

# Term Work - 01

## Problem Definition

Implement merge sort algorithm to sort a given set of elements, and determine time required to sort the elements.

## Theory

Divide & Conquer : The most well known design strategy

- \* Divide instance of a problem into 2 or more smaller instances
- \* Solve smaller instances recursively
- \* Obtain solution to original instance by combining these solns

## Algorithm : Pseudocode of Mergesort :

{ Algorithm Mergesort (A, low, high)

{ if (low < high) then

// Divide P into algorithmic sub problems

// Find where to split is set

mid = [(low+high)/2]

// Solve subproblem

Mergesort (A, low, mid);

Mergesort (A, mid+1, high);

// Combine the solutions

Merge (A, low, mid, high);

}

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## Pseudocode of Merge :

{ Algorithm Merge (A, low, mid, high)

l := low ; i := low; j := mid + 1;

while ((l <= mid) and (j <= high)) do

{

if (A[l] <= A[j]) then

{

if BC[i] = A[l];

l = l + 1;

}

else

```
B[i] = A[j];
j = j+1;
}
i++;
}

if (h > mid) then
    for k=j to high do {
        B[i] = A[k];
        i++;
    }
}
```

else

```
for k=h to mid do {
    B[i] = A[k];
    i++;
}
```

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Source code in Python:

```
import random
import time
man = 100000
def getdata(a):
    for i in range(man):
        ele = random.randint(0, 100000)
        a.append(ele)
```

def mergesort(a):

if len(a) > 1:

mid = len(a)

left\_sub = a[:mid]

right\_sub = a[mid:]

mergesort(left\_sub)

mergesort(right\_sub)

i = j = k = 0

while i < len(left\_sub) and j < len(right\_sub):

if left\_sub[i] < right\_sub[j]:

array[k] = left\_sub[i]

if = 1

else:

array[k] = right\_sub[j]

j += 1

k += 1

while i < len(left\_sub):

array[k] = left\_sub[i]

i += 1

k += 1

while j < len(right\_sub):

array[k] = right\_sub[j]

j += 1

k += 1

```
array - []
get_data(array)
start = time.time()
mergesort(array)
end = time.time()
print(f"Time taken :: {end - start} seconds")
```

### References :

- \* K. Berman, J. Paul, Algorithms, language learning.
- \* Thomas H Cormen - Introduction to Algorithms 2nd edition.

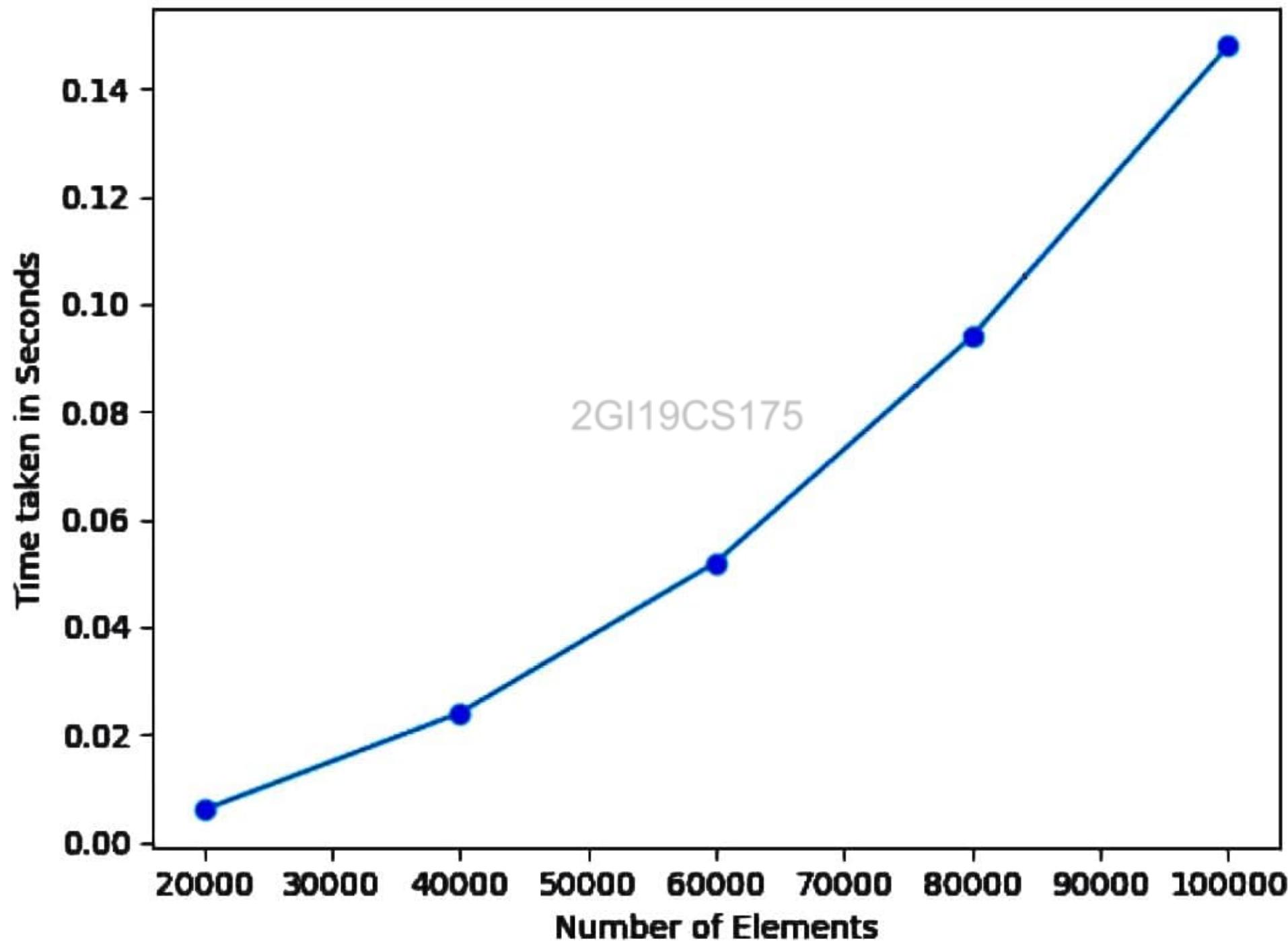
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### Conclusion :

In this TW we learnt about divide & conquer technique & implemented merge sort.

