SAMPLE NUMERICAL (ANN)

Q. FIND WEIGHT ADJUSTMENT AW35 & ERROR GRADIENT AT NODE 4'(84) FOR THE FOLLOWING MLP. ASSUME THE FOLLOWING:

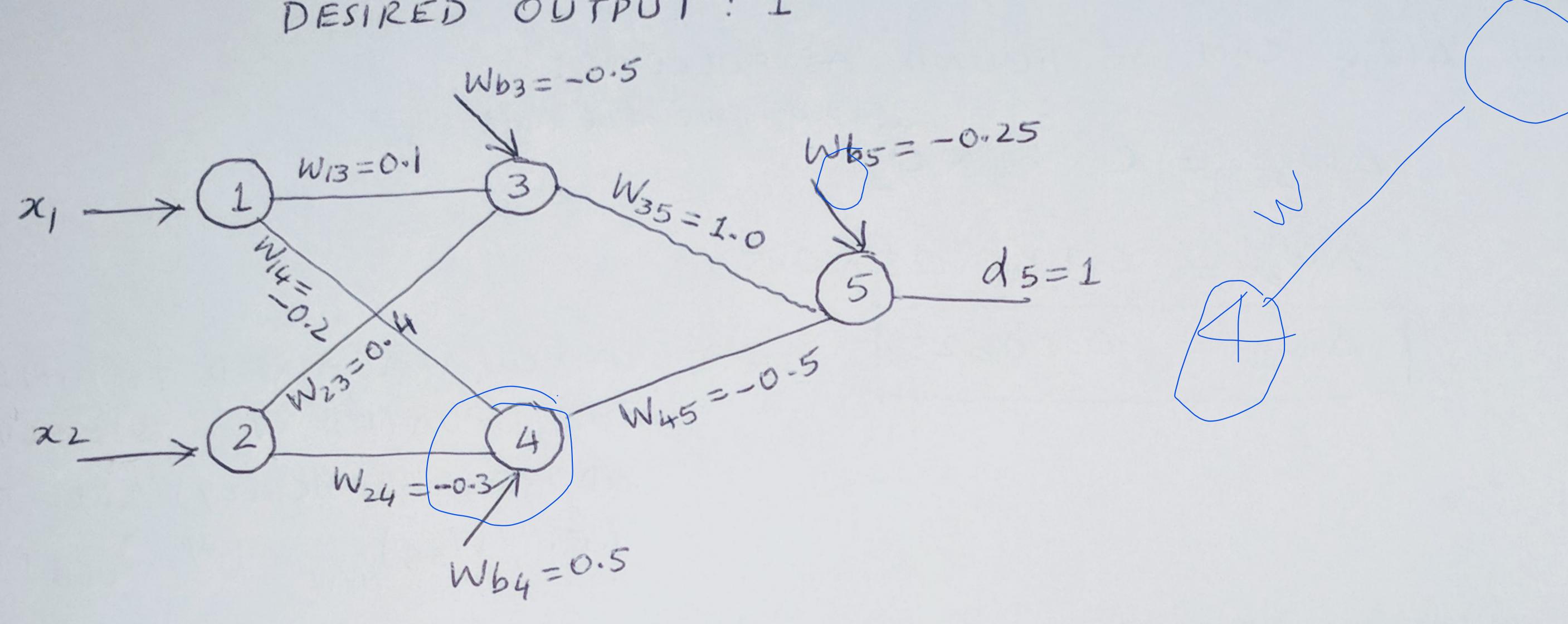
LEARNING CONSTANT "C' = 0.1 MOMENTUM FACTOR B'= 0.9

ERROR FUNCTION: MEAN SQUARED ERROR (MSE)

OUTPUT FUNCTION: LOG-SIGMOID (FOR ALL PROCESSING LAYERS)

INPUT VECTOR: $X = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$; BIASED INPUT: 1

DESIRED OUTPUT: 1



SOLN.

FIRST, FIND THE ACTUAL OUTPUT OF.

$$05 = \frac{1}{1 + e^{-nets}}$$

nets = 03 x W35 + 04 x W45 + Wb5

$$0_3 = \frac{1}{1 + e^{-net_3}}$$

 $net_3 = x_1 \times w_{13} + x_2 w_{23} + w_{b3} = 0.1 + 0.4 + (-0.5) = 0$

 $ret_4 = x_1 \times W_{14} + x_2 \times W_{24} + W_{b4} = -0.2 - 0.3 + 0.5 = 0$

$$0.03 = \frac{1}{1+e^0} = 0.5$$

$$d = \frac{1}{1+e^{\circ}} = 0.5$$

:.
$$net_5 = 0.5 \times 1 + 0.5 \times (-0.5) + (-0.25) = 0$$

$$\Rightarrow 05 = \frac{1}{1+e^{\circ}} = 0.5$$

NOW WE CAN CALCULATE ERROR AT NODE 5

$$e_5 = d_5 - 0_5 = 1 - 0.5 = 0.5$$

 $e_5 = d_5 - O_5 = 1 - 0.5 = 0.5$ TO BACK-PROPAGATE ERROR & ADJUST WEIGHTS, WE WEED TO FIND ERROR GRADIENT AT NODE 5, 85

$$85 = e_5 \times O_5(1-O_5)$$
 $gradient of output fn. at node 5$
 $85 = 0.5(0.5(1-0.5)) = 0.125$

 $\Delta W_{35} = C \times S_5 \times O_3$ NOW AW35 CAN BE FOUND AS FOLLOWS:

$$\Delta W_{35} = 0.1 \times 0.125 \times 0.5$$

$$\Delta w_{35} = 0.00625$$

DW35 = 0.00625 NOTE: IF YOU ARE ASKED TO FIND THE UPDATED WZG, SIMPLY ADD (ALGEBRAICALLY) AW35 TO W35 i.E. (W35) = (W35) OLD + AW35

NEXT, ERROR GRADIENT AT WODE 4, S4 = 7

USING BACKPROPAGATION ALGO, WE CAN ESTIMATE ERROR CONTRIBUTION OF NODE 4' AND WORK OUT 'S4' AS FULLOWS:

WE KNOW
$$S_j = \begin{bmatrix} \sum S_k w_{jk} \\ k \end{bmatrix}$$
 Oj (1-0;)

gradient of output finant node (nidden) j'.

$$\delta_{4} = \sqrt{\delta_{5}} \omega_{45} \times O_{4}(1-O_{4})$$

$$\delta_{4} = \sqrt{0.125} \times (-0.5) \times 0.5(1-0.5)$$

$$\delta_{4} = -0.0156$$