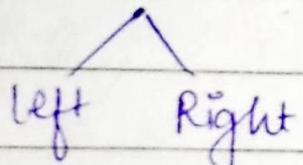


14 Oct '21

Parse Tree . and PDA.

Parse Tree

↪ one way to show derivation.



- ① leaf node → Terminal / ε
- ② Internal node - Non terminal
- ③ Root node - String symbol
- ④ $\rightarrow A \rightarrow B_1 B_2 \dots B_n$
left to Right

eg.

$$E \rightarrow I$$

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow (E)$$

$$I \rightarrow a$$

$$I \rightarrow b$$

$$I \rightarrow IO$$

$$I \rightarrow I1$$

$$I \rightarrow Ia$$

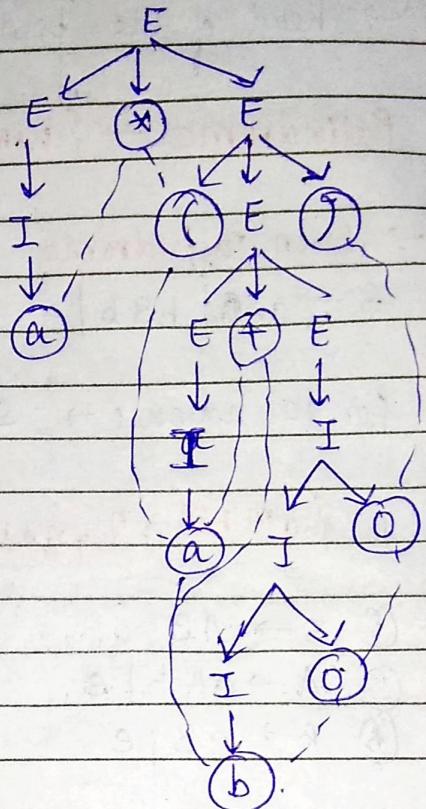
$$I \rightarrow Ib$$

Yield - Concatenation

of all leaf nodes from
left to right.

for string $a * (a + b00)$

Parse Tree .

$$\begin{aligned}
 E &\rightarrow E * E \\
 &\rightarrow I * E \\
 &\rightarrow a * E \\
 &\rightarrow a * (E) \\
 &\rightarrow a * (E + E) \\
 &\rightarrow a * (I + E) \\
 &\rightarrow a * (a + E) \\
 &\rightarrow a * (a + I) \\
 &\rightarrow a * (a + IO) \\
 &\rightarrow a * (a + I00) \\
 &\rightarrow a * (a + b00)
 \end{aligned}$$


yield $\rightarrow a * (a + b00)$

→ Application of CFG

1) Balanced Parenthesis -

$$\begin{aligned}
 B &\rightarrow BB \mid (B) \mid \epsilon \\
 G = &\{ \{B\}, \{(\}, \{\}\}, P, B \}
 \end{aligned}$$

2) if E else S

$(if E, else E, else S)$ as defined previously .

$$\begin{aligned}
 S &\rightarrow E \mid SS \mid is \mid isc \\
 G = &\{ \{E, S\}, \{i, e\}, P, S \}
 \end{aligned}$$

[i represent if
e represent else]

YACC (Yet Another Compiler Compiler) which is a parser generator and check acceptance of a string.
→ syntax analyzer.

- It takes input as token and Grammar (CFG) and we get a parse tree.

Q What's the problem YACC face?

→ Ambiguity - Ambiguous Grammar leads to conflicts
Conflicts

Shift Reduce (SR) Reduce Reduce (RR)
[whether to push [which Production Rule
or pop] → to choose]

eg → string → $a+b^*a$.

