

Lab 1

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11:59PM February 18, 2021

You should have RStudio installed to edit this file. You will write code in places marked “TO-DO” to complete the problems. Most of this will be a pure programming assignment but there are some questions that instead ask you to “write a few sentences”. This is a W class! The tools for the solutions to these problems can be found in the class practice lectures. I prefer you to use the methods I taught you. If you google and find esoteric code you don’t understand, this doesn’t do you too much good.

To “hand in” the homework, you should first download this file. The best way to do this is by cloning the class repository then copying this file from the folder of that clone into the folder that is your personal class repository. Then do the assignment by filling in the TO-DO’s. After you’re done, compile this file into a PDF (use the “knit to PDF” button on the submenu above). This PDF will include output of your code. Then push the PDF and this Rmd file by the deadline to your github repository in a directory called “labs”.

Basic R Skills

- Print out the numerical constant pi with ten digits after the decimal point using the internal constant pi.

```
options(digits=11)
x <- pi
x
```

```
## [1] 3.1415926536
```

- Sum up the first 103 terms of the series $1 + 1/2 + 1/4 + 1/8 + \dots$

```
sum(1/(2^(0:102)))
```

```
## [1] 2
```

- Find the product of the first 37 terms in the sequence $1/3, 1/6, 1/9 \dots$

```
prod(1/(3*(1:37)))
```

```
## [1] 1.613528728e-61
```

```
prod(1/seq(from=3, by=3, length.out=37))
```

```
## [1] 1.613528728e-61
```

- Find the product of the first 387 terms of $1 * 1/2 * 1/4 * 1/8 * \dots$

```
prod(1/(2^(0:386)))
```

```
## [1] 0
```

Is this answer *exactly* correct?

#TO-DO

- Figure out a means to express the answer more exactly. Not compute exactly, but express more exactly.

```
sum(log(1/(2^(0:386))))
```

```
## [1] -51771.856063
```

```
-log(2)*sum(0:386)
```

```
## [1] -51771.856063
```

- Create the sequence $x = [\text{Inf}, 20, 18, \dots, -20]$.

```
x <- c(Inf, seq(from=20, to=-20, by=-2))
x
```

```
## [1] Inf 20 18 16 14 12 10 8 6 4 2 0 -2 -4 -6 -8 -10 -12 -14
```

```
## [20] -16 -18 -20
```

Create the sequence $x = [\log_3(\text{Inf}), \log_3(100), \log_3(98), \dots, \log_3(-20)]$.

```
x <- c(Inf, seq(from=100, to=-20, by=-2))
x <- log(x, base=3)
```

```
## Warning: NaNs produced
```

```
log(100, 3)
```

```
## [1] 4.1918065486
```

Comment on the appropriateness of the non-numeric values.

NAN occurs because you cannot take the log of a negative number. -Inf occurs when you take the log of 0.

- Create a vector of booleans where the entry is true if $x[i]$ is positive and finite.

```
y = !is.nan(x) & is.finite(x) & x > 0
y
```

```
## [1] FALSE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
```

```
## [13] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
```

```
## [25] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
```

```
## [37] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
```

```
## [49] TRUE TRUE TRUE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
```

```
## [61] FALSE FALSE
```

- Locate the indices of the non-real numbers in this vector. Hint: use the `which` function. Don't hesitate to use the documentation via `?which`.

```
?which
which(!y)
```

```
## [1] 1 52 53 54 55 56 57 58 59 60 61 62
```

```
which(y == FALSE)
```

```
## [1] 1 52 53 54 55 56 57 58 59 60 61 62
```

- Locate the indices of the infinite quantities in this vector.

```
which(is.infinite(x))
```

```
## [1] 1 52
```

- Locate the indices of the min and max in this vector. Hint: use the `which.min` and `which.max` functions.

```
which.min(x)
```

```
## [1] 52
```

```
which.max(x)
```

```
## [1] 1
```

- Count the number of unique values in `x`.

```
length(unique(x))
```

```
## [1] 53
```

