

Experiment No: 03

Experiment Name: A herd of 1500 steers was fed to special high protein gain for a month. A random sample of 29 was weighed and had gained an average of 6.7 pounds. If the sd of weight gain for the entire herd is 2.1. Test the hypothesis at 5% level of significance that the average weight gain per steer for the month was more than 5 pounds. Also comments on the test using the p-value. Create the confidence interval

Objectives:

1. To construct the average weight gain per steer for the month.
2. To create the confidence interval
3. To construct p-value.
4. To comment on the data.

Procedure :

Step-1: state the null hypothesis and alternative hypothesis.

The alternate hypothesis was more than 5 pounds.

$$\text{So, } H_1: \mu > 5$$

$$H_0: \mu \leq 5$$

Step-2: select the level of significance. The significance level is ~~is~~ selected 0.05.

Step-3: select the test statistic.

Hence, the standard deviation are known, so we use z-test.

$$Z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$$

$$\bar{x} = \frac{1}{n} \sum x_i$$

Step-4: Formulate the decision rule.

If the tabulated value of z is greater than calculated value of z then null

hypothesis is accepted, otherwise null hypothesis is rejected.

R Source code :

```
H0:  $\mu \leq 5$ 
```

```
H1:  $\mu > 5$ 
```

```
x.bar <- 6.7
```

```
 $\mu <- 5$ 
```

```
Sd <- 7.1
```

```
n <- 29
```

```
z <- (x.bar -  $\mu$ ) / (Sd /  $\sqrt{n}$ )
```

```
alpha = 0.05
```

```
zlab <- qnorm(0.05, lower.tail = FALSE)
```

```
# p-value
```

```
pvalue <- pnorm(z, lower.tail = FALSE)
```

```
H0:  $\mu$  is not equal 5
```

```
zlab1 <- qnorm(0.025)
```

```
zlab2 <- qnorm(0.975)
```

```
p.value <- 2 * pnorm(z, lower.tail = FALSE)
```

```
CI <- c(x.bar + zlab1 * Sd /  $\sqrt{n}$ ,  
x.bar + zlab2 * Sd /  $\sqrt{n}$ )
```


Input and output :

\bar{x} .bar

6.7

μ

5

sd

7.1

n

29

Z

1.28

α

0.05

$Z_{lab} = 1.64$

$pvalue = 0.098$

$Z_{lab1} = -1.96$

$Z_{lab2} = 1.96$

$p.value = 0.19$

CI = 4.1159 , 9.2840

Comment : From the R code we can see that , $Z_{lab} > Z_{cal}$ and also see that $pvalue > \alpha$. so H_0 is accepted. The average weight gain per steer for the month was less than 5 pounds.

Experiment No : 04

Experiment Name: In order to find out whether children with chronic diarrhea have the same average hemoglobin level (Hb) that is normally seen in healthy children in the same area, a random sample of 10 children with chronic diarrhea are selected and their Hb levels (g/dl) are obtained as follows : 12.3, 11.4, 14.2, 15.3, 14.8, 13.8, 11.1, 15.1, 15.8, 13.2.

Do the data provide sufficient evidence to indicate that the mean Hb level for children with chronic diarrhea is less than the normal value of 14.6 (g/dl)? Test at 0.01 level of significance. Draw a boxplot and normal plot for this data and comments.

Objectives:

1. To calculate the mean Hb level for children with chronic diarrhea is less than the normal value of 14.6 (g/dl).
2. To draw a boxplot and normal plot for this data.
3. To comments for this data.

Procedure :

Step-1: state the null hypothesis and alternate hypothesis. The alternate hypothesis is less than the normal value of 14.6. So the null hypothesis is greater than or equal 14.6.

$$H_0: \mu \geq 14.6$$

$$H_1: \mu < 14.6$$

Step-2: select the level of significance. The significance level is selected 0.01.

Step-3: Select the test statistic.
The sample size is less than 30 and population standard deviation are unknown. So we use t-test.

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}}$$

$$s^2 = \frac{1}{n-1} \left[\sum x_i^2 - \frac{(\sum x_i)^2}{n} \right]$$

Step-4: Formulate the decision rule.
If the tabulated value of t is greater than calculated value of t then H_0 is accepted, otherwise rejected.

