## MFE5130 – Financial Derivatives First Term, 2017-18 Midterm Examination

**Exam Duration: 2 hours** 

## Instruction

- 1. Total Marks: 100 points.
- 2. Answer **ALL** questions.
- 3. You must show all the steps in order to get full mark for each question.

1. (15 points) Consider the following two portfolios:

A: Buy a 108-strike European call option and sell a 109-strike European call option.

B: Buy a 109-strike European put option and sell a 108-strike European put option.

Let  $C_A(0)$  and  $C_B(0)$  be the cost at time 0 to construct Portfolio A and Portfolio B respectively.

You are given:

- (i)  $C_A(0) = 0.3$ .
- (ii) All the options in the above two portfolios are 1-year to expiration and are on the same non-dividend paying stock.
- (iii) The continuously compounded annual risk-free interest rate is 22%. Determine  $C_B(0)$ .
- 2. Suppose the dollar-denominated interest rate is 6%, the yen-denominated interest rate is 2% (both rates are continuously compounded), the spot exchange rate is 0.008\$/¥, and the price of a dollar-denominated European yen **put** with 1 year to expiration and a strike price of \$0.008 is \$0.0009.
  - a. (8 points) Consider a dollar-denominated European yen **call** with 1 year to expiration and a strike price of \$0.008, what is the price of this call option such that there is no arbitrage opportunity?
  - b. (10 points) Suppose that a 1-year dollar-denominated European yen call with a strike of \$0.008 has a premium of \$0.0019. Demonstrate the arbitrage.
  - c. (7 points) What is the price of the yen-denominated European dollar put with 1 year to expiration and a strike price of ¥125 such that there is no arbitrage opportunity?

3. Consider a 4-year swap contract on gold. The notional amount of the swap contract is 200 troy ounces of gold. The current spot price of gold is \$1,300 per troy ounce. The lease rate of gold is assumed to be a constant and is equal to 2.5% per annum.

The current prices of zero-coupon bonds with different maturities are given as follows:

Maturity (in Years)	1	2	3	4
Zero-Coupon Bond Price	0.9958	0.9621	0.9411	0.9102
(that pays \$1 at Maturity)				

- a. (10 points) With level payments at the end of each year, find the fixed swap price per troy ounce of gold in the swap.
- b. (15 points) Just after the swap payment at the end of the year 1, the spot price of gold becomes \$1,350 per troy ounce. The lease rate is still a constant but becomes 1.8% per annum. The prices of zero-coupon bonds at that time are

Maturity (in Years)	1	2	3
Zero-Coupon Bond Price	0.9852	0.9598	0.9335
(that pays \$1 at Maturity)			

Find the market value of the swap from the perspective of the long party at that time.

4. (15 points) Suppose the current stock price is \$30.58 and the continuously compounded risk-free interest rate is 6%. The stock pays dividend of \$1.8 and \$2.5 at the end of 3 months and at the end of 6 months respectively. You observe an 8-month forward contract with forward price \$29.15. Is there an arbitrage opportunity on the forward contract? If so, describe the strategy to realize profit and find the accumulated arbitrage profits at the end of 8 months.

5. Two European put options expire in 9 months. The put options have the same underlying stock, but they have different strike prices and premiums.

Put Option	A	В
Strike	120	127
Premium	12	10

The continuously compounded annual risk-free interest rate is 11%.

- a. (5 points) What no-arbitrage property is violated?
- b. (3 points) What spread position would you use to effect arbitrage?
- c. (12 points) Demonstrate that the spread position is an arbitrage.

End

## **Scratch Paper**