

## CHAPTER - 18

# MODERN PHYSICS

### SYNOPSIS

#### Introduction

At normal conditions most of the gases do not conduct electricity. However, it can be made conducting by (i) applying a very high voltage (ii) by reducing the pressure of the gas to a very low value, or (iii) by irradiating the gas with certain radiations such as  $\gamma$ -rays, X-rays, u-v rays etc. The process of splitting up gas molecule into +ve and -ve ions is called ionisation. If the ionisation is taking place in a tube having +ve and -ve electrodes the arrangement is called a discharge tube. Then +ve and -ve ions move in opposite directions constituting an electric current called ionisation current. The flow of electric current through gases is called discharge of electricity through gases.

The experiments with discharge tubes led to the discovery of X-rays by Roentgen in 1895 and cathode rays (electron) by J.J Thomson in 1897.

#### Electrons and Photons

Experimental studies on conduction of electricity through gases at low pressures led to the discovery of electrons by J. J. Thomson.

1. The specific charge  $\left(\frac{e}{m} \text{ value}\right)$  of the electron is determined by Thomson as  $1.76 \times 10^{11} \text{ C/kg}$
2. The charge of the electron is determined by Millikan as  $1.602 \times 10^{-19} \text{ C}$
3. The mass of the electron is then calculated as  $9.11 \times 10^{-31} \text{ kg}$
4. The electron is the integral part of all constituents of matter in all forms and the charge carried by it is considered as the basic unit of charge

According to **Planck's quantum theory**, light consists of tiny packets of energy called quanta or photons of energy  $h\nu$  and momentum  $h/\lambda$ .

#### Electron Emission

Free electrons in the metals are responsible for their electrical conductivity. But, the free electrons normally, can not escape from the metal. A certain energy is required for the emission of electron.

The minimum energy required to escape an electron from a metal surface is called the **work function**  $\phi_0$  of that metal, and is expressed in eV (electron volt) [One eV is the KE acquired by an electron when it is accelerated through a p.d of 1 volt]

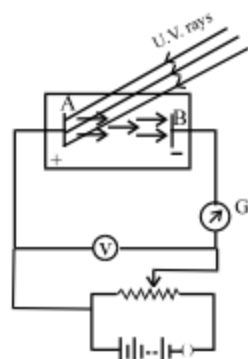
ie,  $1\text{eV} = 1.602 \times 10^{-19}\text{C} \times 1\text{V} = 1.602 \times 10^{-19}\text{J}$ .

<i>Metal</i>	$\phi_0$ in eV	<i>Metal</i>	$\phi_0$ in eV
Cs	2.14	Al	4.25
K	2.30	Cu	4.65
Na	2.75	Ag	4.75
Ca	3.20	Ni	5.15
Pb	4.25	Pt	5.65

The minimum energy required for the electron emission can be supplied by one of the following methods  
 (i) By heating (thermionic emission) (ii) By applying very strong electric field of the order of  $10^8 \text{ V m}^{-1}$  (field emission) (iii) By irradiating the surface with light rays of suitable frequencies (Photoelectric emission)

**Photoelectric Emission :** Discovered by Hertz. The phenomenon of emission of electrons from the surface of the metals when irradiated with  $\gamma$  rays, X-rays, U.V rays or visible rays is called Photoelectric emission.

### Experimental Study



As p.d between A and B is increased, photoelectric current  $i$  decreases and becomes zero at a p.d  $V_0$ . This p.d is called cut off potential or stopping potential. At this conditions, the maximum KE of the

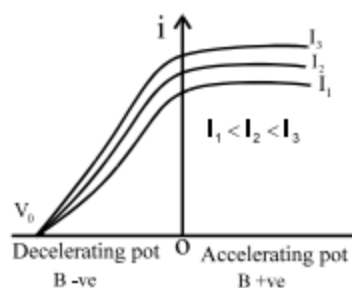
emitted electron  $\frac{1}{2}mv_{\max}^2 = eV_0$

### Effect of intensity of light



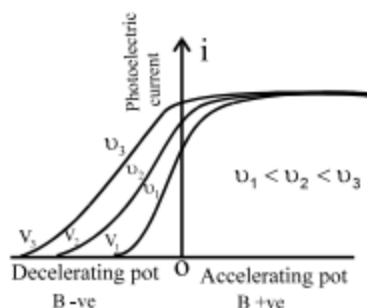
Photoelectric current  $i$  or number of photoelectrons emitted is directly proportional to intensity of light.

### Effect of p.d between A and B



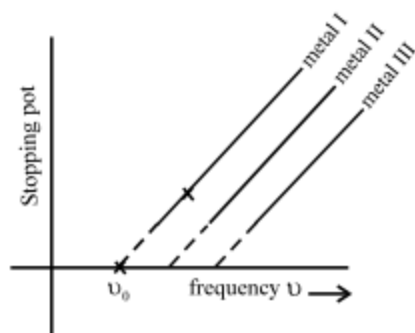
1. Saturation current value increases with intensity  $I$  of incident light
2. Cut-off potential  $V_0$  is independent of intensity

### Effect of Frequency



1. Saturation current is same for all frequencies when intensity remains constant
2. Below saturation value photoelectric current depends on frequency - the higher the frequency the larger the current.
3. Stopping potential is different for different frequencies - the higher the frequency the greater (-ve value) the stopping potential.

### Frequency and stopping potential



The graph with stopping potential against frequency is a straight line for all metals. These lines are

parallel and are having same slope  $\frac{h}{e}$  ( $h$  is Planck's constant and  $e$  is the charge of electron). Frequency

$\nu_0$  is called the **threshold frequency** the minimum frequency for photo electric emission.