- Cast `x` to a factor. Do the number of levels make sense?

```
as.factor(x)
```

```
## [1] Inf 4.19180654857877 4.1734172518943 4.15464876785729
## [5] 4.13548512895119 4.11590933734319 4.09590327428938 4.07544759935851
## [9] 4.05452163806914 4.03310325630434 4.01116871959141 3.98869253500376
## [13] 3.96564727304425 3.94200336638929 3.91772888178973 3.89278926071437
## [17] 3.86714702345081 3.84076143030548 3.81358809221559 3.78557852142874
## [21] 3.75667961082847 3.72683302786084 3.69597450568212 3.66403300987579
## [25] 3.63092975357146 3.59657702661571 3.56087679500731 3.52371901428583
## [29] 3.48497958377173 3.44451784578705 3.40217350273288 3.3577627814323
## [33] 3.31107361281783 3.26185950714291 3.20983167673402 3.15464876785729
## [37] 3.09590327428938 3.03310325630434 2.96564727304425 2.89278926071437
## [41] 2.8135880922156 2.72683302786084 2.63092975357146 2.52371901428583
## [45] 2.40217350273288 2.26185950714291 2.09590327428938 1.89278926071437
## [49] 1.63092975357146 1.26185950714291 0.630929753571457 -Inf
## [53] NaN NaN NaN NaN
## [57] NaN NaN NaN NaN
## [61] NaN NaN
## 53 Levels: -Inf 0.630929753571457 1.26185950714291 ... NaN
```

- Cast `x` to integers. What do we learn about R's infinity representation in the integer data type?

```
as.integer(x)
```

```
## Warning: NAs introduced by coercion to integer range
```

```
## [1] NA 4 4 4 4 4 4 4 4 4 4 3 3 3 3 3 3 3 3 3 3 3
## [26] 3 3 3 3 3 3 3 3 3 3 3 3 3 2 2 2 2 2 2 2 2 1 1 1
## [51] 0 NA NA NA NA NA NA NA NA NA NA NA NA
```

- Use `x` to create a new vector `y` containing only the real numbers in `x`.

```
y = x[!is.nan(x) & is.finite(x)]
```

```
y
```

```
## [1] 4.19180654858 4.17341725189 4.15464876786 4.13548512895 4.11590933734
## [6] 4.09590327429 4.07544759936 4.05452163807 4.03310325630 4.01116871959
## [11] 3.98869253500 3.96564727304 3.94200336639 3.91772888179 3.89278926071
## [16] 3.86714702345 3.84076143031 3.81358809222 3.78557852143 3.75667961083
## [21] 3.72683302786 3.69597450568 3.66403300988 3.63092975357 3.59657702662
## [26] 3.56087679501 3.52371901429 3.48497958377 3.44451784579 3.40217350273
## [31] 3.35776278143 3.31107361282 3.26185950714 3.20983167673 3.15464876786
## [36] 3.09590327429 3.03310325630 2.96564727304 2.89278926071 2.81358809222
## [41] 2.72683302786 2.63092975357 2.52371901429 2.40217350273 2.26185950714
```

- Use the left rectangle method to numerically integrate x^2 from 0 to 1 with rectangle width size $1e-6$.

```
sum(seq(from=0, to=1-(1e-6), by=1e-6)^2)*1e-6
```

- Calculate the average of 100 realizations of standard Bernoullis in one line using the `sample` function.

```
sum(sample(c(0,1), size=100, replace=TRUE))/100
```

- Calculate the average of 500 realizations of Bernoullis with $p = 0.9$ in one line using the `sample` and `mean` functions.

```
sum(sample(c(0,1), size=500, replace=TRUE, prob=c(0.1, 0.9)))/500
```

- Calculate the average of 1000 realizations of Bernoullis with $p = 0.9$ in one line using `rbinom`.

```
?rbinom
rbinom(n=1000, size=1, p=0.9)
```

- In class we considered a variable `x_3` which measured “criminality”. We imagined $L = 4$ levels “none”, “infraction”, “misdemeanor” and “felony”. Create a variable `x_3` here with 100 random elements (equally probable). Create it as a nominal (i.e. unordered) factor.

```
x_3 = as.factor(sample(c("none", "infraction", "misdemeanor", "felony"), size=100, replace=TRUE))
x_3
```

```
## [1] none      felony    none      felony    misdemeanor misdemeanor
## [7] infraction misdemeanor felony    none      none      felony
## [13] misdemeanor infraction felony    none      misdemeanor infraction
## [19] none      misdemeanor infraction none      none      misdemeanor
## [25] none      infraction none      felony    infraction felony
## [31] infraction felony    infraction misdemeanor infraction misdemeanor
## [37] misdemeanor infraction misdemeanor misdemeanor infraction none
## [43] none      none      misdemeanor felony    felony    misdemeanor
## [49] felony    felony    none      misdemeanor misdemeanor felony
## [55] felony    none      none      felony    none      none
## [61] misdemeanor infraction none      misdemeanor misdemeanor none
## [67] none      felony    felony    felony    infraction misdemeanor
## [73] infraction none      misdemeanor felony    misdemeanor felony
## [79] infraction felony    felony    misdemeanor misdemeanor none
## [85] none      felony    felony    felony    none      misdemeanor
## [91] felony    felony    infraction felony    none      misdemeanor
## [97] none      felony    misdemeanor infraction
## Levels: felony infraction misdemeanor none
```

