

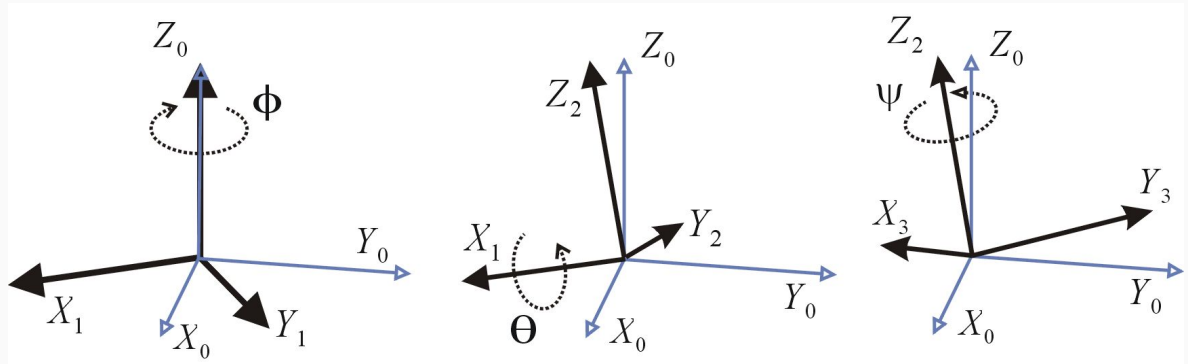
The background of the slide is a collage of four images related to materials science. The top-left image is a micrograph of a polycrystalline material with a complex, multi-colored grain structure. The top-right image shows a blue, textured surface, possibly a thin film or a crystal surface. The bottom-left image is a micrograph of a polycrystalline material with a clear, regular grain structure, featuring a scale bar labeled '30 μ'. The bottom-right image shows a blue, textured surface, similar to the top-right image, but with a different pattern of features.

# Modeling Grain Size Using Grain Orientation in Polycrystalline Materials

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**5/8/2024**

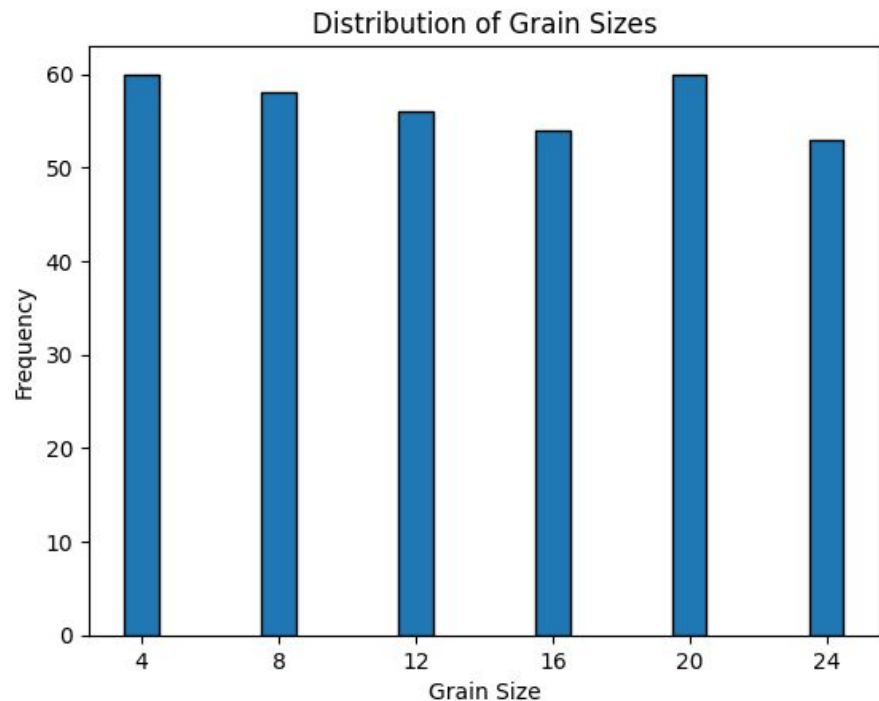
# Euler Angles and Grain Orientation

- 3 successive rotations (3-1-3) that transform a reference coordinate system to align with the grains micro axes
- Explain how a grain is oriented relative to material macro axes
- Describe non-uniform properties like directional strength and deformation behavior
- Question: Does the distribution of grain orientations correlate with grain size?



