

According to the question,

diagonal matrix of eigenvalues,  $L = \begin{pmatrix} \lambda_1 & & 0 \\ & \lambda_2 & \\ 0 & & \ddots \\ & & & \lambda_n \end{pmatrix}$

and

matrix formed of columns of eigenvector,  $V = (\vec{v}_1 \ \vec{v}_2 \ \dots \ \vec{v}_n)$

Now, as  $\{\vec{v}_1, \vec{v}_2, \vec{v}_3, \dots, \vec{v}_n\}$  is a linearly independent set, therefore  $V$  is invertible.

Now,

$$\begin{aligned} \underline{M} \underline{V} &= (\underline{M} \vec{v}_1 \quad \underline{M} \vec{v}_2 \quad \dots \quad \underline{M} \vec{v}_n) \\ &= (\lambda_1 \vec{v}_1 \quad \lambda_2 \vec{v}_2 \quad \dots \quad \lambda_n \vec{v}_n) \\ &= (\vec{v}_1 \ \vec{v}_2 \ \dots \ \vec{v}_n) \begin{pmatrix} \lambda_1 & & 0 \\ & \lambda_2 & \\ 0 & & \ddots \\ & & & \lambda_n \end{pmatrix} \\ &= \underline{V} \underline{L} \end{aligned}$$

$$\Rightarrow \underline{M} = \underline{V} \underline{L} \underline{V}^{-1}; \text{ Here } v_{ij} = (v_j)_i$$