

Symbol

/ NT

/ variables

↓ steps of simplification

useless Symbol

useless production

CFG

G

→ CFL

↓

G

G'



Simplified
version

$S \rightarrow \epsilon$
 $\{a^n b^n \mid n \geq 0\}$

$L(G)$ $\Leftrightarrow L(G')$

↓

$\{\epsilon\}$

$\epsilon \in L(G')$

Eliminate Null productions

↳ $A \rightarrow \epsilon$

↳ Nullable production

$A \rightarrow BC$

$R \rightarrow \epsilon \mid \dots \mid A$

$S \rightarrow \dots$

$A \rightarrow \dots$

$B \rightarrow \dots$

$\epsilon \in L(G')$

③ Elimination of unit productions

$A \rightarrow B$

$S \rightarrow aAa \mid aBc$

minimize
redundant
symbols

$$\begin{aligned}
 A' &\rightarrow aS \mid bD \\
 B' &\rightarrow aBa \mid b \\
 C' &\rightarrow abb \mid DD \\
 D &\rightarrow aDa
 \end{aligned}$$

D is not generating

$S \rightarrow aAa \mid aBc$

$A \rightarrow aS$

$B \rightarrow aBa \mid b$

$C \rightarrow abb$

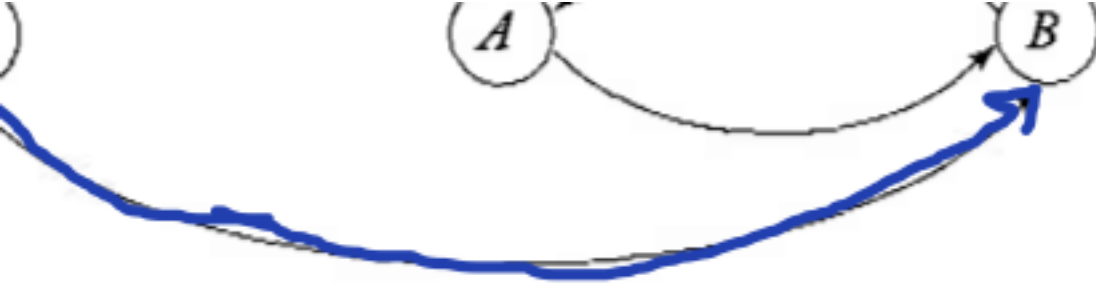
Ans. B & C are N

Which are generating

S is also generating
because $S \rightarrow aBC$

A is also generating
because $A \rightarrow aS$





move all unit-productions from

$$\begin{aligned} S &\rightarrow Aa|B, \\ B &\rightarrow A|bb, \\ A &\rightarrow a|bc|B. \end{aligned}$$

Substitution Rule

$$\begin{aligned} ① \quad S &\rightarrow \underline{A}a \mid a \mid bc \mid bb \\ ② \quad B &\rightarrow \underline{b}b \mid a \mid bc \\ ③ \quad A &\rightarrow \underline{a} \mid b\underline{c} \mid bb \end{aligned}$$

$$① \quad S \rightarrow Aa$$

$$S \rightarrow B$$

$$B \rightarrow \cdot A$$

$$\frac{S \rightarrow \cdot A}{S \rightarrow A}$$

$$\frac{S \rightarrow A}{S \rightarrow A}$$

$$② \quad B \rightarrow bb$$

$$③ \quad A \rightarrow a$$

$$④ \quad A \rightarrow bc$$

$$A \rightarrow B$$

$$F \rightarrow I \mid (E)$$

$$T \rightarrow F \mid T * F$$

$$E \rightarrow T \mid E + T$$

ϵ is a Starting N

$$G = \{ \epsilon, \top, \bot, \perp \}$$

$$\{ \underline{a}, \underline{b}, \underline{0}, \underline{1}, \underline{c}, \underline{*}, \underline{+} \}$$
$$/, *, \pm \}$$

$$I \rightarrow a \mid b \mid I_a \mid I_b \mid IO \mid \pm \quad , \quad (E, P)$$

$$F \rightarrow (E) \mid a \mid b \mid I_a \mid I_b \mid I_0 \mid I)$$

$$T \rightarrow T * F \mid (E) \mid a \mid b \mid I_a \mid I_b \mid I_0 \mid I_1 \quad A \rightarrow B$$

$$E \rightarrow E + T \mid T * F \mid (E) \mid a \mid b \mid I_a \mid I_b \mid I_0 \mid I_1$$