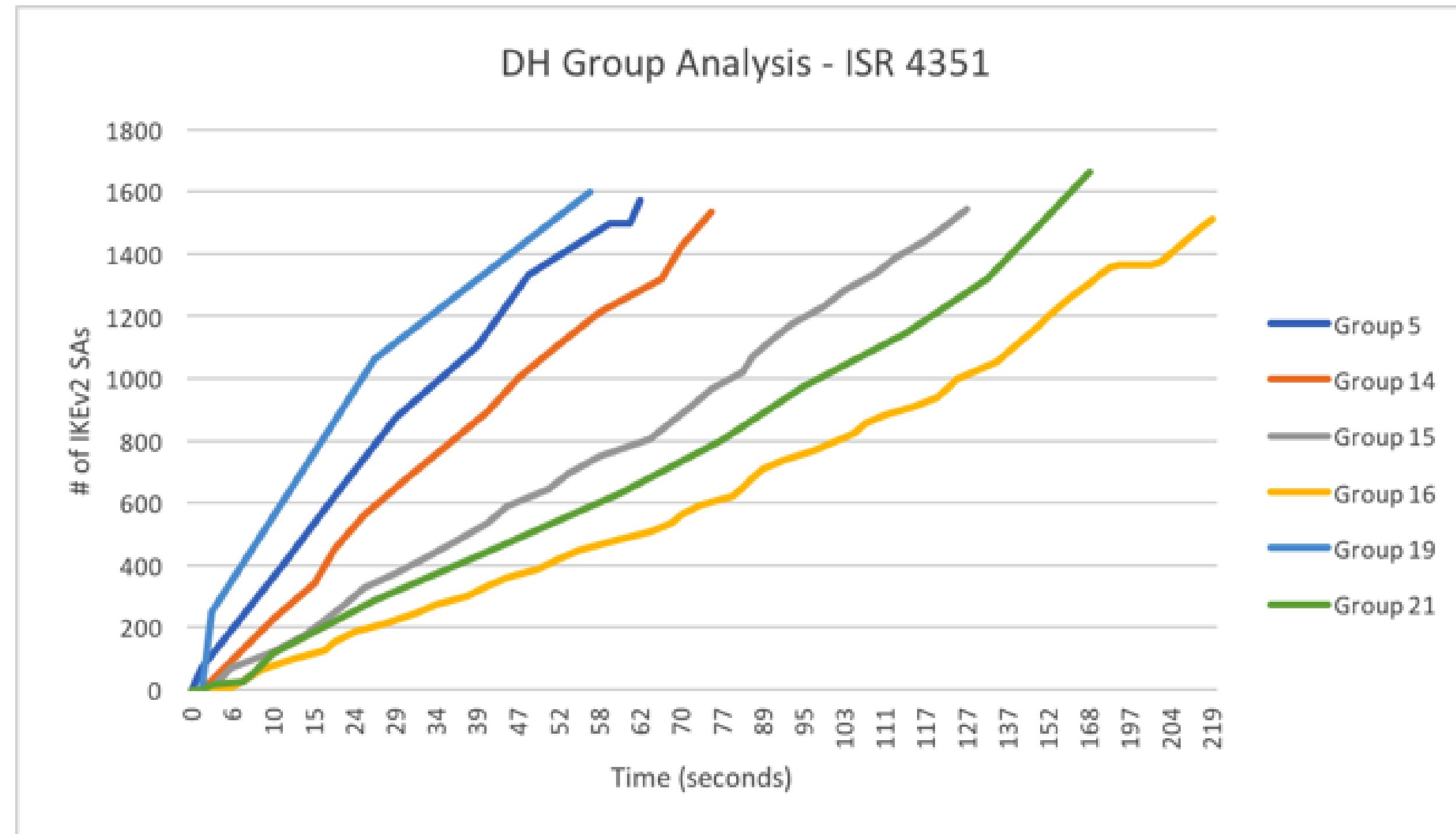
```
Router#show crypto ikev2 proposal default
IKEv2 proposal: default
Encryption : AES-CBC-256 AES-CBC-192 AES-CBC-128
Integrity  : SHA512 SHA384 SHA256 SHA96 MD596
PRF         : SHA512 SHA384 SHA256 SHA1 MD5
DH Group   : DH_GROUP_1536_MODP/Group 5 DH_GROUP_1024_MODP/Group 2
```

Today

```
Router#show crypto ikev2 proposal default
Encryption : AES-CBC-256
Integrity  : SHA512 SHA384
PRF         : SHA512 SHA384
DH Group   : DH_GROUP_256_ECP/Group 19 DH_GROUP_2048_MODP/Group 14
              DH_GROUP_521_ECP/Group 21 DH_GROUP_1536_MODP/Group 5
```

CSCuy44786  
16.8.1

# IOS IKEv2 Smart Defaults Performance



# Rough Performance Comparison

Very rough comparison – orders of magnitude only (\*)

Strength	AES-CBC			DES / 3DES CBC			RSA			ECDSA		
	Key size	16 B	8192 B	Key size	16 B	8192 B	Modulus	Sign	Verify	Field	Sign	Verify
< 80 bits	-	-	-	56 <sub>(DES)</sub>	64 MBps	66 MBps	512 bits	18K /s	194K /s	-	-	-
80 bits	-	-	-	168 <sub>(3DES)</sub>	25MBps	25MBps	1024 bits	6.5K /s	90K /s	p160	13K /s	4K /s
112 bits	-	-	-	-	-	-	2048 bits	1.5K /s	30K /s	p256	20K /s	8.5K /s
128 bits	128	116MBps	130MBps	-	-	-	4096 bits	136 /s	8.5K /s	k283	1.6K /s	1K /s
192 bits	192	98.5 MBps	109 MBps	-	-	-	7680 bits	-	-	k409	723 /s	568 /s
256 bits	256	85 MBps	94 MBps	-	-	-	15360 bits	-	-	k571	348 /s	249 /s

Optimizations...