### Einstein's Equation

The electron absorbs the entire energy of only one photon. Part of this is used as work function ( $\phi_0 = h\nu_0$ ) and the rest remains as KE.

$$\text{Then } \frac{1}{2}mv_{\max}^2 = h\nu - h\nu_0$$

$$\text{Also } \frac{1}{2}mv_{\max}^2 = h(\nu - \nu_0) = eV_0$$

### Discussion

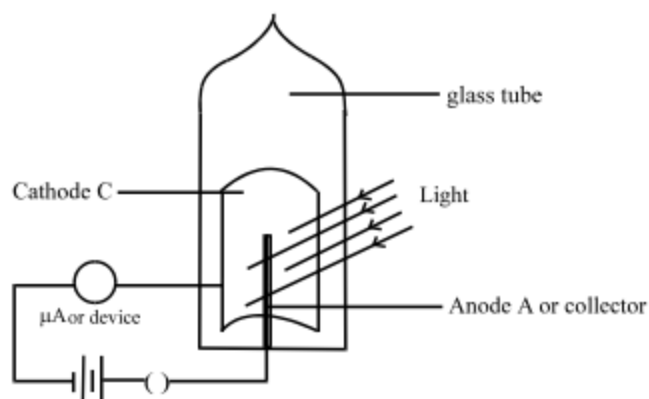
1. Velocity and hence KE of photoelectrons depends on the frequency  $\nu$  of incident lights.
2. If  $\nu \leq \nu_0$  there is no emission of photoelectrons
3. When intensity of light increases, number of photoelectrons emitted increases and hence photoelectric current increases
4. When frequency of light increases stopping potential increases (-ve value).
5. If  $V_0$  is the stopping potential,  $\frac{1}{2}mv_{\max}^2 = eV_0 = h\nu - h\nu_0$

$$V_0 = \frac{h}{e}\nu - \frac{h}{e}\nu_0$$

$\frac{h}{e}$  is the slope of the graph between  $V_0$  and  $\nu$

**Photocell** : is a device used to convert light energy to electrical energy. There are three types of photocells. Viz (i) photo emissive cell (ii) photo voltaic cell and (iii) photo conductive cell.

### Photo emissive cell



It consists of a glass tube containing a cathode C and anode A. When light incident on C, photoelectrons are emitted and are collected by A producing a current in the circuit. The change in intensity of light produces corresponding change in photoelectric current in the circuit.

Photocells are used in burglar alarms, automatic switching arrangements, reproduction of sound in cinemas, automatic counting devices etc.

**Particle nature of Radiation** - According to Planck, light consists of tiny packets of energy called quanta or photons of energy value  $h\nu$  and momentum  $\frac{h}{\lambda}$ . Momentum of photon  $P = mc = \frac{h}{\lambda}$  or  $\lambda = \frac{h}{mc}$

$\lambda$  is the attribute of a wave while  $mc$  is an attribute of a particle. This shows the dual nature of radiation.

### Wave nature of particle

From the particle nature of radiation, Louis de Broglie, argued that what is true for radiation must be true for particles also. ie, for a particle of mass  $m$  moving with a velocity  $v$  a wave must be associated with it. This wave is called de Broglie wave or matter wave. The wave length of de Broglie wave,

$$\lambda = \frac{h}{mv}$$

### de Broglie wavelength of an accelerated electron

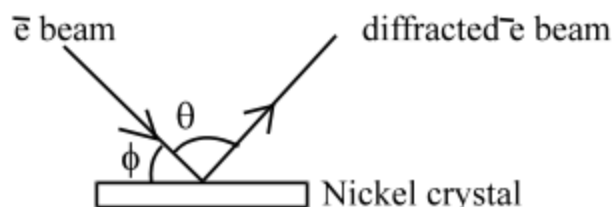
Velocity of electron accelerated through a p.d of  $V$  volts.  $v = \sqrt{\frac{2eV}{m}}$

$$\therefore \text{de Broglie wavelength of the electrons } \lambda = \frac{h}{mv} = \frac{h}{\sqrt{2meV}} = \frac{12.27}{\sqrt{V}} \text{ \AA}$$

For  $V = 100$  volts,  $\lambda = 1.227 \text{ \AA}$

This was verified by Davisson and Germer.

## Davisson and Germer Experiment



Davisson and Germer allowed the electron beam accelerated through 54 volt to fall on a nickel crystal. They measured maximum intensity of diffracted electron beam at an angle  $\theta = 50^\circ$ . Then, the glancing

angle  $\phi = \frac{180 - \theta}{2} = 65^\circ$ . Using this value in Bragg's equation for X-ray diffraction  $2d \sin \phi = n\lambda$  (here

$d = 0.91 \text{ \AA}$  for nickel and  $n = 1$ ) they calculated  $\lambda$  as  $1.65 \text{ \AA}$ . This is in close agreement with the

theoretical value  $\lambda = \frac{h}{p} = \frac{12.27}{\sqrt{54}} \times 10^{-10} = 1.66 \text{ \AA}$ .

