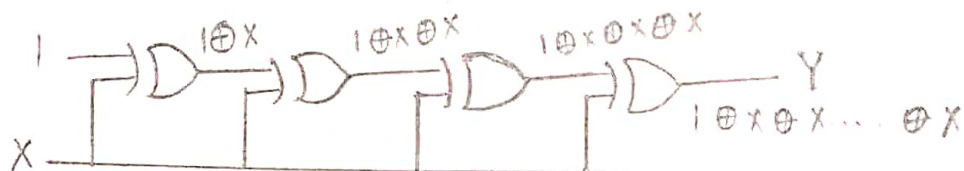


Q1.

Ans



[illegible]

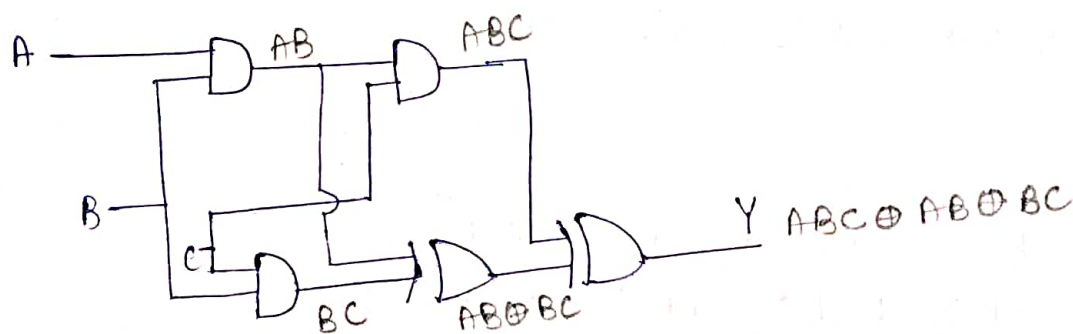
$$Y = 1 \oplus 0 \oplus 0$$

$$= 1 \oplus 0$$

b) $\gamma \in 1$.

Q2.

Ans.



$$Y = ABC \oplus AB \oplus BC$$

$$= AB(C \oplus I) \oplus BC$$

$$= A\bar{B}\bar{C} \oplus BC$$

$$= B(A\bar{C} \oplus C)$$

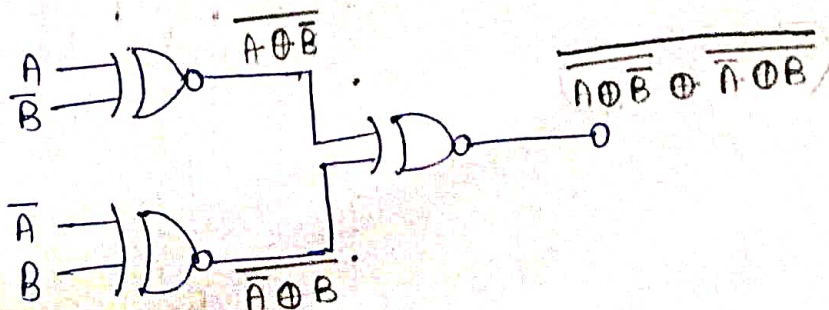
$$= B [\overline{A\bar{C}} C + A\bar{C} \cdot \bar{C}]$$

$$= B[(\bar{A} + C)C + A\bar{C}]$$

$$= B[\bar{A}C + C + A\bar{C}]$$

$$= B[C + A] = B[C + A] \quad \text{option (C).}$$

Q3



$$Y = \overline{A \oplus B} \oplus \overline{A \oplus B}$$

$$Y = \overline{A \oplus B} \oplus \overline{A \oplus B}$$

Q4.

Ans.

1	0	0	1
0	d	0	0
0	0	d	1
1	0	0	1

NO. of minimized sum
of product = 2.

$$f(a, b, c, d) = b'd' + acd$$

Q5.

Ans.

$$Z = RS\bar{I}_3 + R\bar{S}\bar{I}_2 + \bar{R}S\bar{I}_1 + \bar{R}\bar{S}I_0$$

$$= PRS + P\bar{Q}R\bar{S} + \bar{P}\bar{R}S + (P + \bar{Q})\bar{R}\bar{S}$$

$$= PRS + P\bar{Q}R\bar{S} + \bar{P}\bar{R}S + \bar{P}\bar{R}S + \bar{Q}\bar{R}\bar{S}$$

