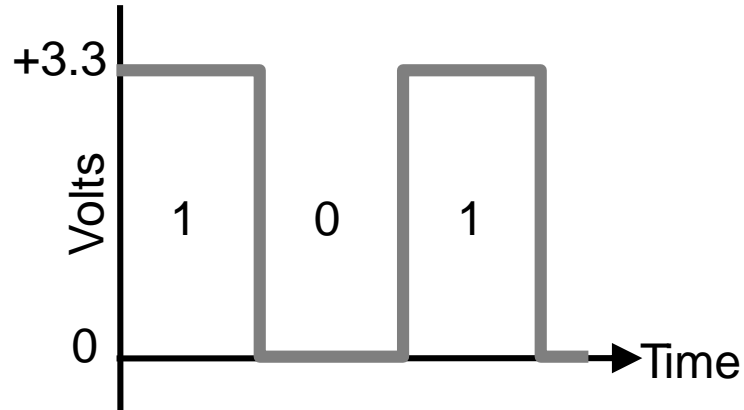


# Course Motivation

- ❖ Smaller, faster, cheaper hardware has enabled so many advances in electronics
  - Computers & phones
  - Vehicles (cars, planes)
  - Robots
  - Portable & household electronics
- ❖ An *introduction* to digital logic design
  - **Lecture:** How to think about hardware, basic higher-level circuit design techniques – preparation for EE/CSE469
  - **Lab:** Hands-on FPGA programming using Verilog – preparation for EE/CSE371

# Digital vs. Analog



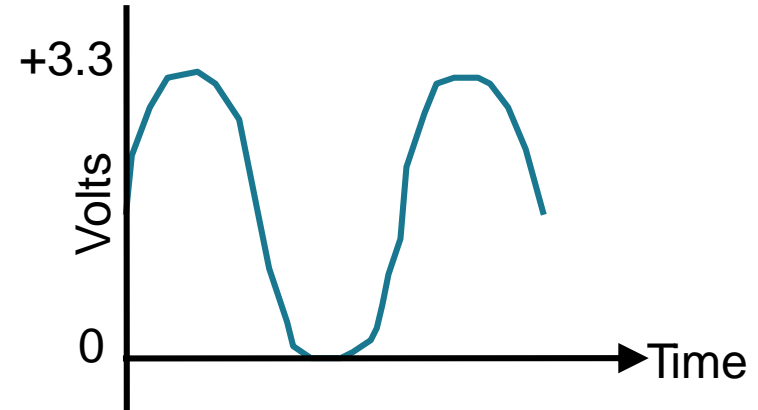
## Digital:

Discrete set of possible values

## Binary (2 values):

On, 3.3 V, high, TRUE, "1"

Off, 0 V, low, FALSE, "0"



## Analog:

Values vary over a continuous range

# Digital vs. Analog Systems

- ❖ Digital systems are more reliable and less error-prone
  - Slight errors can cascade in Analog system
  - Digital systems reject a significant amount of error; easy to cascade
- ❖ Computers use digital circuits internally
  - CPU, memory, I/O
- ❖ Interface circuits with “real world” often analog
  - Sensors & actuators

*This course is about logic design,  
not system design (processor architecture),  
and not circuit design (transistor level)*

# Digital Design: What's It All About?

- ❖ Create an implementation using a set of building blocks given a functional description and constraints
- ❖ Digital design is in some ways more art than a science
  - The creative spirit is in combining primitive elements and other components in new ways to achieve a desired function
- ❖ However, unlike art, we have objective measures of a design (*i.e.* constraints):
  - Performance
  - Power
  - Cost

# Digital Design: What's It All About?

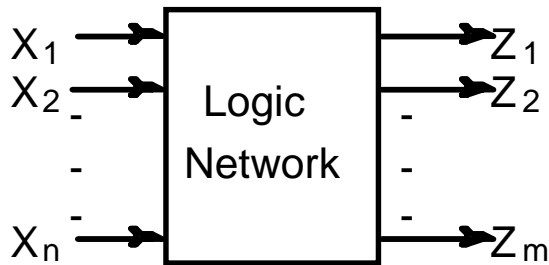
- ❖ How do we learn how to do this?
  - Learn about the building blocks and how to use them
  - Learn about design representations
  - Learn formal methods and tools to manipulate representations
  - Look at design examples
  - Use trial and error – CAD tools and prototyping (practice!)

# Lecture Outline

- ❖ Course Logistics
- ❖ Course Motivation
- ❖ **Combinational Logic Review**
- ❖ Combinational Logic in the Lab

# Combinational vs. Sequential Logic

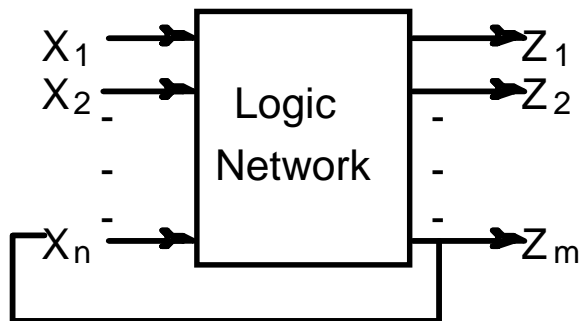
## ❖ Combinational Logic (CL)



Network of logic gates without feedback.

Outputs are functions only of inputs.

## ❖ Sequential Logic (SL)



The presence of feedback introduces the notion of “state.”

Circuits that can “remember” or store information.

