```
In [432]:
              import pandas as pd
           2 import matplotlib.pyplot as plt
           3
              import seaborn as sns
              import numpy as np
              from scipy.stats import norm
              from sklearn.preprocessing import StandardScaler
           7
              from scipy import stats
              import warnings
           9
              import missingno as mno
          10
              from sklearn.pipeline import Pipeline
          11
          12
          13
              #warnings.filterwarnings('ignore')
          14
              %matplotlib inline
              df = pd.read_csv('LifeExpectancyData.csv')
In [218]:
           1
              df.head(10)
```

### Out[218]:

|   | Country     | Year | Status     | Life expectancy | Adult<br>Mortality | infant<br>deaths | Alcohol | percentage<br>expenditure | Hepatitis<br>B | Ме |
|---|-------------|------|------------|-----------------|--------------------|------------------|---------|---------------------------|----------------|----|
| 0 | Afghanistan | 2015 | Developing | 65.0            | 263.0              | 62               | 0.01    | 71.279624                 | 65.0           |    |
| 1 | Afghanistan | 2014 | Developing | 59.9            | 271.0              | 64               | 0.01    | 73.523582                 | 62.0           |    |
| 2 | Afghanistan | 2013 | Developing | 59.9            | 268.0              | 66               | 0.01    | 73.219243                 | 64.0           |    |
| 3 | Afghanistan | 2012 | Developing | 59.5            | 272.0              | 69               | 0.01    | 78.184215                 | 67.0           |    |
| 4 | Afghanistan | 2011 | Developing | 59.2            | 275.0              | 71               | 0.01    | 7.097109                  | 68.0           |    |
| 5 | Afghanistan | 2010 | Developing | 58.8            | 279.0              | 74               | 0.01    | 79.679367                 | 66.0           |    |
| 6 | Afghanistan | 2009 | Developing | 58.6            | 281.0              | 77               | 0.01    | 56.762217                 | 63.0           |    |
| 7 | Afghanistan | 2008 | Developing | 58.1            | 287.0              | 80               | 0.03    | 25.873925                 | 64.0           |    |
| 8 | Afghanistan | 2007 | Developing | 57.5            | 295.0              | 82               | 0.02    | 10.910156                 | 63.0           |    |
| 9 | Afghanistan | 2006 | Developing | 57.3            | 295.0              | 84               | 0.03    | 17.171518                 | 64.0           |    |
|   |             |      |            |                 |                    |                  |         |                           |                |    |

10 rows × 22 columns

```
In [698]: 1 type(df['Country'])
```

Out[698]: pandas.core.series.Series

In [219]:

df.sample(10)

Out[219]:

|      | Country                    | Year | Status     | Life expectancy | Adult<br>Mortality | infant<br>deaths | Alcohol | percentage<br>expenditure | Hepatitis<br>B | N |
|------|----------------------------|------|------------|-----------------|--------------------|------------------|---------|---------------------------|----------------|---|
| 2104 | Republic<br>of<br>Moldova  | 2014 | Developing | 71.8            | 162.0              | 1                | 9.99    | 0.000000                  | 92.0           |   |
| 1188 | India                      | 2013 | Developing | 67.6            | 187.0              | 1000             | 3.11    | 67.672304                 | 7.0            |   |
| 1685 | Mexico                     | 2013 | Developing | 76.6            | 12.0               | 32               | 5.23    | 150.408875                | 82.0           |   |
| 136  | Austria                    | 2007 | Developed  | 81.0            | 8.0                | 0                | 12.50   | 7453.864400               | 85.0           |   |
| 1794 | Myanmar                    | 2001 | Developing | 62.5            | 239.0              | 72               | 0.38    | 1.917164                  | NaN            |   |
| 2760 | United<br>Arab<br>Emirates | 2001 | Developing | 74.5            | 14.0               | 1                | 1.67    | 243.753913                | 92.0           |   |
| 973  | Gambia                     | 2004 | Developing | 57.3            | 296.0              | 3                | 2.51    | 0.000000                  | 95.0           |   |
| 388  | Bulgaria                   | 2011 | Developed  | 73.7            | 144.0              | 1                | 10.67   | 875.149519                | 96.0           |   |
| 1646 | Malta                      | 2003 | Developed  | 78.5            | 71.0               | 0                | 6.70    | 1678.392773               | 89.0           |   |
| 260  | Belize                     | 2011 | Developing | 69.4            | 188.0              | 0                | 6.64    | 605.628689                | 95.0           |   |

