Lab 4

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Completed with James Kinney, around 50/50 work completed between us.

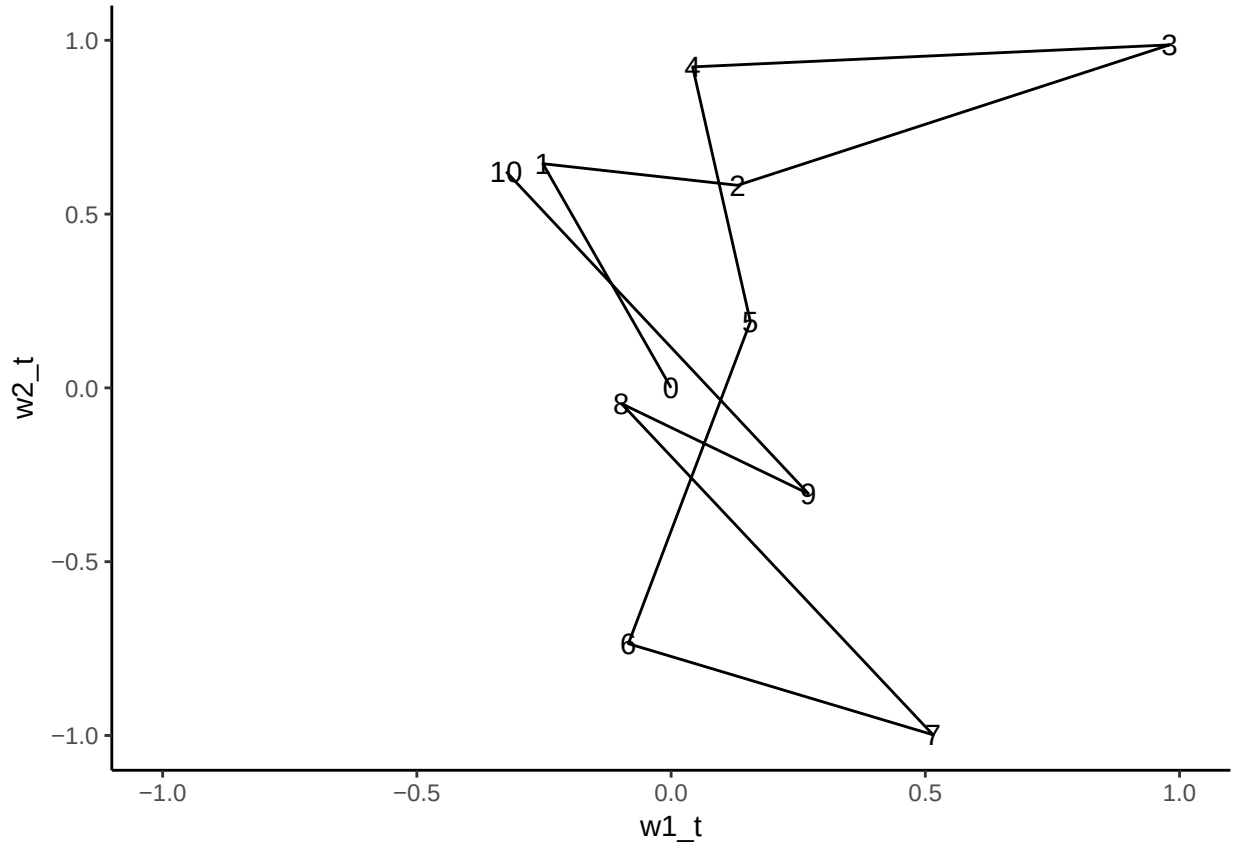
Question 1.

```
# Define function that returns a dataframe of a random walk in 2 dimensions

random_walker <- function(w1_0, w2_0, epsilon, n){
  t <- c(0:n) # define chain
  w1_t <- c(w1_0) # define chain
  w2_t <- c(w2_0) # define chain
  for (i in c(1:n) ){
    # First coordinate
    error1 <- runif(1, -epsilon , epsilon)
    w1_move <- w1_t[i] + runif(1, -epsilon , epsilon)
    while (w1_move > 1 |  w1_move < -1){
      error1 <- runif(1, -epsilon , epsilon)
      w1_move <- w1_t[i] + runif(1, -epsilon , epsilon)
    }
    w1_t[i+1] <- w1_move

    # Second coordinate
    error2 <- runif(1, -epsilon , epsilon)
    w2_move <- w2_t[i] + runif(1, -epsilon , epsilon)
    while (w2_move > 1 |  w2_move < -1){
      error2 <- runif(1, -epsilon , epsilon)
      w2_move <- w2_t[i] + runif(1, -epsilon , epsilon)
    }
    w2_t[i+1] <- w2_move
  }
  return(data.frame(w1_t, w2_t, t))
}

# Define function that returns a graph of a random walk in 2 dimensions

random_walker_graph <- function(w1_0, w2_0, epsilon, n){
  data <- random_walker(w1_0, w2_0, epsilon, n)
  graph <- data %>% ggplot(aes(x = w1_t, y = w2_t)) +
    geom_text(aes(label = t)) +
    geom_path() +
    coord_cartesian(xlim = c(-1, 1), ylim = c(-1, 1)) +
    theme_classic()
  return(graph)
}

# Define function that returns an estimate of pi from a random walk in 2 dimensions
random_walker_pi <- function(w1_0, w2_0, epsilon, n){
```