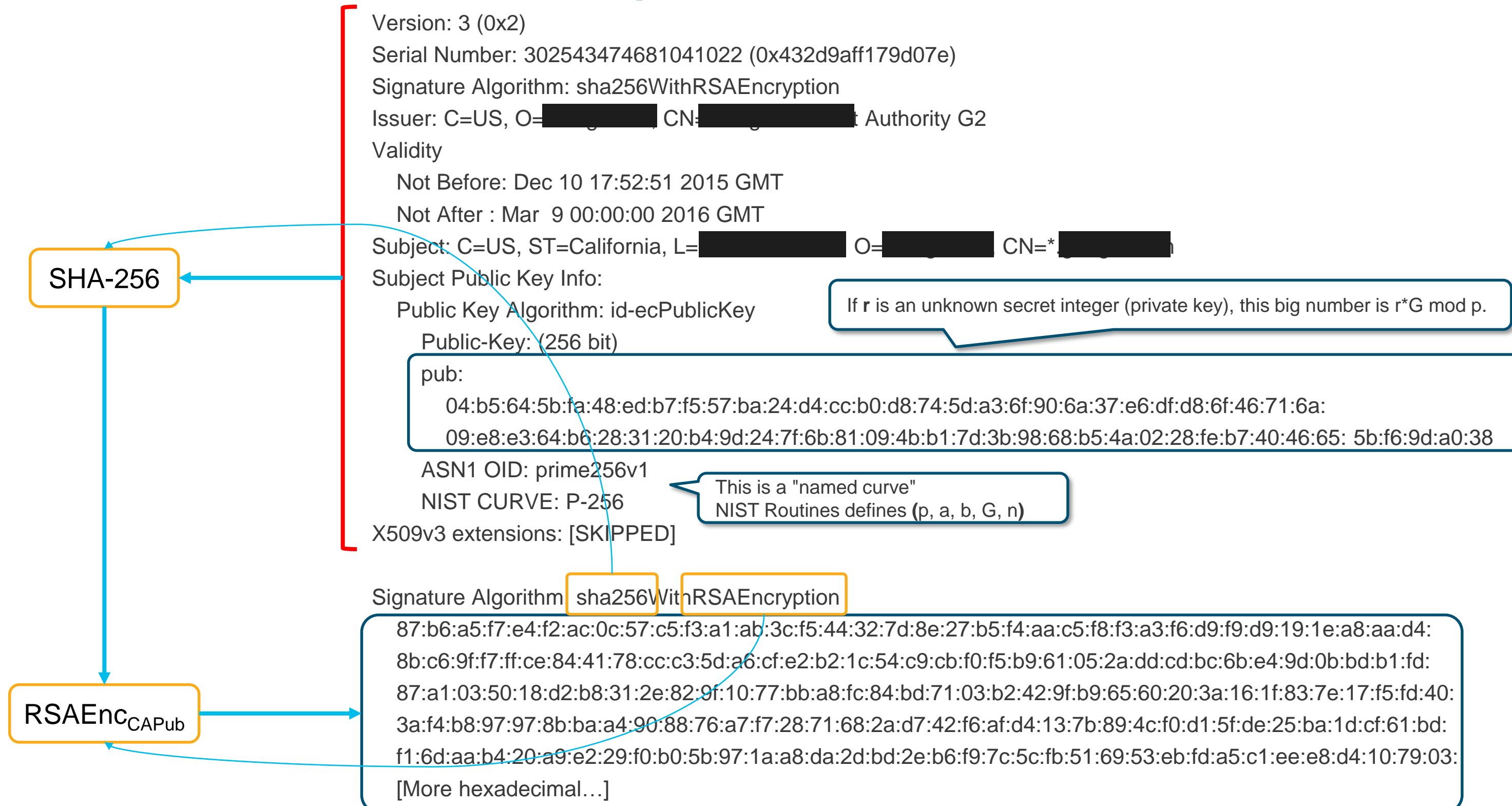
(\*) computed on my laptop – whatever that means

# See Performances for Yourself 😊

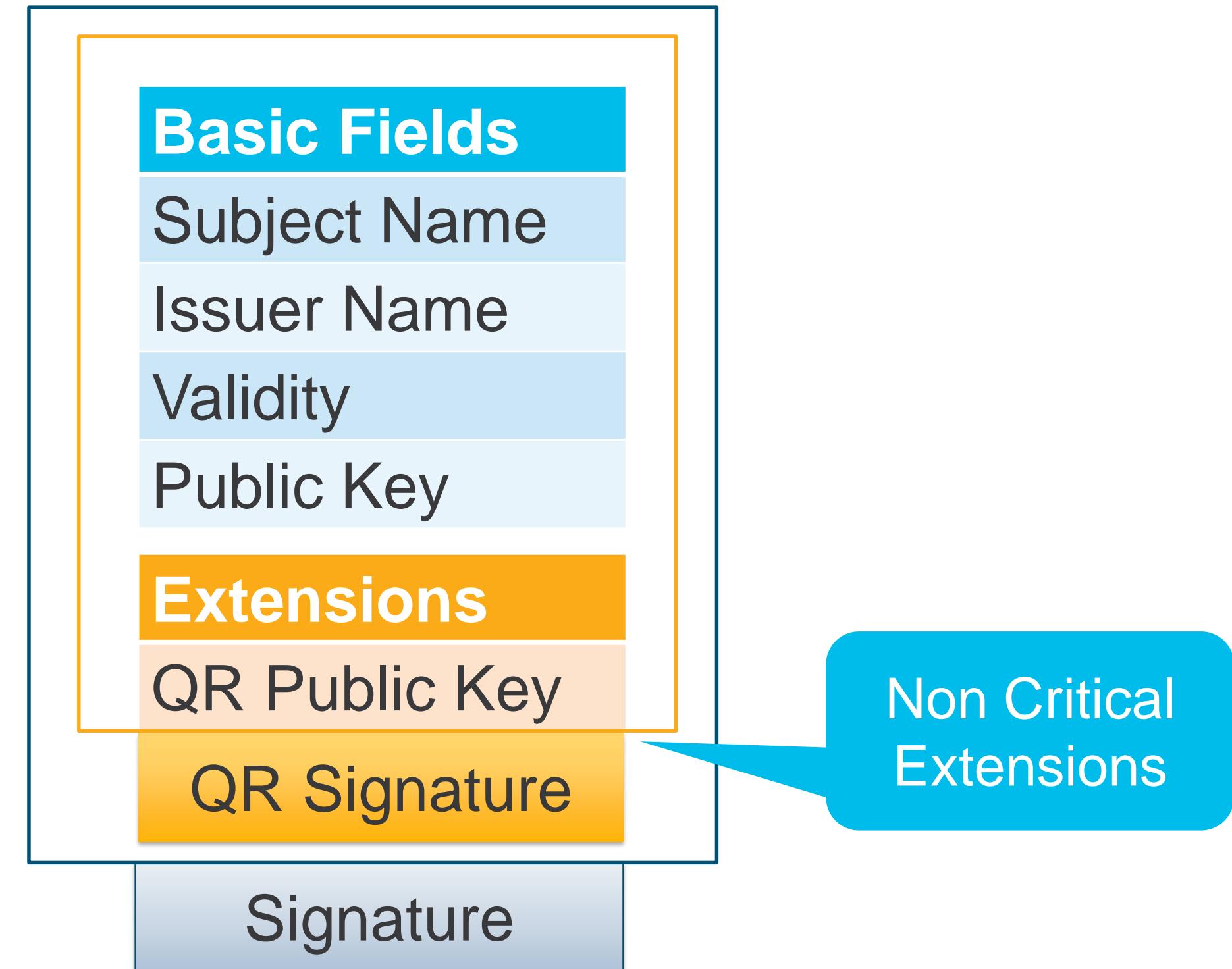
- openssl speed aes
- openssl speed des-cbc
- openssl speed des-ede3 ← 3-DES (Encrypt-Decrypt-Encrypt)
- openssl speed rsa
- openssl speed ecdsa
- openssl speed dh ← does not exist □
- openssl speed ecdh