R Source code :

```
H0: mu >= 14.6
```

```
H1: mu < 14.6
```

```
mu <- 14.6
```

```
data <- c(12.3, 11.4, 14.2, 15.3, 14.8, 13.8, 11.1,  
15.1, 15.8, 13.2)
```

```
n <- length(data)
```

```

x.bar <- mean(data)
sd.est <- sd(data)
t <- (x.bar - mu) / (sd.est / sqrt(n))
t.ab <- qt(0.01, n-1)
Pvalue.t <- pt(t, df = n-1)
boxplot(data, ylab = "Hb level", col = "gray")
qqnorm(data, main = "Normal Q-Q plot
of Hb level")
qqline(data)

```

Input and output :

```

mu = 14.6
n = 10
x.bar = 13.7
sd.est = 1.655
t = -1.71
t.ab = -2.89
Pvalue.t = 0.059

```

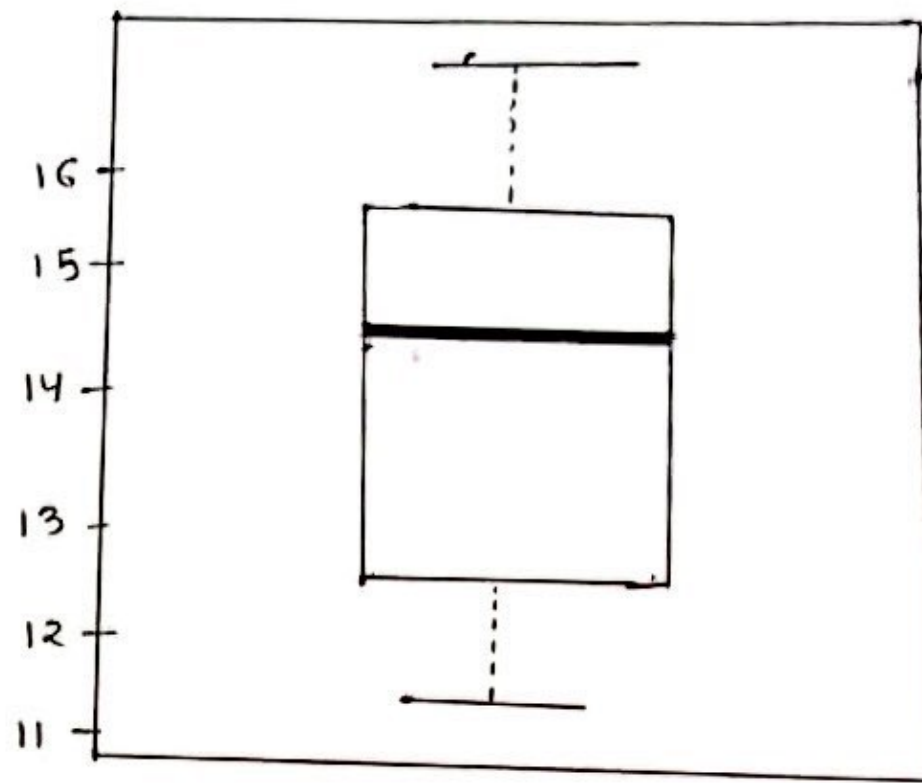



Fig: Boxplot
Normal Q-Q plot of Hb level

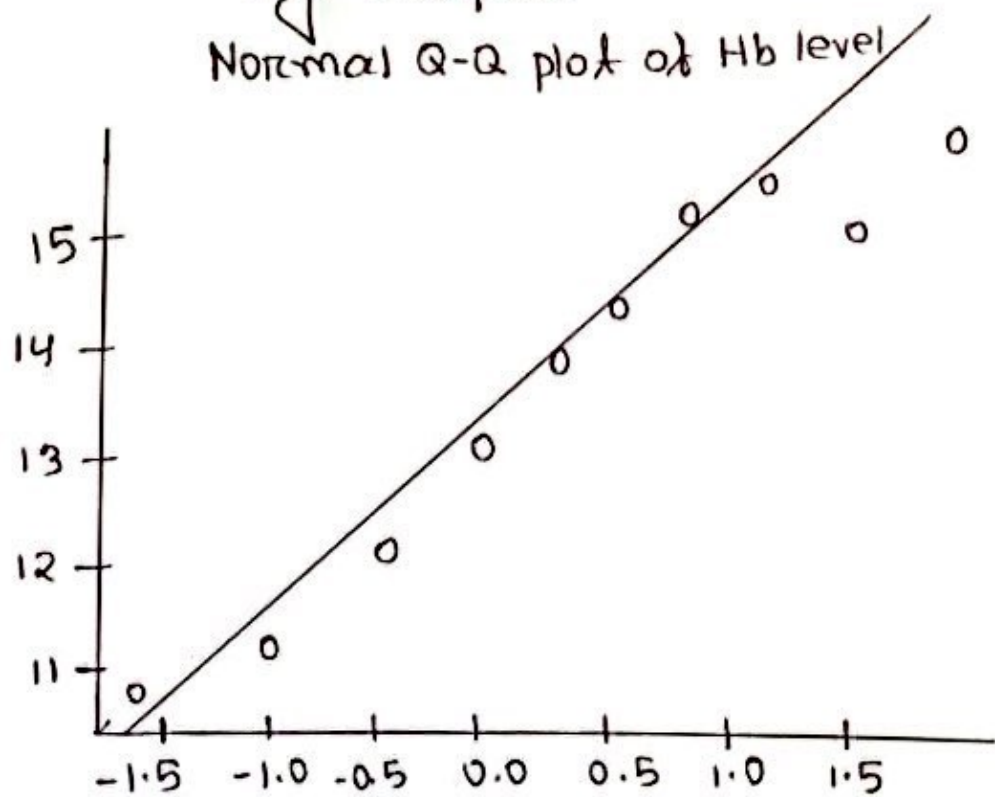


Fig: Normal plot

Comment: From the R code we can see that $t_{ab} > t_{cal}$ and also $pvalue > \alpha$ so H_0 is accepted. Then the mean Hb level for children with chronic diarrhea is more than the normal value of 14.6.

Experiment No: 05

Experiment Name: In order to find out whether children with chronic diarrhea have the same average hemoglobin level (Hb) that is normally seen in healthy children in the same area a random sample of 10 children with chronic diarrhea are selected and their Hb level (g/dl) are obtained as follows: 12.3, 11.4, 14.2, 15.3, 14.8, 13.8, 11.1, 15.1, 15.8, 13.2 another random sample of 12 children with chronic diarrhea are 11.1, 17.2, 13.4, 15.2, 14.1, 13.0, 12.5, 11.5, 12.7, 14.5, 15.3, 14.0. Is there any difference in the mean Hb level between the two groups of children

Objectives :

1. To calculate any difference in the mean Hb level between the two groups of children.
2. To comment on the data.

Procedure :

Step-1: State that the null hypothesis the mean Hb level between the two group of children is equal and the alternate hypothesis state that the mean Hb level between two group of children is not equal.

$$H_0: \mu_1 = \mu_2$$

$$H_A: \mu_1 \neq \mu_2$$

