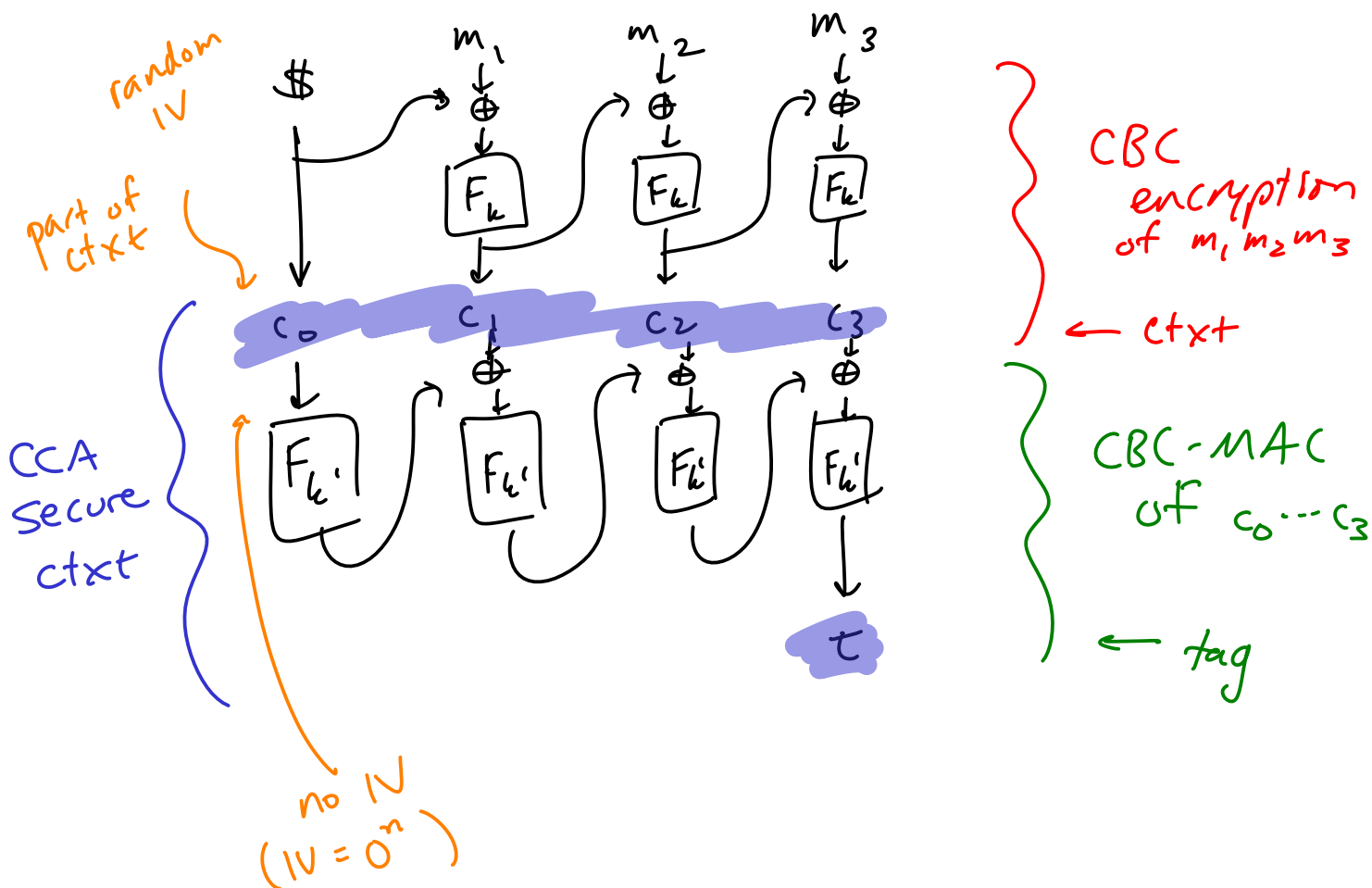


MACs

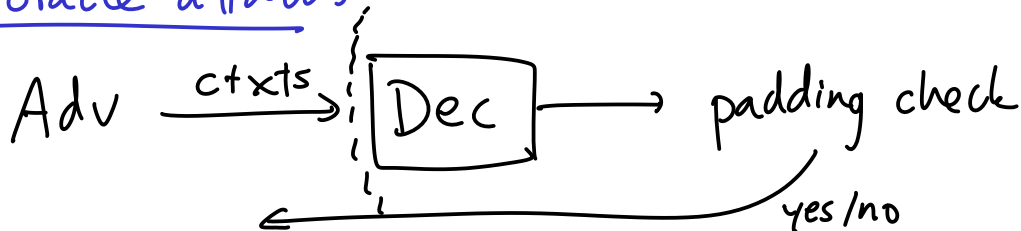
Exam Friday, review Wednesday, proj guidelines soon

