### K- means

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2. Please refer K-means example to calculate 2-cluster K-means for the following subjects

| Subject | A   | В   |
|---------|-----|-----|
| 1       | 1.5 | 1.0 |
| 2       | 1.0 | 2.0 |
| 3       | 2.0 | 3.5 |
| 4       | 5.0 | 6.0 |
| 5       | 3.5 | 4.0 |
| 6       | 4.5 | 5.0 |
| 7       | 2.5 | 4.5 |

#### **Solution:**

### Step 1:

Data: the scores of two variables on each of seven individuals

| Subject | A   | В   |
|---------|-----|-----|
| 1       | 1.5 | 1.0 |
| 2       | 1.0 | 2.0 |
| 3       | 2.0 | 3.5 |
| 4       | 5.0 | 6.0 |
| 5       | 3.5 | 4.0 |
| 6       | 4.5 | 5.0 |
| 7       | 2.5 | 4.5 |

#### Note:

- o Two known information before k-means clustering
  - The data in matrix format
  - Assuming that the data set is to be grouped into 2

# **Step 2: Initial Partition**

1. Calculate the centroid

| Subject | A   | В   | Centroid = (A+B)/2 |
|---------|-----|-----|--------------------|
| 1       | 1.5 | 1.0 | 1.25               |
| 2       | 1.0 | 2.0 | 1.5                |
| 3       | 2.0 | 3.5 | 2.75               |
| 4       | 5.0 | 6.0 | 5.5                |
| 5       | 3.5 | 4.0 | 3.75               |
| 6       | 4.5 | 5.0 | 4.75               |
| 7       | 2.5 | 4.5 | 3.5                |

- 2. Find the minimum and maximum centroids
- 3. Let the A & B values of the two individuals furthest apart (using the Euclidean distance measure), define the initial cluster means.

|         | Individual | Mean Vector (centroid) |
|---------|------------|------------------------|
| Group 1 | 1          | (1.5, 1.0)             |
| Group 2 | 4          | (5.0, 6.0)             |

# **Step 3: First clustering**

Process:

1. Calculate the distance of each subject and the 2 centroids

| Subject | A   | В   | Centroid = (A+B)/2 | Distance<br>from Centroid<br>1.25 | Distance<br>from Centroid<br>5.5 |
|---------|-----|-----|--------------------|-----------------------------------|----------------------------------|
| 1       | 1.5 | 1.0 | 1.25               | 0                                 | 4.25                             |
| 2       | 1.0 | 2.0 | 1.5                | 0.25                              | 4.0                              |
| 3       | 2.0 | 3.5 | 2.75               | 1.5                               | 2.75                             |
| 4       | 5.0 | 6.0 | 5.5                | 4.25                              | 0                                |
| 5       | 3.5 | 4.0 | 3.75               | 2.5                               | 1.75                             |
| 6       | 4.5 | 5.0 | 4.75               | 3.5                               | 0.75                             |
| 7       | 2.5 | 4.5 | 3.5                | 2.25                              | 2.0                              |

- 2. The remaining individuals are now examined in sequence and allocated to the cluster to which they are closest, in terms of Euclidean distance to the cluster mean.
- 3. The mean vector is recalculated each time a new member is added.

|      | Cluster 1  |                        | Cluster 2  |                        |
|------|------------|------------------------|------------|------------------------|
| Step | Individual | Mean Vector (centroid) | Individual | Mean Vector (centroid) |
| 1    | 1          | (1.0, 1.0)             | 4          | (5.0, 7.0)             |
| 2    | 1, 2       | (1.2, 1.5)             | 4          | (5.0, 7.0)             |
| 3    | 1, 2, 3    | (1.5, 2.16)            | 4          | (5.0, 7.0)             |
| 4    | 1, 2, 3    | (1.5, 2.16)            | 4, 5       | (4.2, 5.0)             |
| 5    | 1, 2, 3    | (1.5, 2.16)            | 4, 5, 6    | (4.3, 5.0)             |
| 6    | 1, 2, 3    | (1.5, 2.16)            | 4, 5, 6, 7 | (3.8, 4.8)             |

Note:

```
1.5 = (1.5 + 1.0 + 2.0) / 3
2.16 = (1.0 + 2.0 + 3.5) / 3
3.8 = (5.0 + 3.5 + 4.5 + 2.5) / 4
4.8 = (6.0 + 4.0 + 5.0 + 4.5) / 4
```

## Step 4: Check the result of the new clustering

Now the initial partition has changed, and the two clusters at this stage having the following characteristics:

|           | Individual | Mean<br>Vector<br>(centroid) |
|-----------|------------|------------------------------|
| Cluster 1 | 1, 2, 3    | (1.5, 2.16)                  |
| Cluster 2 | 4, 5, 6, 7 | (3.8, 4.8)                   |

## Step 5: Compare each individual's distance to the 2 clusters

But we cannot yet be sure that each individual has been assigned to the right cluster.

- So, we compare each individual's distance to its own cluster mean and to that
  of the opposite cluster. For example,
  - The distance between individual 1 and the centroid of Cluster 1
    - $sqrt((1.5 1.5)^2 + (2.16 1.0)^2) = 1.16$
  - The distance between individual 1 and the centroid of Cluster 2
    - sqrt  $((3.8 1.5)^2 + (4.8 1.0)^2) = 4.4$

| Individual | Distance to mean<br>(centroid) of<br>Cluster 1:<br>(1.5,2.16) | Distance to mean<br>(centroid) of<br>Cluster 2:<br>(3.8,4.8) |
|------------|---|--|
| 1          | 1.16  | 4.4  |
| 2          | 0.5   | 3.9  |
| 3          | 1.4   | 2.2  |
| 4          | 5.2   | 1.69   |
| 5          | 2.7   | 0.85   |
| 6          | 4.1   | 0.72   |
| 7          | 2.5   | 1.33   |