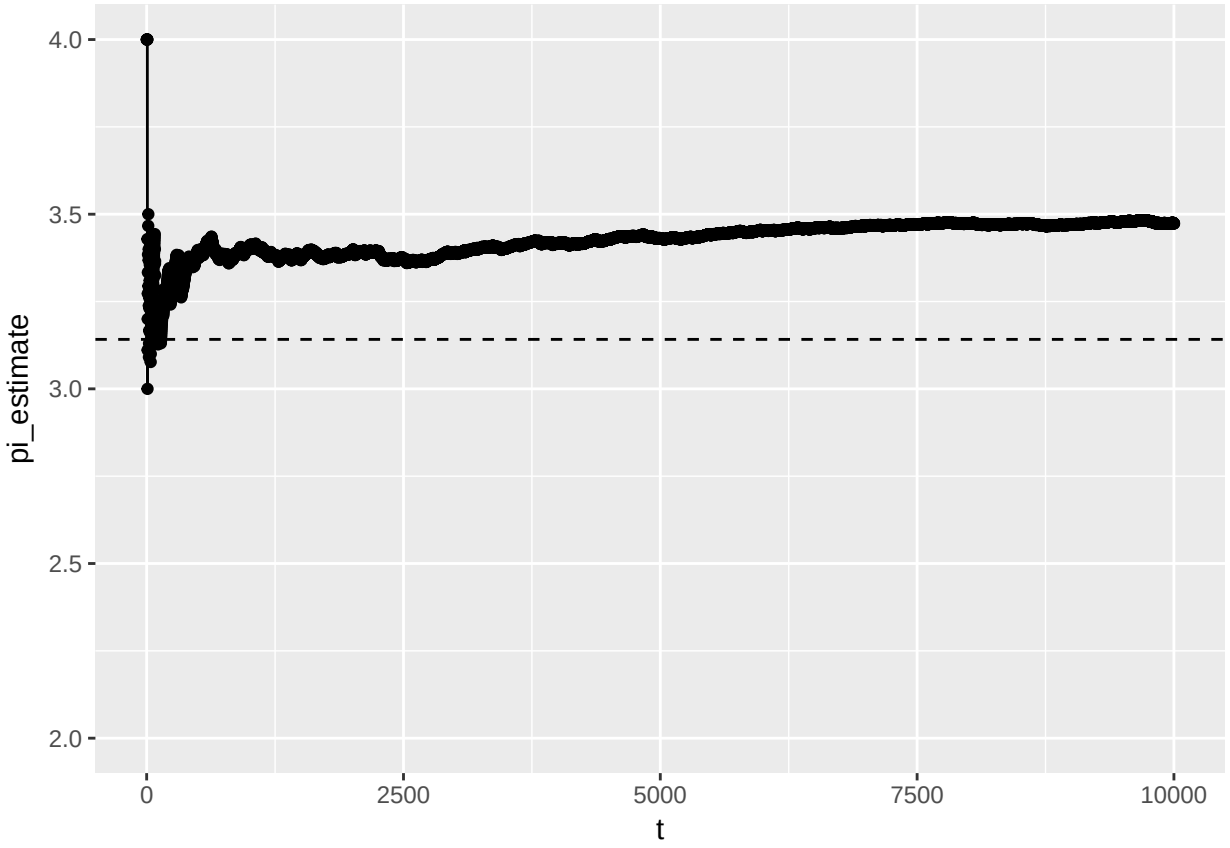
```
  data <- random_walker(w1_0, w2_0, epsilon, n)
  t <- c(1:nrow(data))
  w1 <- w2 <- pi_estimate <- c()
  for (i in t){
    w1 <- c(w1, data$w1_t[i])
    w2 <- c(w2, data$w2_t[i])
    w <- w1^2 + w2^2
    pi_estimate <- c(pi_estimate, 4*length(w[w < 1])/length(w))
  }
  graph <- data.frame(t, pi_estimate) %>%
    ggplot(aes(x=t, y = pi_estimate)) +
    geom_point() + geom_line() +
    geom_hline(yintercept=pi, linetype='dashed') +
    coord_cartesian(ylim = c(2, 4))
  return(graph)
}
```