# Practical Use... The Crypto Angle

# Certificates – Just an example...



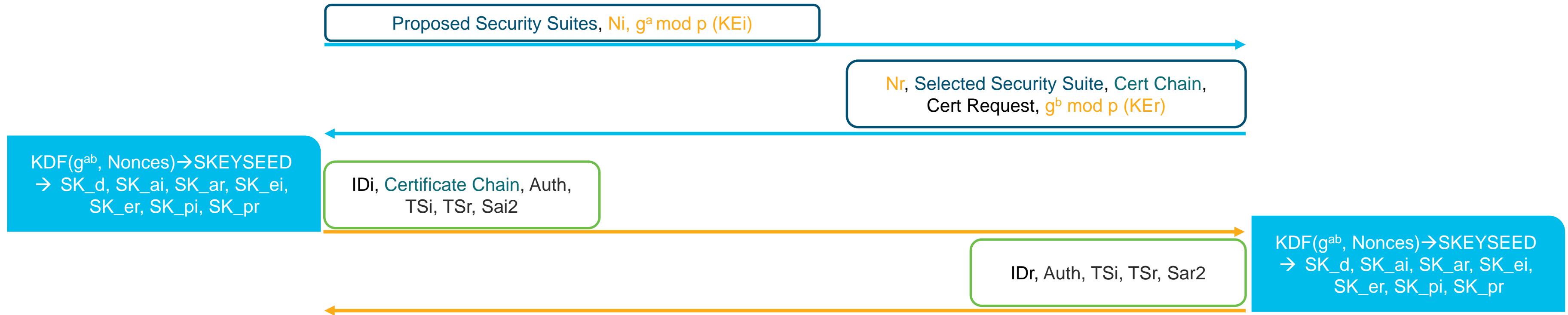
# Quantum Resistant Hybrid Certificate



# IKEv2

## Initiator

## Responder



Diffie-Hellman ensures Perfect Forward Secrecy: the ephemeral keys are independent of the authentication keys.

Ephemeral keys for IPsec SA's can be regenerated at regular interval using a fresh Diffie-Hellman exchange.

# Hash DRBG for Key Derivation and Authentication

Hash DRBG prf+:

$$\text{prf+ } (K, S) = T_1 | T_2 | T_3 | T_4 | \dots$$

where:

$$T_1 = \text{prf } (K, S | 0x01)$$

$$T_2 = \text{prf } (K, T_1 | S | 0x02)$$

$$T_3 = \text{prf } (K, T_2 | S | 0x03)$$

$$T_4 = \text{prf } (K, T_3 | S | 0x04)$$

...

Key Generation:

$$\text{SKEYSEED} = \text{prf } (N_i | N_r, g^{\wedge}r)$$

$$\{SK_d | SK_{ai} | SK_{ar} | SK_{ei} | SK_{er} | SK_{pi} | SK_{pr}\} = \text{prf+ } (\text{SKEYSEED}, N_i | N_r | SPI_i | SPI_r)$$

Key Derivation Function

Authentication: RSA<sub>Priv</sub>

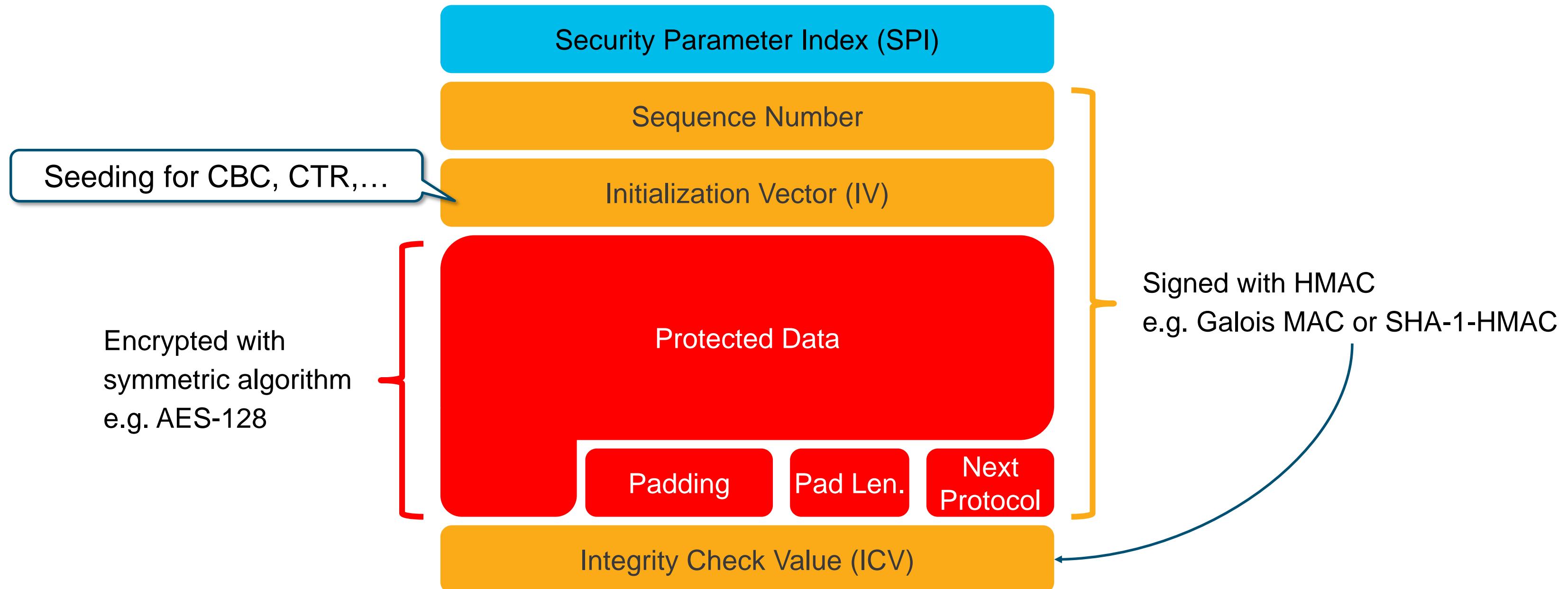
Let's call all this the "conversation"