$$PRS(\bar{Q} + Q) = PRS\bar{Q} + PQ\bar{R}S$$

$$\bar{P}\bar{R}S(\bar{Q} + Q) = P\bar{Q}\bar{R}S + P\bar{Q}\bar{R}S$$

$$P\bar{Q}\bar{R}S(\bar{Q} + Q) = P\bar{Q}\bar{R}\bar{S} + P\bar{Q}\bar{R}S$$

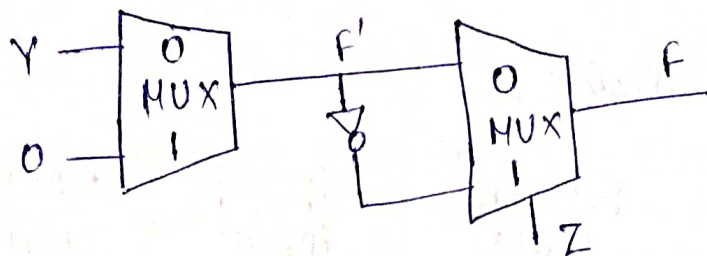
$$\bar{Q}\bar{R}S(P + \bar{P}) = P\bar{Q}\bar{R}S + \bar{P}\bar{Q}\bar{R}S$$

$$Z = P\bar{Q}\bar{R}\bar{S} + P\bar{Q}\bar{R}S + P\bar{Q}\bar{R}S + P\bar{Q}\bar{R}S + P\bar{Q}\bar{R}S + P\bar{Q}\bar{R}S + P\bar{Q}\bar{R}S + \bar{P}\bar{Q}\bar{R}S$$

So, by k-map

$$(a) Z = P\bar{Q} + P\bar{Q}\bar{S} + \bar{Q}\bar{R}\bar{S}$$

RS \ PQ				
	00	01	11	10
00	1		1	1
01			1	1
11			1	1
10			1	

Q6Ans

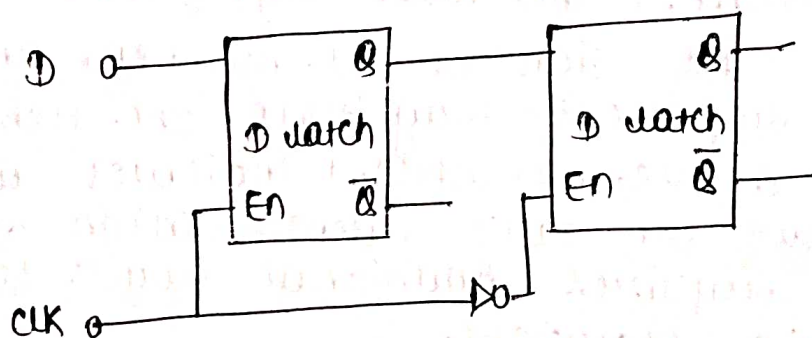
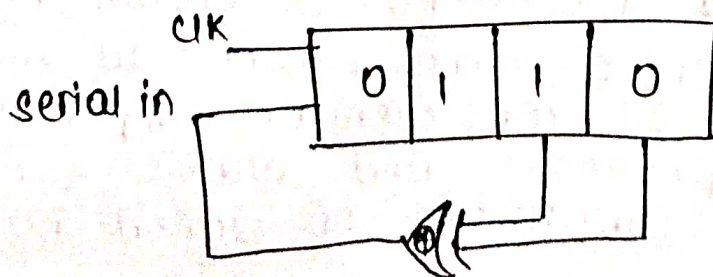
$$F' = \bar{X}Y + X \cdot 0$$

$$F' = \bar{X}Y$$

$$\begin{aligned} \text{and } F &= \bar{Z}F' + Z\bar{F}' \\ &= \bar{Z}(\bar{X} \cdot Y) + Z(\overline{\bar{X} \cdot Y}) \\ &= \bar{X}Y\bar{Z} + Z(X + \bar{Y}) \end{aligned}$$

b]

$$F = \bar{X}Y\bar{Z} + XZ + \bar{Y}Z$$

Q7 Ans [C] $\bar{P}\bar{Q}R + \bar{P}QR + P\bar{Q}R$ Q8Ans [d] Master-slave D flip-flop.Q9Ans

CLK	Q_0	Q_1	Q_2	Q_3
0	0	1	1	0
1	1	0	1	1
2	0	1	0	1
3	1	0	1	0

$$Q_0 = Q_2 \oplus Q_3$$

[C] 1010.

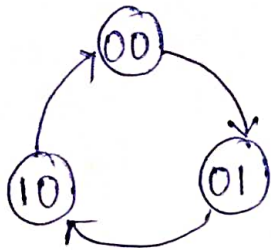
Q10

Ans.

From the given circuit;

$$D_1 = Q_0$$

$$D_0 = \overline{Q_1} + Q_0$$



Present state		Flipflop inputs		Next state	
Q_1	Q_0	D_1	D_0	Q_1^+	Q_0^+
0	0	0	1	0	1
0	1	1	0	1	0
1	0	0	0	0	0

[b] 00, 01, 10, 00, 01

Q11.

Ans.