### Teaching Points

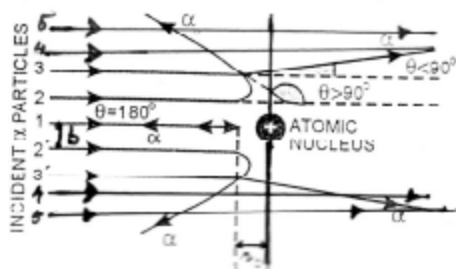
1. Basic idea of electron emission
  - i) Thermionic emission
  - ii) Field emission
  - iii) Photoelectric emission
  - iv) Secondary emission
2. Photoelectric effect
  - i) Basic idea
  - ii) Experimental study
  - iii) Effect of intensity of light on photocurrent
  - iv) Effect of potential on photoelectric current
  - v) Effect of frequency of incident radiation on stopping potential
3. Drawbacks of wave theory
4. Einstein's photo electric explanation
  - $\Rightarrow$  Idea of quantum of energy
  - $\Rightarrow$  Photoelectric equation
  - $\Rightarrow$  Particle nature of radiation
5. Wave nature of Matter
  - i) De Broglie wavelength
  - ii) Relation between accelerating potential & de Broglie wavelength
  - iii) Matter-wave picture & uncertainty principle

## 6. Davisson and Germer experiment

### Atomic Structure and Spectrum

The first atom model was proposed by Thomson. The model failed to explain the origin of spectral lines from the atom and the large angle scattering of  $\alpha$ -particles. Then Rutherford proposed another model of atom. According to Rutherford, the atom consists of a central core called atomic nucleus, where the mass and positive charge of the atom are concentrated and the electrons are moving round the nucleus in circular orbits. This model explained large angle scattering of  $\alpha$ -particles. The distance of closest

$$\text{approach } r_0 = \frac{1}{4\pi\epsilon_0} \frac{Ze \cdot 2e}{\frac{1}{2}mv^2}$$



$$\text{Impact parameter } b \text{ is given by } b = \frac{1}{4\pi\epsilon_0} \frac{Ze^2}{\frac{1}{2}mv^2} \cot(\theta/2)$$

$$\text{Number of atoms scattered at an angle } \theta, N_\theta = \frac{N_0 n t (2Ze^2)^2}{4(4\pi\epsilon_0)^2 r^2 (mv^2)^2 \sin^4(\theta/2)} \quad \text{or, } N_\theta \propto \frac{1}{\sin^4(\theta/2)}$$

Rutherford measured the size of the nucleus as of the order  $10^{-15}$  m (ie, fm) and atoms as of the order of  $10^{-10}$  m (ie,  $\text{\AA}$ ). But, the model failed to explain the origin of spectral lines from the atoms.

### Bohr Atom Model

Bohr modified Rutherford atom model by introducing certain postulates.

1. Every atom consists of the central nucleus and the electrons are revolving round the nucleus in specified orbits. The centripetal force required for the motion is given by

$$\frac{mv^2}{r} = \frac{1}{4\pi\epsilon_0} \frac{Ze^2}{r^2}$$

$$\text{For hydrogen } Z = 1; \therefore \frac{mv^2}{r} = \frac{1}{4\pi\epsilon_0} \cdot \frac{e^2}{r^2} \dots\dots\dots(1)$$

2. The electrons can revolve only in orbits for which the angular momentum is an integral multiple of  $\frac{h}{2\pi}$

$$\text{ie; } mvr = n \frac{h}{2\pi} \dots\dots\dots(2)$$



3. Electrons revolving in the orbit do not radiate energy.
4. Energy is radiated when the electrons jump from an outer orbit to inner orbit. The energy radiated is given by,  $h\nu = E_2 - E_1$  .....(3)

### **Calculations for hydrogen atom $Z = 1$**

Radius of the orbit  $r_n$

Sq. eq (2) and divide by eq. (1)  $r = r_n = \frac{\epsilon_0 h^2}{\pi m e^2} \cdot n^2$  .....(4)

or ;  $r_n = 0.53 n^2 \text{ \AA}$  .....(5)

Velocity of electron  $v_n$

Dividing eqn. (1) by eq (2)  $v = v_n = \frac{e^2}{2 \epsilon_0 h} \cdot \frac{c}{n}$

or,  $v_n = \frac{1}{137} \frac{c}{n}$  .....(6)

$\frac{e^2}{2 \epsilon_0 h c} = \frac{1}{137} = \alpha$  is called fine structure constant.

Period of revolution of the electron  $T_n$

Period  $T_n = \frac{2\pi r_n}{v_n} \propto n^3$  .....(7)

Energy of electron in the orbit  $E_n$

$KE = \frac{1}{8\pi \epsilon_0} \frac{e^2}{r^2}$ ;  $PE = -\frac{1}{4\pi \epsilon_0} \frac{e^2}{r^2}$

$TE = KE + PE = E = E_n = \frac{-1}{8\pi \epsilon_0} \frac{e^2}{r^2}$

Substituting for  $r$ ,  $E = E_n = \frac{-me^4}{8 \epsilon_0^2 h^2} \cdot \frac{1}{n^2}$  ..... (8)

In terms of fine structure constant  $E_n = -\frac{1}{2} mc^2 \alpha^2 \cdot \frac{1}{n^2}$

In eV,  $E_n = -13.6 \cdot \frac{1}{n^2}$  .....(9)

For  $n = 1$  ie; ground state,  $E_1 = -13.6\text{eV}$ ,  $KE = 13.6\text{eV}$ ,  $PE = -27.2\text{eV}$

### **Spectral lines**



From eqn (3)  $h\nu = E_{n_2} - E_{n_1}$

$$\text{ie; } h\nu = h\frac{c}{\lambda} = \frac{1}{2}mc^2\alpha^2 \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right] \quad \text{or, } \frac{1}{\lambda} = \bar{\nu} = R \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right] \dots\dots\dots(10)$$

$\lambda$  is the wavelength,  $\bar{\nu}$  wave number

R is Rydberg constant,  $R = \frac{1}{2}mc^2\alpha^2 = 1.097 \times 10^7 \text{ m}^{-1}$