We also learnt computing time required for recursive & iterative algorithms.

## Term Work-1 Merge Sort



# Term Work - 2

## Problem Definition:

Implement Quick sort algorithm & determine the time required to sort elements.

## Theory

### Quicksort Algorithm.

Given an array of  $n$  elements

- \* If an array contains only one element, then return
- \* Else
  - Pick one element as pivot
  - Partition elements into 2 sub arrays
    - \* First array that contains elements less than equal to pivot
    - \* Second array that contains elements greater than pivot
  - Quick sort 2 sub arrays
  - Return result

## Algorithm

Quicksort ( $A[l \dots r]$ )

if ( $l < r$ )

s ← partition ( $A[l \dots r]$ )

Quicksort ( $A[l \dots s-1]$ )

Quicksort ( $A[s+1 \dots r]$ )

return

Algorithm Partition ( $A[l \dots r]$ )

$p \leftarrow A[i]$

$i \leftarrow l; j \leftarrow r+1$

repeat

repeat  $i \leftarrow j+1$  until  $s[i] \geq p$

repeat  $j \leftarrow j-1$  until  $A[j] < p$

swap ( $A[i], A[j]$ )

until  $i \geq j$

swap ( $A[i], A[j]$ )

swap ( $A[i], A[j]$ )

return  $j$

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### Source Code in Python:

```
import random  
import time
```

```
max = 100000
```

```
def getdata(a):
```

```
    for i in range(max):
```

```
        e = random.randint(0, 80000)
```

```
        a.append(e)
```

```
def partition(a, beg, end):
```

```
    pivot_index = beg
```

```
    pivot = a[pivot_index]
```

```
    while beg < end:
```

```
        while beg < len(a) and a[beg] <= pivot:
```

```
            beg += 1
```

```
        while a[end] > pivot:
```

```
            end -= 1
```

```
        if beg < end:
```

```
            a[beg], a[end] = a[end], a[beg]
```

```
a[end], a[pivot_index] = a[pivot_index], a[end]
```

```
return end
```

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def quicksort (a, beg, end) :

    if beg < end :

        partition\_index = partition (a, beg, end)

        quicksort (a, beg, partition\_index - 1)

        quicksort (a, partition\_index + 1, end)

array = []

get\_data (array)

quicksort (array, 0, len (array) - 1)

### References:

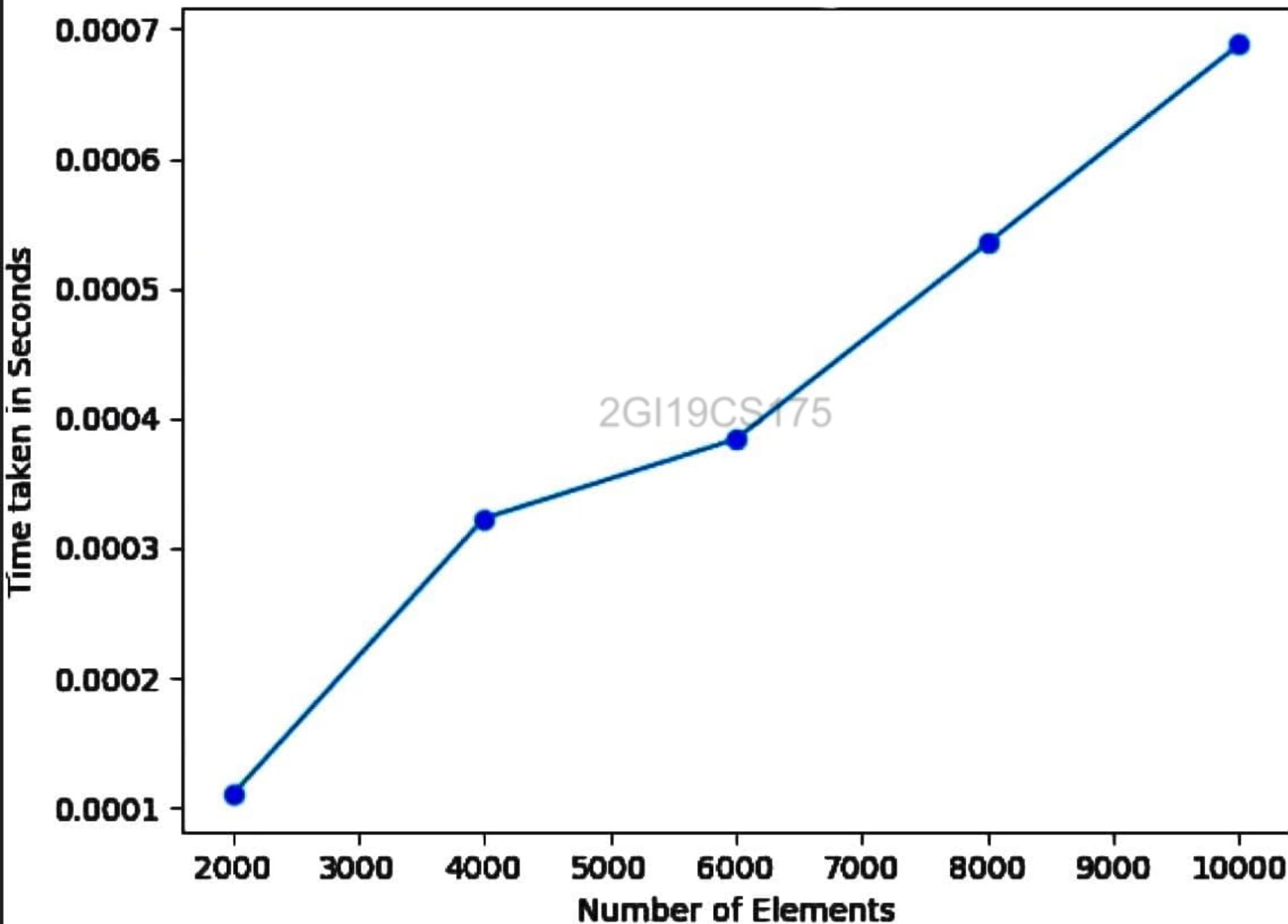
\* K. Boran , J. Paul , Algorithms Cengage Learning