- Use `x_3` to create `x_3_bin`, a binary feature where 0 is no crime and 1 is any crime.

```
x_3_bin = x_3 != "none"
x_3_bin
```

```
## [1] FALSE TRUE FALSE TRUE TRUE TRUE TRUE TRUE TRUE FALSE FALSE TRUE
## [13] TRUE TRUE TRUE FALSE TRUE TRUE FALSE TRUE TRUE FALSE FALSE TRUE
## [25] FALSE TRUE FALSE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
## [37] TRUE TRUE TRUE TRUE TRUE FALSE FALSE FALSE TRUE TRUE TRUE TRUE
## [49] TRUE TRUE FALSE TRUE TRUE TRUE TRUE FALSE FALSE TRUE FALSE FALSE
## [61] TRUE TRUE FALSE TRUE TRUE FALSE FALSE TRUE TRUE TRUE TRUE TRUE
## [73] TRUE FALSE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE FALSE
## [85] FALSE TRUE TRUE TRUE FALSE TRUE TRUE TRUE TRUE TRUE TRUE FALSE TRUE
## [97] FALSE TRUE TRUE TRUE
```

- Use `x_3` to create `x_3_ord`, an ordered factor variable. Ensure the proper ordinal ordering.

```
x_3_ord = factor(x_3, levels = c("none", "infraction", "misdemeanor", "felony"), order=TRUE)
x_3_ord
```

```
## [1] none      felony    none      felony    misdemeanor misdemeanor
## [7] infraction misdemeanor felony    none      none      felony
## [13] misdemeanor infraction felony    none      misdemeanor infraction
## [19] none      misdemeanor infraction none      none      misdemeanor
## [25] none      infraction none      felony    infraction felony
## [31] infraction felony    infraction misdemeanor infraction misdemeanor
## [37] misdemeanor infraction misdemeanor misdemeanor infraction none
## [43] none      none      misdemeanor felony    felony    misdemeanor
## [49] felony    felony    none      misdemeanor misdemeanor felony
## [55] felony    none      none      felony    none      none
## [61] misdemeanor infraction none      misdemeanor misdemeanor none
## [67] none      felony    felony    felony    infraction misdemeanor
## [73] infraction none      misdemeanor felony    misdemeanor felony
## [79] infraction felony    felony    misdemeanor misdemeanor none
```

```
## [85] none      felony      felony      felony      none      misdemeanor
## [91] felony     felony      infraction  felony      none      misdemeanor
## [97] none      felony      misdemeanor infraction
## Levels: none < infraction < misdemeanor < felony
```

- Convert this variable into three binary variables without any information loss and put them into a data matrix.

```
x_3_infraction = as.integer(x_3 == "infraction")
x_3_misdemeanor = as.integer(x_3 == "misdemeanor")
x_3_felony = as.integer(x_3 == "felony")
X = cbind(x_3_infraction, x_3_misdemeanor, x_3_felony)
head(X)
```

```
##      x_3_infraction x_3_misdemeanor x_3_felony
## [1,]              0                0          0
## [2,]              0                0          1
## [3,]              0                0          0
## [4,]              0                0          1
## [5,]              0                1          0
## [6,]              0                1          0
```

```
p_level_names = levels(x_3)[-1]
X = matrix(NA, nrow = length(x_3), ncol = length(p_level_names))
colnames(X) = p_level_names
for (j in 1 : length(p_level_names)){
  X[, j] = as.integer(x_3 == p_level_names[j])
}
head(X)
```

```
##      infraction misdemeanor none
## [1,]          0           0    1
## [2,]          0           0    0
## [3,]          0           0    1
## [4,]          0           0    0
## [5,]          0           1    0
## [6,]          0           1    0
```

- What should the sum of each row be (in English)?

#TO-DO

Verify that.

```
rowSums(X)
```

```
## [1] 1 0 1 0 1 1 1 1 0 1 1 0 1 1 0 1 1 1 1 1 1 1 0 1 0 1 0 1 1 1 1
## [38] 1 1 1 1 1 1 1 1 0 0 1 0 0 1 1 1 0 0 1 1 0 1 1 1 1 1 1 1 1 0 0 0 1 1 1 1
## [75] 1 0 1 0 1 0 0 1 1 1 1 0 0 0 1 1 0 0 1 0 1 1 1 0 1 1
```

- How should the column sum look (in English)?

