

## Problem 5

Let  $G$  be the graph with  $n$  nodes and  $m$  edges

Initialize a list, **order**, to contain nodes in topological order

def topological\_sort( $G$ , order):

    IF  $G$  is empty:

        Return order

    initialize a dictionary, **incoming**, keyed by vertices to store number of incoming edges of each node. Initially all values will be zero.

    FOR every edge  $u, v$  in  $G$ :

        Incoming[ $v$ ] = Incoming[ $v$ ] + 1

    WHILE (incoming is not empty):

        Initialize a list, **zero**, to contain nodes with no incoming edges

        FOR every  $k$  in incoming:

            IF incoming[ $k$ ] == 0:

                add  $k$  to list zero

                delete incoming[ $k$ ]

                add  $k$  to order

                delete  $k$  from  $G$

        IF zero is empty:

            Return  $G$

    topological\_sort( $G$ , order)

### Time Complexity:

The first for loop will run for at most  $m$  times so  $O(m)$

The while loop with a for loop will run for at most  $O(n+m)$

So total time =  $O(m+n)$