

CHAPTER - 02

STRUCTURE OF ATOM

1. 3 Atomic number = no. of protons

Mass number = no. of protons + no. of neutrons

∴ Nucleus contains 11 protons and 12 neutrons

2. 4 Particle Charge Mass (approx.)

e -1 0 u

p 1 1 u

n 0 1 u

α 2 4 u

∴ order of e/m ratio is $n < \alpha < p < e$

3. 2 $E = \frac{hc}{\lambda}$ or $E \propto \frac{1}{\lambda}$

$$\text{Thus, } \frac{E_1}{E_2} = \frac{\lambda_2}{\lambda_1} = \frac{16000 \text{ \AA}}{8000 \text{ \AA}} = 2 \Rightarrow E_1 = 2E_2$$

4. 3 Electrons are ejected when frequency of incident light crosses the threshold value (ν_0)

5. 2 Both assertion and reason are true but reason is not the correct explanation of assertion. The difference between the energies of adjacent energy levels decreases as we move away from the nucleus. Thus in H atom
 $E_2 - E_1 > E_3 - E_2 > E_4 - E_3, \dots$

6. 3
$$\frac{1}{\lambda_{\min}} = R_H \left[\frac{1}{2^2} - \frac{1}{\infty^2} \right] = \frac{R_H}{4}$$

$$\frac{1}{\lambda_{\max}} = R_H \left[\frac{1}{2^2} - \frac{1}{3^2} \right] = \frac{5R_H}{36}$$

Thus, $\frac{\lambda_{\max}}{\lambda_{\min}} = \frac{9}{5}$

7. 1 $n_{\text{higher}} = 11$ and $n_{\text{lower}} = 1$

Number of uv radiations = 10

Number of visible radiations = 9

$$\text{Number of infrared radiations} = \text{Total radiations} - (10 + 9) = \frac{11 \times 10}{2} - 19 = 36$$

$$\text{Thus, } Z - (x + y) = 36 - (10 + 9) = 17$$

8. 2 $r \propto \frac{n^2}{Z}; \frac{r_{\text{He}^+}}{r_{\text{Be}^{3+}}} = \frac{2^2/2}{3^2/4} = \frac{8}{9} \Rightarrow r_{\text{Be}^{3+}} = \frac{9}{8} r_{\text{He}^+}$

9. 1 $2\pi r_n = n\lambda$ and $r_n = a_0 \frac{n^2}{Z}$

$$\lambda = \frac{2\pi r_n}{n} = \frac{2\pi a_0 n}{Z} = x\pi a_0$$

$$\text{Thus, } x = \frac{2}{3}$$

10. 4 According to Heisenberg's principle, exact position and exact velocity of an electron cannot be determined simultaneously. Also, $\Delta x \cdot \Delta p \geq \frac{h}{4\pi}$

11. 1 $\Delta p = m \times \Delta v$

$$\Delta p = 9.1 \times 10^{-28} \times 3.0 \times 10^4 \times \frac{0.001}{100}$$

$$\Delta p = 2.73 \times 10^{-24}$$

$$\text{Hence } \Delta x = \frac{h}{\Delta p \times 4\pi} = \frac{6.626 \times 10^{-27}}{2.73 \times 10^{-24} \times 4 \times 3.14}$$

$$\Delta x = 1.92 \text{ cm}$$

12. 3 Number of radial nodes = $n - \ell - 1$

$$\text{Number of angular nodes} = \ell$$

$$\text{Thus, number of radial nodes of 5s orbital} = 5 - 0 - 1 = 4$$

$$\text{Number of angular nodes of } 3d_{yz} \text{ orbital} = 2$$

$$\text{Total number of nodes of } 4d_{xy} \text{ orbital} = (4 - 2 - 1) + (2) = 3 \text{ and number of radial nodes of } 3p \text{ orbital} = 3 - 1 - 1 = 1$$

13. 3 In chromium 19th electron is present in 4s orbital
14. 1 'yz'-plane is a node for p_x orbital
15. 4 Value of $|\psi|^2$ is maximum at $r = 0$, thus it is an 's' orbital. It has only one radial node, thus it is a '2s' orbital.
16. 1 Energy of a given orbital decreases with increase in the atomic number.
17. 2 Energy of incident light = $h\nu = 6.6 \times 10^{-34} \times 5.8 \times 10^{14} \times 6.24 \times 10^{18} = 2.38 \text{ eV}$.
Thus, metals Na and K only can give photocurrent with 2.38 eV photons
18. 54

$$E_n = \frac{-13.6 Z^2}{n^2}$$

For $\text{Be}^{3+} \Rightarrow Z = 4$

First excited state $n = 2$

$$E_n = \frac{-13.6 \times 4^2}{2^2} = -13.6 \times 4 = -54.4 \text{ eV}$$

19. 3 $n - \ell - 1 = 2$ and $\ell = 0 \Rightarrow n = 3$
20. 25 No. of orbitals in a shell = n^2