\* Thomas H Cormen , Charles E , Algorithms 2<sup>nd</sup> edition.

### Conclusion:

In this TW we learn about divide conquer technique  
Implementation of quicksort algorithm design technique  
We also learned computing time required for  
recursive & iterative algorithms.

## Term Work-2 Quick Sort



## -----Quick Sort-----

Array before sorting :: 45244 11747 59295 3006 9775 71382 68397 11127 35777 75406 43269 35340 32097 21899

Array after sorting :: 3006 9775 11127 11747 21899 32097 35340 35777 43269 45244 59295 68397 71382 75406

# -----Quick Sort-----

Array before sorting :: 5713 74921 69489 73382 62588 64818 21148 31565 51198 59838 8789 61678 76381

Array after sorting :: 5713 8789 21148 24849 28726 31565 51198 59838 61678 62588 64818 74921 76381

# Term Work : 03

## Problem Definition

Implement insertion sort algorithm & determine the time required to sort elements

## Theory

- \* To sort array  $A[0 \dots n-1]$ , sort  $A[0 \dots n-2]$  recursively & then input  $A[n-1]$  in its proper array the sorted  $A[0 \dots n-2]$
- \* Usually implemented bottom up
- \* Insertion sort is an example of decrease by a constant type of decrease & conquer technique
- \* Decrease & conquer
  - Reduce problem instance to smaller instance of same problem
  - Solve smaller instance
  - Extend solution of smaller instance to obtain solution to original instance.

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## Algorithm :

Insertionsort ( $A[0 \dots n-1]$ )