10 rows × 22 columns

```
In [220]:
              print("Names of Columns : ")
           2
              print()
           3
              for x in df.columns :
           4
                  print("{}".format(x))
           5
           6
          Names of Columns :
          Country
          Year
          Status
          Life expectancy
          Adult Mortality
          infant deaths
          Alcohol
          percentage expenditure
          Hepatitis B
          Measles
           BMI
          under-five deaths
          Polio
          Total expenditure
          Diphtheria
           HIV/AIDS
          GDP
          Population
           thinness 1-19 years
           thinness 5-9 years
          Income composition of resources
          Schooling
              print("Number of ROWS in the dataset : {} ".format(df.shape[0]))
In [221]:
           1
              print("Number of COLUMNS in the dataset : {} ".format(df.shape[1]))
           3
```

```
Number of ROWS in the dataset : 2938

Number of COLUMNS in the dataset : 22
```

```
In [222]: 1
```

df.describe()

#### Out[222]:

|       | Year        | Life expectancy | Adult<br>Mortality | infant<br>deaths | Alcohol     | percentage<br>expenditure | Hepatitis E |
|-------|-------------|-----------------|--------------------|------------------|-------------|---------------------------|-------------|
| count | 2938.000000 | 2928.000000     | 2928.000000        | 2938.000000      | 2744.000000 | 2938.000000               | 2385.000000 |
| mean  | 2007.518720 | 69.224932       | 164.796448         | 30.303948        | 4.602861    | 738.251295                | 80.940461   |
| std   | 4.613841    | 9.523867        | 124.292079         | 117.926501       | 4.052413    | 1987.914858               | 25.070016   |
| min   | 2000.000000 | 36.300000       | 1.000000           | 0.000000         | 0.010000    | 0.000000                  | 1.000000    |
| 25%   | 2004.000000 | 63.100000       | 74.000000          | 0.000000         | 0.877500    | 4.685343                  | 77.000000   |
| 50%   | 2008.000000 | 72.100000       | 144.000000         | 3.000000         | 3.755000    | 64.912906                 | 92.000000   |
| 75%   | 2012.000000 | 75.700000       | 228.000000         | 22.000000        | 7.702500    | 441.534144                | 97.000000   |
| max   | 2015.000000 | 89.000000       | 723.000000         | 1800.000000      | 17.870000   | 19479.911610              | 99.000000   |

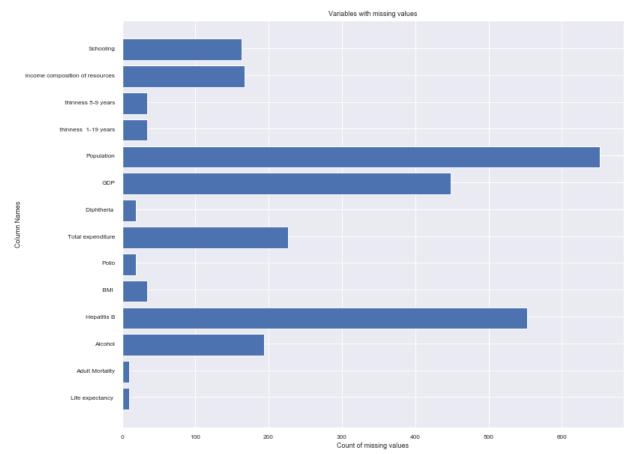
```
In [223]: 1 df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2938 entries, 0 to 2937
Data columns (total 22 columns):
Country
                                    2938 non-null object
Year
                                    2938 non-null int64
                                    2938 non-null object
Status
Life expectancy
                                    2928 non-null float64
Adult Mortality
                                    2928 non-null float64
infant deaths
                                    2938 non-null int64
Alcohol
                                    2744 non-null float64
                                    2938 non-null float64
percentage expenditure
                                    2385 non-null float64
Hepatitis B
Measles
                                    2938 non-null int64
 BMI
                                    2904 non-null float64
under-five deaths
                                    2938 non-null int64
                                    2919 non-null float64
Polio
Total expenditure
                                    2712 non-null float64
Diphtheria
                                    2919 non-null float64
HIV/AIDS
                                    2938 non-null float64
GDP
                                    2490 non-null float64
                                    2286 non-null float64
Population
 thinness 1-19 years
                                    2904 non-null float64
 thinness 5-9 years
                                    2904 non-null float64
Income composition of resources
                                    2771 non-null float64
Schooling
                                    2775 non-null float64
dtypes: float64(16), int64(4), object(2)
memory usage: 505.0+ KB
```