### For hydrogen like atoms

$$r_n = \frac{1}{Z} \cdot r_n \text{ of H,}$$

$$V_n = Z \times V_n \text{ of H}$$

$$E_n = Z^2 \times E_n \text{ of H,}$$

$$\frac{1}{\lambda} = Z^2 \times \frac{1}{\lambda} \text{ of H}$$

### **Spectral series**

- |   |            |                                     |
|---|------------|-------------------------------------|
| 1. For Lyman Series (U.V. rays)         | $n_1 = 1,$ | $n_2 = 2, 3, 4, 5, \dots\dots\dots$ |
| 2. For Balmer series (Visible rays)     | $n_1 = 2,$ | $n_2 = 3, 4, 5, \dots\dots\dots$    |
| 3. For Paschen series (Infra red rays)  | $n_1 = 3,$ | $n_2 = 4, 5, 6, \dots\dots\dots$    |
| 4. For Bracket series (Infra red rays)  | $n_1 = 4,$ | $n_2 = 5, 6, 7, \dots\dots\dots$    |
| 5. For Pfund series (Far infrared rays) | $n_1 = 5,$ | $n_2 = 6, 7, 8, \dots\dots\dots$    |

### **Spectrum - Emission spectra and Absorption spectra**

#### Emission spectra are of three types

- Line spectrum : is obtained when substances in atomic state are excited.  
Eg : H spectrum, Hg spectrum, Sodium lamp
- Band spectrum : is obtained when substance is in molecular state are excited.  
Eg :  $\text{O}_2$ ,  $\text{N}_2$ ,  $\text{CO}_2$
- Continuous spectrum : is obtained when matter in bulk is excited  
Eg : Carbon arc, copper arc, hot filament lamp.

**Absorption spectra** is obtained when a composite light is passing through a less intense medium and the transmitted light is examined through a spectro graph. If the medium is in atomic state, *absorption line spectrum* is obtained and if the medium is in molecular state *absorption band spectrum* is obtained.

### **ATOMIC NUCLEI**

Atomic nucleus is the central part of every atom. Its size is of the order of 1 fm or  $10^{-15}$  m. The mass of the nucleus is more than 99.9% of the mass of the atom and is expressed in atomic mass unit (a.m.u) or simply u.

1 amu =  $\frac{1}{12}$  of mass of  ${}_6\text{C}^{12} = 1.66 \times 10^{-27} \text{ kg}$ . When 1 a.m.u is fully converted into energy, the energy produced is  $1.49 \times 10^{-10} \text{ J}$ .

$$1 \text{ a.m.u.} = 931 \text{ MeV}$$

The nucleus of an atom is represented by  ${}_Z\text{X}^A$  or  ${}_Z^A\text{X}$

Where Z is the atomic number ie, number of protons and A is the atomic mass number ie, total number of protons and neutrons

**Nuclear size** : The nucleus is assumed to be almost spherical. Its volume  $\frac{4}{3}\pi R^3 \propto A$

$$\therefore R^3 \propto A \quad \text{or,} \quad R = R_0 A^{1/3}; \quad R_0 = 1.2 \text{ fm to } 1.3 \text{ fm}$$

$$\text{Nuclear density : } \rho = \frac{\text{mass}}{\text{volume}} = \frac{\mu A}{\frac{4}{3}\pi R_0^3 A} = 2.29 \times 10^{17} \text{ kg/m}^3$$

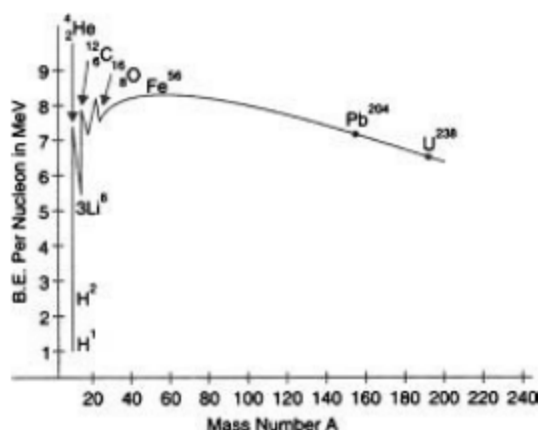
**Conservation Laws** : The sum of mass-energy, the momentum and the total charge are conserved before and after any nuclear interactions.

### **Binding Energy and mass defect**

$$\text{BE} = \text{mass defect} \times c^2$$

$$\text{BE} = (Z m_p + (A - Z) m_n - M_N) c^2$$

$M_N \rightarrow$  mass of nucleus



The importance of BE curve is that it led to the possibility of release of energy during nuclear fission and fusion.

**Nuclear forces** : Nuclear forces are the strongest attractive forces and are existing between nucleons - which are independent of charge, short range, non central, non-conservative and not obeying inverse square law. The nuclear forces are dependent on spin or angular momentum of nuclei. According to Yukawa, the exchange of  $\pi$  mesons is responsible for nuclear forces.

**Natural Radio Activity**

It is the spontaneous emission of certain active radiations from the nucleus of the atoms of certain elements. The emitted radiations contain  $\alpha$  -particles,  $\beta$  -particles and  $\gamma$  -rays.