for  $i \leftarrow 1$  to  $n-1$  do

$v \leftarrow A[i]$

$j \leftarrow i-1$

while  $j \geq 0$  and  $A[j] > v$  do

$A[j+1] \leftarrow A[j]$

$j \leftarrow j-1$

$A[j+1] \leftarrow v$

## Source Code in Python:

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```
import random
```

```
import time
```

```
man = 100000
```

```
def getdata(a):
```

```
    for i in range(0, 80000):
```

```
        e = random.randint(0, 80000)
```

```
        a.append(e)
```

```
def insertionSort(a):
```

```
    for i in range(man):
```

```
        num = a[i]
```

```
        j = i-1
```

```
        while j >= 0 and num < a[j]:
```

```
            a[j+1] = a[j]
```

```
            j = j-1
```

```
a[j+1] = num
```

$a = []$

`get_data(a)`

$s = \text{time.time}()$

`insertionsort(a)`

$e = \text{time.time}()$

`print(f"Time taken is : {e-s} seconds")`

### References:

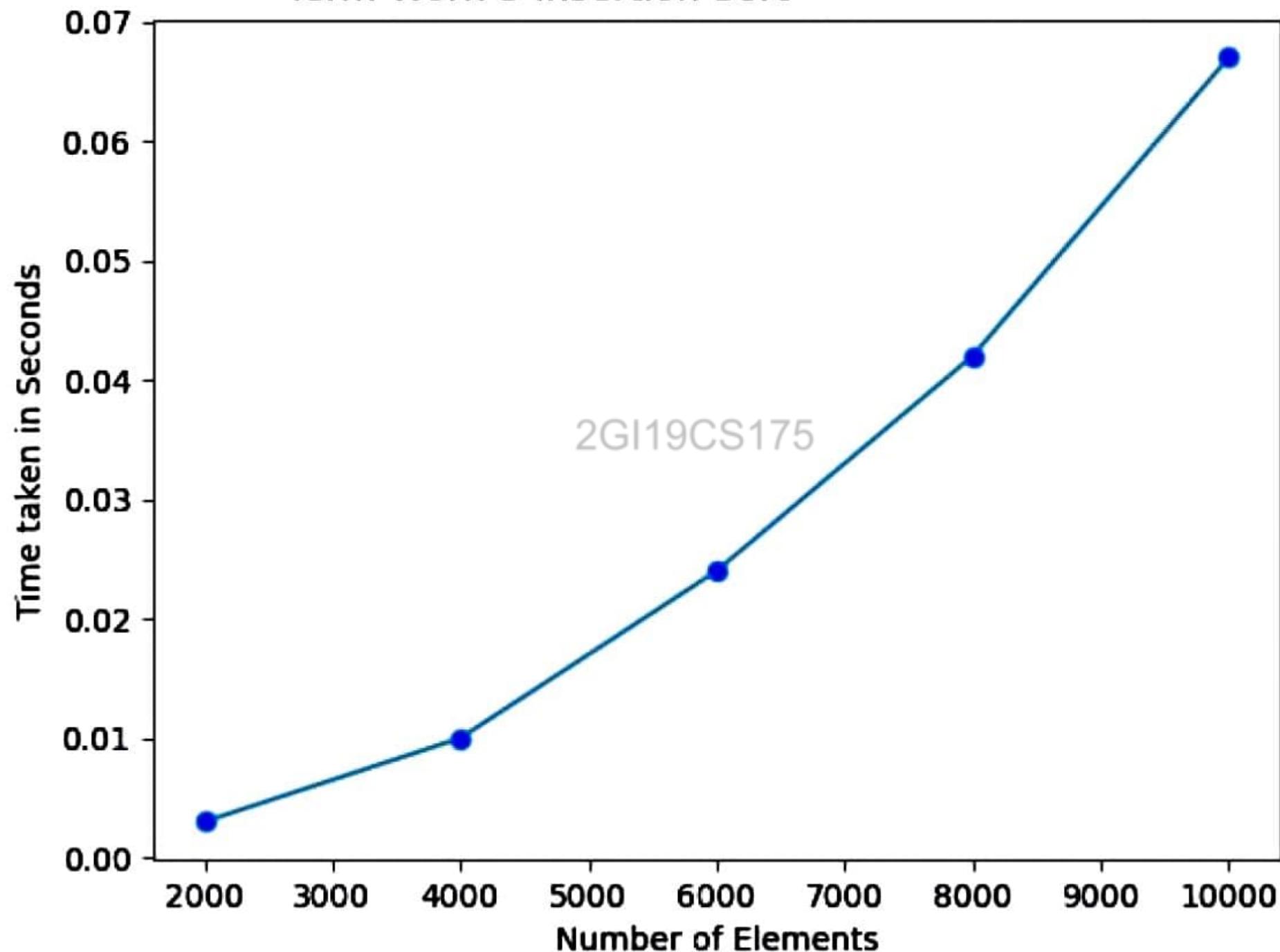
- K. Berman - Algorithms Cengage learning.

- Thomas H - Algorithms 2nd edition & onwards

### Conclusion:

In this framework, we learnt about decrease & conquer technique & implementation of insertion sort -

## Term Work-3 Insertion Sort



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## Term Work - 4

### Problem Definition

Implementation Heaps Sort algorithm & determines the time required to sort elements.

Repeat experiment for different values of N.

### Theory:

Transform & Conquer: Solves a problem by transformation to:

- A simple instance of same problem.
- A different representation of same instance.
- A different problem for which an algorithm is available

### Heaps & Heap Sort:

\* A heap is a binary tree with keys at its nodes

\* It is essentially complete i.e all the levels some rightmost keys may be missing.

\* The key at each node is  $\geq$  all keys in its children

## Algorithms:

Heapsort ( $H[1..n]$ )

for  $i \leftarrow [n/2]$  down to 1 do

$k \leftarrow i$ ;  $v \leftarrow H[k]$

$\text{heap} \leftarrow \text{false}$

while not heap &  $2*k \leq n$  do

$j \leftarrow 2*k$

if  $j < n$

if  $H[j] < H[j+1]$

$j \leftarrow j + 1$

if  $v \geq H[j]$

$\text{heap} \leftarrow \text{true}$

else

$H[R] \leftarrow H[j]$

$R \leftarrow j$

$H[k] \leftarrow v$

## Source Code in Python

```
import random
```

```
import time
```

```
max = 10000
```

```
def getdata(a):
```

```
    e = random.randint(0, 80000)
```

```
    a.append(e)
```

(15)

def heapify(a, al, i) :

parent index = 1

left =  $2*i + 1$

right =  $2*i + 2$

if left < al and a[parent index] < a[left] :  
parent index = left

if right < al and a[parent index] < a[right] :  
parent index = right.

if parent index != i :

a[i], a[parent index] = a[parent index], a[i]

heapify(a, al, parent index)

def heapsort(a):

al = len(a)

for i in range(al//2 - 1, -1, -1) :

    heapify(a, al, i)

for i in range(al - 1, 0, -1) :

    a[i], a[0] = a[0], a[i]

    heapify(a, i, 0)

$a = []$

getdata(a)

$s = \text{time.time}()$

heapsort(a)

$e = \text{time.time}()$

print(f"Time :: {e-s} seconds")

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## References:

- K. Berman - Algorithms Cengage learning.
- Thomas H - Algorithms 2<sup>nd</sup> edition & onwards

## Conclusion:

In this framework, we learnt about decrease & conquer techniques & implementation of insertion sort -

-----Heap Sort-----

Array before sorting :: 76388 24284 46877 14828 68573 77938 23725 76796 42958 21868 39752 54837 51388

Array after sorting :: 14828 21868 23725 24284 39752 42958 51388 54837 68573 76796 77938

# Term Work : 05

## Problem Definition :

From a given vertex in a weighted connected graph, find shortest path to other vertices using Dijkstra's algorithm

## Theory :

Greedy Technique : Constructs a solution to an optimization problem piece by piece through a sequence of choices that are

- Feasible
- Locally optimal

Dijkstra's Algorithm : With a different way of computing numerical labels. Among vertices not already in tree it finds vertex  $u$  with the smallest sum

$$\boxed{d_v + w(v, u)}$$

where  $v$  is a vertex,

$d_v$  is length of shortest path from source is to  $v$

## Algorithms:

Dijkstr'a's (S) ..

