

from #3(a), the ordinary differential equation -

$$-c \cdot \frac{dv}{dy} + 6v(y) \cdot \frac{dv}{dy} + \frac{d^3v}{dy^3} = 0$$

Now, $z = y\sqrt{c}$

$$\Rightarrow y = \frac{1}{\sqrt{c}} z$$

$$\Rightarrow dy = \frac{1}{\sqrt{c}} dz$$

and, $v(y) = c w(z)$

$$\Rightarrow dv = c dw$$

So, we obtain,

$$-c \cdot \frac{c dw}{\frac{1}{\sqrt{c}} dz} + 6 \cdot c \cdot w(z) \cdot \frac{c dw}{\frac{1}{\sqrt{c}} dz} + \frac{1}{(\frac{1}{\sqrt{c}})^3} \cdot c \cdot \frac{d^3w}{dz^3} = 0$$

$$\Rightarrow -c^{\frac{3}{2}} \cdot \frac{dw}{dz} + 6c^{\frac{3}{2}} \cdot w(z) \cdot \frac{dw}{dz} + c^{\frac{3}{2}} \cdot \frac{d^3w}{dz^3} = 0$$

$$\Rightarrow \boxed{\frac{dw}{dz} + 6w(z) \frac{dw}{dz} + \frac{d^3w}{dz^3} = 0}$$

which is a parameter-free form of equation as there is no " c " (velocity of wave) present in the equation.

So, substituting $z = y\sqrt{c}$ and $v(y) = c w(z)$ gives us a parameter-free steady-state KdV equation.

[shown]

