

Transducers (Finite)

Mealy & Moore M/c:-

- They are DFA with some o/p. There is no final state in these DFA.

$M(Q, \Sigma, \Gamma, \delta, \Delta, q_0)$

δ -tuple

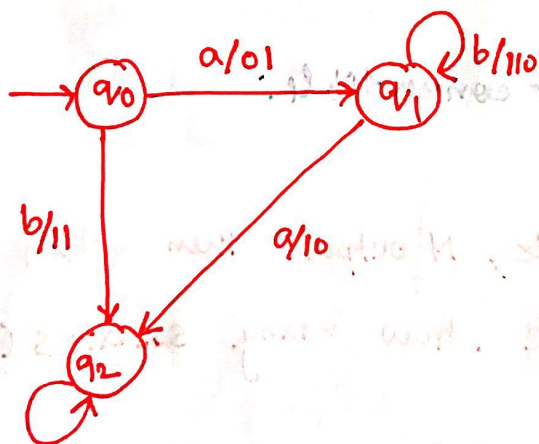
o/p alphabet

o/p function

$(\delta_{Q \times \Sigma \rightarrow Q})$ Mealy & Moore M/c

- Mealy: $\Delta_{Q \times \Sigma \rightarrow \Gamma^*}$ (O/p depends upon current state & I/p)
- Moore: $\Delta_Q \rightarrow \Gamma^*$ (O/p depends upon current state only)

Mealy M/c:-



$\left\{ \begin{array}{l} \delta(q_0, a) = q_1 \\ \Delta(q_0, a) = 01 \end{array} \right\}$

as~~t~~, we can see O/p = 01.

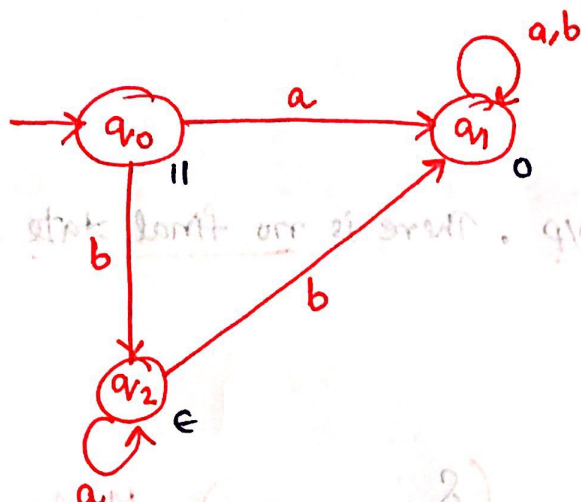
depends upon q_0 & a

q_i	δ, Δ	a	b
$\rightarrow q_0$		$q_1, 01$	$q_2, 11$
q_1		$q_2, 10$	$q_1, 110$
q_2		$q_2, 1$	$q_2, 0$

I/p :- aabba

O/p :- 0110001

> Moore M/c :-



O/P is associated with state only

	a	b	O/P
→ q ₀	q ₁	q ₂	11
q ₁	q ₁	q ₁	0
q ₂	q ₂	q ₁	ε

I/p :- aabba

O/p :- 1100000

I/p :- baaba

O/p :- 11εεε00 = 1100

NOTE:-

Mealy & Moore are not equivalent as there O/p may or maynot be same for a given I/p.

Mealy and Moore are inter convertible.

Q.

A Mealy M/c of M state, N output then when we convert it into Moore M/c, how many states (atmost) are there.

M State, N - O/P Mealy M/c \Rightarrow Moore M/c $\leq mn + 1$ States
 or $\leq mn$

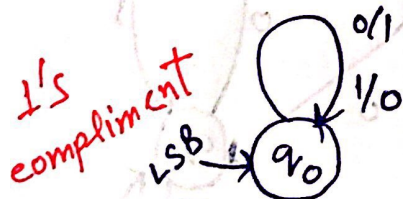
Q. M -state, and N -output Moore M/c when converted to Mealy M/c. How many states (atmost) will be there in Mealy M/c.