④ 1st parse tree.

$$E \rightarrow E * E$$

Derivation - (left most)

$$E \rightarrow E + E$$

$$E \Rightarrow E + E$$

$$E \rightarrow I$$

$$\Rightarrow I + E$$

$$I \rightarrow a$$

$$\Rightarrow a + E$$

$$I \rightarrow b$$

$$\Rightarrow a + E * E$$

$$I \rightarrow Ia$$

$$\Rightarrow a + I * E$$

$$I \rightarrow Ib$$

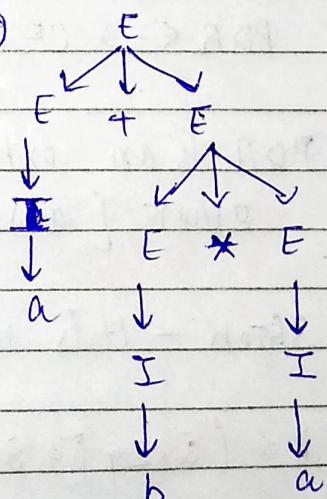
$$\Rightarrow a + b * E$$

$$I \rightarrow IO$$

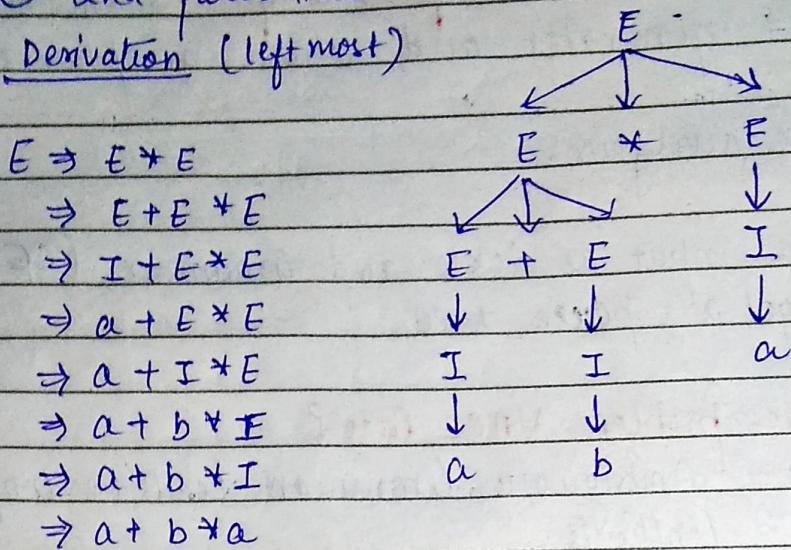
$$\Rightarrow a + b * I$$

$$I \rightarrow Ib$$

$$\Rightarrow a + b * a$$



② 2nd Parse Tree
Derivation (left most)



* if we get two different parse tree or two different left most or two different right most derivations, then the grammar given is ambiguous.

PDA (Push Down Automata)

↳ used to define CFG
 $PDA \longleftrightarrow CFG$

PDA is an extension of a NFA - with ϵ edge + stack [also called push down stack]

Stack - It is used to remember infinite no. of info

Def. $P = (Q, \Sigma, \Gamma, S, q_0, z_0, F)$

Q - finite set of states

Σ - finite set of symbols / Alphabet

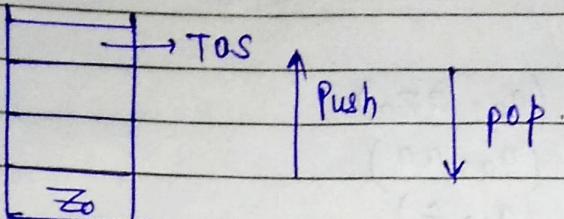
Γ - Stack Alphabet (Pushed into stack)

S - Transition fn $S: Q \times (\Sigma \cup \epsilon) \times \Gamma \rightarrow Q \times \Gamma^*$

- 0 | 0 | 1 | 1 | -

↑ → read head

finite control is used to decide where to go.



for $L = \{0^n 1^n \mid n > 0\}$

Push 0's into stack and for each 1, we will pop a symbol from stack.

q_0 - Initial state

z_0 - Initial stack symbol

F - set of final states (0 or more)

