

本次作業採用 C++ 配合 OpenCV 完成

## Thinning

步驟一：二值化，利用先前 HW2 的 function

```
//先進行二值化
Mat b_img = binary(img, THRESHOLD, widthLimit, heightLimit);
```

步驟二：用  $8 \times 8$  的 blocks 進行 downsample

```
Mat lena_down(64, 64, CV_8U, Scalar(0));
for (int height = 0; height < 64; height++) {
    for (int width = 0; width < 64; width++) {
        lena_down.at<uchar>(height, width) = b_img.at<uchar>(8 * height, 8 *
width);
    }
}
```

步驟三：進行 Thinning

Main Function:

```
bool flag = true;

while (flag) {

    flag = false;

    Mat old = img_thin.clone();

    //step 1: mark the interior/border pixels
    Mat s1 = Matmark_interior_border(img_thin, widthLimit, heightLimit);

    //step 2: pair relationship operator
    Mat s2 = mark_pair_relationship(s1, widthLimit, heightLimit);

    //step 3: check and delete the deletable pixels
    Mat s3 = step3(s1);

    for (int i = 0; i < heightLimit; i++) {
        for (int j = 0; j < widthLimit; j++) {
```

```

        if (s3.at<uchar>(i, j) == 1 && s2.at<uchar>(i, j) == 1)
            img_thin.at<uchar>(i, j) = 0;
    }
}

for (int i = 0; i < heightLimit; i++) {
    for (int j = 0; j < widthLimit; j++) {
        if (img_thin.at<uchar>(i, j) != old.at<uchar>(i, j))
            flag = true;
    }
}

}

```

### marked-interior/border-pixel operator

```

Mat Matmark_interior_border(Mat img, int widthLimit, int heightLimit) {
    Mat result(heightLimit, widthLimit, CV_8U, Scalar(0));
    int x1, x2, x3, x4;
    for (int i = 0; i < heightLimit; i++) {
        for (int j = 0; j < widthLimit; j++) {
            if (img.at<uchar>(i, j) > 0) {
                x1 = x2 = x3 = x4 = 0;
                if (i == 0) {
                    if (j == 0) {
                        x1 = img.at<uchar>(i, j + 1);
                        x4 = img.at<uchar>(i + 1, j);
                    }
                    else if (j == widthLimit - 1) {
                        x3 = img.at<uchar>(i, j - 1);
                        x4 = img.at<uchar>(i + 1, j);
                    }
                    else {
                        x1 = img.at<uchar>(i, j + 1);
                        x3 = img.at<uchar>(i, j - 1);
                        x4 = img.at<uchar>(i + 1, j);
                    }
                }
            }
            else if (i == heightLimit - 1) {

```

```

        if (j == 0) {
            x1 = img.at<uchar>(i, j + 1);
            x2 = img.at<uchar>(i - 1, j);
        }
        else if (j == widthLimit - 1) {
            x2 = img.at<uchar>(i - 1, j);
            x3 = img.at<uchar>(i, j - 1);
        }
        else {
            x1 = img.at<uchar>(i, j + 1);
            x2 = img.at<uchar>(i - 1, j);
            x3 = img.at<uchar>(i, j - 1);
        }
    }
    else {
        if (j == 0) {
            x1 = img.at<uchar>(i, j + 1);
            x2 = img.at<uchar>(i - 1, j);
            x4 = img.at<uchar>(i + 1, j);
        }
        else if (j == widthLimit - 1) {
            x2 = img.at<uchar>(i - 1, j);
            x3 = img.at<uchar>(i, j - 1);
            x4 = img.at<uchar>(i + 1, j);
        }
        else {
            x1 = img.at<uchar>(i, j + 1);
            x2 = img.at<uchar>(i - 1, j);
            x3 = img.at<uchar>(i, j - 1);
            x4 = img.at<uchar>(i + 1, j);
        }

        x1 /= 255;
        x2 /= 255;
        x3 /= 255;
        x4 /= 255;

        char a1 = h1('1', x1 + '0');
    }
}