Encrypt - then - MAC

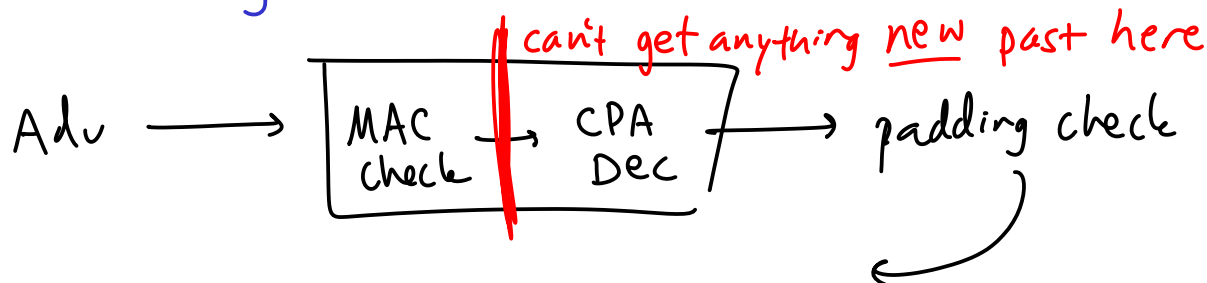
↖ CBC mode ↖ CBC-MAC ??



Padding oracle attacks



when using Enc - then - MAC scheme:



Enc-then-MAC proof:

(prove CCA-secure)

IDEA: Adv can ask for things to be decrypted

claim: Adv doesn't get any info from DEC subroutine

→ if Adv asks for DEC (something generated by library)

library will return error (part of CCA definition)

→ if Adv asks for DEC (something new)

library returns error unless Adv happened to find a forgery of the MAC

So if DEC subroutine is useless, things just collapse to CPA security

Big MAC Attack:

```
k ← MAC.KeyGen  
GEIMAC(m):  
  ret MAC(k, m)  
  
VER(m, t):  
  ret MAC(k, m)  $\stackrel{?}{=} t$ 
```

?
~
~
~

```
k ← MAC.KeyGen  
T = ∅  
  
GEIMAC(m):  
  t = MAC(k, m)  
  add (m, t) to T  
  return t  
  
VER(m, t):  
  ret (m, t)  $\stackrel{?}{\in} T$ 
```

BADMAC:

$$F = \text{PRP}$$

Idea: use block cipher somehow even when m is long

$$\text{MAC}(k, m_1 m_2 \dots m_n) = F(k, m_1 \oplus m_2 \oplus \dots \oplus m_n)$$

Attack: (Idea)

- ① Ask for MAC's of some msgs,
- ② use the results to determine MAC of some other msg,
- ③ call VER on new MAC
 - ↳ in left library, VER says yes since it is a valid MAC
 - ↳ in right library, VER says no since it's a "new" thing ($\notin T$)

Obs: permuting the order of $m_1 \dots m_n$ blocks doesn't change the MAC

Attack (more formal):

$t = \text{GETMAC}(0^\lambda 1^\lambda)$
return $\text{VER}(1^\lambda 0^\lambda, t)$

$0^\lambda 1^\lambda$ and $1^\lambda 0^\lambda$
have same MAC

Another:

$$\begin{aligned} \text{MAC}(k, m_1 \dots m_n) = & F(k, 1 \parallel m_1) \\ & \oplus F(k, 2 \parallel m_2) \\ & \oplus \dots \\ & \oplus F(k, n \parallel m_n) \end{aligned}$$

Idea: Ask for 3 MACs

$$m_1, m_2 \longrightarrow F(k, 1 \| m_1) \oplus F(k, 2 \| m_2)$$

$$m'_1, m_2 \longrightarrow F(k, 1 \| m'_1) \oplus F(k, 2 \| m_2)$$

$$m_1, m'_2 \longrightarrow F(k, 1 \| m_1) \oplus F(k, 2 \| m'_2)$$

XOR all 3 MACs = valid MAC of m'_1, m'_2 :

$$m'_1, m'_2 \longrightarrow F(k, 1 \| m'_1) \oplus F(k, 2 \| m'_2)$$

can compute this MAC w/o asking library
 \Rightarrow forgery !!