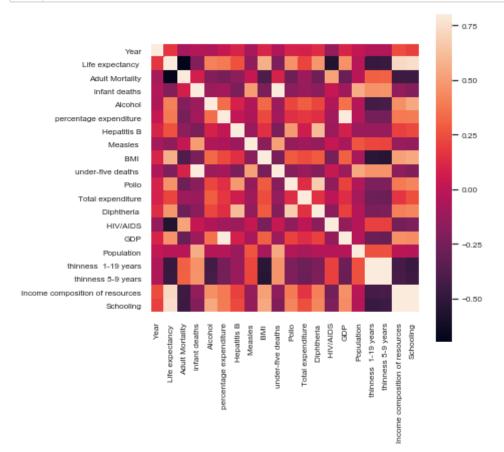
In [224]: 1 df.dtypes

| Out[224]: | Country                         | object  |
|-----------|---------------------------------|---------|
|           | Year                            | int64   |
|           | Status                          | object  |
|           | Life expectancy                 | float64 |
|           | Adult Mortality                 | float64 |
|           | infant deaths                   | int64   |
|           | Alcohol                         | float64 |
|           | percentage expenditure          | float64 |
|           | Hepatitis B                     | float64 |
|           | Measles                         | int64   |
|           | BMI                             | float64 |
|           | under-five deaths               | int64   |
|           | Polio                           | float64 |
|           | Total expenditure               | float64 |
|           | Diphtheria                      | float64 |
|           | HIV/AIDS                        | float64 |
|           | GDP                             | float64 |
|           | Population                      | float64 |
|           | thinness 1-19 years             | float64 |
|           | thinness 5-9 years              | float64 |
|           | Income composition of resources | float64 |
|           | Schooling                       | float64 |
|           | dtype: object                   |         |
|           |                                 |         |

```
null columns=df.columns[df.isnull().any()]
In [167]:
            1
            2
               df[null_columns].isnull().sum()
            3
            4
               labels = []
            5
               values = []
            6
               for col in null_columns:
            7
                   labels.append(col)
                   values.append(df[col].isnull().sum())
            8
            9
               ind = np.arange(len(labels))
               width = 0.1
           10
           11
               fig, ax = plt.subplots(figsize=(12,10))
           12
               rects = ax.barh(ind, np.array(values))
           13
               ax.set_yticks(ind+((width)/2.))
           14
               ax.set yticklabels(labels, rotation='horizontal')
               ax.set_xlabel("Count of missing values")
           15
               ax.set_ylabel("Column Names")
           16
               ax.set_title("Variables with missing values");
           17
           18
```



```
df.isna().sum().sort_values(ascending=False) / len(df) * 100
In [168]:
            1
            2
Out[168]: Population
                                               22.191967
          Hepatitis B
                                               18.822328
          GDP
                                               15.248468
          Total expenditure
                                                7.692308
          Alcohol
                                                6.603131
          Income composition of resources
                                                5.684139
          Schooling
                                                5.547992
           BMI
                                                1.157250
           thinness 1-19 years
                                                1.157250
           thinness 5-9 years
                                                1.157250
          Diphtheria
                                                0.646698
          Polio
                                                0.646698
          Adult Mortality
                                                0.340368
          Life expectancy
                                                0.340368
          under-five deaths
                                                0.000000
           HIV/AIDS
                                                0.000000
          Measles
                                                0.00000
          percentage expenditure
                                                0.000000
          infant deaths
                                                0.00000
          Status
                                                0.000000
          Year
                                                0.00000
          Country
                                                0.00000
          dtype: float64
```



```
In [170]:
              correlations=df.corr()
              attrs = correlations.iloc[:-1,:-1] # all except target
            2
            3
            4
              threshold = 0.5
            5
               important_corrs = (attrs[abs(attrs) > threshold][attrs != 1.0]) \
            6
                   .unstack().dropna().to_dict()
            7
               unique_important_corrs = pd.DataFrame(
            8
           9
                   list(set([(tuple(sorted(key)), important_corrs[key]) \
                   for key in important_corrs])),
           10
                       columns=['Attribute Pair', 'Correlation'])
           11
           12
                   # sorted by absolute value
           13
           14
               unique important corrs = unique important corrs.ix[
                   abs(unique_important_corrs['Correlation']).argsort()[::-1]]
           15
           16
           17
              unique important corrs
```