**Decay Law** - Rutherford and Soddy law.

Number of atoms disintegrated per second at any instant is directly proportional to the number of radio active atoms actually present in the sample at that instant.

$$\text{ie; } \frac{dN}{dt} \propto N \quad \text{or,} \quad \frac{dN}{dt} = -\lambda N$$

$$\therefore \text{ Number of atoms left undecayed after } t \text{ seconds } N = N_0 e^{-\lambda t}$$

**Half life period T** is the time required to decay half the number of atoms initially present in the sample.

$$T = \frac{0.693}{\lambda}$$

$$\text{Number of atoms left undecayed after } n \text{ half life periods is, } N_n = N_0 \left(\frac{1}{2}\right)^n = N_0 \left(\frac{1}{2}\right)^{\frac{t}{T}}$$

**Mean life time  $\tau$** 

$$\tau = \frac{1}{\lambda} = \frac{T}{0.693} = 1.44 T$$

**Activity A**. The rate of disintegration is the activity A. Then,  $A = \frac{dN}{dt} = \lambda N = \lambda N_0 e^{-\lambda t}$

$$\text{Or, } A = A_0 e^{-\lambda t}$$

**Units of Radioactivity**

- 1) Curie (Ci)
- 2) Becquerel (Bq) SI unit
- 3) Rutherford (Rd)

**$\alpha$  -decay**: Emission of an  $\alpha$  -particle from the nucleus of an atom is  $\alpha$  -decay. It is represented by  ${}_Z X^A \rightarrow {}_{Z-2} Y^{A-4} + {}_2 \text{He}^4 + Q$ .

${}_Z X^A$  is parent nucleus  ${}_{Z-2} Y^{A-4}$  is daughter nucleus Q is disintegration energy which remains as KEs of product particles.

**$\beta$  -decay** means emission of an electron ( $\beta^-$ ) or positron ( $\beta^+$ ) from the nucleus. It is found that a ( $\beta^-$ )

emission is accompanied with the emission of an antineutrino ( $\bar{\nu}$ ) and ( $\beta^+$ ) emission is accompanied with emission of a neutrino ( $\nu$ ).

#### $\gamma$ -decay or emission

After an  $\alpha$ -decay or  $\beta$ -decay the daughter nucleus is usually in an excited state. It attains stability by the emission of one or more  $\gamma$ -ray photons.

**Nuclear fission** is the process of splitting the nucleus of a heavy atom into two nuclei of nearly equal mass with release of large energy.



The three neutrons released can produce further fission and the process is going on, resulting in chain reaction. An uncontrolled chain reaction results in explosion (atom bomb) and a controlled chain reaction gives controlled release of energy and is achieved in nuclear reactors. The main parts of a nuclear reactor are (1) nuclear fuel ( $\text{U}^{235}$  or  $\text{Pu}^{239}$ ) (2) Moderators - (heavy water, paraffin) and control rods (Boron, Cadmium)

**Nuclear Fusion** : is the fusion of two light nuclei into a single nucleus with release of large energy. This requires large KE and hence very high temperature of the order of  $10^7$  K. So, fusion process is taking place in the sun and the stars. Then, the process is also called thermonuclear process.

#### Teaching Points

- I. Basic idea of atomic structure
  - a) Plum pudding model
  - b)  $\alpha$ -particle scattering experiment and Rutherford's atom model
  - c) Scattering angle
  - d) Closest distance of approach
  - e) Impact parameter
- II. Rutherford's model of hydrogen atom
  - a) Radius of orbit
  - b) Orbital velocity
  - c) Energy of atom
- III. Draw back of Rutherford's model
- IV. Bohr model
  - a) Bohr hypothesis or Bohr postulates
  - b) Bohr model of hydrogen atom
  - c) Bohr model of hydrogen-like atom
- V. Atomic spectra
  - a. Emission spectrum
  - b. Absorption spectrum

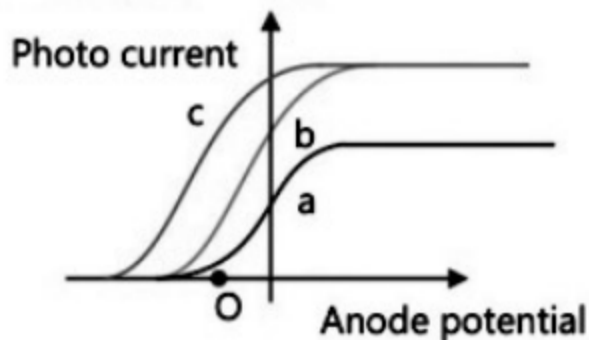
**NUCLEI**

- I. Atomic mass and composition of nucleus
  - a) Atomic mass unit
  - b) Proton and neutron
  - c) Atomic number, mass number, isotope, isobar, isotone
- II. Size of nucleus
  - a) Radius of a nucleus
  - b) Nuclear density
- III. Mass-Energy relation
  - a) Einstein's relation
  - b) Mass defect, Binding energy, Binding energy per nucleon
  - c) Binding energy per nucleons and mass number curve
  - d) Nuclear fission and nuclear fusion
  - e) Packing fraction
- IV. Nuclear forces
  - a) Nuclear stability
- V. Radioactivity
  - a) Basic idea
  - b)  $\alpha$ -decay,  $\beta$ -decay,  $\gamma$ -decay
  - c) Law of radioactive decay
  - d) Half life, mean life
  - f) Activity
- VI. Nuclear fission and working of reactor

**PART I - (JEEMAIN)****SECTION - I - Straight objective type questions**

1. In a photoemissive cell with exciting wavelength  $\lambda$ , the fastest electron has a speed  $v$ . If the exciting wavelength is changed to  $\frac{3\lambda}{4}$ , the speed of the fastest emitted electrons will be
  - 1)  $v\sqrt{\frac{3}{4}}$
  - 2)  $v\sqrt{\frac{4}{3}}$
  - 3) less than  $v\sqrt{\frac{4}{3}}$
  - 4) greater than  $v\sqrt{\frac{4}{3}}$