InitiatorSignedOctets = RealMessage1 | NonceRData | MACedIDForI  
GenIKEHDR = [ four octets 0 if using port 4500 ] | RealIKEHDR  
RealIKEHDR = SPI<sub>i</sub> | SPI<sub>r</sub> | . . . | Length  
RealMessage1 = RealIKEHDR | RestOfMessage1  
NonceRPayload = PayloadHeader | NonceRData  
InitiatorIDPayload = PayloadHeader | RestOfInitIDPayload  
RestOfInitIDPayload = IDType | RESERVED | InitIDDData  
MACedIDForI = prf(SK<sub>pi</sub>, RestOfInitIDPayload)

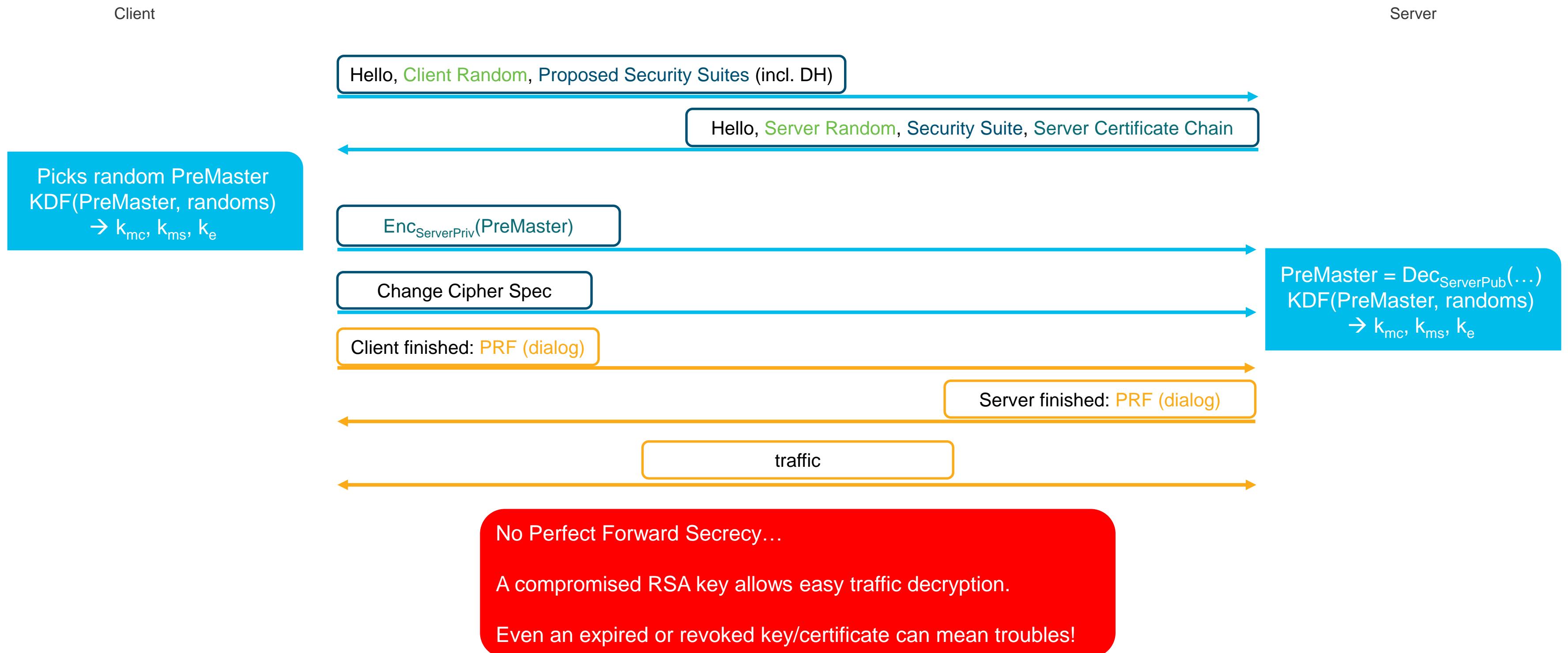
# IPsec: ESP packet format

IPsec HMAC and Encryption keys independent of IKE sessions keys.

