

Answer 2>

In Lamport's mutex algorithm paper, it is not specified anywhere as to what should be the order of sequence of the five rules. Also, the meaning of 'any' in Rule 3 and Rule 4 is not mentioned clearly, Rule 3 and Rule 4 are as follows

Rule 3: To release the resource, process P_i removes any $T_m:P_i$ requests resource message from its request queue and sends a timestamped P_i release resource message to every other process.

Rule 4: When process P_j receives a P_i releases resource message, it removes any $T_m:P_i$ requests resource message from its request queue.

Since the word 'any' and T_m in the above two rules leads to ambiguity among the processes decisions, hence it results in an incorrect system.

If we take 'any' to mean any request, the system might violate

- (a) Safety
- (b) Liveliness

Scenario:

1. Consider a case where Process ' P_1 ' sends a request ' R_1 ' resource at $LC = 0$.
2. P_2 also sends a request ' R_2 ' at $LC = 1$.
3. Now before P_2 could acknowledge the request ' R_2 ', Process P_1 sends another request ' R_1 ' at $LC = 2$

At this point of time the message queues of P_1 and P_2 will look like this

Case 1: Safety Violation (Removal Shown in red color)

Process P1					
$R_1, 0$	$R_2, 1$	$R_1, 2$			
Queue Start					
Process P2					
$R_1, 0$	$R_2, 1$	$R_1, 2$			
Queue Start					

4. Now, since P_1 has the request, which has the minimum LC value, P_1 will get the resource and once it is done, it will remove any $T_m:P_1$ request. Suppose it removes the request ' $R_1, 2$ ' from its queue and sends the release message. On receiving this release message P_2 removes the ' $R_1, 0$ '.
5. Since now, both processes will have their own requests at the top of the queue, they will both try to enter the Critical section (CS) at the same time thus violating the Safety Principle.

Case 2: Liveliness Violation (removal shown in red color)

Process P1					
$R_1, 0$	$R_2, 1$	$R_1, 2$			
Queue Start					
Process P2					
$R_1, 0$	$R_2, 1$	$R_1, 2$			
Queue Start					

4. Now, since P_1 has the request which has the minimum LC value, P_1 will get the resource and once it is done, it will remove any $T_m:P_1$ request. Suppose it removes the request ' $R_1, 0$ ' from its queue and sends the release message. On receiving this release message P_2 removes the ' $R_1, 2$ '.
5. Now, Process P_1 will expect P_2 to enter into the Critical section and P_2 will expect P_1 to enter the Critical Section as it has P_1 's request on the top of the queue. Therefore, they will both be stuck in a deadlock thus violating the Liveliness Principle.