Recursion with multiple base cases

- Fibonacci numbers
  - Leonardo of Pisa (aka Fibonacci) modeled the following challenge
    - Newborn pair of rabbits (one female, one male) are put in a pen
    - Rabbits mate at age of one month
    - Rabbits have a one month gestation period
    - Assume rabbits never die, that female always produces one new pair (one male, one female) every month from its second month on.
    - How many female rabbits are there at the end of one year?

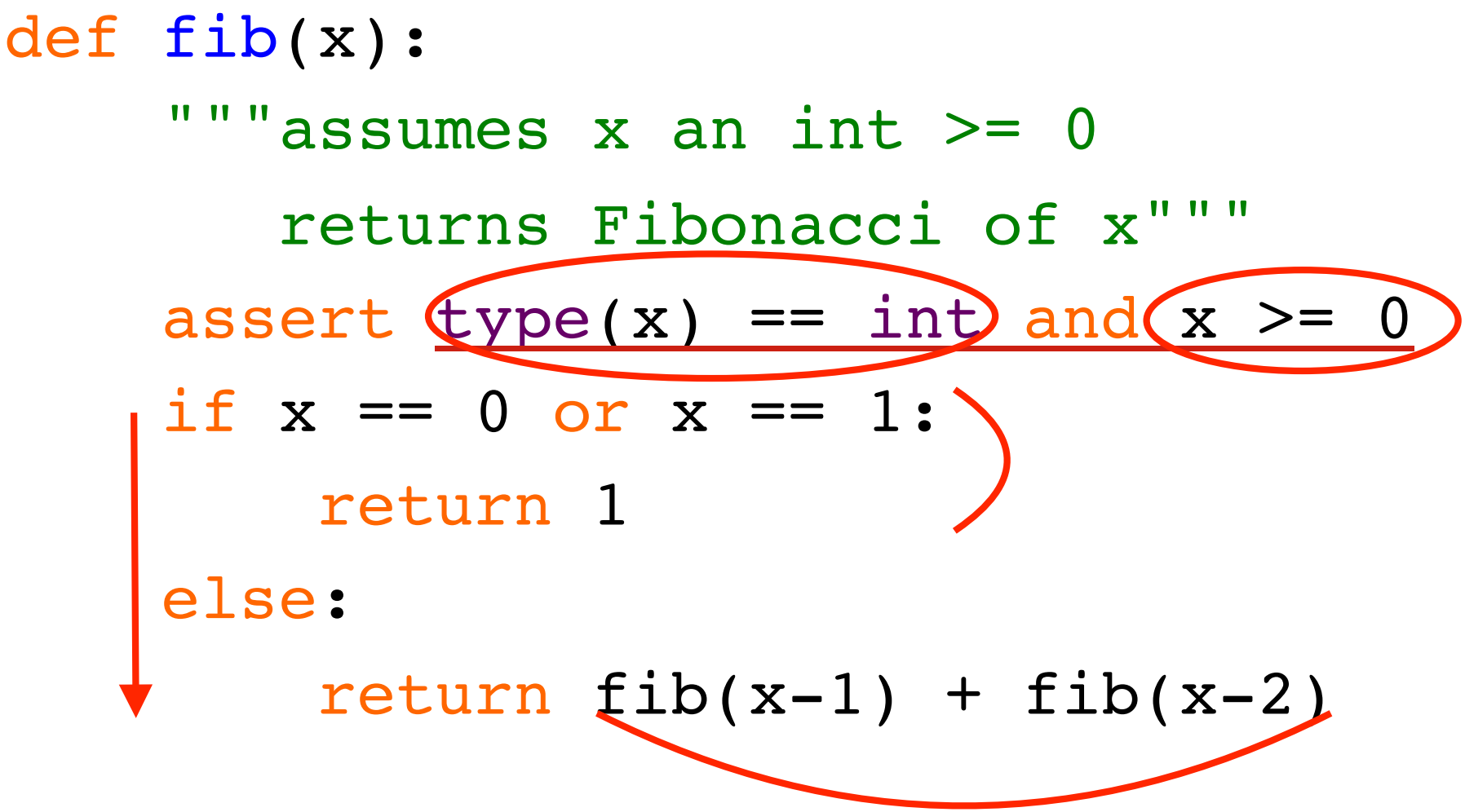
Fibonacci

- After one month (call it 0) – 1 female
- After second month – still 1 female (now pregnant)
- After third month – two females, one pregnant, one not
- In general, females(n) = females(n-1) + females(n-2)
  - Every female alive at month n-2 will produce one female in month n;
  - These can be added those alive in month n-1 to get total alive in month n

Month	Females
0	1
1	1
2	2
3	3
4	5
5	8
6	13

Fibonacci

- Base cases:
  - Females(0) = 1
  - Females(1) = 1
- Recursive case
  - Females(n) = Females(n-1) + Females(n-2)


def fib(x):
"""assumes x an int >= 0
returns Fibonacci of x"""
assert type(x) == int and x >= 0
if x == 0 or x == 1:
return 1
else:
return fib(x-1) + fib(x-2)