21. C

$$n_2 + n_1 = 4 \quad \text{--- (1)}$$

$$n_2^2 - n_1^2 = 8 \quad \text{--- (2)}$$

From eqn (2)

$$(n_2 - n_1)(n_2 + n_1) = 8$$

$$n_2 - n_1 = \frac{8}{4} = 2 \quad \text{--- (3)}$$

From (1) and (3)

$$2n_2 = 6$$

$$n_2 = 3$$

$$\therefore n_1 = 1$$

Transition is $n_2 = 3 \rightarrow n_1 = 1$

$$\frac{1}{\lambda} = R_H (2)^2 \left[\frac{1}{1^2} - \frac{1}{3^2} \right]$$

$$= 4R_H \left[1 - \frac{1}{9} \right]$$

$$= 4R_H \times \frac{8}{9}$$

$$\lambda = \frac{9}{32R_H}$$

22.

$$R_3 = \frac{q_0(3)^2}{3} = 3q_0 = X$$

$$q_0 = \frac{X}{3}$$

$$\lambda = \frac{2\pi R_1}{n} = \frac{2\pi q_0 (1)^2}{3 \times 1}$$

$$= \frac{2\pi q_0}{3} = \frac{2\pi X}{9}$$

23. C

$$\begin{aligned}
 F &= \frac{hc}{\lambda} = \frac{2 \times 10^{-25}}{4000 \times 10^{-10}} \text{ J} \\
 &= 0.5 \times 10^{-18} \text{ J} \\
 &= 5 \times 10^{-19} \text{ J} = 30.11 \times 10^4 \text{ J mol}^{-1} \\
 &= 301.1 \text{ kJ mol}^{-1}
 \end{aligned}$$

$$\text{BDE} = 246.5 \text{ kJ mol}^{-1}$$

$$\text{KE} = E - \text{BDE} = 301.1 - 246.5 = 54.6 \text{ kJ mol}^{-1}$$

$$\begin{aligned}
 \% \text{ Energy Converted into KE} &= \frac{54.6}{301.1} \\
 &= 18\%
 \end{aligned}$$

24. C

$$E_f = -E$$

$$\begin{aligned}
 \text{KE} &= \frac{1}{2} mv^2 \\
 v &= \sqrt{\frac{2 \text{KE}}{m}}
 \end{aligned}$$

$$\text{But KE} = h\nu - h\nu_0$$

$$E_f(4^{2+}) = \frac{-E(3)^2}{1} = -9E$$

$$\therefore \nu_0 = 9E$$

$$\text{KE} = E_p - 9E$$

$$\therefore v = \sqrt{\frac{2(E_p - 9E)}{m}}$$

25. A

$$\text{KE}_1 = x \quad \text{PE}_1 = -2x$$

$$\text{KE}_2 = \frac{x}{4} \quad \text{PE}_2 = -\frac{2 \times x}{4} = -\frac{x}{2}$$

$$\Delta \text{PE} = -\frac{x}{2} - (-2x) = -\frac{x}{2} + 2x = \frac{3x}{2}$$

26. B

$$\begin{aligned}
 mvr &= \frac{n h}{2\pi} = 3.1652 \times 10^{-34} \\
 n \times 1.05 \times 10^{-34} &= 3.1652 \times 10^{-34} \\
 n &= 3 \\
 n_2 = 3 &\longrightarrow n_1 = 2 \\
 \bar{\nu} &= R_H (2)^2 \left[\frac{1}{2^2} - \frac{1}{3^2} \right] \\
 &= 4 R_H \left[\frac{1}{4} - \frac{1}{9} \right] = 4 R_H \times \frac{5}{36} \\
 &= \frac{5 R_H}{9}
 \end{aligned}$$

27. B

$$\begin{aligned}
 \lambda &= \frac{h}{mv} = \frac{h}{\sqrt{2mKE}} \\
 KE &= h(\nu - \nu_0) \\
 \therefore \lambda &= \frac{h}{\sqrt{2mh(\nu - \nu_0)}} \\
 \therefore \lambda &\propto \frac{1}{(\nu - \nu_0)^{1/2}}
 \end{aligned}$$