# Representations of Combinational Logic

- ❖ Text Description
- ❖ Circuit Description
  - ~~Transistors~~ Not covered in 369
  - Logic Gates
- ❖ Truth Table
- ❖ Boolean Expression
- ❖ *All are equivalent!*



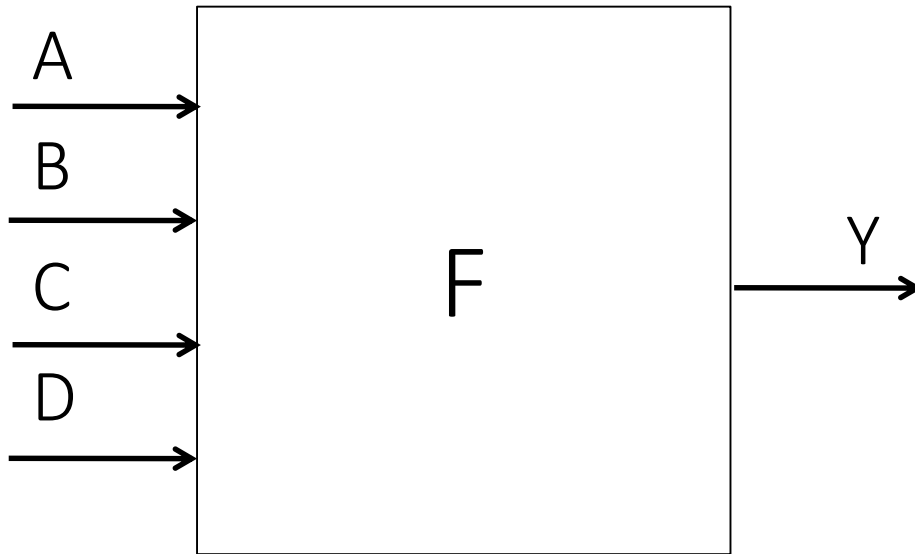
# Example: Simple Car Electronics

- ❖ Door Ajar (DriverDoorOpen, PassengerDoorOpen)
- ❖ High Beam Indicator (LightsOn, HighBeamOn)
- ❖ Seat Belt Light (DriverBeltIn, PassengerBeltIn, Passenger)

# Truth Tables

- ❖ Table that relates the inputs to a combinational logic (CL) circuit to its output
  - Output *only* depends on current inputs
  - Use abstraction of 0/1 instead of high/low voltage
  - Shows output for *every* possible combination of inputs (“black box” approach)
- ❖ How big is the table?
  - 0 or 1 for each of  $N$  inputs
  - Each output is a separate function of inputs, so don't need to add rows for additional outputs

# CL General Form



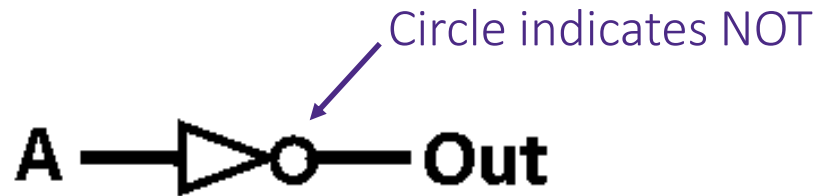
If  $N$  inputs, how many distinct functions  $F$  do we have?

a	b	c	d	y
0	0	0	0	$F(0,0,0,0)$
0	0	0	1	$F(0,0,0,1)$
0	0	1	0	$F(0,0,1,0)$
0	0	1	1	$F(0,0,1,1)$
0	1	0	0	$F(0,1,0,0)$
0	1	0	1	$F(0,1,0,1)$
0	1	1	0	$F(0,1,1,0)$
1	1	1	1	$F(0,1,1,1)$
1	0	0	0	$F(1,0,0,0)$
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1	0	1	0	$F(1,0,1,0)$
1	0	1	1	$F(1,0,1,1)$
1	1	0	0	$F(1,1,0,0)$
1	1	0	1	$F(1,1,0,1)$
1	1	1	0	$F(1,1,1,0)$
1	1	1	1	$F(1,1,1,1)$

# Logic Gates (1/2)

- ❖ Special names and symbols:

NOT



A	Out
0	1
1	0

AND



A	B	Out
0	0	0
0	1	0
1	0	0
1	1	1

OR



A	B	Out
0	0	0
0	1	1
1	0	1
1	1	1

# Logic Gates (2/2)

❖ Special names and symbols:

NAND



A	B	Out
0	0	1
0	1	1
1	0	1
1	1	0

NOR



A	B	Out
0	0	1
0	1	0
1	0	0
1	1	0

XOR



A	B	Out
0	0	0
0	1	1
1	0	1
1	1	0

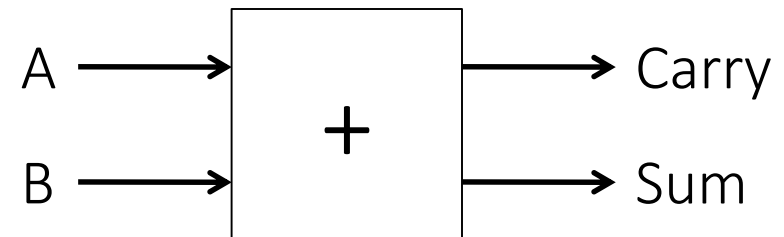
# More Complicated Truth Tables

## 3-Input Majority

How many rows?

A	B	C	Out
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

## 1-bit Adder



A	B	Carry	Sum
0	0		
0	1		
1	0		
1	1		

# Boolean Algebra

- ❖ Represent inputs and outputs as variables
  - Each variable can only take on the value 0 or 1
- ❖ Overbar is NOT: “logical complement”
  - If  $A$  is 0, then  $\bar{A}$  is 1 and vice-versa
- ❖ Plus (+) is 2-input OR: “logical sum”
- ❖ Product ( $\cdot$ ) is 2-input AND: “logical product”
- ❖ All other gates and logical expressions can be built from combinations of these
  - e.g.  $A \text{ XOR } B = A \oplus B = \bar{A}B + \bar{B}A$