M -state, N -op Moore M/c \equiv (Mealy M/c $\leq m$ states)

Standard functions in Mealy & Moore :-

1. 1's compliment
2. 2's compliment
3. Binary Adder (Full)
4. Incremented by 1
5. Change the sign bit
6. Integer Division tester
7. Logical funcⁿ

Mealy M/c



Moore M/c

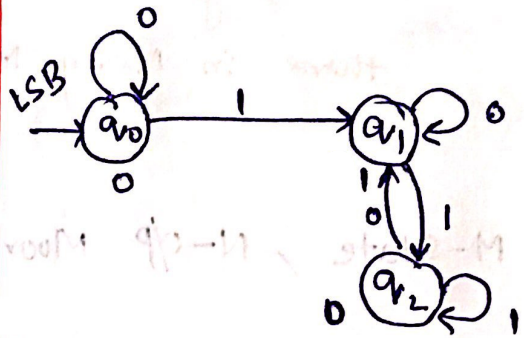
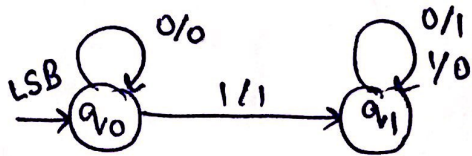


funcⁿ

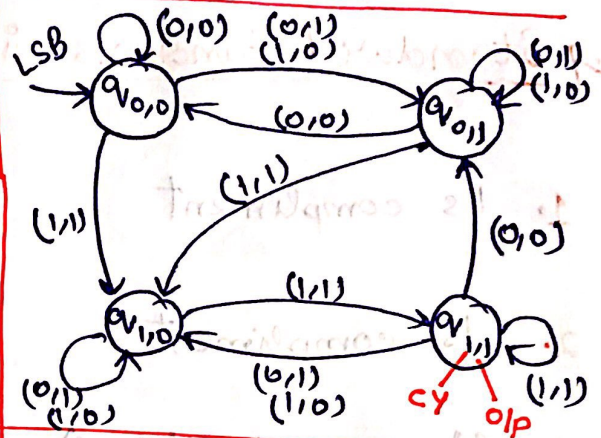
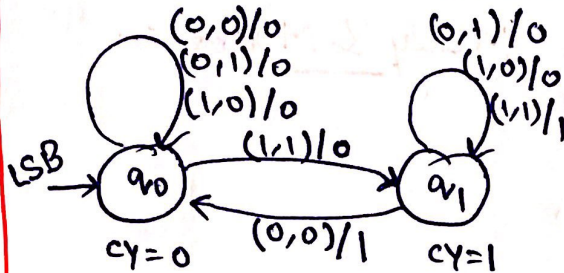
Mealy M/c

