

Sol

$$P(X) = 0.45$$

$$P(Y|X) = 0.35$$

$$\bar{X} = 1 - 0.45$$

$$\bar{X} = 0.55$$

$$\bar{Y} = 1 - 0.35 = 0.65$$

$$Y = 1 - 0.75 = 0.25$$

$$\bar{Y} = 0.75$$

$$\begin{aligned} \text{(a)} \quad P(Y) &= P(X \cap Y) + P(\bar{X} \cap Y) \\ &= (0.35 \times 0.45) + (0.55 \times 0.25) \\ &= 0.295 \end{aligned}$$

$$\begin{aligned} \text{(b)} \quad P(X|Y) &= \frac{P(X \cap Y)}{P(Y)} \\ &= \frac{P(X) \cdot P(Y|X)}{P(Y)} \\ &= \frac{(0.45) \times (0.35)}{0.295} \end{aligned}$$

$$P(X|Y) = 0.534$$



$$c) \quad P(X|Y') = \frac{P(X \cap Y')}{P(Y')}$$

$$= \frac{(0.45)(0.65)}{(0.45)(0.65) + (0.55)(0.75)}$$

$$= \frac{0.2925}{0.705}$$

$$P(X|Y') = 0.415$$

$$1 - 0.415 = 0.585 \quad \text{Ans.}$$