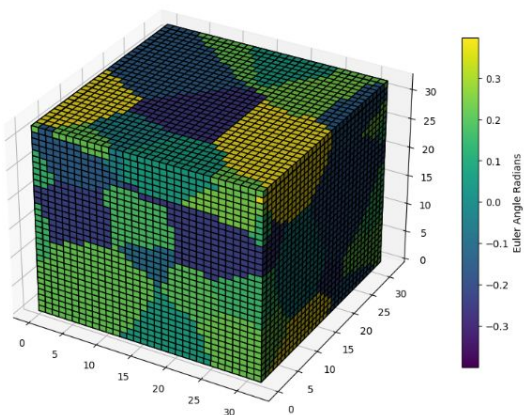
# Data Extraction and Preparation

- Dataset is synthetically created using NEPER at ORNL.
- Consists of 341 complete sample folders containing: .grn2 (grain ID), .ori (Euler angles) and grain size files.
- Reshaped 2D 1024 x 32 grain ID data into 3D 32 x 32 x 32 voxel arrays storing grain IDs.
- Included the 3 Euler angle rotations for each voxel forming 4D 32 x 32 x 32 x 3 arrays.

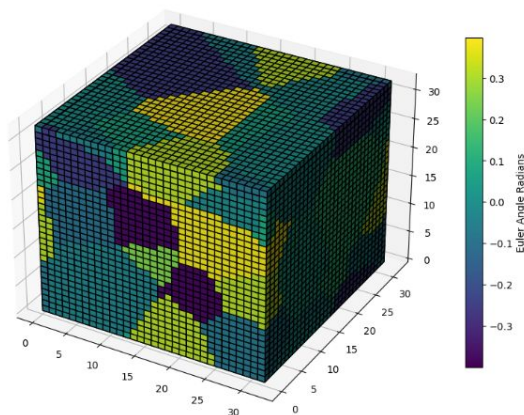


# Data Exploration

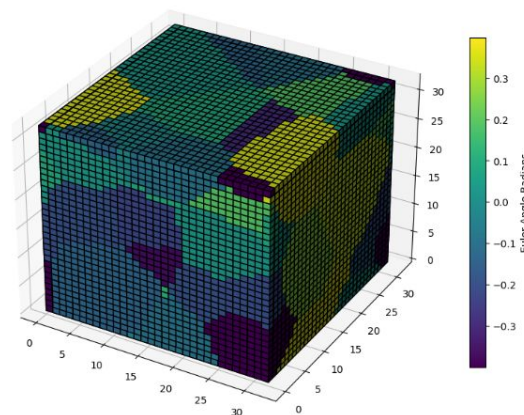
Sample 278 Euler Angle 1 with Grain Size 12



Sample 278 Euler Angle 2 with Grain Size 12

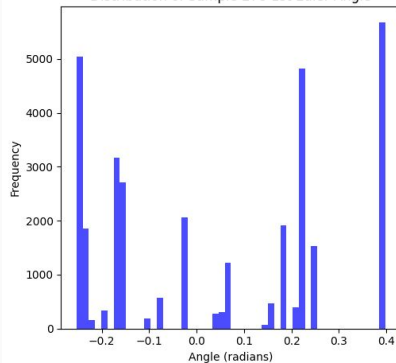


Sample 278 Euler Angle 3 with Grain Size 12

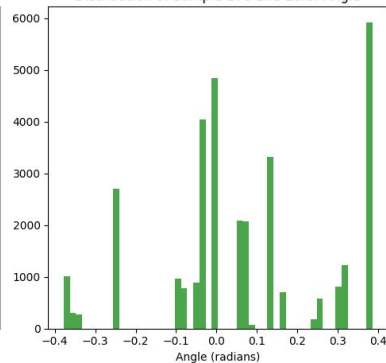


- Randomly selected Sample # 278
- Colorbar is Euler angles range  $-0.3, 0.3$  (radians) or  $-17, 17$  (degrees)
- Grain size for this sample = 12

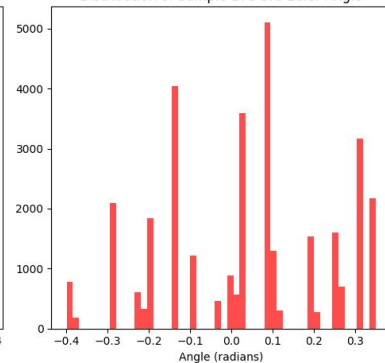
Distribution of Sample 278 1st Euler Angle