```

<pre> char a2 = hl(a1, x2 + '0'); char a3 = hl(a2, x3 + '0'); char a4 = hl(a3, x4 + '0');  if (a4 == 'b')     result.at&lt;uchar&gt;(i, j) = 2; else     result.at&lt;uchar&gt;(i, j) = 1;     }     }     }     }     } return result; } </pre>
<p>説明：</p> $h(c, d) = \begin{cases} c & \text{if } c = d \\ b & \text{if } c \neq d \end{cases}$ $f(c) = \begin{cases} b & \text{if } c = b \\ i & \text{if } c \neq b \end{cases}$

## pair relationship operator

<pre> Mat mark_pair_relationship(Mat img, int widthLimit, int heightLimit) {     Mat pair(heightLimit, widthLimit, CV_8U, Scalar(0));     int x1, x2, x3, x4;     for (int i = 0; i &lt; heightLimit; i++) {         for (int j = 0; j &lt; widthLimit; j++) {             if (img.at&lt;uchar&gt;(i, j) &gt; 0) {                 x1 = x2 = x3 = x4 = 0;                 if (i == 0) {                     if (j == 0) {                         x1 = img.at&lt;uchar&gt;(i, j + 1);                         x4 = img.at&lt;uchar&gt;(i + 1, j);                     }                     else if (j == widthLimit - 1) {                         x3 = img.at&lt;uchar&gt;(i, j - 1);                         x4 = img.at&lt;uchar&gt;(i + 1, j);                     }                 }                 else { </pre>
---

```
        x1 = img.at<uchar>(i, j + 1);
        x3 = img.at<uchar>(i, j - 1);
        x4 = img.at<uchar>(i + 1, j);
    }
}
else if (i == heightLimit - 1) {
    if (j == 0) {
        x1 = img.at<uchar>(i, j + 1);
        x2 = img.at<uchar>(i - 1, j);
    }
    else if (j == widthLimit - 1) {
        x2 = img.at<uchar>(i - 1, j);
        x3 = img.at<uchar>(i, j - 1);
    }
    else {
        x1 = img.at<uchar>(i, j + 1);
        x2 = img.at<uchar>(i - 1, j);
        x3 = img.at<uchar>(i, j - 1);
    }
}
else {
    if (j == 0) {
        x1 = img.at<uchar>(i, j + 1);
        x2 = img.at<uchar>(i - 1, j);
        x4 = img.at<uchar>(i + 1, j);
    }
    else if (j == widthLimit - 1) {
        x2 = img.at<uchar>(i - 1, j);
        x3 = img.at<uchar>(i, j - 1);
        x4 = img.at<uchar>(i + 1, j);
    }
    else {
        x1 = img.at<uchar>(i, j + 1);
        x2 = img.at<uchar>(i - 1, j);
        x3 = img.at<uchar>(i, j - 1);
        x4 = img.at<uchar>(i + 1, j);
    }
}
```

```

        if (h2(x1, 1) + h2(x2, 1) + h2(x3, 1) + h2(x4, 1) >= 1 &&
img.at<uchar>(i, j) == 2)
            pair.at<uchar>(i, j) = 1;
        else
            pair.at<uchar>(i, j) = 2;
    }
}
}
return pair;
}

```

說明：

$$h(a, m) = \begin{cases} 1 & \text{if } a = m \\ 0 & \text{otherwise} \end{cases}$$

$$\text{採用4-connected : output} = \begin{cases} q & \text{if } \sum_{n=1}^4 h(x_n, m) < \theta \vee x_0 \neq l \\ p & \text{if } \sum_{n=1}^4 h(x_n, m) \geq \theta \wedge x_0 = l \end{cases}$$

marked-pixel connected shrink operator 先做類似 Yokoi Connectivity Number 處理。

結果如下：（64x64 放大 300%）