i. Choice of ϵ.

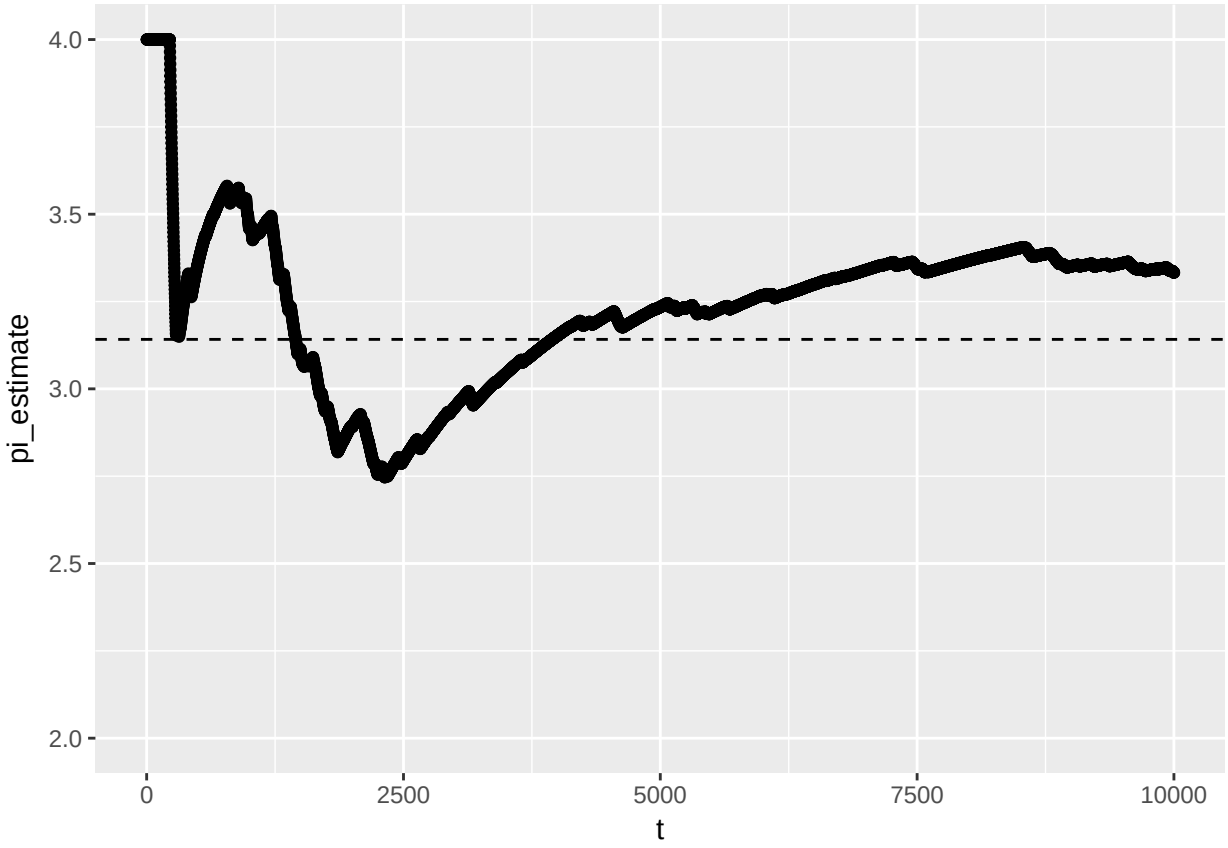
```
random_walker_graph(0, 0, 1 , 10)
```




```
random_walker_pi(0, 0, 0.5 , 10000)
```




```
random_walker_pi(0, 0, 0.1 , 10000)
```



ii. Choice of w_0.

iii. Choice of chain length, n.

Question 2.