Distribution of Sample 278 2nd Euler Angle

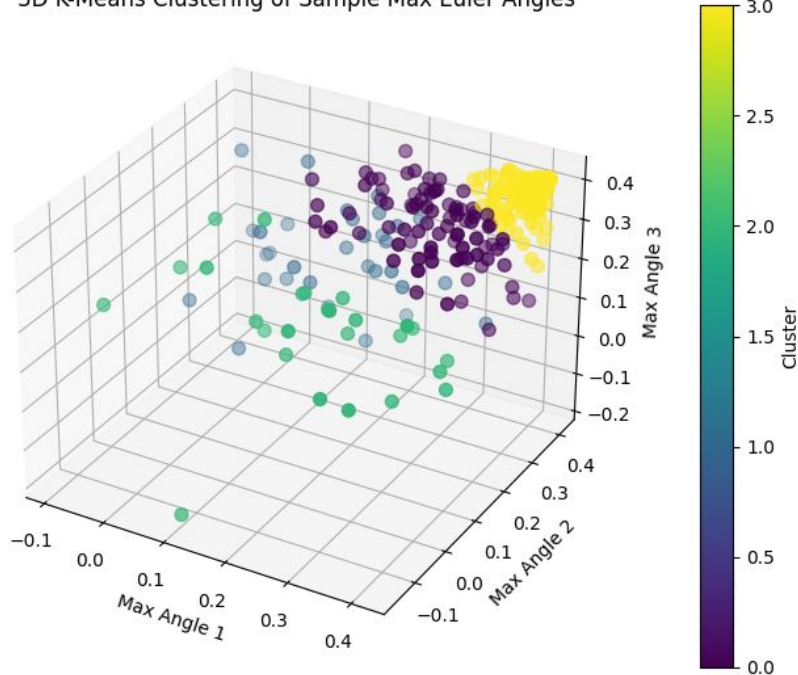


Distribution of Sample 278 3rd Euler Angle

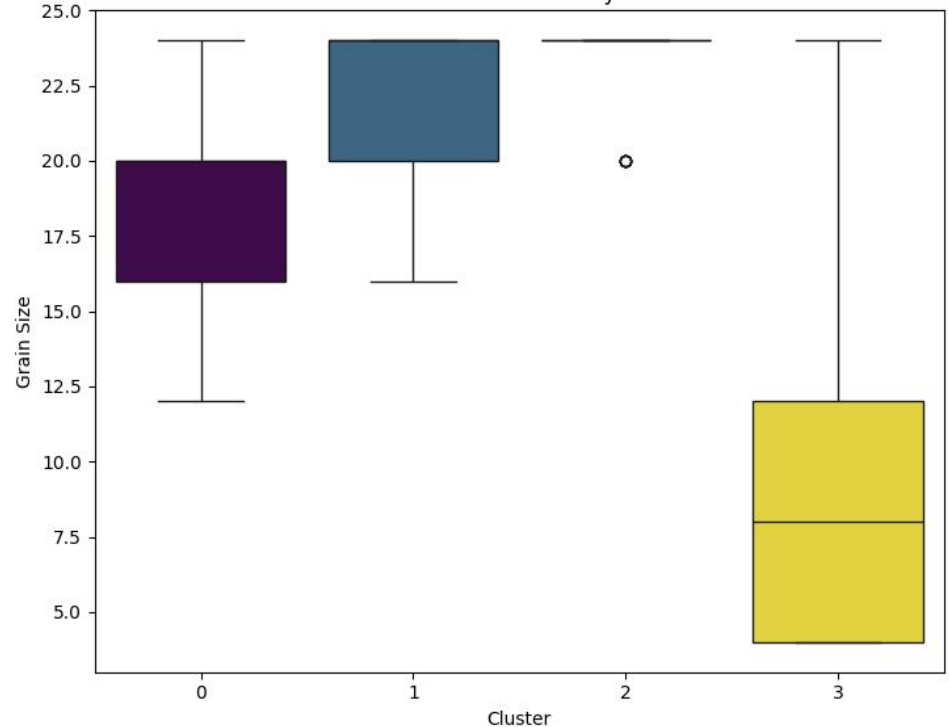


# Unsupervised Learning - K-Means Clustering

3D K-Means Clustering of Sample Max Euler Angles

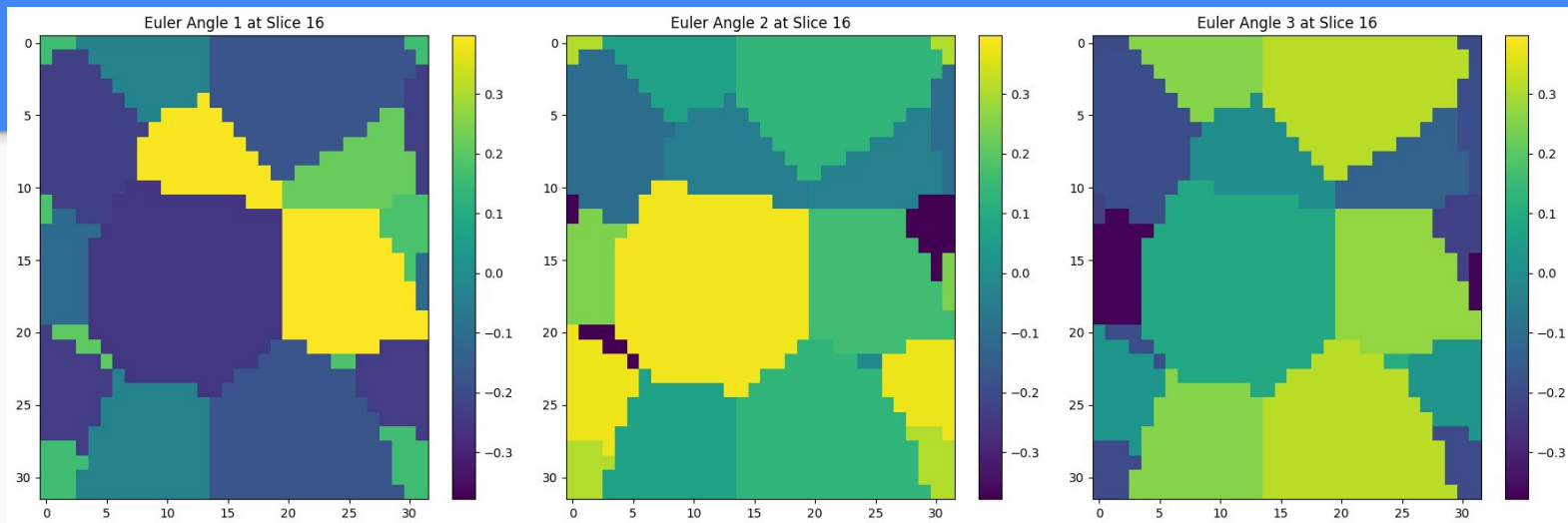


Grain Size Distribution by Cluster





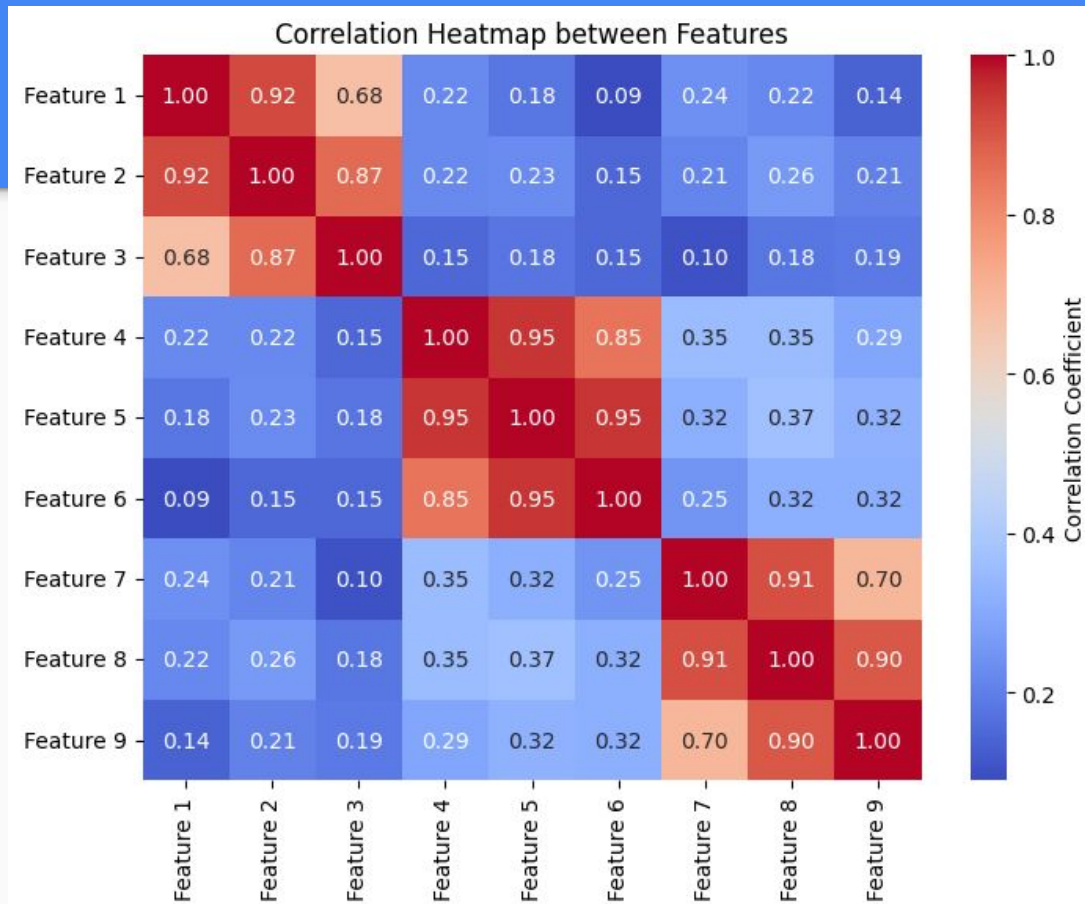
# Two-Point Correlation Statistics



- Take 2D center slice (#16) from 3D sample, define the distance between pairs to calculate statistics for  $\text{lag}_n = 4, 8, 16$
- Iterate through each voxel in the slice, compute correlation between original voxel and another voxel that is at the specified lag distance away and within the plane of the slice
- Calculate the correlations of all voxel pairs at  $\text{lag}_n$  by computing the product of the pair's Euler angles then take the average of those products for all pairs for each  $\text{lag}_n$  and
- Repeat process for each Euler angle orientation