#TO-DO

Verify that.

```
colSums(X)
```

```
##      infraction misdemeanor      none
##          17          27          27
```

- Generate a matrix with 100 rows where the first column is realization from a normal with mean 17 and variance 38, the second column is uniform between -10 and 10, the third column is poisson with mean 6, the fourth column in exponential with lambda of 9, the fifth column is binomial with $n = 20$ and $p = 0.12$ and the sixth column is a binary variable with exactly 24% 1's dispersed randomly. Name the rows the entries of the `fake_first_names` vector.

```
fake_first_names = c(
  "Sophia", "Emma", "Olivia", "Ava", "Mia", "Isabella", "Riley",
  "Aria", "Zoe", "Charlotte", "Lily", "Layla", "Amelia", "Emily",
  "Madelyn", "Aubrey", "Adalyn", "Madison", "Chloe", "Harper",
  "Abigail", "Aaliyah", "Avery", "Evelyn", "Kaylee", "Ella", "Ellie",
  "Scarlett", "Arianna", "Hailey", "Nora", "Addison", "Brooklyn",
  "Hannah", "Mila", "Leah", "Elizabeth", "Sarah", "Eliana", "Mackenzie",
  "Peyton", "Maria", "Grace", "Adeline", "Elena", "Anna", "Victoria",
  "Camilla", "Lillian", "Natalie", "Jackson", "Aiden", "Lucas",
  "Liam", "Noah", "Ethan", "Mason", "Caden", "Oliver", "Elijah",
  "Grayson", "Jacob", "Michael", "Benjamin", "Carter", "James",
  "Jayden", "Logan", "Alexander", "Caleb", "Ryan", "Luke", "Daniel",
  "Jack", "William", "Owen", "Gabriel", "Matthew", "Connor", "Jayce",
  "Isaac", "Sebastian", "Henry", "Muhammad", "Cameron", "Wyatt",
  "Dylan", "Nathan", "Nicholas", "Julian", "Eli", "Levi", "Isaiah",
  "Landon", "David", "Christian", "Andrew", "Brayden", "John",
  "Lincoln"
)
rownames(X)= fake_first_names
X
```

```
##          infraction misdimeanor none
## Sophia           0           0    1
## Emma             0           0    0
## Olivia           0           0    1
## Ava              0           0    0
## Mia              0           1    0
## Isabella          0           1    0
## Riley            1           0    0
## Aria             0           1    0
## Zoe              0           0    0
## Charlotte        0           0    1
## Lily             0           0    1
## Layla            0           0    0
## Amelia           0           1    0
## Emily            1           0    0
## Madelyn          0           0    0
## Aubrey           0           0    1
## Adalyn           0           1    0
## Madison          1           0    0
## Chloe            0           0    1
## Harper           0           1    0
## Abigail          1           0    0
## Aaliyah          0           0    1
## Avery            0           0    1
## Evelyn           0           1    0
## Kaylee           0           0    1
## Ella             1           0    0
## Ellie            0           0    1
```

## Scarlett	0	0	0
## Arianna	1	0	0
## Hailey	0	0	0
## Nora	1	0	0
## Addison	0	0	0
## Brooklyn	1	0	0
## Hannah	0	1	0
## Mila	1	0	0
## Leah	0	1	0
## Elizabeth	0	1	0
## Sarah	1	0	0
## Eliana	0	1	0
## Mackenzie	0	1	0
## Peyton	1	0	0
## Maria	0	0	1
## Grace	0	0	1
## Adeline	0	0	1
## Elena	0	1	0
## Anna	0	0	0
## Victoria	0	0	0
## Camilla	0	1	0
## Lillian	0	0	0
## Natalie	0	0	0
## Jackson	0	0	1
## Aiden	0	1	0
## Lucas	0	1	0
## Liam	0	0	0
## Noah	0	0	0
## Ethan	0	0	1
## Mason	0	0	1
## Caden	0	0	0
## Oliver	0	0	1
## Elijah	0	0	1
## Grayson	0	1	0
## Jacob	1	0	0
## Michael	0	0	1
## Benjamin	0	1	0
## Carter	0	1	0
## James	0	0	1
## Jayden	0	0	1
## Logan	0	0	0
## Alexander	0	0	0
## Caleb	0	0	0
## Ryan	1	0	0
## Luke	0	1	0
## Daniel	1	0	0
## Jack	0	0	1
## William	0	1	0
## Owen	0	0	0
## Gabriel	0	1	0
## Matthew	0	0	0
## Connor	1	0	0
## Jayce	0	0	0
## Isaac	0	0	0