```

dist[S] ← 0
for all  $v \in V - \{S\}$ 
    do dist[v] ← ∞
S ← ∅
Q ← V
while Q ≠ ∅ do
    u ← distance(Q, dist)
    S ← S ∪ {u}

```

```

for all  $v \in \text{neighbours}[u]$  do
    if dist[v] > dist[u] + w(u, v)
        then d[v] ← d[u] + w(u, v)

```

return dist

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Source code in Python:

infinity = 99999

def shortest\_dist(vertices, shortest\_path, path\_set):

shortest = infinity

for vertex in range(vertices):

if shortest\_path[vertex] < shortest & path\_set[vertex] == False:

shortest = shortest\_path[vertex]

shortest\_path\_index = vertex

return shortest\_path\_index

```
def Dijkstra's (v, g, s_v):  
    shortest_path = [infinity] * vertices  
    shortest_path[s_v] = 0  
    path_set = [False] * vertices  
    for i in range (vertices):  
        dist_inset = shortest_dist (v, shortest_path, path_set)  
        path_set[i] = True
```

```
for vertex in range (v):
```

```
    shortest_path[vertex] = shortest_paths[dist_inset / graph]
```

```
print ("Vertex & Distance")
```

```
for node in not range (v):
```

```
    print (node, " & ", shortest_path[node])
```

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```
def main()
```

```
v = int(input ("Enter no of vertices :"))
```

```
g = [[infinity] for _ in range (0, v)] for _ in range (v)]
```

```
ch = 1
```

```
n, y, w = map (int, input ("Enter vertices w/ edge :"). split ())
```

```
graph [n][y-1] = w
```

```
ch = int (input ("Press 1 to continue or 0 to exit"))
```

```
print (graph)
```

```
Dijkstra's (vertices, graph, 0)
```

## References:

- \* K. Berman - Algorithms Cengage Learning
- \* Thomas H., 2<sup>nd</sup> edition onwards Algorithms.

## Conclusion:

In this TW, we learnt about Greedy Technique & implementation of Dijkstra's algorithm.

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Enter How many nodes : 5

Input Directed Edge <v1, v2, Wt> : 1 2 3

One More Edge then press 1 else type any key 1

Input Directed Edge <v1, v2, Wt> : 2 4 2

One More Edge then press 1 else type any key 1

Input Directed Edge <v1, v2, Wt> : 1 4 7

One More Edge then press 1 else type any key 1

Input Directed Edge <v1, v2, Wt> : 2 3 4

One More Edge then press 1 else type any key 1

Input Directed Edge <v1, v2, Wt> : 3 4 5

One More Edge then press 1 else type any key 1

Input Directed Edge <v1, v2, Wt> : 3 5 6

One More Edge then press 1 else type any key 1

Input Directed Edge <v1, v2, Wt> : 4 5 4

One More Edge then press 1 else type any key 2

Enter the Starting Vertex : 1

The Given Graph in Matrix Format :

9999	3	9999	7	9999
9999	9999	4	2	9999
9999	9999	9999	5	6
9999	9999	9999	9999	4
9999	9999	9999	9999	9999

Single Vertex Shortest Paths :

From Node-1 to Node-1 : 0

From Node-1 to Node-2 : 3

From Node-1 to Node-3 : 7

From Node-1 to Node-4 : 5

From Node-1 to Node-5 : 9

# Term Work : 06

## Problem Definition:

Find the minimum cost spanning tree of a given undirected graph using Prim's algorithm.

## Theory:

Prim's Algorithm: A spanning tree of a undirected graph G is a subgraph of G that is a tree containing all vertices of G.

In a weighted graph, the weight of a subgraph is sum of weights of the edges in subgraph.

Prim's algorithm constructs a minimum spanning tree through a sequence of expanding subsets -

## Algorithm

Prim(G)

Tree of G

$V_T \leftarrow \{v_0\}$

$E_T \leftarrow \emptyset$

for  $i \leftarrow 1$  to  $|V| - 1$  do

    find a minimum weight edge  $e^* = (v^*, u^*)$

    among all the edges  $(u, v)$  such that  $v$  is in  $V_T$  &  $u$  in  $V - V_T$ .

$V_T \leftarrow V_T \cup \{u^*\}$

$E_T \leftarrow E_T \cup \{e^*\}$

return  $E_T$

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## Source Code in C

```
#include <stdio.h>
#include <stdlib.h>
#define infinity 9999
#define MAX 20
```

```
int G[MAX][MAX], spanning[MAX][MAX], n;
```

```
int prims();
```

```
int main()
```

```
int i, j, total;
```

```
for (i=0; i<n; i++)
```

```
    for (j=0; j<n; j++)
```

```
        scanf("%d", &G[i][j]);
```

```

total = prims();
for(i=0; i<n; i++) {
    for(j=0; j<n; j++) {
        printf("%d\t", spanning[i][j]);
    }
    printf("\n\n Total cost of spanning tree = %d", total);
}
return 0;
}

```

```

int prims() {
    int cost[MAX][MAX];
    for(i=0; i<n; i++) {
        for(j=0; j<n; j++) {
            if(G[i][j] == 0)
                cost[i][j] = infinity;
            else
                cost[i][j] = G[i][j];
            spanning[i][j] = 0;
        }
    }
}

```

```

for(i=0; i<n; i++) {
    distance[i] = cost[0][i];
    from[i] = 0;
    visited[i] = 0;
}