# Why?

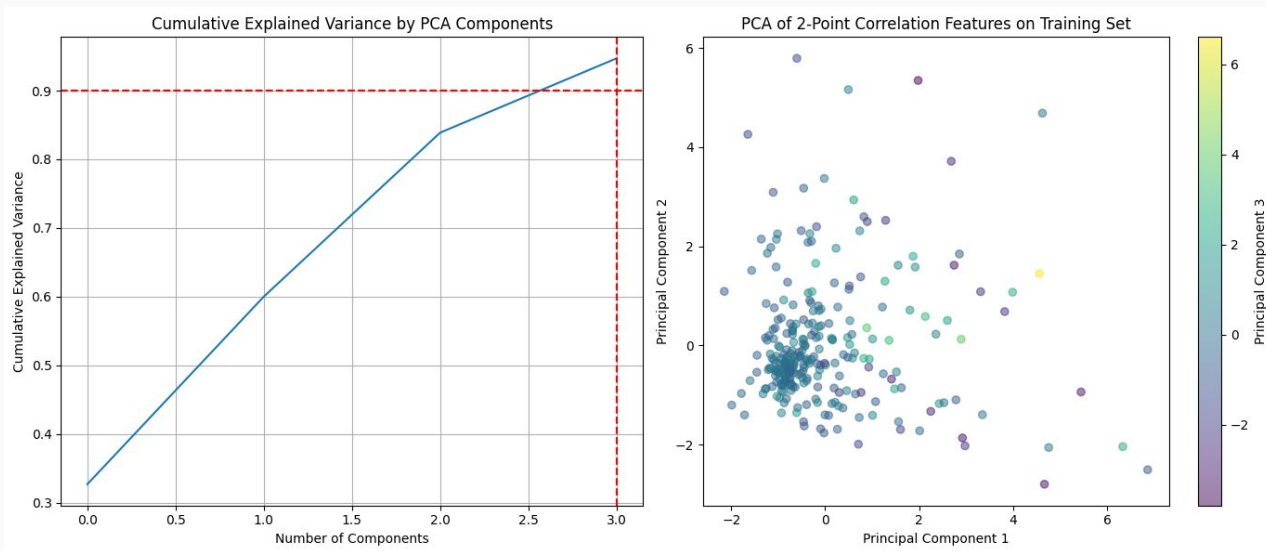
- Flattening the 341 sample's data from 32x32x32x3 to 1D yields 98,304 features, need another way to describe data
- Describes how the orientation of grains vary spatially for each angle orientation within the distance of 4, 8 and 16 voxels



# Principal Component Analysis (PCA)

Total number of principal components: 4

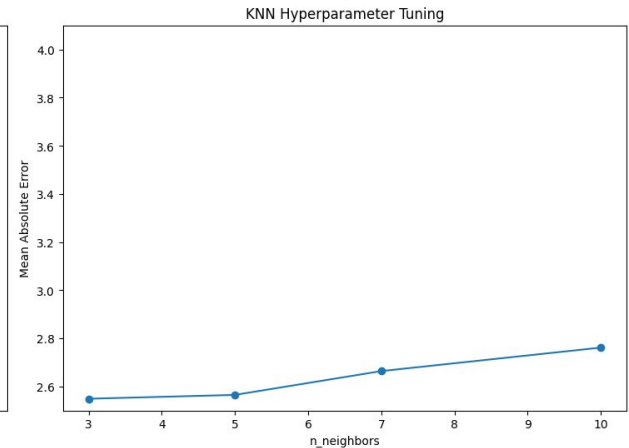
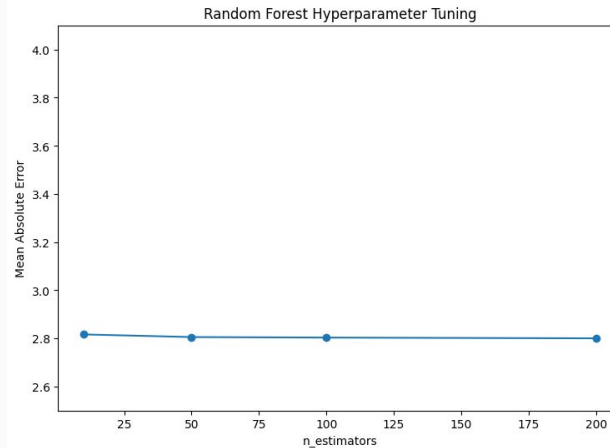
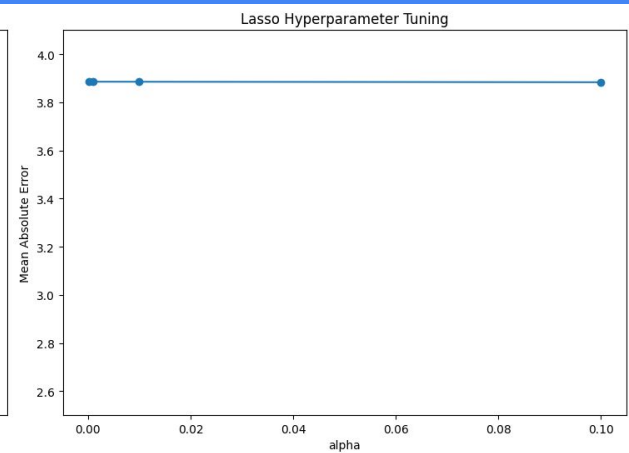
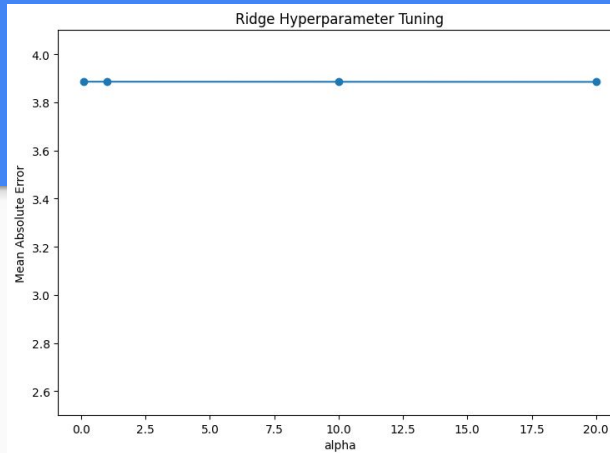
Explained variance by each component: [0.32677825 0.27318454 0.23887114 0.10820887]