Moore M/c

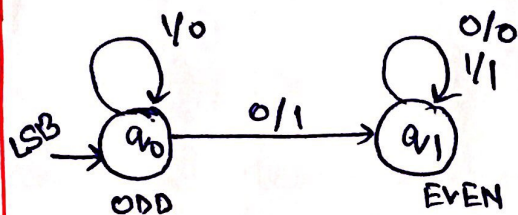
2's complement



Binary Full Adder

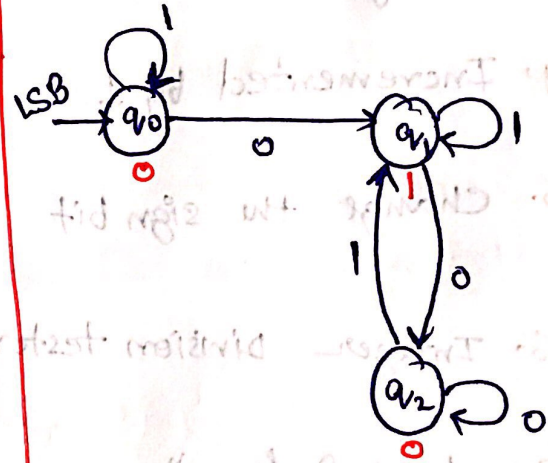


Increment by 1

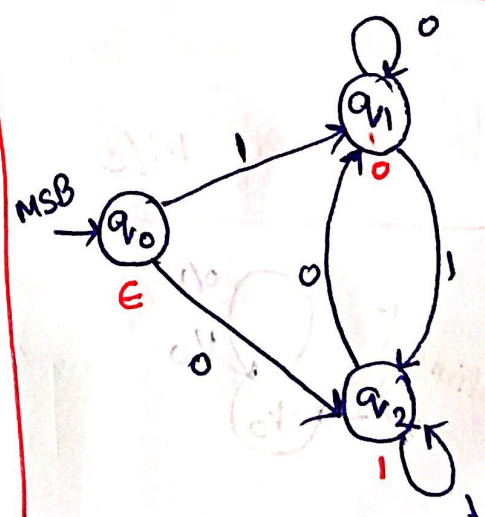
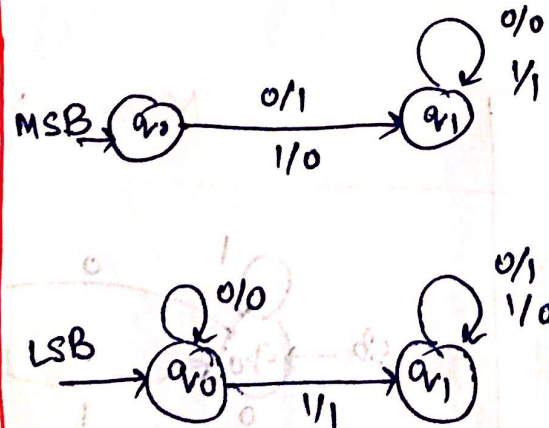


$$\begin{array}{r} 110001 \\ + 1 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 110000 \\ + 1 \\ \hline 1 \end{array}$$

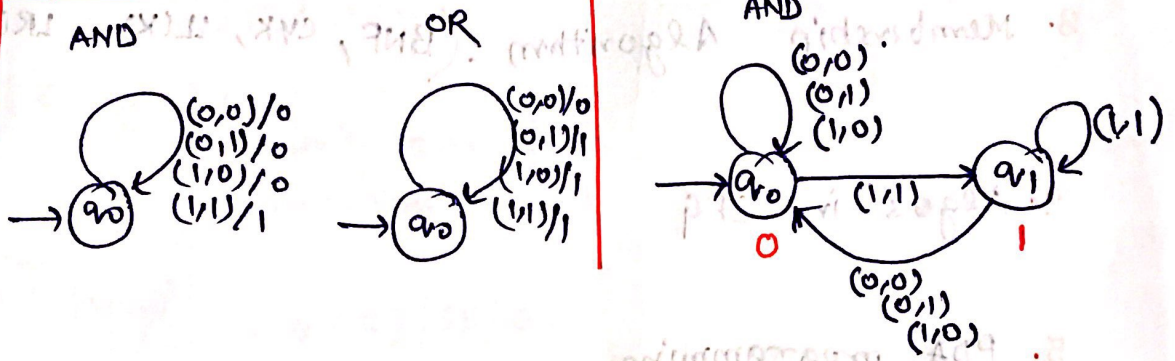


change the sign bit

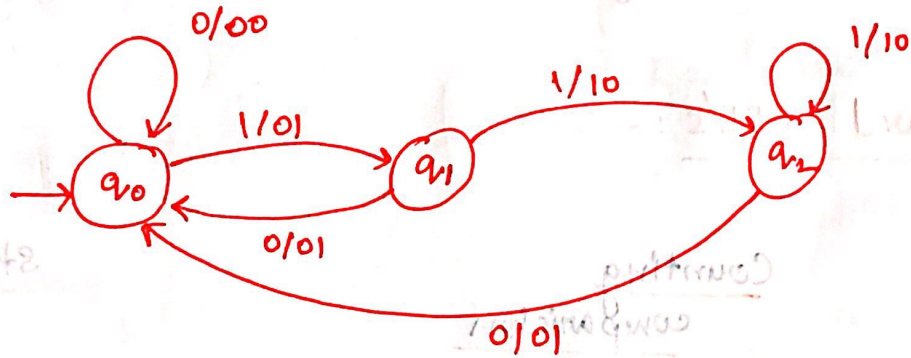


func ⁿ	Mealy M/c	Mooze M/c
Integer divisible by Integer		$f(w) = dw \bmod 3$

Logical funcⁿ



Q.



(a) O/p is "00" for every 0

(b) O/p is "01" for every 1

(c) ✓ O/p is sum of present and previous bit of I/p.

(d) None of above.

Let take I/p = 101101 → 010101100101
 O/p = 010101100101