28. ABC

$$\begin{aligned}
 E &= -\frac{Ze^2}{2a} \\
 \text{At } a &= a_0 \\
 E_1 &= -\frac{Ze^2}{2a_0} \\
 \text{At } a &= 2a_0 \\
 E_2 &= \frac{-Ze^2}{2(2a_0)} = -\frac{Ze^2}{4a_0} \\
 E_2 &> E_1
 \end{aligned}$$

29. AC

30. AD

$$\begin{aligned}
 E_3 &= E_1 + E_2 \\
 h\nu_3 &= h\nu_1 + h\nu_2 \\
 \nu_3 &= \nu_1 + \nu_2 \\
 \text{Also } \frac{hc}{\lambda_3} &= \frac{hc}{\lambda_1} + \frac{hc}{\lambda_2} \\
 \frac{1}{\lambda_3} &= \frac{1}{\lambda_1} + \frac{1}{\lambda_2} \\
 \lambda_3 &= \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2}
 \end{aligned}$$

31. BC

$$\begin{aligned}
 RE &= \frac{a_0 n^2}{Z} \times -\frac{R_H Z^2}{n^2} \\
 &= -a_0 R_H Z \\
 \nu_R &= \frac{\nu_0 Z}{n} \times \frac{a_0 n^2}{Z} \\
 &= \nu_0 a_0 n \\
 \therefore \nu_R &\propto n \\
 \frac{\nu}{E} &= \frac{\nu_0 Z \times n^2}{n \times -R_H (Z^2)} \\
 \frac{\nu}{E} &\propto n \\
 \frac{\nu}{E} &= \frac{a_0 n^2 \times n^2}{Z \times -R_H Z^2} \\
 \frac{\nu}{E} &\propto n^4
 \end{aligned}$$

32. 3.00

$$n \rightarrow n=2$$

$$E_1: 10.2 + 17.0 = 27.2 \text{ eV} = \frac{hc}{\lambda_1}$$

$$\frac{1}{\lambda_1} = R_H Z^2 \left[\frac{1}{2^2} - \frac{1}{n^2} \right]$$

$$\frac{27.2}{hc} = R_H Z^2 \left[\frac{1}{4} - \frac{1}{n^2} \right] \quad \text{--- (1)}$$

$$n \rightarrow n=3$$

$$E_2 = 4.25 + 5.95 = 10.20 \text{ eV} = \frac{hc}{\lambda_2}$$

$$\frac{10.2}{hc} = R_H Z^2 \left[\frac{1}{9} - \frac{1}{n^2} \right] \quad \text{--- (2)}$$

$$\textcircled{1}/\textcircled{2} \Rightarrow \frac{27.2}{10.2} = \frac{\frac{1}{4} - \frac{1}{n^2}}{\frac{1}{9} - \frac{1}{n^2}}$$

$$\frac{27.2}{9} - \frac{27.2}{n^2} - \frac{10.2}{4} + \frac{10.2}{n^2} = 0$$

$$\frac{-17}{n^2} + \frac{17}{36} = 0$$

$$-\frac{1}{n^2} = -\frac{1}{36}$$

$$n=6$$

Sub $n=6$ in eqn (1)

$$\frac{27.2}{hc} = R_H (Z^2) \left[\frac{1}{2^2} - \frac{1}{6^2} \right]$$

$$27.2 = hc R_H (Z^2) \left[\frac{1}{4} - \frac{1}{36} \right]$$

$$27.2 = 13.6 (Z^2) \left[\frac{8}{36} \right]$$

$$Z^2 = \frac{27.2 \times 36}{13.6 \times 8} = \frac{2 \times 36}{8 \times 4} = 9$$

$$Z = \underline{\underline{3}}$$

33. 2.00

$$\begin{aligned} \text{At } r_0, \\ \psi_{2s}^2 &= \left[\frac{1}{4\sqrt{2}\pi} \left(\frac{1}{a_0} \right)^{3/2} \left(2 - \frac{r_0}{a_0} \right) e^{-\frac{r_0}{a_0}} \right]^2 = 0 \\ \Rightarrow \left(2 - \frac{r_0}{a_0} \right)^2 &= 0 \\ 2 &= \frac{r_0}{a_0} \end{aligned}$$

34. B

35. C