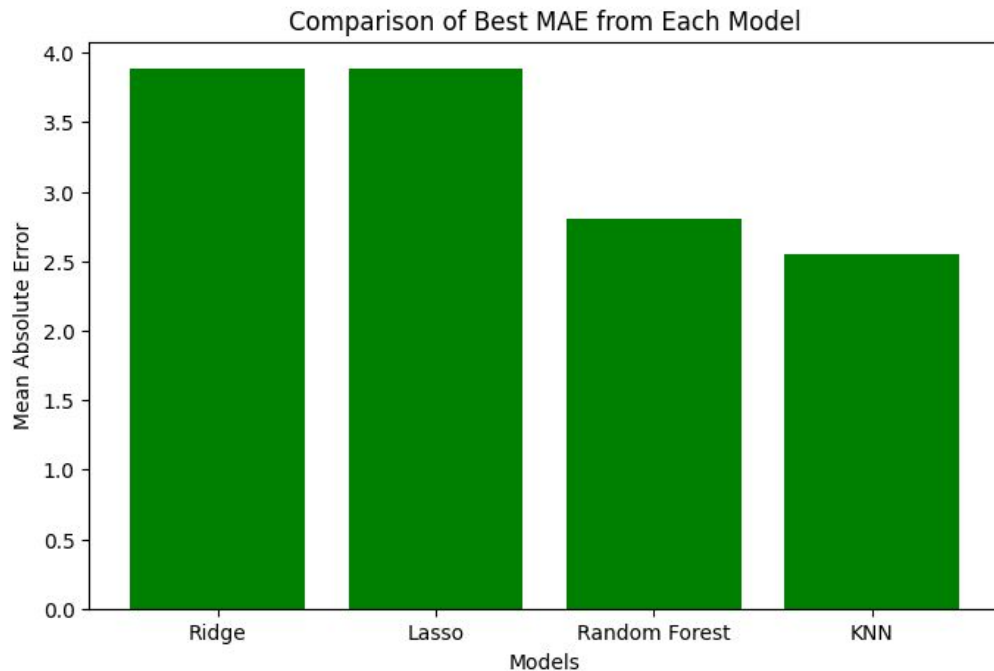
# Regression Models and Hyperparameter Tuning

- Ridge - alpha: large increases coef. shrinkage
- Lasso - alpha: large increases coef. shrinkage to 0
- Random Forest - n\_estimators: # of trees, more trees more complexity
- KNN - n\_neighbors: smaller is more flexible