```

$\min\_cost = 0;$

$\# \text{ edges} = n - 1;$

```
while (edges > 0) {  
    min_distance = infinity;  
    for (r=0; i<n; i++) {  
        if (visited[i] == 0 && distance[i] < min_distance) {  
            v = i;  
            min_distance = distance[i];  
        }  
    }  
    a = from[v];
```

$$\text{spanning}[v][v] = \text{distance}[v];$$

$$\text{spanning}[v][v] = \text{distance}[v];$$

edges  $\leftarrow$

visited[v] = 1

```
for (i=0; i<n; i++) {  
    if (visited[i] == 0 && cost[i][v] < distance[i]) {  
        distance[i] = cost[i][v];  
        from[i] = v;
```

$$\text{min\_cost} = \text{min\_cost} + \text{cost}$$

}

return (min\_cost);

}

```
while (edges > 0) {
    min_distance = infinity;
    for (i=0; i<n; i++) {
        if (visited[i] == 0 && distance[i] < min_distance) {
            v = i;
            min_distance = distance[i];
    }
}
```

$a = \text{from}[v]$

$\text{spanning}[v][v] = \text{distance}[v];$

$\text{spanning}[v][v] = \text{distance}[v];$

edges  $\leftarrow$

$\text{visited}[v] = 1$

```
for (i=0; i<n; i++) {
```

if ( $\text{visited}[i] == 0$  &&  $\text{cost}[i][v] < \text{distance}[i]$ ) {

$\text{distance}[i] = \text{cost}[i][v];$

$\text{from}[i] = v;$

$\text{min\_cost} \leftarrow \text{min\_cost} + \text{cost}$

}

$\text{return}(\text{min\_cost});$

}

## References

- \* K. Berman - Algorithms, Cengage language
- \* Thomas H., PH Introduction to algorithms 2<sup>nd</sup> edition.

## Conclusion

In this termwork we learnt about Prim's algorithm & techniques & implementation of Prim's algorithm.

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Enter no. of vertices:5

Enter the adjacency matrix:

0 2 0 6 0

2 0 3 8 5

0 3 0 0 7

6 8 0 0 9

0 5 7 9 0

spanning tree matrix:

0 2 0 6 0

2 0 3 0 5

0 3 0 0 0

6 0 0 0 0

0 5 0 0 0

Total cost of spanning tree=16

# Term Work : 07

## Problem Definition

Implement all pairs shortest path problem using Floyd's algorithm.

## Theory

All pairs shortest path :

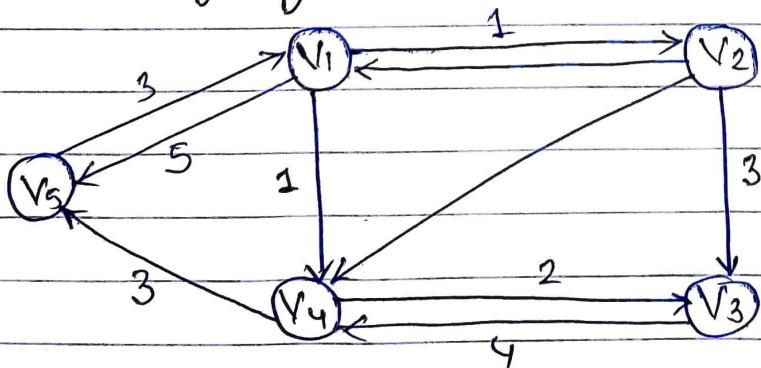
A representation : a coeigth matrix where

$$w(i, j) = 0 \quad \text{if } i=j$$

$$w(i, j) = \infty \quad \text{if there is no edge b/w } i \& j$$

$$w(i, j) = \text{"coeigth of edge"}$$

## \* The weight graph



## Algorithm:

Floyd's algorithm using  $n+1$  matrices

1 Initializing array to  $w[]$

$$D^0 \leftarrow w$$

$$P \leftarrow 0$$

for  $k \leftarrow 1$  to  $n$  do

    for  $i \leftarrow 1$  to  $n$  do

        for  $j \leftarrow 1$  to  $n$

$$D^k[i, j] = \min(D^{k-1}[i, j], D^{k-1}[i, k] + D^{k-1}[k, j])$$

## Source Code in Python

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infinity = 999

def solve(graph, vertices):

    distance = list(map(lambda i: list(map(lambda j: j, i)), graph))

    for m in range(vertices):

        for n in range(vertices):

            for o in range(vertices):

                distance[n][o] = min(distance[n][o], distance(n)(m) + distance[n][o])

    display(distance, vertices)

```
def display(distance, vertices):  
    for i in range(vertices):  
        for j in range(vertices):  
            if distance[i][j] == infinity:  
                distance[i][j] = "inf"
```

```
for rows in distance:  
    print(rows)
```

```
def main():  
    vertices = int(input("Enter the number of vertices :: "))  
    graph = [[infinity for _ in range(vertices)] for _ in range(vertices)]  
    edges = int(input("Enter the no. of edges :: "))  
  
    for i in range(edges):  
        x, y, w = map(int, input("Enter vertices of edges :: ").split())  
        graph[x-1][y-1] = w  
        print(graph)  
    solve(graph, vertices)  
  
if __name__ == "__main__":  
    main()
```

## References :

- \* K. Bernan, Algorithms, Cengage Learning
- \* Thomas H, Introduction to algorithm 2<sup>nd</sup> edition.

## Conclusion :

In this tormwork, we learnt about all pairs shortest path design technique & weight matrix representation.

We also learned computing time required by recursive & iterative algorithm.