## Sebastian	0	1	0
## Henry	0	1	0
## Muhammad	0	0	1
## Cameron	0	0	1
## Wyatt	0	0	0
## Dylan	0	0	0
## Nathan	0	0	0
## Nicholas	0	0	1
## Julian	0	1	0
## Eli	0	0	0
## Levi	0	0	0
## Isaiah	1	0	0
## Landon	0	0	0
## David	0	0	1
## Christian	0	1	0
## Andrew	0	0	1
## Brayden	0	0	0
## John	0	1	0
## Lincoln	1	0	0

- Create a data frame of the same data as above except make the binary variable a factor “DOMESTIC” vs “FOREIGN” for 0 and 1 respectively. Use RStudio’s **View** function to ensure this worked as desired.

```
#levels = c(0,1)
#fact = c('DOMESTIC', 'FOREIGN')
#s_frame = data.frame(fake_first_names, fact, levels)
#View(name_frame)
```

- Print out a table of the binary variable. Then print out the proportions of “DOMESTIC” vs “FOREIGN”.

```
#print.table(s_frame)
```

Print out a summary of the whole dataframe.

```
#summary(s_frame)
```

- Let $n = 50$. Create a $n \times n$ matrix **R** of exactly 50% entries 0’s, 25% 1’s 25% 2’s. These values should be in random locations.

```
#R = data.matrix(sample(c(rep(0, n^2*.5), rep(1, n^2*.25), rep(2, n^2*.25))), nrow=50, ncol=50)
```

- Randomly punch holes (i.e. NA) values in this matrix so that an each entry is missing with probability 30%.

```
n = 100
X = matrix(rnorm(n^2), nrow = n, ncol = n)
for (i in 1 : n){
  for (j in 1 : n){
    if (runif(1) < 0.3){
      X[i,j] = NA
    }
  }
}
```

- Sort the rows in matrix **R** by the largest row sum to lowest. Be careful about the NA’s!

```
#TO DO
```

- We will now learn the **apply** function. This is a handy function that saves writing for loops which

should be eschewed in R. Use the `apply` function to compute a vector whose entries are the standard deviation of each row. Use the `apply` function to compute a vector whose entries are the standard deviation of each column. Be careful about the NA's! This should be one line.

```
#apply(B, nrow=B, sd, na.rm = TRUE)
#apply(B, ncol=B, sd, na.rm = TRUE)
```

- Use the `apply` function to compute a vector whose entries are the count of entries that are 1 or 2 in each column. This should be one line.

```
#apply(B>0, MARGIN=2, na.rm=TRUE, sum)
```

- Use the `split` function to create a list whose keys are the column number and values are the vector of the columns. Look at the last example in the documentation `?split`.

```
#split(B, col(B))
#?split
```

- In one statement, use the `lapply` function to create a list whose keys are the column number and values are themselves a list with keys: “min” whose value is the minimum of the column, “max” whose value is the maximum of the column, “pct_missing” is the proportion of missingness in the column and “first_NA” whose value is the row number of the first time the NA appears.

```
#TO DO
```

- Set a seed and then create a vector `v` consisting of a sample of 1,000 iid normal realizations with mean -10 and variance 100.

```
set.seed(3)
i = rnorm(n = 1000, mean=-10, sd=10)
```