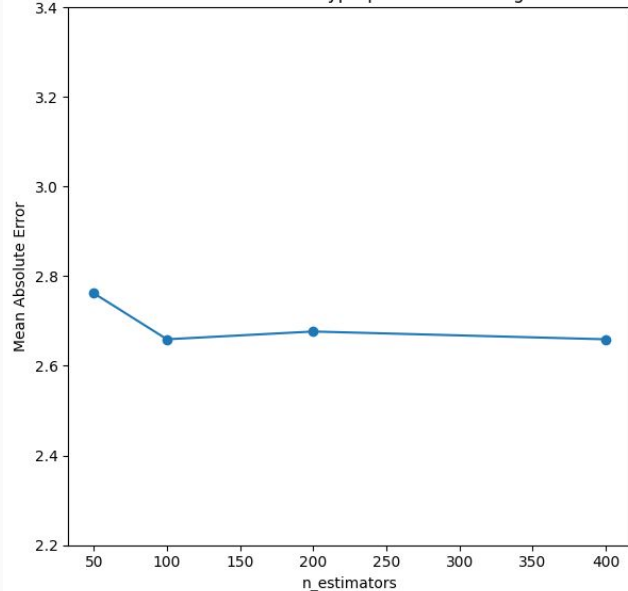
# Regression Model Performance

- Model = Ridge,  
Min MAE = 3.88,  
 $\alpha = 20$
- Model = Lasso,  
Min MAE 3.88,  
 $\alpha = 0.1$
- Model = Random Forest,  
Min MAE = 2.8,  
 $n\_estimators = 200$
- Model = KNN,  
Min MAE = 2.55,  
 $n\_neighbors = 3$