2. The figure shows the variation of photocurrent with anode potential for a photo-sensitive surface for three different radiations. Let  $I_a$ ,  $I_b$  and  $I_c$ , be the intensities and  $f_a$ ,  $f_b$  and  $f_c$  be the frequencies for the curves a, b and c respectively



- 1)  $f_a = f_b$  and  $I_a \neq I_b$
- 2)  $f_a = f_c$  and  $I_a = I_c$
- 3)  $f_a = f_b$  and  $I_a = I_b$
- 4)  $f_a \neq f_b$  and  $I_a = I_b$
3. A proton, a deuteron and an alpha particle are accelerated through potentials of V, 2V and 4V respectively. Their velocities will bear a ratio
- 1) 1 : 1 : 1                      2)  $1:\sqrt{2}:1$                       3)  $\sqrt{2}:1:1$                       4)  $1:1:\sqrt{2}$
4. An electron of mass 'm' is moving with initial velocity  $v_0 \hat{i}$  in an electric field  $\vec{E} = E_0 \hat{i}$  ( $E_0$  is positive). Which of the following is correct de Broglie wavelength at a given time t ( $\lambda_0$  is initial de Broglie wavelength).
- 1)  $\frac{\lambda_0}{\left(1 + \frac{eE_0}{m\lambda_0}t\right)}$                       2)  $\frac{\lambda_0}{\left(1 + \frac{eE_0}{mv_0}t\right)}$                       3)  $\frac{h}{\left(1 + \frac{mv_0}{Ev_0}t\right)}$                       4)  $\frac{h}{\left(1 + \frac{eE}{mv_0}t\right)}$
5. A particle A of mass m and initial velocity v collides with a particle B of mass  $\frac{m}{2}$  which is at rest. The collision is head on and elastic. The ratio of the de Broglie wavelengths  $\lambda_A$  to  $\lambda_B$  after the collision is
- 1)  $\frac{\lambda_A}{\lambda_B} = \frac{1}{3}$                       2)  $\frac{\lambda_A}{\lambda_B} = 2$                       3)  $\frac{\lambda_A}{\lambda_B} = \frac{2}{3}$                       4)  $\frac{\lambda_A}{\lambda_B} = \frac{1}{2}$
6. In Rutherford's scattering experiment, if the number of  $\alpha$  particles scattered at an angle of  $90^\circ$  is 55, then calculate the number of  $\alpha$  particles scattered at an angle of  $60^\circ$
- 1) 120                      2) 220                      3) 320                      4) 420



7. A small particle of mass  $m$  moves in such a way that the potential energy  $U = -\frac{1}{2}mb^2r^2$ , where  $b$  is a constant and  $r$  is the distance of the particle from the origin taken at the nucleus, Assuming Bohr model of quantization of angular momentum and circular orbits. Radius of the  $n^{\text{th}}$  allowed orbit is proportional to
- 1)  $n$                                       2)  $\sqrt{n}$                                       3)  $n^2$                                       4)  $n^3$
8. A hydrogen atom emits a photon corresponding to an electron transition from  $n = 5$  to  $n = 1$ . The recoil speed of hydrogen atom is almost
- 1)  $10^{-4} \text{ ms}^{-1}$                                       2)  $2 \times 10^{-2} \text{ ms}^{-1}$                                       3)  $4 \text{ ms}^{-1}$                                       4)  $8 \times 10^2 \text{ ms}^{-1}$
9. The binding energy per nucleon of  ${}^7_3\text{Li}$  and  ${}^4_2\text{He}$  nuclei are 5.60 MeV and 7.06 MeV, respectively. In the nuclear reaction  ${}^7_3\text{Li} + {}^1_1\text{H} \rightarrow {}^4_2\text{He} + {}^4_2\text{He} + Q$ , the value of energy  $Q$  released is
- 1) 19.6 MeV                                      2) -2.4 MeV                                      3) 8.4 MeV                                      4) 17.3 MeV
10. One milligram of matter is converted into energy, the energy released will be
- 1) 90 J                                      2)  $9 \times 10^3 \text{ J}$                                       3)  $9 \times 10^5 \text{ J}$                                       4)  $9 \times 10^{10} \text{ J}$

### SECTION - II

#### Numerical Type Questions

11. Calculate the nuclear radius of  ${}^{125}_{54}\text{Xe}$  knowing that the nuclear radius of  ${}^{27}_{13}\text{Al}$  is 3.6 fermi. (Answer in fermi)
12. The radionuclide  ${}^{11}_6\text{C}$  decays by  $\beta^+$  emission. Write symbolically this decay process.
- Given that
- $$m({}^{11}_6\text{C}) = 11.011434 \text{ u}$$
- $$m({}^{11}_6\text{B}) = 11.009305 \text{ u}$$
- $$m_e = 0.000548 \text{ u}, 1 \text{ u} = 931.5 \text{ MeV} / c^2$$
- then  $Q$  value is nearly \_\_\_\_\_ MeV.
13. An electron in a hydrogen atom undergoes a transition from an orbit with quantum number  $n_i$  to another with quantum number  $n_f$ .  $V_i$  and  $V_f$  are respectively the initial and final potential energies of the electron.
- If  $\frac{V_i}{V_f} = 6.25$ , then the smallest possible  $n_f$  is:

### PART - II (JEE ADVANCED)

#### SECTION - III (Only one option correct type)

14. A metal plate is exposed to light with wavelength  $\lambda$ . It is observed that electrons are ejected from the surface of the plate. When a retarding uniform electric field  $E$  is imposed, no electron can move away from the plate farther than a certain distance  $d$ . Then the threshold wavelength  $\lambda_0$  for the material of plate is ( $e$  is the electronic charge,  $h$  is Planck's constant and  $c$  is the speed of light)

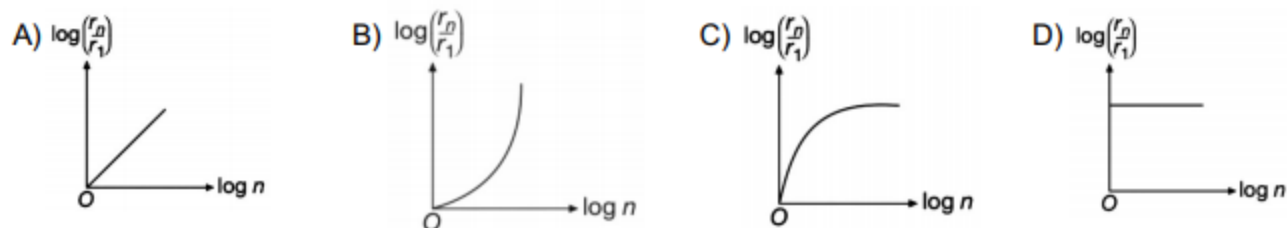
A)  $\lambda_0 = \left( \frac{1}{\lambda} - \frac{hc}{eEd} \right)^{-1}$       B)  $\lambda_0 = \left( \frac{1}{\lambda} - \frac{eEd}{hc} \right)^{-1}$       C)  $\lambda_0 = \lambda - \frac{hc}{eEd}$       D)  $\lambda_0 = \lambda - \frac{eEd}{hc}$



15. A charged particle  $q$  of mass  $m$  is projected along the  $y$ -axis at  $t = 0$  from origin with a velocity  $v_0$ . If a uniform electric field  $E$  also exists along the  $x$ -axis, then the time at which de-Broglie wavelength of the particle becomes half of the initial value is

A)  $\frac{mv_0}{qE}$       B)  $2\left(\frac{mv_0}{qE}\right)$       C)  $\sqrt{3}\left(\frac{mv_0}{qE}\right)$       D)  $3\left(\frac{mv_0}{qE}\right)$

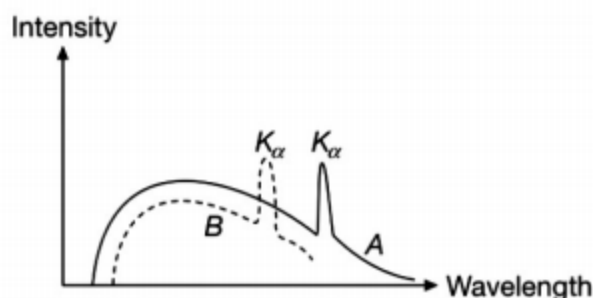
16. In hydrogen atom, the radius of  $n^{\text{th}}$  Bohr orbit is  $r_n$ . The graph between  $\log\left(\frac{r_n}{r_1}\right)$  and  $\log n$  will be



17. The ratio of the maximum wavelength of the Lyman series in hydrogen spectrum to the maximum wavelength in the Paschen series is

A)  $\frac{3}{105}$       B)  $\frac{6}{15}$       C)  $\frac{52}{7}$       D)  $\frac{7}{108}$

18. The figure represents the observed intensity of X-rays emitted by two different tubes A and B as a function of wavelength  $\lambda$ . For the tube A, the potential difference between the filament and target is  $V_A$  and atomic number of target is  $Z_A$ . For the tube B, corresponding potential difference is  $V_B$  and the atomic number is  $Z_B$ . The solid curve is for tube A and dotted curve for tube B, then

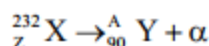


A)  $Z_A > Z_B, V_A > V_B$       B)  $Z_A = Z_B, V_A = V_B$       C)  $Z_A < Z_B, V_A > V_B$       D)  $Z_A < Z_B, V_A < V_B$

19. There are two radio nuclei A and B out of which A is an alpha emitter and B is a beta emitter. Their disintegration constants are in the ratio of 1:2. The ratio of number of atoms of A and B at any time  $t$  so that probabilities of getting alpha and beta particles are same at that instant is

A) 1 : 2      B) 1 : e      C) 2 : 1      D) e : 1

20. A nucleus X initially at rest, undergoes alpha decay according to the equation



What fraction of the total energy released in the decay will be the kinetic energy of the alpha particle?

- A)  $\frac{90}{92}$                       B)  $\frac{228}{232}$                       C)  $\sqrt{\frac{228}{232}}$                       D)  $\frac{1}{2}$
21. The binding energy per nucleon of  ${}_1\text{H}^2$  and  ${}_2\text{He}^4$  are 1.1 eV and 7 MeV respectively. The energy released in the process  ${}_1\text{H}^2 + {}_1\text{H}^2 = {}_2\text{He}^4$  is
- A) 20.8 MeV                      B) 16.6 MeV                      C) 25.2 MeV                      D) 23.6 MeV