#### Out[170]:

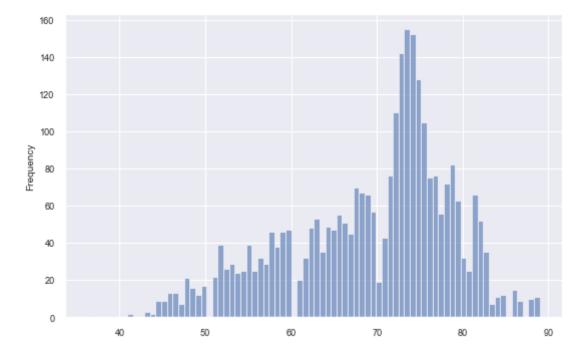
|    | Attribute Pair                                 | Correlation |
|----|--|-------------|
| 5  | (infant deaths, under-five deaths)             | 0.996629    |
| 14 | (thinness 1-19 years, thinness 5-9 years)      | 0.939102    |
| 15 | (GDP, percentage expenditure)                  | 0.899373    |
| 1  | (Income composition of resources, Life expecta | 0.724776    |
| 10 | (Adult Mortality, Life expectancy)             | -0.696359   |
| 12 | (Diphtheria , Polio)                           | 0.673553    |
| 0  | (Diphtheria , Hepatitis B)                     | 0.611495    |
| 11 | ( BMI , Life expectancy )                      | 0.567694    |
| 6  | (Population, infant deaths)                    | 0.556801    |
| 9  | ( HIV/AIDS, Life expectancy )                  | -0.556556   |
| 13 | (Population, under-five deaths)                | 0.544423    |
| 4  | (BMI, thinness 5-9 years)                      | -0.538911   |
| 2  | ( BMI , thinness 1-19 years)                   | -0.532025   |
| 16 | ( HIV/AIDS, Adult Mortality)                   | 0.523821    |
| 8  | ( BMI , Income composition of resources)       | 0.508774    |
| 7  | (Measles , under-five deaths )                 | 0.507809    |
| 3  | (Measles , infant deaths)                      | 0.501128    |

```
In [171]: 1  #num_feat
```

```
In [172]:
            1
               num_feat
Out[172]: Index(['Year', 'Life expectancy ', 'Adult Mortality', 'infant deaths',
                   'Alcohol', 'percentage expenditure', 'Hepatitis B', 'Measles ', '
           BMI ',
                   'under-five deaths ', 'Polio', 'Total expenditure', 'Diphtheria ',
                   ' HIV/AIDS', 'GDP', 'Population', ' thinness 1-19 years',
                   'thinness 5-9 years', 'Income composition of resources', 'Schooli
           ng'],
                 dtype='object')
               mno.matrix(df, figsize = (20, 6))
In [173]:
            2
Out[173]: <matplotlib.axes._subplots.AxesSubplot at 0x1a295eae10>
                County test States The satestatics with the satestatics
           2938
In [175]:
            1
                #np.corrcoef?
                #(df['Year'].values, df['Life expectancy '].values)[0,0]
```

```
In [176]: 1 plt.figure(num=None, figsize=(8, 5), dpi=80, facecolor='w', edgecolor='
2
3
4
```