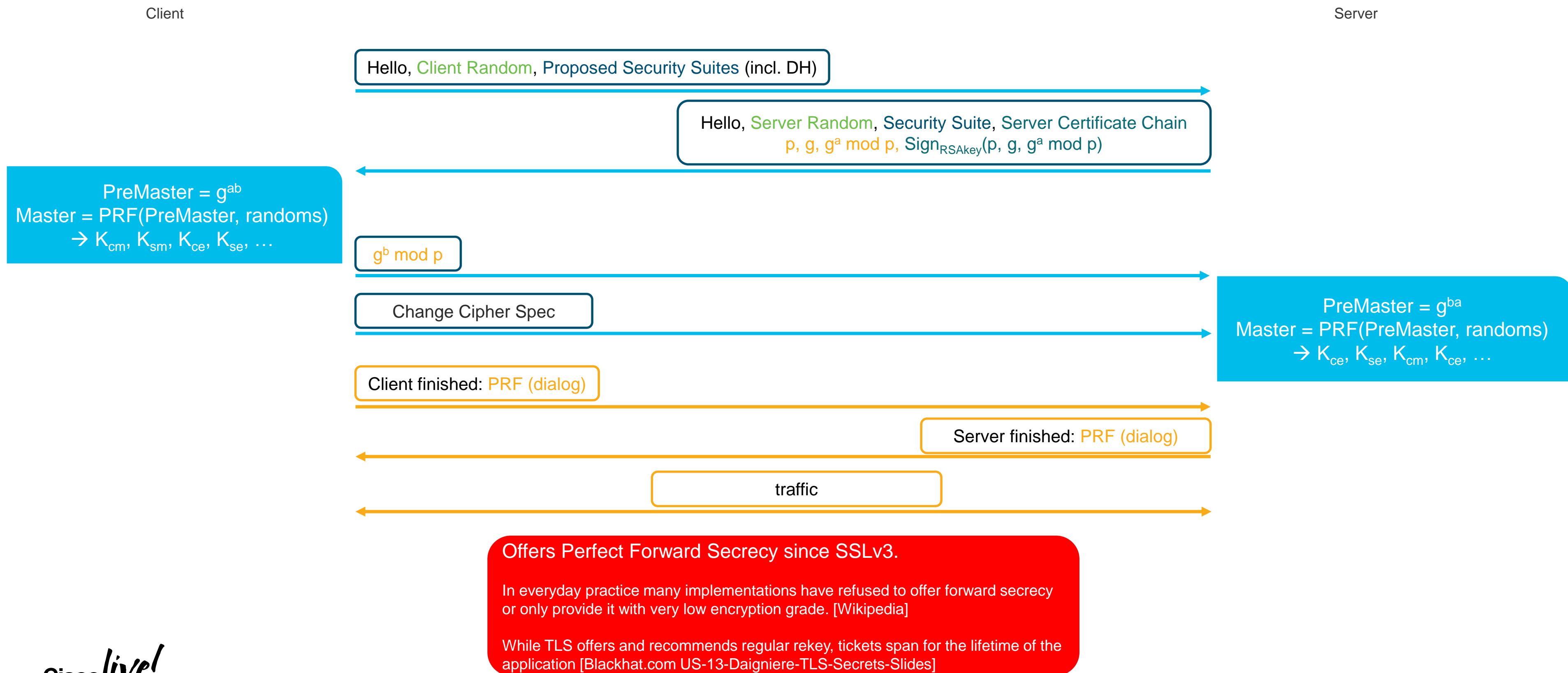
IPsec keys can be derived from a fresh DH exchange (aka PFS)



# SSL/TLS with Pre-Master Secret (no DH)



# SSL/TLS with Ephemeral Diffie-Hellman



# TLS Key Derivation and Authentication

$$P_{\text{hash}}(\text{secret}, \text{seed}) = \text{HMAC\_hash}(\text{secret}, A(1) + \text{seed}) + \\ \text{HMAC\_hash}(\text{secret}, A(2) + \text{seed}) + \dots$$

$A()$  is defined as

Hash DRBG prf:

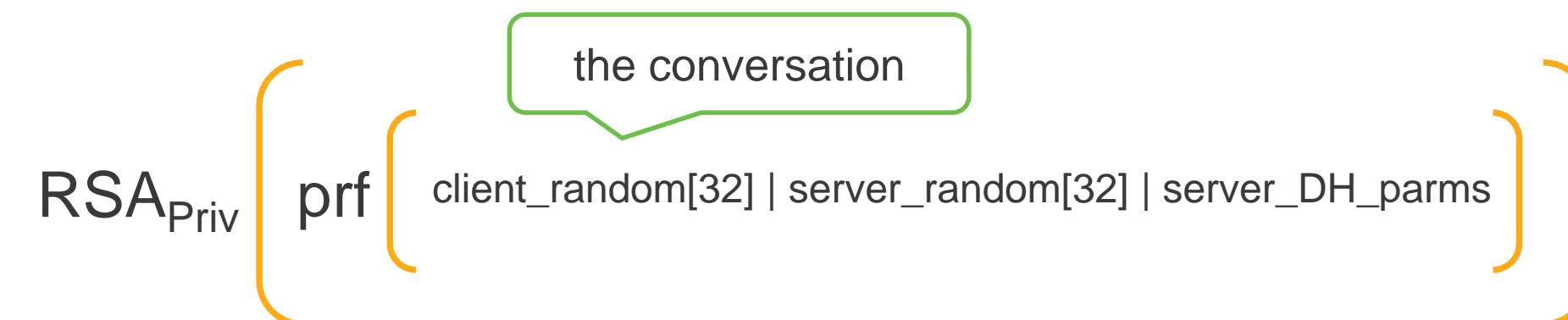
$$A(0) = \text{seed}$$
$$A(i) = \text{HMAC\_hash}(\text{secret}, A(i-1))$$
$$\text{PRF}(\text{secret}, \text{label}, \text{seed}) = P_{<\text{hash}>}(\text{secret}, \text{label} + \text{seed})$$

Key Derivation Function

Key Generation:

$$\text{key\_block} = \text{PRF}(\text{master\_secret}, \text{"key expansion"}, \text{server\_random}, \text{client\_random})$$
$$\{K_{cm}, K_{sm}, K_{ce}, K_{se}, \dots\} = \text{key\_block}$$

Server Authentication:



# Recommendations and Conclusion

# Reassurance

- Crypto is not broken but it has to be used intelligently
  - Post quantum cryptography
  - Supersingular isogeny key exchange
  - Learning With Errors (LWE) challenge
  - Lattice Based Cryptography
- All the problems cited were known or expected
- Snowden's revelations only showed how dedicated attackers are
- We should not be scared, we should simply act!

# Recommendations

- Protocols
  - IKEv2 is cool – use it if you can (not always possible)
  - Keep an eye on TLS1.3 for improvements
- Public Key Infrastructure (PKI)
  - Prefer **ECDSA** (> 256) or **RSA** (modulus size **>> 1024** ; 1536 or 2048 preferred)
  - **SHA-256-HMAC** or better is a must
- Key Exchange
  - **Use PFS**
  - Prefer **ECDH 263 bits** for mid term security (~15 years) or **MODP 3184 bits** for 15+ years
  - If MODP, use DH group **>> 1024** (1536 or 2048 preferred).
    - IKEv2: group 5 (~1500 bits) or better
    - TLS 1.2: FIX YOUR SERVERS!! <https://weakdh.org/sysadmin.html>
    - Upgrade to TLS 1.3 whenever possible (still draft)
- Symmetric key cryptography
  - **AES-128** (or better) CBC or Counter mode
  - SHA-1 is still ok for data crypto but plan moving to **GCM, GMAC or SHA-2** (256 or above)