- Repeat this exercise by resetting the seed to ensure you obtain the same results.

```
num=(1:10)
for(number in num)
  set.seed(n)
  i = rnorm(n=1000, mean=-10, sd=10)
  print(i)
```

```
##      [1] -15.021923505315  -8.684688346727 -10.789170898189  -1.132151905822
##      [5]  -8.830287294892  -6.813699123830 -15.817906847159  -2.854672891084
##      [9] -18.252594258628 -13.598621313955  -9.101138562225  -9.037255397149
##     [13] -12.016339521834  -2.601595001216  -8.766204989111 -10.293167092293
##     [17] -13.888542469035  -4.891437426301 -19.138141853692  13.102968227791
##     [21] -14.380899811273  -2.359393835896  -7.380387086071  -2.265954032216
##     [25] -18.143791248755 -14.384505690746 -17.202215502161  -7.690554677474
##     [29] -21.577294623998  -7.529240072712 -10.911135614728   7.573756220280
##     [33] -11.379296117311 -11.111934952824 -16.900143205694 -12.217942300197
##     [37]  -8.170923164053  -5.826767137733   0.654023270455  -0.297979826595
##     [41] -11.016292384616   4.032034885582 -27.767756322946  -3.771326090090
##     [45] -15.222833512770   3.222309556847 -13.634403268447   3.190657425688
##     [49]  -9.562209323557 -28.786558820062 -14.470621820196 -27.385979472079
##     [53]  -8.211351513728   8.974657001462 -32.719254860193  -0.195358612654
##     [57] -23.988256162924   8.248724229436   3.812987299288 -18.388518750344
##     [61] -12.619957745140 -10.688440280170 -13.788835565301  15.819589277243
##     [65]  -8.701658626544 -17.130249802164  -3.620057570805  -7.983084083841
##     [69] -10.699169482402 -10.924898754027  -5.510967268886 -20.643556706874
##     [73] -21.624193221422   6.485217467045 -30.620960193399  -9.872502790350
##     [77] -20.875283493104  -7.294605067957   0.084518732727 -30.744047542564
```

```

## [81] -1.031777282144 -10.499957668760 -23.453493104434 -29.312115343497
## [85] -2.904184165229 -11.579050319163 -7.836321272915 -1.826379242247
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##	[885]	-28.294749201132	-7.716197571993	-3.004702758495	2.866863109608
##	[889]	-23.576061011541	-9.335186162349	-4.378440055093	-8.196009271002
##	[893]	-28.842102405057	13.426585304189	-1.876222989011	-10.351342766012
##	[897]	-18.868691963919	-5.309768035340	7.008740335064	6.712866195953
##	[901]	-8.225007433935	-15.037254206835	-8.949689592260	-21.791536707698
##	[905]	-1.631024812692	-7.388238034354	-19.809081661673	12.326762889991
##	[909]	-15.851966436160	-19.064920698506	-18.964359415602	-15.289195276919
##	[913]	-7.408057563467	-12.203092254263	5.404225244923	-22.452496476916
##	[917]	2.535620565517	-12.433293230296	-16.227403021459	-20.141699367382
##	[921]	-10.519150843030	-18.977110476583	-19.308737994439	2.517658922154
##	[925]	7.999633897174	-16.284043044961	-11.912881229706	-22.428087190895
##	[929]	-11.937271390340	-5.705226492975	-8.565712740119	-12.549452666641
##	[933]	-17.205138331166	-8.544916382586	-29.283177074879	-17.864687875171
##	[937]	-2.097864452843	-17.450033336766	-35.026115993680	-25.604590523748
##	[941]	5.268796341894	8.658880547211	-28.244468172721	-4.359755578285

```
## [945] -13.616177827989 -15.843079583096 -3.909900791438 -4.722101718252
## [949] -13.448838473814 -16.742192484055 -13.014487387267 -15.675218492798
## [953] -25.128015926462 1.873220324264 -22.758556273965 -16.749254222418
## [957] -14.222786007467 -22.569656151057 -17.988782295215 1.377032622586
## [961] -2.634736689856 5.852416662837 1.028381336585 -19.825917624721
## [965] -1.674698789021 -25.691685002019 3.176814875670 5.341506547902
## [969] -10.241321442807 -16.096518698408 -8.883639047669 -6.173186060105
## [973] -19.507196965928 2.875467340177 -1.419430742749 -0.172746378397
## [977] -13.153690515729 -9.675387086743 -2.089631947452 -6.605033688577
## [981] -0.553953229636 -4.312072453225 -7.415832076048 -12.280701590417
## [985] -6.896104877402 -26.078787727753 -18.974102470302 -1.443043727644
## [989] -29.620625688288 -0.512790349649 -8.959460034445 -20.442572814595
## [993] -2.904799096818 -8.247066734808 -20.584697205160 -16.806536472064
## [997] -20.146769499865 13.366152539103 -21.714500261255 -31.414276596459
```

- Find the average of v and the standard error of v .

```
mean_i = mean(i,sqrt(1000))
```

- Find the 5%ile of v and use the `qnorm` function to compute what it theoretically should be. Is the estimate about what is expected by theory?

```
#qnorm(i, mean=mean_i, sd=.05, lower.tail = TRUE, log.i = TRUE )
```

- What is the percentile of v that corresponds to the value 0? What should it be theoretically? Is the estimate about what is expected by theory?

```
#TO-DO
```