Out[176]: <matplotlib.axes.\_subplots.AxesSubplot at 0x1a29e5ec50>



```
In [177]: 1 #df.dtypes 2
```

```
In [231]:
            1
               from sklearn.preprocessing import LabelEncoder
            2
            3
               class MultiColumnLabelEncoder:
            4
                   def __init__(self,columns = None):
            5
                        self.columns = columns # array of column names to encode
            6
            7
                   def fit(self, X, y=None):
                        return self # not relevant here
            8
            9
           10
                   def transform(self,X):
           11
                       Transforms columns of X specified in self.columns using
           12
           13
                       LabelEncoder(). If no columns specified, transforms all
           14
                       columns in X.
                        1.1.1
           15
                       output = X.copy()
           16
           17
                        if self.columns is not None:
           18
                            for col in self.columns:
           19
                                output[col] = LabelEncoder().fit_transform(output[col])
           20
                        else:
           21
                            for colname,col in output.iteritems():
           22
                                output[colname] = LabelEncoder().fit_transform(col)
           23
                        return output
           24
           25
                   def fit transform(self, X, y=None):
           26
                        return self.fit(X,y).transform(X)
In [232]:
            1
               df = MultiColumnLabelEncoder(columns = ['Country', 'Status']).fit transf
            2
            1
In [233]:
               df.dtypes
Out[233]: Country
                                                  int64
          Year
                                                  int64
          Status
                                                  int64
          Life expectancy
                                                float64
          Adult Mortality
                                                float64
          infant deaths
                                                  int.64
          Alcohol
                                                float64
          percentage expenditure
                                               float64
          Hepatitis B
                                                float64
          Measles
                                                  int64
           BMT
                                                float64
          under-five deaths
                                                  int.64
          Polio
                                                float64
          Total expenditure
                                                float64
          Diphtheria
                                                float64
           HIV/AIDS
                                                float64
          GDP
                                                float64
          Population
                                                float.64
           thinness 1-19 years
                                                float64
           thinness 5-9 years
                                                float64
           Income composition of resources
                                               float64
           Schooling
                                                float64
          dtype: object
```

```
In [322]:
            1
               class MultiColumnSimpleImputer:
            2
            3
                   def __init__(self,columns = None):
            4
                       self.columns = columns # array of column names to encode
            5
            6
                   def fit(self, X, y=None):
            7
                       return self # not relevant here
            8
            9
                   def transform(self,X):
           10
                       output = X.copy()
           11
                       if (self.columns is not None):
           12
                           for col in self.columns:
           13
                                if ((output[col].dtypes == 'float64') or (output[col].d
           14
                                    output[col] = SimpleImputer(missing values=np.nan,
           15
                               else:
           16
                                    output[col] = SimpleImputer(missing_values=np.nan,
           17
                       else:
           18
                           for colname,col in output.iteritems():
           19
                               output[col] = SimpleImputer(missing values=np.nan, stra
           20
           21
                       return output
           22
           23
                   def fit_transform(self,X,y=None):
           24
                       return self.fit(X,y).transform(X)
  In [ ]:
            1
In [324]:
            1
               #MultiColumnSimpleImputer(df.columns).fit transform(df)
            2
In [304]:
               from sklearn.impute import SimpleImputer
            1
               imp mean = SimpleImputer(missing values=np.nan, strategy='mean')
            2
               df transform = imp mean.fit transform(df)
            3
               #df
In [186]:
            1
               df_transformed = pd.DataFrame(df_transform, columns = df.columns)
```