# Reputedly Safe Elliptic Curves

		Parameters:			ECDLP security:				ECC security:				
Curve	Safe?	field	equation	base	rho	transfer	disc	rigid	ladder	twist	complete	ind	
Anomalous	False	True✓	True✓	True✓	True✓	False	False	True✓	False	False	False	False	False
M-221	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓
E-222	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓
NIST P-224	False	True✓	True✓	True✓	True✓	True✓	True✓	False	False	False	False	False	False
Curve1174	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓
Curve25519	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓
BN(2,254)	False	True✓	True✓	True✓	True✓	True✓	False	False	True✓	False	False	False	False
brainpoolP256t1	False	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	False	False	False	False
ANSSI FRP256v1	False	True✓	True✓	True✓	True✓	True✓	True✓	False	False	False	False	False	False
NIST P-256	False	True✓	True✓	True✓	True✓	True✓	True✓	False	False	True✓	False	False	False
secp256k1	False	True✓	True✓	True✓	True✓	True✓	True✓	False	True✓	False	True✓	False	False
E-382	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓
M-383	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓
Curve383187	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓
brainpoolP384t1	False	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	False	True✓	False	False
NIST P-384	False	True✓	True✓	True✓	True✓	True✓	True✓	False	False	True✓	False	False	False
Curve41417	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓
Ed448-Goldilocks	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓
M-511	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓
E-521	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓	True✓

source: <http://safecurves.cr.yp.to>

# Some Random Software... FlexVPN (IOS)

## Keypair for certificates

```
crypto key generate ec keysiz 256  
crypto key generate rsa 1536 (or better)
```

## IKEv2 Profile

```
crypto ikev2 proposal default  
    encryption aes-256 aes-cbc-192 aes-cbc-128  
    integrity sha512 sha384 sha256  
    prf sha512 sha384 sha256  
group 14 5
```

Defaults are Top!

```
show crypto ikev2 proposal  
IKEv2 proposal: default  
    Encryption : AES-CBC-256  
    Integrity  : SHA512 SHA384  
    PRF        : SHA512 SHA384  
    DH Group   : DH_GROUP_256_ECP/Group 19 DH_GROUP_2048_MODP/Group  
                14 DH_GROUP_521_ECP/Group 21 DH_GROUP_1536_MODP/Group 5
```

# Some Random Software... WSA

Hear it from the horse's mouth

See BRKSEC-3006 – Tobias Mayer on TLS Decryption using the Web Security Appliance

# Some Random Software... OpenSSH

/etc/ssh/ssh\_config

KexAlgorithms curve25519-sha256@libssh.org

ssh-keygen -G moduli-2048.candidates -b 2048  
ssh-keygen -T moduli-2048 -f moduli-2048.candidates

Generate your own DH

# Some Random Software... Apache (mod\_ssl)

/etc/dovecot.conf

SSLProtocol all -SSLv2 -SSLv3

SSLCipherSuite ECDHE-RSA-AES128-GCM-SHA256:ECDHE-ECDSA-AES128-GCM-SHA256:ECDHE-RSA-AES256-GCM-SHA384:ECDHE-ECDSA-AES256-GCM-SHA384:DHE-RSA-AES128-GCM-SHA256:DHE-DSS-AES128-GCM-SHA256:kEDH+AESGCM:ECDHE-RSA-AES128-SHA256:ECDHE-ECDSA-AES128-SHA256:ECDHE-RSA-AES128-SHA:ECDHE-ECDSA-AES128-SHA:ECDHE-RSA-AES256-SHA384:ECDHE-ECDSA-AES256-SHA384:ECDHE-RSA-AES256-SHA:ECDHE-ECDSA-AES256-SHA:DHE-RSA-AES128-SHA256:DHE-RSA-AES128-SHA:DHE-DSS-AES128-SHA256:DHE-RSA-AES256-SHA256:DHE-DSS-AES256-SHA:DHE-RSA-AES256-SHA:AES128-GCM-SHA256:AES256-GCM-SHA384:AES128-SHA256:AES256-SHA256:AES128-SHA:AES256-SHA:AES:CAMELLIA:DES-CBC3-SHA:!aNULL:!eNULL:!EXPORT:!DES:!RC4:!MD5:!PSK:!aECDH:!EDH-DSS-DES-CBC3-SHA:!EDH-RSA-DES-CBC3-SHA:!KRB5-DES-CBC3-SHA

SSLHonorCipherOrder on

Point to custom DH parameters

SSLOpenSSLConfCmd DHParameters "{path to dhparams.pem}"

openssl dhparam -out dhparams.pem 2048

# Some Random Software... Dovecot

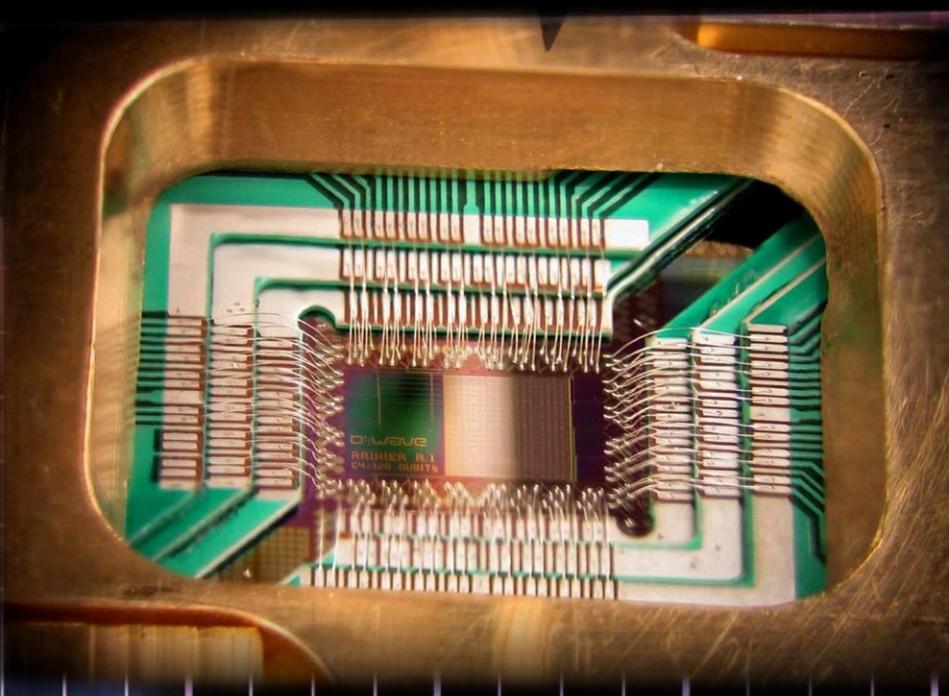
/etc/dovecot.conf

```
ssl_cipher_list=ECDHE-RSA-AES128-GCM-SHA256:ECDHE-ECDSA-AES128-GCM-SHA256:ECDHE-RSA-AES256-GCM-SHA384:ECDHE-ECDSA-AES256-GCM-SHA384:DHE-RSA-AES128-GCM-SHA256:DHE-DSS-AES128-GCM-SHA256:kEDH+AESGCM:ECDHE-RSA-AES128-SHA256:ECDHE-ECDSA-AES128-SHA256:ECDHE-RSA-AES128-SHA:ECDHE-ECDSA-AES128-SHA:ECDHE-RSA-AES256-SHA384:ECDHE-ECDSA-AES256-SHA384:ECDHE-RSA-AES256-SHA:ECDHE-ECDSA-AES256-SHA:DHE-RSA-AES128-SHA256:DHE-RSA-AES128-SHA:DHE-DSS-AES128-SHA256:DHE-RSA-AES256-SHA256:DHE-DSS-AES256-SHA:DHE-RSA-AES256-SHA:AES128-GCM-SHA256:AES256-GCM-SHA384:AES128-SHA256:AES256-SHA256:AES128-SHA:AES256-SHA:AES:CAMELLIA:DES-CBC3-SHA:!aNULL:!eNULL:!EXPORT:!DES:!RC4:!MD5:!PSK:!aECDH:!EDH-DSS-DES-CBC3-SHA:!EDH-RSA-DES-CBC3-SHA:!KRB5-DES-CBC3-SHA
```