→ Two versions of PDA

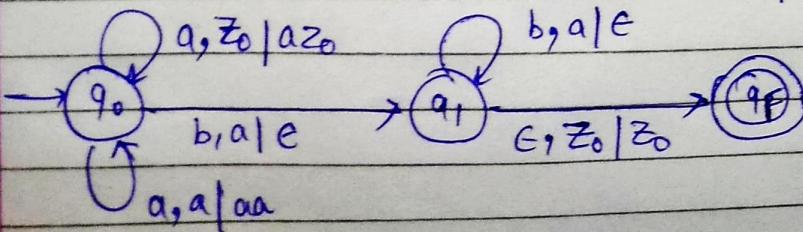
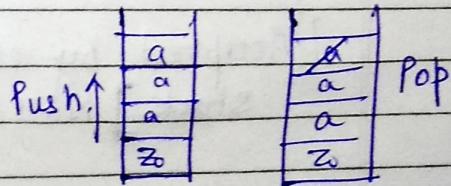
① One that accepts by entering an accepting state like in FA

② Another that accepts by emptying the stack regardless of state it is in.

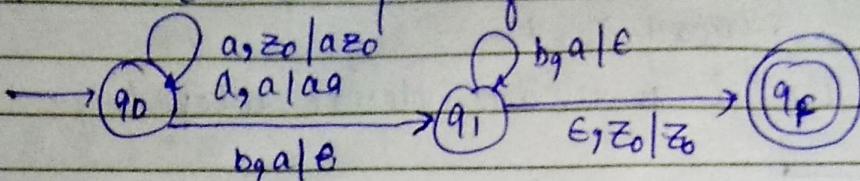
Q Construct a PDA that accepts the language $\{a^n b^n \mid n \geq 1\}$ where $\Sigma = \{a, b\}$.

→ $L = \{ab, aabb, aaabbb, \dots\}$

Initial → a a a b b b e



Instantaneous Description of PDA



$$\delta(q_0, a, z_0) = (q_0, az_0)$$

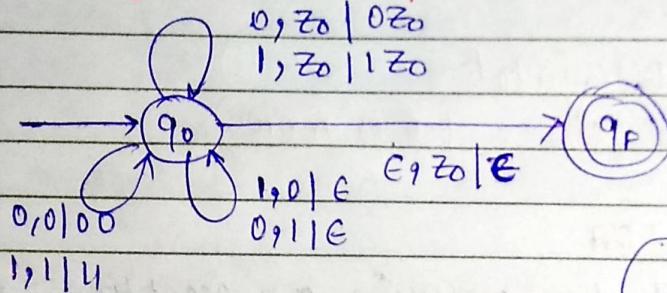
$$\delta(q_0, a, a) = (q_0, aa)$$

$$\delta(q_0, b, a) = (q_1, \epsilon)$$

$$\delta(q_1, b, a) = (q_1, \epsilon)$$

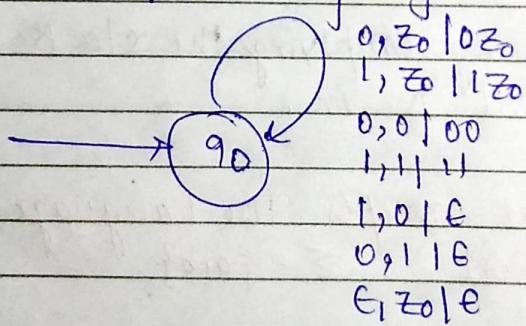
$$\delta(q_1, \epsilon, z_0) = (q_F, z_0)$$

Q2 $L = \{ w \in \{0,1\}^* \mid n_0(w) = n_1(w) \}$



Instantaneous Description

After fusing edges.



$$\delta(q_0, 0, z_0) = (q_0, 0z_0)$$

$$\delta(q_0, 1, z_0) = (q_0, 1z_0)$$

$$\delta(q_0, 1, 0) = (q_0, \epsilon)$$

$$\delta(q_0, 0, 1) = (q_0, \epsilon)$$

$$\delta(q_0, 0, 0) = (q_0, 00)$$

$$\delta(q_0, 1, 1) = (q_0, 11)$$

$$\delta(q_0, \epsilon, z_0) = (q_0, \epsilon)$$

[Accepted by emptying stack] [null stack]