Out[186]:

|   | Country | Year   | Status | Life expectancy | Adult<br>Mortality | infant<br>deaths | Alcohol | percentage<br>expenditure | Hepatitis<br>B | Measles |
|---|---------|--------|--------|-----------------|--------------------|------------------|---------|---------------------------|----------------|---------|
| 0 | 0.0     | 2015.0 | 1.0    | 65.0            | 263.0              | 62.0             | 0.01    | 71.279624                 | 65.0           | 1154.0  |
| 1 | 0.0     | 2014.0 | 1.0    | 59.9            | 271.0              | 64.0             | 0.01    | 73.523582                 | 62.0           | 492.0   |
| 2 | 0.0     | 2013.0 | 1.0    | 59.9            | 268.0              | 66.0             | 0.01    | 73.219243                 | 64.0           | 430.0   |
| 3 | 0.0     | 2012.0 | 1.0    | 59.5            | 272.0              | 69.0             | 0.01    | 78.184215                 | 67.0           | 2787.0  |
| 4 | 0.0     | 2011.0 | 1.0    | 59.2            | 275.0              | 71.0             | 0.01    | 7.097109                  | 68.0           | 3013.0  |

5 rows × 22 columns

df transformed.head()

```
In [ ]: 1
```

```
In [327]:
               mno.matrix(df_transformed, figsize = (20, 6))
Out[327]: <matplotlib.axes._subplots.AxesSubplot at 0x1a2afa9c50>
                                                                     Thines 1,19 years
                                                                        Hillings 50 years
               County Year Status life storethich
In [329]:
               df transformed.columns
Out[329]: Index(['Country', 'Year', 'Status', 'Life expectancy ', 'Adult Mortalit
          у',
                  'infant deaths', 'Alcohol', 'percentage expenditure', 'Hepatitis
           В',
                  'Measles ', ' BMI ', 'under-five deaths ', 'Polio', 'Total expendi
          ture',
                  'Diphtheria ', ' HIV/AIDS', 'GDP', 'Population',
                  'thinness 1-19 years', 'thinness 5-9 years',
                  'Income composition of resources', 'Schooling'],
                 dtype='object')
In [341]:
               from sklearn.model selection import train test split
               X = df transformed.drop(['Life expectancy '], axis=1)
               y = df transformed['Life expectancy ']
               X train, X test, y train, y test = train test split(X, y, test size=0.3
```

```
In [351]:
              from sklearn.ensemble import RandomForestRegressor
              from sklearn.model selection import RandomizedSearchCV
           2
              # Number of trees in random forest
           3
              n_estimators = [int(x) for x in np.linspace(start = 200, stop = 2000, r
              # Number of features to consider at every split
           5
              max features = ['auto', 'sqrt']
              # Maximum number of levels in tree
           7
              max depth = [int(x) for x in np.linspace(10, 110, num = 11)]
              max depth.append(None)
              # Minimum number of samples required to split a node
          10
          11
              min samples split = [2, 5, 10]
              # Minimum number of samples required at each leaf node
          12
          13
              min samples leaf = [1, 2, 4]
          14
              # Method of selecting samples for training each tree
              bootstrap = [True, False]
          15
          16
              random_grid = {'n_estimators': n_estimators,
          17
                              'max_features': max_features,
          18
                              'max depth': max depth,
          19
                              'min_samples_split': min_samples_split,
          20
                              'min samples leaf': min samples leaf,
          21
                              'bootstrap': bootstrap}
In [398]:
             rf = RandomForestRegressor()
           1
              # Random search of parameters, using 3 fold cross validation,
           2
              # search across 100 different combinations, and use all available cores
              #rf random = RandomizedSearchCV(estimator = rf, param_distributions = 1
              # Fit the random search model
              rf.fit(X_train, y_train)
Out[398]: RandomForestRegressor(bootstrap=True, criterion='mse', max_depth=None,
                                max features='auto', max leaf nodes=None,
                                min impurity decrease=0.0, min impurity split=None,
                                min samples leaf=1, min samples split=2,
                                min weight fraction leaf=0.0, n estimators=10,
                                n jobs=None, oob score=False, random state=None,
                                verbose=0, warm start=False)
In [404]:
              new ans = rf.predict(X test)
In [414]:
           1
              import graphviz
           2
              from sklearn.tree import DecisionTreeClassifier, export graphviz
           3
              import pydot
           4
           5
              from IPython.display import display
           6
              #forest clf = RandomForestClassifier()
           7
              #forest clf.fit(X train, y train)
              tree.export graphviz(rf.estimators [0], out file='tree from forest.dot
           9
              (graph,) = pydot.graph from dot file('tree from forest.dot')
              graph.write png('tree from forest.png')
          10
           11
              #Let's go back to our hypothetical medication study. Suppose the hypoth
In [431]:
           1
           2
            3
              #If the medicine has no effect in the population as a whole, 3% of stud
```

```
In [422]: 1
2   import numpy as np
3   import statsmodels.api as sm
4   import matplotlib.pyplot as plt
5   from statsmodels.sandbox.regression.predstd import wls_prediction_std
In [430]: 1 len(X_train['Country'])
2
```

