Sol. of Prob-S-II Spring 2022 Sol 1 (a) Let D = Detection E = Axxive via Email We want P(D). 1 = Arrive via Internet By Law of Total Probability P(D)= P(DIE)P(E) + P(DII)P(I) Substituting P(I)=70/100, P(E)=30/100? P(DII)=0.6 & P(DIE)=0.8 we get $P(D) = (0.8) \left(\frac{30}{100} \right) + (0.6) \left(\frac{70}{100} \right)$ =) P(D)=0.86 So 66% of times the spyware is detected. (b) P(AUBUC) = P(AU(BUC)) = P(A) + P(BUC) - P(An(BUC)) = P(A) + P(B) + P(C) - P(BC)- P (ABUAC) = P(A) + P(B) + P(C) - P(BC)- [P(AB)+P(AC) - P(ABAC)] P(AUBUC)= P(A)+P(B)+P(C)-P(AB)-P(BC)
-P(AC)+ P(AR-1) -P(AC) + P(ABC)

$$\int_{X}^{\infty} (x) = \int_{Y}^{\infty} f(x,y) dy$$

$$\Rightarrow \int_{X}^{\infty} (x) = \int_{Y}^{\infty} e^{y(1+x)} dy$$

$$= \int_{-(1+x)}^{2} e^{y(1+x)} dy$$

$$= -\frac{1}{1+x} \left(\frac{y}{e^{y(2+x)}} \right)^{\infty} + \frac{1}{1+x} \frac{e}{-(1+x)} dy$$

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$$= -\frac{1}{(1+x)^{2}} \left(\frac{y}{(1+x)^{2}} \right)^{\infty} + \frac{1}{1+x} \frac{e}{-(1+x)} dy$$

$$= -\frac{1}{(1+x)^{2}} \left(\frac{y}{(1+x)^{2}} \right)^{\infty} + \frac{1}{(1+x)^{2}} \left(\frac{y}{e^{y(1+x)}} \right)^{\infty} dx$$

$$= \int_{-1}^{2} \frac{1}{(1+x)^{2}} dx = \int_{-1}^{2} \frac{1}{(1+x)^{2}} dx = \int_{-1}^{2} \frac{1}{(1+x)^{2}} dx$$

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$$= \int_{-1}^{2} \frac{1}{(1+x)^{2}} dx = \int_{-1$$

$$P\{X > 2, Y > 2\}$$

$$= \int \int y e^{-y(1+x)} dx dy$$

$$= \int \int y e^{-y(1+x)} dy = -\int e^{-y(1+x)} dy$$

$$= -\int (0 - e^{-3y}) dy = \int e^{-3y} dy = -\frac{3y}{2}$$

$$= -\frac{1}{3} (\frac{1}{e^{3y}}) = -\frac{1}{3} (0 - \frac{1}{6}) = \frac{1}{3}e^{6}$$

$$=) P\{X72,Y72\} = \frac{1}{3e^{6}} \approx 0.000826$$

$$D_P = D_e + e_c + e_d$$
 Present $= D_P = N_o + e_d$ Present $= P_R = P_e = N_o + e_d$ In Lange

Given that

$$P(D_{P}|P_{R}^{c}) = \frac{5}{100} \Rightarrow P(D_{P}|P_{R}^{c}) = \frac{95}{100}$$

$$P(R) = \frac{7}{100} \Rightarrow P(R) = 1 - \frac{7}{100} = \frac{93}{100}$$

By Bayes Rule

$$P(Dp|P_R)P(P_R) + P(Dp|P_R)P(P_R)$$

$$= \frac{5}{100} \cdot \frac{93}{100} = \frac{5 \times 93}{98x7 + 5x93}$$

$$\frac{98}{100} + \frac{5}{100} \cdot \frac{93}{100}$$

(a)
$$p(x) = \begin{cases} \frac{1}{2} & \text{if } x = 1 \\ \frac{1}{3} & \text{if } x = 2 \\ \frac{1}{6} & \text{if } x = 3 \end{cases}$$

(b)
$$P \{x < 4\} = \int_{2}^{4} \frac{2(1+x)}{2+x} dx$$

 $= \frac{2}{2+} \int_{2}^{4} (1+x) dx = \frac{2}{2+} \left[x + \frac{x^{2}}{2}\right]_{2}^{4}$
 $= \frac{2}{2+} \left[4 + 4^{2} - (2+2)\right]$
 $= \frac{2}{2+} \left[4 + 8 - (2+2)\right]$

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