ssl\_prefer\_server\_ciphers = yes (Dovecot 2.2.6 or greater)

Regenerate DH Parameters

```
#regenerates every week ssl_dh_parameters_length = 2048
```



The image features a dark blue background with a light blue grid overlay. A diagonal band of white binary digits (0s and 1s) runs from the top-left towards the bottom-right. The digits are arranged in a staggered, overlapping pattern, creating a sense of depth and movement. The overall effect is reminiscent of binary code being processed or displayed on a screen.

A close-up photograph of a row of mechanical film reels, likely from a projector, set against a background of blurred binary code digits (0s and 1s) on a grid pattern. The film reels are dark and metallic, showing some numbers and markings. The background is a soft-focus, repeating pattern of binary digits in red, purple, and blue, suggesting digital data or film frames.

# A Short Bibliography

- NIST SP 800-90A : Recommendations for Random Number Generation Using Deterministic Random Bit Generators
- NIST SP 800-38D : Recommendation for Block Cipher Modes of Operation: Galois/Counter Mode (GCM) and GMAC
- NIST SP 800-56A (R2): Pair-Wise Key Establishment Schemes Using Discrete Logarithm Cryptography (i.e. DH, ECDH + key derivation methods)
- NIST 800-131Ar1: Transitions: Recommendations fro Transitioning the Use of Cryptographic Algorithms and Key Lengths
- NIST FIPS 140-2: Security Requirements for Cryptographic Modules
- NIST FIPS 186-4: Digital Signature Standard (DSS) (DSA, RSA (PKCS#1), ECDSA,...)
- NIST FIPS 180-4: Secure Hash Standard (SHA-1, SHA-256,..., SHA-512)
- NIST Routines: [https://www.nsa.gov/ia/\\_files/nist-routines.pdf](https://www.nsa.gov/ia/_files/nist-routines.pdf) (Curve P-192, P-224, P-256 etc.)
- Safe Curves: <http://safecurves.cr.yp.to>
- Transcript Collision Attacks: Breaking authentication in TLS, IKE and SSH: <http://www.mitls.org/downloads/transcript-collisions.pdf>

# Call to Action

- Visit the World of Solutions for
  - Cisco Campus – (speaker to add relevant demos/areas to visit)
  - Walk in Labs – (speaker to add relevant walk in labs)
  - Technical Solution Clinics
- Meet the Engineer (Speaker to specify when they will be available for meetings)
- Lunch and Learn Topics
- DevNet zone related sessions

# Cisco Spark

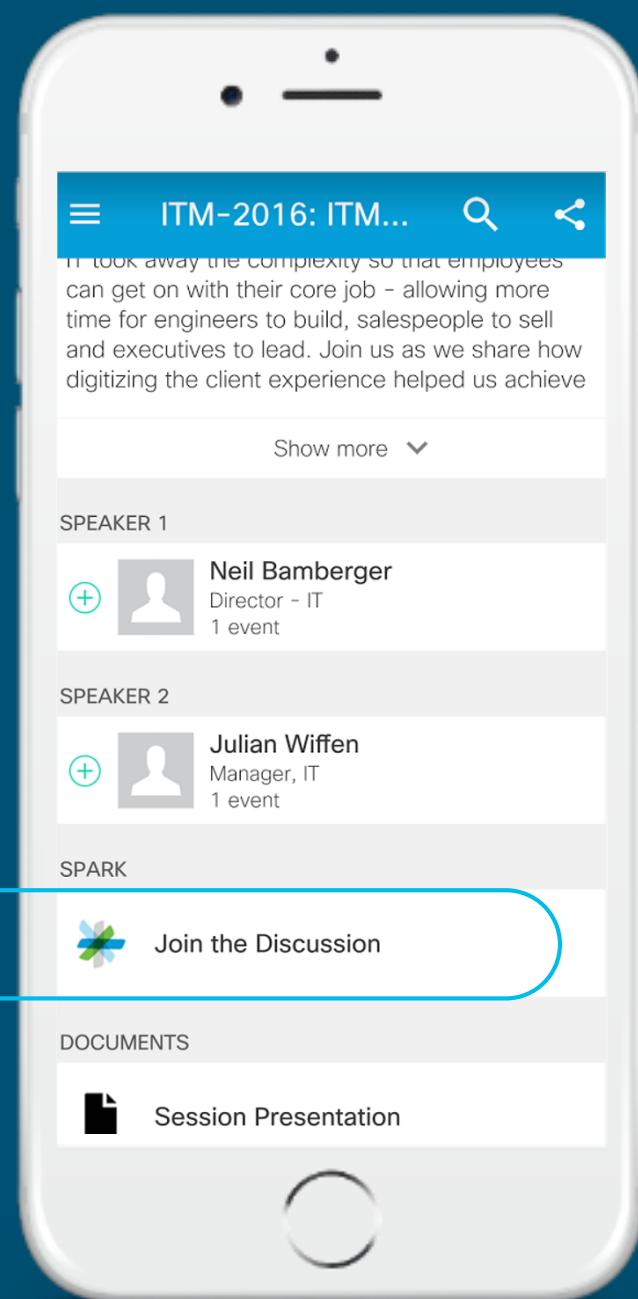


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with the speaker after the session