Out[430]: 1968

```
In [423]: 1 model = sm.OLS(y_train, X_train)
2 results = model.fit()
3 print(results.summary())
```

# OLS Regression Results

| =========                             |                |                 |       |             |             |        |  |
|---------------------------------------|----------------|-----------------|-------|-------------|-------------|--------|--|
| Dep. Variable: 0.997                  | Life e         | expectancy      | R-sq  | uared (unce | entered):   |        |  |
| Model: 0.997                          |                | OLS             | Adj.  | R-squared   | (uncentered | ):     |  |
| Method:                               | Lea            | st Squares      | F-st  | atistic:    |             |        |  |
| 2.764e+04<br>Date:                    | Sun, O         | 08 Dec 2019     | Prob  | (F-statist  | ic):        |        |  |
| 0.00<br>Time:                         |                | 23:48:18        | Τισα- | Likelihood: |             |        |  |
| -5546.9                               |                |                 | -     |             |             |        |  |
| No. Observations: 1.114e+04           |                | 1968            | AIC:  |             |             |        |  |
| Df Residuals:<br>1.125e+04            |                | 1947            | BIC:  |             |             |        |  |
| <pre>Df Model: Covariance Type:</pre> |                | 21<br>nonrobust |       |             |             |        |  |
| ===========                           |                |                 | ===== | =======     | -======     | ====== |  |
| ===========                           | =======        |                 | coef  | std err     | t           | P>     |  |
| t  [0.025                             | 0.975]         |                 |       |             |             |        |  |
| Country                               |                | 0.              | .0032 | 0.002       | 1.955       | 0.0    |  |
| 51 -9.78e-06                          | 0.006          | <b>V</b> •      |       | 0000        | 2000        |        |  |
| Year 0.028                            | 0.029          | 0.              | 0283  | 0.000       | 68.254      | 0.0    |  |
| Status                                |                | -1.             | 6003  | 0.328       | -4.880      | 0.0    |  |
| 00 -2.244<br>Adult Mortality          | -0.95/         | -0.             | 0198  | 0.001       | -19.913     | 0.0    |  |
| 00 -0.022 infant deaths               | -0.018         | 0.              | 1009  | 0.010       | 9.663       | 0.0    |  |
| 0.080                                 | 0.121          |                 |       |             |             |        |  |
| Alcohol 0.005                         | 0.130          | 0.              | 0671  | 0.032       | 2.106       | 0.0    |  |
| percentage expend<br>01 -6.96e-05     | iture<br>0.000 | 0.              | 0001  | 0.000       | 1.280       | 0.2    |  |
| Hepatitis B                           |                | -0.             | 0146  | 0.005       | -3.044      | 0.0    |  |
| 02 -0.024<br>Measles                  | -0.005         | -2.515          | 5e-05 | 9.12e-06    | -2.758      | 0.0    |  |
| 06 -4.3e-05<br>BMI                    | -7.26e-06      | 0.              | 0407  | 0.006       | 6.690       | 0.0    |  |
| 00 0.029                              | 0.053          |                 |       |             |             |        |  |
| under-five deaths 00 -0.090           | -0.060         | -0.             | 0746  | 0.008       | -9.780      | 0.0    |  |
| Polio<br>00 0.014                     | 0.036          | 0.              | 0249  | 0.006       | 4.390       | 0.0    |  |
| Total expenditure                     | !              | 0.              | 0218  | 0.041       | 0.525       | 0.5    |  |
| 99 -0.060<br>Diphtheria               | 0.103          | 0.              | 0374  | 0.006       | 6.376       | 0.0    |  |
| 0.026                                 | 0.049          |                 |       |             |             |        |  |