1. Sign magnitude: The most significant bit (MSB) represents the sign of the number, and the rest of the bits represent magnitude. The MSB of 0 indicates a +ve no. while 1 indicates a -ve no. This allows for easy identification of the sign but requires additional logic for arithmetic operations.
2. Two's complement: used for signed integers. The MSB is the sign bit, with 0 indicating a +ve no. and 1 indicating a -ve no. To obtain the 2's complement of a -ve no., invert all the bits and add 1. 2's complement simplifies arithmetic operations and allows for easy addition and subtraction of signed no.
3. Biased: It involves adding a bias or offset value to the actual data. The bias is typically added to the exponent field in floating point representation to allow a wider range of +ve and -ve exponents. It ensures that the representation is always +ve, simplifying comparison and sorting operations.

To compute $P = X \times Y$ using Booth's algorithm,

1. Initialise P and Q with the value of x and y in 2's complement notation.

$$P = 00000000 \quad 00000101$$

$$Q = 11111111 \quad 1111010$$

2. create an auxiliary register (AC) initialized with 0.

$$AC = 00000000 \quad 00000000$$

3. Perform iterations :

→ If the LSB of Q and the previous LSB of Q (Q_0 and Q_{-1}) are 01 or 10, arithmetic right shift of P and AC , and add x to P .

→ If Q_0 and Q_{-1} are 00 and 11, arithmetic right shift of P and AC , and subtract x from P .

Iteration 1: $Q_0 = 0 \quad Q_{-1} = 0$, shift P and AC right

$$P: 00000000 \quad 00000010$$

$$AC: ' \quad ' \quad 00000000$$

Iteration 2: $Q_0 = 1 \quad Q_{-1} = 0$ shift P and AC right. Add x to P .

$$P: 10000000 \quad 00000001$$

$$AC: 00000000 \quad 00000000$$

Iteration 3: $Q_0 = 1 \quad Q_{-1} = 1$ shift P and AC right. + x to P .

$$P: 11000000 \quad 00000000$$

$$AC: 00000000 \quad ''$$

Iteration 4: $Q_0 = 0 \quad Q_{-1} = 1$ shift P and AC right. subtract x from P .

$$P: 11100000 \quad 00000000$$

$$AC: 00000000 \quad ''$$

Iteration 5: $Q_0 = 0 \quad Q_{-1} = 0$ shift P and AC right.

$$P: 11110000 \quad 00000000$$

$$AC: 00000000 \quad ''$$

Iteration 6: $Q_0 = 0$ $Q_{-1} = 0$ shift P and AC right

P: 11111000 00000000

AC: 00000000 "

Iteration 7: $Q_0 = 1$ $Q_{-1} = 0$ shift P and AC right
add x to P.

P: 11111100 00000001

AC: 00000000 00000000

4. The final value of P is the product P.

$P = 11111100\ 00000001 \Rightarrow P = x \times y$ is
-90 in 2's complement.

Q13.

Ans a] $b + 13$

$b = 00000110$

$13 = 00001101$

sum: $19 = 00010011$

b] $-b + 13$

$-b = 1111010$

$13 = 00001101$

sum: $7 = 00000111$

c] $b - 13$

$b = 00000110$

$13 = 00001101$

diff = 11110111 (-7)

d] $-b - 13$

$-b = 1111010$

$-13 = 00001101$

diff = 11101101 (-19)

Q14.

Ans.

a]
$$\begin{array}{r} 111000 \\ -110011 \\ \hline 000101 \end{array} \leftarrow \begin{array}{r} 111000 \\ +001101 \\ \hline 1000101 \end{array} \Rightarrow \text{2's complement}$$

b]
$$\begin{array}{r} 11001100 \\ -00101110 \\ \hline 10011110 \end{array} \leftarrow \begin{array}{r} 11001100 \\ +11010010 \\ \hline 10011110 \end{array} \Rightarrow \text{2's complement}$$

$$\begin{array}{r}
 \text{c] } \begin{array}{r} 111100001111 \\ - 110011110011 \\ \hline 001000011100 \end{array} \leftarrow \begin{array}{r} 111100001111 \\ + 001100001100 \text{ } 2's \\ \hline \boxed{1}001000011100 \\ \text{X} \end{array}
 \end{array}$$

$$\begin{array}{r}
 \text{d] } \begin{array}{r} 11000011 \\ - 11101000 \\ \hline -00100101 \end{array} \leftarrow \begin{array}{r} 11000011 \\ + 00010111 \\ \hline 11011011 \\ \text{2's comp} \end{array}
 \end{array}$$

-ve sign in front (no end carry).

Q15.

Ans

72530 - 13250 using 10's complement:

10's complement of 72530 = 27470

" " " 13250 = 86750

$$\boxed{27470 + 86750 = 114220}$$

- Check if there is an end-around carry (carry-out) in the result:
in case, there's no end-around carry.

10's complement of 114220 = 885780

Add a -ve sign to the result to indicate subtraction:

$$\therefore 72530 - 13250 = -885780.$$