



# Lecture # 17

## State Space Explosion

# STATE SPACE EXPLOSION

```
MODULE main  
VAR  
    x:  boolean;
```

Transition system of above NuSMV program has 2 states

$x=\text{FALSE}$     and     $x=\text{TRUE}$

# STATE SPACE EXPLOSION

```
MODULE main
VAR
    x:  boolean;
    y:  boolean;
```

Transition system of above NuSMV program has 4 states

x=FALSE  
y=FALSE

x=FALSE  
y=TRUE

x=TRUE  
y=FALSE

x=TRUE  
y=TRUE

# STATE SPACE EXPLOSION

```
MODULE main
VAR
    x:  boolean;
    y:  boolean;
    input:  sys();

MODULE sys()
VAR
    state:  { s1, s2, s3, s4, s5 };

```

Transition system of above NuSMV program has  $2 * 2 * 5$  states

# STATE SPACE EXPLOSION

If NuSMV program has 10 boolean variables, transition system will have  $2^{10}$  states!

If NuSMV program has 10 module variables, each of which has 10 states, the transition system will have  $10^{10}$  states!

# Tackling state space explosion

- ▶ **Efficient data structures:** Binary Decision Diagrams
- ▶ **Abstraction:** Interpret model with fewer variables relevant to property
- ▶ **Partial order reduction:** for asynchronous systems, combining several interleavings
- ▶ **Composition:** Break verification into simpler verification problem
- ▶ **Bounded model-checking:** Unroll transition system upto a fixed length of paths