#### **SECTION - IV (More than one correct answer)**

22. Radiations of monochromatic waves of wavelength 400nm are made incident on the surface of metals Zn, Fe and Ni of work functions 3.4 eV, 4.8 eV and 5.9 eV respectively (take  $hc = 12400 \text{ eV } \overset{\circ}{\text{A}}$ )
- A) maximum KE associated with photoelectrons from the surface of any metal is 0.3eV
- B) no photoelectrons are emitted from the surface of Ni
- C) if the wavelength of source of radiation is doubled then KE of photoelectrons is also doubled
- D) photoelectrons will be emitted from the surface of all the three metals if the wavelength of incident radiations is less than 200nm
23. The radius of the orbit of an electron in a Hydrogen like atom is  $4.5 a_0$ , where  $a_0$  is the Bohr radius. Its orbital angular momentum is  $\frac{3h}{2\pi}$ . It is given that  $h$  is Planck constant and  $R$  is Rydberg constant. The possible wavelength(s), when the atom de-excites, is (are)
- A)  $\frac{9}{32R}$                       B)  $\frac{9}{16R}$                       C)  $\frac{9}{5R}$                       D)  $\frac{4}{3R}$
24. A photon collides with a stationary hydrogen atom in ground state inelastically. Energy of the colliding photon is 10.2eV. After a time interval of the order of macro second another photon collides with same hydrogen atom inelastically with an energy of 15eV. What will be observed by the detector?
- A) 2 photon of energy 10.2eV
- B) 2 photon of energy 1.4 eV
- C) One photon of energy 10.2eV and an electron of energy 1.4 eV
- D) One photon of energy 10.2 eV and another photon of energy 1.4 eV

25. Consider two radioactive samples A and B. Their respective half lives are 1 hour and 2 hours. Initially their mass ratio is 3:4, initial activity of A is 5 units. The ratio of their atomic masses is 6:7. After 8 hours
- A) ratio of their masses is 3:64  
B) ratio of their masses is 7:58  
C) the activity of B is  $\frac{5}{28}$  units  
D) the activity of B is  $\frac{3}{14}$  units
26. Polonium  ${}_{84}\text{Po}^{210}$  emits  $\alpha$  – particles and is converted into  ${}_{82}\text{Pb}^{206}$ . This reaction is used for producing electric power in a space mission.  $\text{Po}^{210}$  has half life of 138.6 days. Assuming an efficiency of 10%. Select the correct statement(s)
- Given :  $M(\text{Po}^{210}) = 209.98264 \text{ amu}$ ;  $M(\alpha) = 4.0026 \text{ amu}$   $M(\text{Pb}^{206}) = 205.97440 \text{ amu}$  ;  
 $1 \text{ amu} = 931 \text{ MeV energy}$
- A) 10g  $\text{Po}^{210}$  is required to produce  $1.2 \times 10^7$  Joule energy  
B) Decay constant of  $\text{Po}^{210}$  is  $0.005 \text{ day}^{-1}$   
C) Q-value of  $\alpha$  – decay process is  $8.4 \times 10^{-13} \text{ J}$   
D) None of these is correct

**SECTION - V (Numerical Type - Upto two decimal place)**

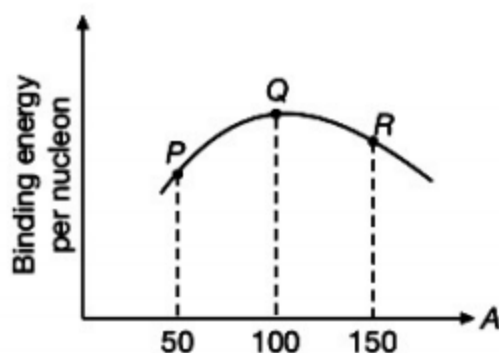
27. An electron in an excited state of  $\text{Li}^{2+}$  ion has angular momentum  $\frac{3h}{2\pi}$ . The de-Broglie wavelength of the electron in this state is  $p \pi a_0$  (where  $a_0$  is the Bohr radius). The value of  $p$  is
28. Light from a discharge tube containing hydrogen atoms falls on a piece of sodium due to the transition of electron from 4<sup>th</sup> orbit to 2<sup>nd</sup> orbit. Work function of sodium is 1.83 eV. The fastest moving photoelectron is allowed to enter in a magnetic field, which is perpendicular to the direction of motion of photoelectron as shown in figure. Find distance (in  $\mu\text{m}$ ) covered by the electron in the magnetic field. [ $B=1$  Tesla,  $\pi^2 = 10$ , mass of electron  $= 9 \times 10^{-31}$  kg] where  $R$  is the radius of the path that the most energetic electron takes in the presence of applied magnetic field.



29. Nuclei A and B convert into a stable nucleus C. Nucleus A is converted into C by emitting 2  $\alpha$  – particles and 3  $\beta$  – particles. Nucleus B is converted into C by emitting one  $\alpha$  – particles and 5 – particles. At time  $t=0$ , nucleus of A are  $4N_0$  and nuclei of B are  $N_0$ . Initially number of nuclei of C are zero. Half life of A (into conversion of C) is 1min and that of B is 2 min. Find the time (in minutes) at which rate of disintegration of A and B are equal
30. The radioactivity of a sample is  $R_1$  at a time  $T_1$  and  $R_2$  at a time  $T_2$ . If the half-life of the specimen is  $T$ , the number of atoms that have disintegrated in the time  $(T_2 - T_1)$  is equal to  $\frac{n(R_1 - R_2)T}{\ln 4}$ . Here  $n$  is some integral number. What is the value of  $n$ ?

### SECTION - VI (Matrix Matching)

31. Corresponding to the graph of binding energy per nucleon vs mass number (A) shown in figure, match the following two columns



Column -I	Column-II
A) $P + P \rightarrow Q$	p) Energy is released
B) $P + P + P \rightarrow R$	q) Energy is absorbed
C) $P + R \rightarrow 2Q$	r) No energy transfer will take place
D) $P + Q \rightarrow R$	s) Data insufficient