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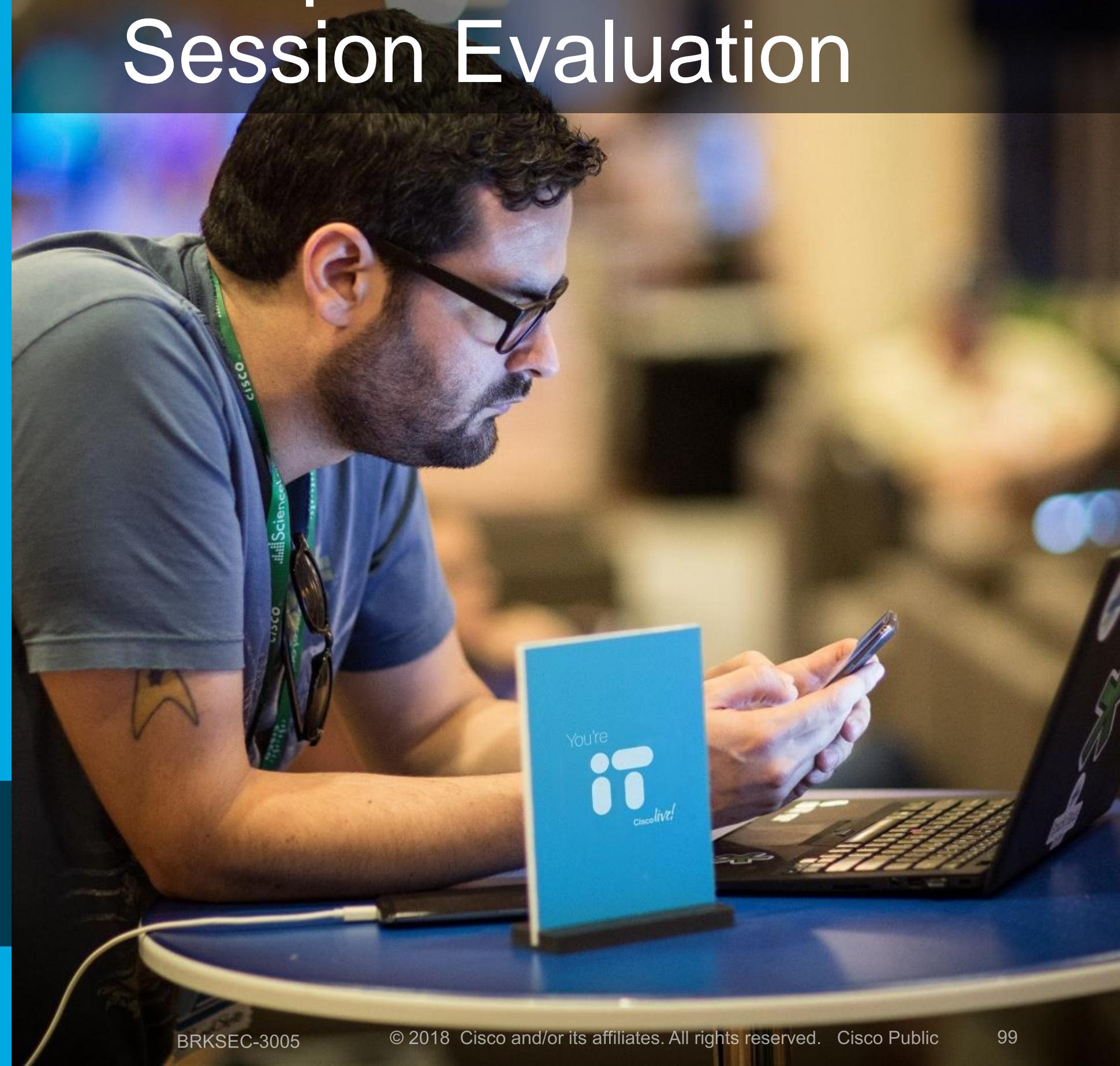


[cs.co/ciscolivebot#BRKSEC-3005](https://cs.co/ciscolivebot#BRKSEC-3005)

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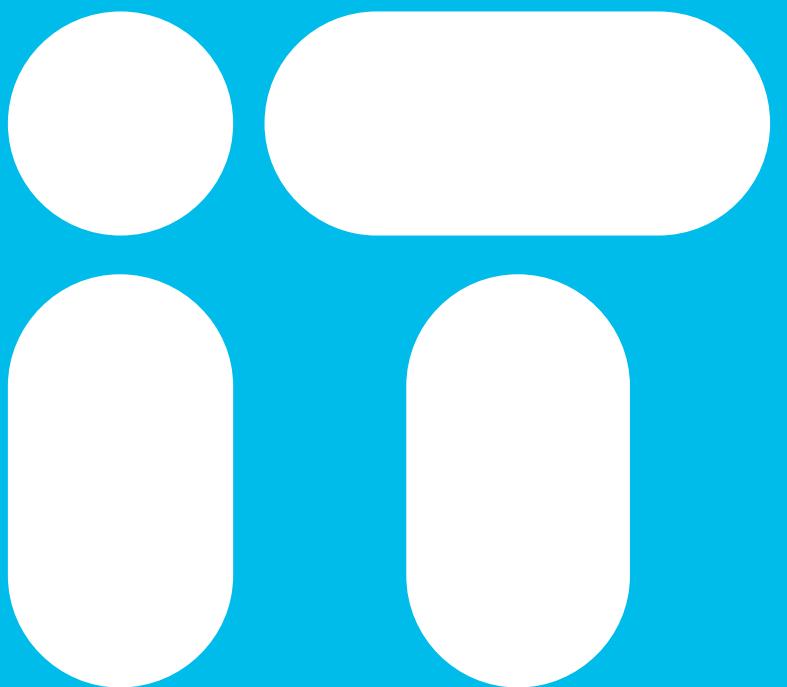
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- Walk-in Self-Paced Labs
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