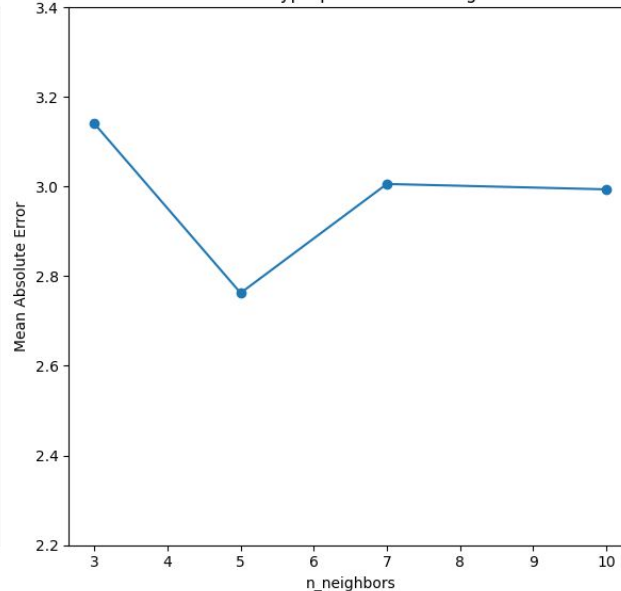


# Classification Model and Hyperparameter Tuning

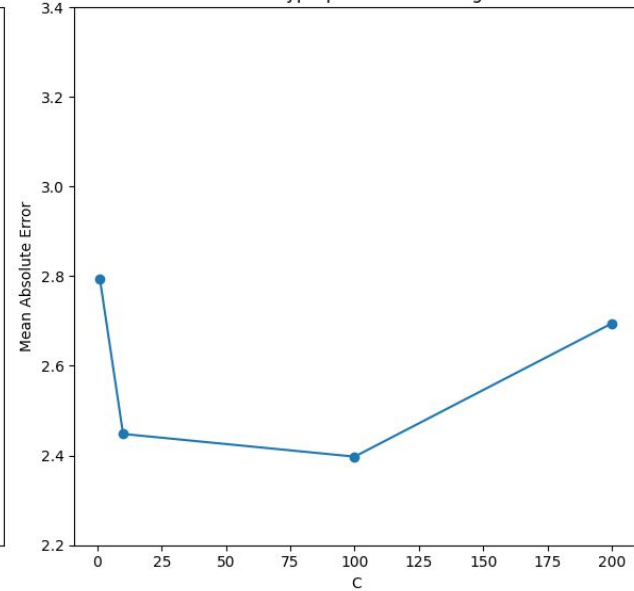
Random Forest Hyperparameter Tuning



KNN Hyperparameter Tuning

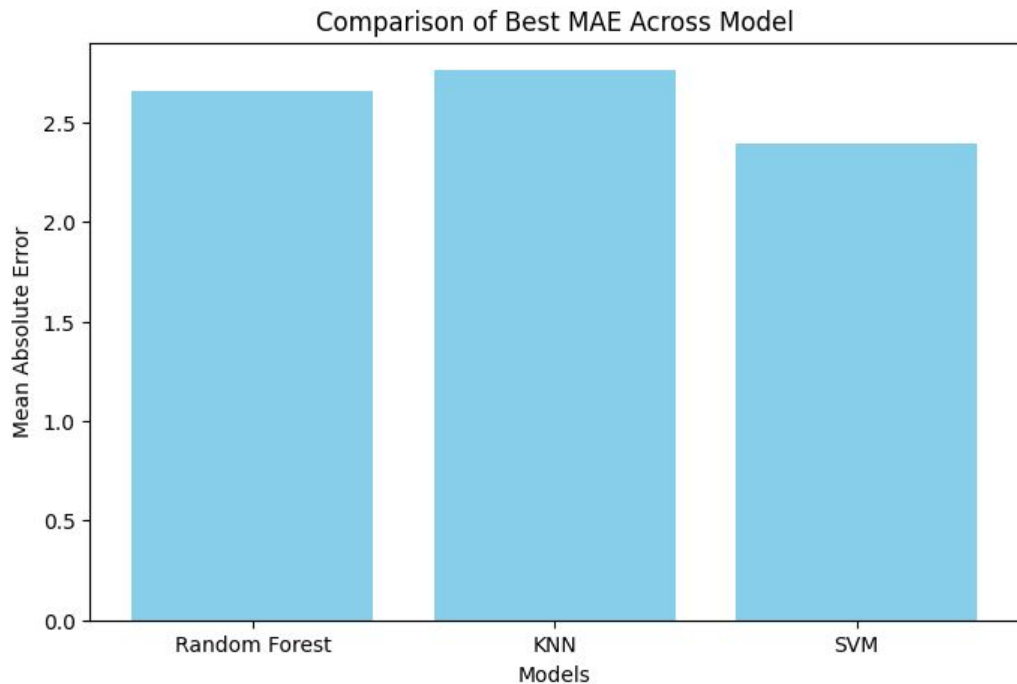


SVM Hyperparameter Tuning



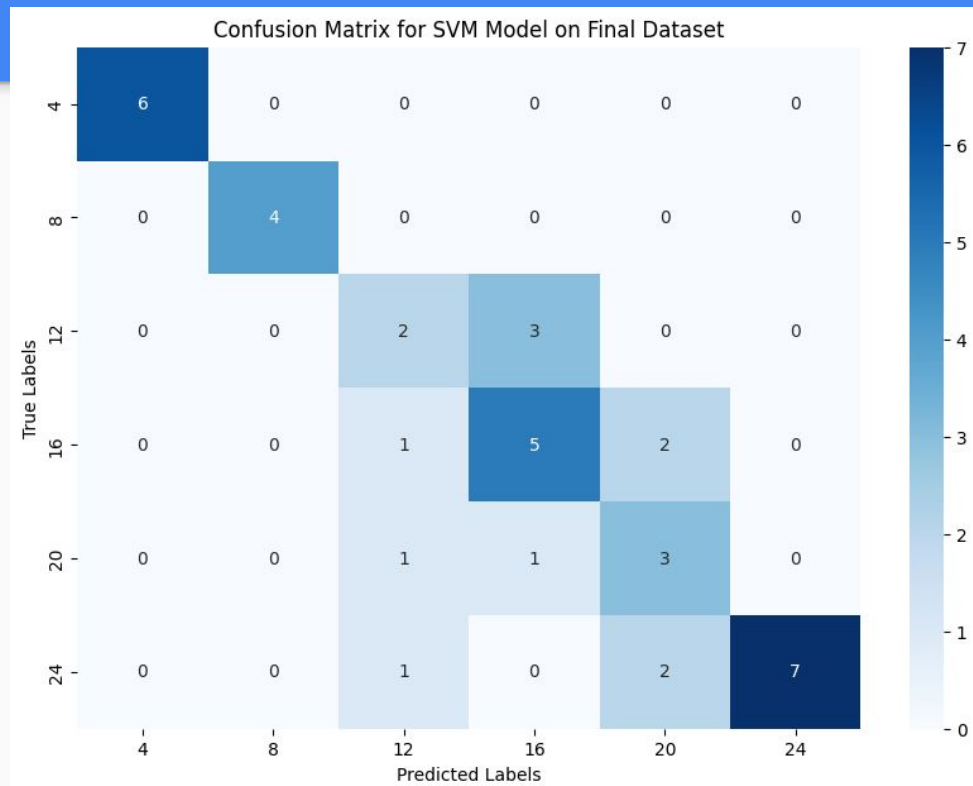
# Classification Model Performance

- Model = Random Forest,  
Min MAE = 2.66,  
n\_estimators = 400
- Model = KNN,  
Min MAE = 2.76,  
n\_neighbors = 5
- Model = SVM,  
Min MAE = 2.4,  
C = 100
- Higher C reg. to lower bias



# Mean Absolute Error and Final Results

- Why MAE?  $\frac{1}{n} \sum |y_i - \hat{y}_i|$
- Uses units of target, ordinal labels, classification and regression models
- MAE Test Data: 1.47
- Accuracy Test Data: .71
- Perfect at grain sizes 4, 8, okay at 24, bad at 12, 16, 20



# Q & A

- Project notebook: [Click here](#)
- References:
  - A Comparative Study of the Efficacy of Local/Global and Parametric/ Nonparametric Machine Learning Methods for Establishing Structure–Property Linkages in High-Contrast 3D Elastic Composites Patxi Fernandez-Zelaia, Yuksel C. Yabansu & Surya R. Kalidindi  
<https://par.nsf.gov/servlets/purl/10147978>
  - Microstructure informatics using higher-order statistics and efficient data-mining protocols <https://link.springer.com/article/10.1007/s11837-011-0057-7>