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Enter the number of vertices:4

Enter the number of edges:

5

Enter the end vertices of edge1 with its weight

2 1 2

Enter the end vertices of edge2 with its weight

3 2 7

Enter the end vertices of edge3 with its weight

1 3 3

Enter the end vertices of edge4 with its weight

3 4 1

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Enter the end vertices of edge5 with its weight

4 1 6

Matrix of input data:

999	999	3	999
2	999	999	999
999	7	999	1
6	999	999	999

The shortest paths are:

0	10	3	4
2	0	5	6
7	7	0	1
6	16	9	0

Press any key to continue . . .

# Term Work : 08

## Problem Definition

Implement 0/1 Knapsack problem using Dynamic programming

## Theory :

Dynamic Programming is a general algorithm design technique for solving problems defined by or formulated as recurrences with overlapping.

### Main idea:

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- Set up a recurrence relating a solution to a larger instance of some smaller instances.
- Solve smaller instances once
- Record solutions in a table
- Extract solution to the initial instance from table

## Algorithm:

OP Knapsack ( $w[1..n]$ ,  $v[1..n]$ ,  $w$ )

var  $v[0..n, 0..w]$ ,  $p[1..n, 1..w]$ : int

for  $i=0$  to  $n$  do

$v[0, j] \leftarrow 0$

for  $i=0$  to  $n$  do

$v[i, 0] \leftarrow 0$

for  $i=1$  to  $n$  do

    for  $j=1$  to  $w$  do

        if  $w[i] \leq j$  &  $v[i] + v[i-1, j-w[i]] > v[i-1, j]$  then

$v[i, j] \leftarrow v[i] + v[i-1, j-w[i]]$ ;

$p[i, j] \leftarrow j - w[i]$

    else

$v[i, j] \leftarrow v[i-1, j]$ ;

$p[i, j] \leftarrow j$

return  $v[n, w]$

## Source code in C :

```
#include <stdio.h>
#include <conio.h>
#define MAX 20
int main () {
    int i, j, m, n, val1, val2, w[MAX], v[MAX], v1[MAX];
    printf ("Enter the weights & values ");
    for (i=0; i<n; i++) {
        scanf ("%d %d", &weights[i], &values[i]);
    }
    printf ("Enter Knapsack capacity ");
    scanf ("%d", &m);
    for (i=0; i<=n; i++) {
        for (j=0; j<=m; j++) {
            if (i==0 || j==0)
                v[i][j] = 0;
            else
                v[i][j] = -1;
        }
    }
    for (i=1; i<=n; i++) {
        for (j=1; j<=m; j++) {
            if (j < weights[i])
                v[i][j] = v[i-1][j];
            else
                v[i][j] = max (v[i-1][j], v[i-1][j-weights[i]] + values[i]);
        }
    }
}
```

```

else {
    val1 = values[i] + v[i-1][j - weights[i]];
    val2 = v[i-1][j];
    if (val1 > val2)
        v[i][j] = val1;
    else
        v[i][j] = val2;
}
}

```

```

printf("Maximum profit obtained is : ", v[n][m]);
i=n;
j=m;

```

```

while(i!=0 && j!=0) {
    if (v[i][j] != v[i-1][j]) {
        n[i] = 1
        j = j - weight[i];
    }
}

```

```

i=i-1;
}
for(i=0; i<=n; i++) {
    if (n[i] == 1)
        printf("%d", i);
}

```

return 0;

}

### Reference :

- \* K. Berman - Algorithms - Cengage Learning
- \* Thomas H., Introduction to Algorithms PHI, 2<sup>nd</sup> edition onwards

### Conclusion :

In this framework, we learnt about dynamic programming & implementation of it.

We also learned computing knapsack problem

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th Sem\SEM-4-main\DAALAB\TW\_8\_knapsack(Dynamic Programming)\TW8.exe"

ENTER THE NUMBER OF ITEMS : 4

ENTER WEIGHTS -

2

1

3

2

ENTER VALUES -

12

10

20

15

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ENTER THE KNAPSACK CAPACITY : 5

THE MATRIX IS....

0	0	0	0	0	0
0	0	12	12	12	12
0	10	12	22	22	22
0	10	12	22	30	32
0	10	15	25	30	37

MAXIMUM PROFIT OBTAINED IS : 37

ITEM SELECTED ARE --

{ 1 2 4 }

# Term Work : 09

## Problem Definition

Find a subset of a given set  $S = \{s_1, s_2, s_3, \dots, s_n\}$  of  $n$  free integers whose sum is equal to a given positive integer.

## Theory :

Backtracking Technique : The procedure whereby after determining that a node lead to nothing but dead ends, we go back to node's parent & proceed with the search on next child.

- \* Promising : The node can lead to a solution, otherwise it is called as 'non promising'
- \* Pruning : Check each node whether it is promising, if not backtracking to node's parent

Algorithm:

void sumof\_subsets (index, i, weight, total) {

    if promising (i)

        if weight == w

            display include [i] through include [i];

    else

        include [i+1] ← "yes"

        sum of subset ← [i+1, weight + w[i+1], total - w[i+1]];

        include [i+1] ← "no";

        sum of subsets (i+1, weight, total - w[i+1]);

}

bool promising (index i){

    return (weight + total  $\geq$  w) & weight = w || weight + w[i]  $\leq$  w);

