The system

$$\begin{cases} y'' = -2 \\ y(-1) + y'(-1) & = 2 \\ y(1) + y'(1) & = -2 \end{cases}$$

has solution $y = 1 - x^2$