## **Calculations**

zBeta: 
$$z_{\beta} = \phi^{-1}(p)$$

Estimated Test Average:  $\mu_1 = \mu_0(1 + m)$ 

## No Bonferroni:

zAlpha: 
$$z_{\alpha} = \phi^{-1} (1 - \frac{1-c}{T})$$

Sample Size Required Per Recipe:  $n = \frac{(z_{\alpha} + z_{\beta})^2 2\sigma^2}{(\mu_1 - \mu_0)^2}$ 

Total Sample Size Required:  $N_{total} = n(K + 1)$ 

Estimated Duration:  $D = \lceil \frac{N_{total}}{D} \rceil$ 

## With Bonferroni:

zAlpha: 
$$z_{\alpha,Bon} = \phi^{-1} (1 - \frac{1-c}{TK})$$

Sample Size Required Per Recipe:  $n_{bon} = \frac{(z_{\alpha,Bon} + z_{\beta})^2 2\sigma^2}{(\mu_1 - \mu_0)^2}$ 

Total Sample Size Required:  $N_{total,Bon} = n_{bon}(K + 1)$ 

Estimated Duration:  $D_{Bon} = \lceil \frac{N_{total,Bon}}{D} \rceil$ 

## Legend

 $c = \text{Confidence} \in (0, 1) \text{ This is } 1 - \alpha$ 

 $p = Power \in (0, 1)$  This is  $1 - \beta$ 

 $m = \text{MDE} \in (0, 1)$ : minimum detectable effect as a relative lift

 $T = \text{Tails} \in \{1, 2\}$ : One or Two-Tailed test

 $K = \text{Number of Test Variants} \in \mathbb{N} \text{ Number of test variants not including control}$ 

 $\mu_0 = \text{Mean Value} \in \mathbb{R}$ 

 $\sigma = \text{Standard Deviation} \in \mathbb{R}$ 

 $D = \text{Daily Traffic} \in \mathbb{R}^+$ 

 $\phi^{-1}(p)$  = Inverse of the normal distribution function. This Function takes a probability and returns the corresponding z.

Credits: Calculator by Geoffrey Wortham; Documentation by Merritt Aho

Github Repo: <a href="https://github.com/shongzahToo/continuous-sample-size-calculator">https://github.com/shongzahToo/continuous-sample-size-calculator</a>