Step-2: Select the level of significance. The selected level of significance is 0.05.

step-3: select the test statistics.
The sample size is less than 30 and population standard deviation is unknown also the variance is not equal of the two groups of data. so we use t-test.

$$t = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{s^2 \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

$$\bar{x}_1 = \frac{1}{n_1} \sum x_{i1}$$

$$\bar{x}_2 = \frac{1}{n_2} \sum x_{i2}$$

$$s_1^2 = \frac{1}{n_1 - 1} \left[\sum x_{i1}^2 - \frac{(\sum x_{i1})^2}{n_1} \right]$$

$$s_2^2 = \frac{1}{n_2 - 1} \left[\sum x_{i2}^2 - \frac{(\sum x_{i2})^2}{n_2} \right]$$

$$s^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

Step-4: Formulate the decision rule.

The tabulated value of t is greater than the calculated value than the null hypothesis is accepted, otherwise rejected.

R-Source code :

```
x1<-c(12.3, 11.4, 14.2, 15.3, 14.8, 13.8, 11.1, 15.1, 15.8, 13.2)
```

```
x2<-c(11.1, 17.2, 13.4, 15.2, 14.1, 13.0, 12.5, 11.5, 12.7, 14.5, 15.3, 14.0)
```

```
s1<-sd(x1)
```

```
s2<-sd(x2)
```

```
s1/s2
```

```
n1<-length(x1)
```

```
n2<-length(x2)
```

```
x1.bar<-mean(x1)
```

```
x2.bar<-mean(x2)
```

```
x1.var<-var var(x1)
```

```
x1.var<-var(x2)
```

```
sp<-(((n1-1)*x1.var + (n2-1)*x2.var)/  
      (n1+n2-2))
```

```
t<-(x1.bar - x2.bar)/sqrt(sp*(1/n1 + 1/n2))
```


$$\alpha = 0.05$$

$$t_{\text{tab}} = qt(\alpha/2, n_1 + n_2 - 2)$$

Input and output:

$$S_1 = 1.65$$

$$S_2 = 1.72$$

$$S_1/S_2 = 0.96$$

$$n_1 = 10$$

$$n_2 = 12$$

$$\bar{x}_1 = 2.74 \quad 13.7$$

$$\bar{x}_2 = 2.96 \quad 13.708$$

$$s_1^2 = 2.74$$

$$s_2^2 = 2.96$$

$$SP = 2.86$$

$$t = -0.011$$

$$\alpha = 0.05$$

$$t_{\text{tab}} = -2.085$$

Comment: From the R code we can see that $t_{\text{tab}} > t_{\text{cal}}$. So H_0 is accepted. So we can say There is no difference in the mean Hb label between the two groups of children.