}

## Source Code:

```
#include <stdio.h>
#include <conio.h>
#define TRUE 1
#define FALSE 0

int promising (int i, int wt, int total) {
    return ((wt + total) >= sum) && ((wt == sum) || (wt + w[i+1]) <= sum)
}

void sumset (int i, int wt, int total) {
    int j;
    if (promising (i, wt, total)) {
        if (wt == sum) {
            printf ("In {1t}\n");
            for (j = 0; j <= i; j++)
                if (inc[j])
                    printf ("y.%d", w[j]);
            printf ("\n");
        }
    }
    else {
        inc[i+1] = TRUE;
        sumset (i+1, wt+w[i+1], total-w[i+1]);
        inc[i+1] = FALSE;
        sumset (i+1, wt, total-w[i+1]);
    }
}
```

```
int main() {
    int i, j, n, temp, total = 0;
    for (i = 0; i < n; i++) {
        scanf("%d", &w[i]);
        total += w[i];
    }
    scanf("%d", &sum)
```

```
for (i = 0; i < n; i++) {
    for (j = 0; j < n - 1; j++) {
        if (w[j] > w[j + 1]) {
            temp = w[j];
            w[j] = w[j + 1];
            w[j + 1] = temp;
        }
    }
}
```

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```
for (i = 0; i < n; i++)
    printf("%d", w[i]);
```

```
if ((total < sum))
    printf("Subset construction not possible");
```

```
else {
    for (i = 0; i < n; i++)
        inc[i] = 0
```

```
subset(-1, 0, total);
```

}

```
return 0;
```

## References :

- \* K. Berman ; Cengage Learning - Algorithms
- \* Thomas H., Introduction To Algorithms - 2<sup>nd</sup> edition

## Conclusion:

In this termwork, we learnt about backtracking technique & implementation of backtracking design technique.

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Enter how many numbers:

5

Enter 5 numbers to the set:

5 6 10 11 16

Input the sum value to create sub set:

21

The given 5 numbers in ascending order:

5 6 10 11 16

The solution using backtracking is:

{ 5 6 10 }

{ 5 16 }

{ 10 11 }

Press any key to continue . . .

# Term Work : 10

## Problem Definition:

Implementation N Queen's problem using Back Tracking.

## Theory :

- \* Construct the state-space tree
  - nodes : partial solutions
  - edges : choices in extending partial solutions.
- \* Explore the state space tree using depth-first search.
- \* N Queen :
  - The object is to place queens on a chess board such a way as no queen can capture another one in a single move.
  - Recall that queen can move horizontal, vertical (or) diagonally an infinite distance
  - This implies that two, queen can be on the same row, column (or) diagonal

## Algorithm :

Procedure queen ( $i$ ,  $\text{index}$ ,  $n$ )

var  $j \leftarrow \text{index}$

begin

if promising ( $i$ ) then

if  $i = n$  then

write [  $\text{col}[i]$  through  $\text{col}[n]$  ]

else

for  $j \leftarrow 1$  to  $n$  do  
 $\text{col}[i+1] \leftarrow j$

queens ( $i+1, n$ )

end

end

end.

end

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function promising ( $i$ :  $\text{index}$ ): boolean;

var  $k \rightarrow \text{index}$ ;

begin

$k \leftarrow 1$ ;

promising  $\leftarrow$  true;

while  $k < i$  and promising do

if  $\text{col}[i] = \text{col}[k]$  or  $\text{abs}(\text{col}[i] - \text{col}[k]) = i$

then promising  $\leftarrow$  false

end

$k \leftarrow k + 1$

end end

## Source Code :

```
def isAttack (i,j, board):
    if board[i][j] == 1 or board[k][j] == 1:
        return True

    for k in range (len(board)):
        for l in range (len(board)):
            if k+1 == i+j or k-1 == i-j:
                if board[k][l] == 1:
                    return True
    return False
```

```
def N-queen (n, board):
    if n == 0:
        return True

    for i in range (len(board)):
        for j in range (len(board)):
            if (not (isAttack (i,j, board))) and (board[i][j] != 1):
                board[i][j] = 1
                if N-queen (n-1, board) == True:
                    return True
                board[i][j] = 0

    return False
```

```
def main():
    ch = 1
    while ch == 1:
        ch = int(input())
        if ch == 1:
            N = int(input())
            board = [[0]*N for i in range(N)]
            N-queen(N, board)
        else:
            for i in board:
                print(i)
            print()
    elif ch == 2:
        print("Exiting !!")
    else:
        print("Invalid choice")
```

if \_\_name\_\_ == "\_\_main\_\_":
 Main()

## References :

- \* K. Berman - Algorithms , Cengage learning
- \* Thomas H Cormen, Introduction to Algorithms PHI 2<sup>nd</sup> edition

## Conclusion :

- \* In this termwork we learnt about backtracking technique & implementation of back tracking algorithm design technique 2GI19CS175
- \* we also learned computing time required , design algorithm for specific applications <sup>using</sup> appropriate techniques

```
Press 1 to Test the program
Press 2 to Exit the program
Enter your choice :: 1
Enter the number of queens :: 5
[1, 0, 0, 0, 0]
[0, 0, 1, 0, 0]
[0, 0, 0, 0, 1]
[0, 1, 0, 0, 0]
[0, 0, 0, 1, 0]
```

```
Press 1 to Test the program
Press 2 to Exit the program
Enter your choice :: 1
Enter the number of queens :: 2
[0, 0] 2GI9CS175
[0, 0]
```

```
Press 1 to Test the program
Press 2 to Exit the program
Enter your choice :: 1
Enter the number of queens :: 3
[0, 0, 0]
[0, 0, 0]
[0, 0, 0]
```

```
Press 1 to Test the program
Press 2 to Exit the program
Enter your choice :: 2
Exiting ...
```