

Lecture 1:-

"Theory of Automata"

less practical &
More Mathematical

Automation,
→ Self acting.

→ theoretical aspects of CS.

Book: "Introduction to Computer theory". 1991.

Daniel I. Cohen.

Applications:-
- Compiler Construction.
- Parsing
- Formal Verification.
- Defining Computer languages.

Languages → formal:- C++, C, Java, ---
Rules → language.
→ Informal:- Human
first language → Rules.

Language Basic Elements:-
Alphabets:- A finite non empty set of Symbols (letters).
called alphabets.

Eg:- $\Sigma = \{1, 2, 3\}$.
 $\Sigma = \{0, 1\}$. Binary.
 $\Sigma = \{a, b, c, \dots, z\}$.

Strings:- A combination of alphabets.

Example $\Sigma = \{0, 1\}$. 0, 1, 00, 01, 10, 11, ---
 $\Sigma = \{a, b\}$. a, b, aa, bb, ab, ba, ---

Null String:- A string with no symbol. "λ" "Λ"

Words:- words are string that belongs to a language.

Ex:- $\Sigma = \{a\}$ a, aa, aaa,
ab
λ. String but not a word in Σ .

$\tau_n \rightarrow 0$ as $n \rightarrow \infty$, $\tau_n = 1/n$

Rules for alphabets:-

- 1- $\neg (A)$
- 2- Should be finite.
- 3- Should not be ambiguous.

Ex:- $\Sigma = \{ \underline{A}, Aa, bab, d \}$.

AababA. \rightarrow is it a word?

$(\overset{\checkmark}{A}a), (C\overset{\checkmark}{b}ab) (C\overset{\checkmark}{A}) \rightarrow x.$
 $(\overset{\checkmark}{A}), (abab) (C\overset{\checkmark}{A}) \rightarrow ?$

→ A symbol should not start with a letter already being used by some other letter.

Example:- $\Sigma_1 = \{A, aA, bab, d\}$. ✓

$$\Sigma_2 = \{A, Aa, bab, d\}^*$$
$$\Sigma_1 = \{ \underline{a}, ab, ac \} \times$$
$$\Sigma_2 = \{a, ba, ca\} \checkmark$$

Length of String :- Number of letters or Symbols in a String. $|S|$.
 $\Sigma = \{a, b\}$.

S_2 a a a b b .

$$(S) \approx S$$

Example: $\Sigma = \{A, aA, baA, d\}$.

S_2 AaAbabAd.

Factoring: $151 \approx 5$ 8

Length of a String over n alphabets.

Formula:- Number of strings of length 'n' defined over alphabets 'u' is $|u|^n$.

defined over alphabets 'u' is $\boxed{u^m}$.

Ex:- $\Sigma = \{a, b\}$.

length 2 strings:- aa, ab, ba, bb.
3 4 :- aaa, aab, aba, abb,
baa, bab, bba, bbb.

Reverse:- s reverse(s) s^r
 $s = aba$ reverse(s) = aba .

Ex:- $\Sigma = \{A, a, b, d\}$.
 $s = \underline{AaA} \underline{bab} \underline{Ad}$.

$s^r = \underline{dA} \underline{bab} \underline{aAA}$