|                     |          | iiie-exp | )         |             |         |     |
|---------------------|----------|----------|-----------|-------------|---------|-----|
| HIV/AIDS            |          | -0.4     | 1772      | 0.021       | -22.266 | 0.0 |
|                     | -0.435   |          |           |             |         |     |
| GDP<br>80 -3.23e-06 | 5.7e-05  | 2.696    | 9-05      | 1.54e-05    | 1.751   | 0.0 |
| Population          | 5.7e-05  | -6 6546  | _10       | 2.44e-09    | -0.273  | 0.7 |
| 85 -5.45e-09        | 4.12e-09 | -0.0340  |           | 2.446-09    | -0.273  | 0.7 |
| thinness 1-19 y     |          | -0.0     | 796       | 0.060       | -1.335  | 0.1 |
| 82 -0.197           | 0.037    |          |           |             |         |     |
| thinness 5-9 yea    | rs       | 0.0      | 0037      | 0.059       | 0.063   | 0.9 |
| 50 -0.112           | 0.120    |          |           |             |         |     |
| Income composition  |          | ces 6.1  | L349      | 0.802       | 7.645   | 0.0 |
|                     | 7.709    |          |           | 0.050       | 10 604  | 0 0 |
| Schooling           | 0 565    | 0.6      | 5616      | 0.052       | 12.604  | 0.0 |
| 00 0.559            | 0.765    |          |           |             |         |     |
| =====               |          |          |           |             |         |     |
| Omnibus:            |          | 87.099   | Durb      | oin-Watson: |         |     |
| 1.999               |          |          |           |             |         |     |
| Prob(Omnibus):      |          | 0.000    | Jaro      | que-Bera (J | B):     | 23  |
| 6.355               |          |          |           |             |         |     |
| Skew:               |          | -0.184   | Prob      | )(JB):      |         | 4.7 |
| 5e-52               |          | 4 657    | <b>a</b>  | 1           |         | 2.0 |
| Kurtosis:<br>2e+08  |          | 4.657    | Conc      | l. No.      |         | 3.9 |
| ∠e⊤∪ŏ<br>========== |          | ======   |           | ======      | ======  |     |
|                     |          |          | <b></b> - |             |         |     |

=====

## Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 3.92e+08. This might indicate that the re are

strong multicollinearity or other numerical problems.

```
print('Parameters: ', results.params)
In [419]:
            1
              print('R2: ', results.rsquared)
            2
            3
          Parameters: Country
                                                           3.228836e-03
          Year
                                              2.834522e-02
          Status
                                             -1.600320e+00
          Adult Mortality
                                             -1.982795e-02
          infant deaths
                                              1.009259e-01
          Alcohol
                                              6.707656e-02
          percentage expenditure
                                              1.308046e-04
          Hepatitis B
                                             -1.458378e-02
          Measles
                                             -2.514781e-05
           BMI
                                              4.070490e-02
          under-five deaths
                                             -7.461739e-02
                                              2.485544e-02
          Polio
          Total expenditure
                                              2.179709e-02
          Diphtheria
                                              3.737595e-02
           HIV/AIDS
                                             -4.772125e-01
          GDP
                                              2.690468e-05
          Population
                                             -6.654124e-10
           thinness 1-19 years
                                             -7.962809e-02
           thinness 5-9 years
                                              3.741886e-03
          Income composition of resources
                                              6.134878e+00
          Schooling
                                              6.615710e-01
          dtype: float64
          R2: 0.9966563487669086
In [433]:
            1
              import numpy as np
              from sklearn.linear model import LinearRegression
            2
            3
              \#>>> X = np.array([[1, 1], [1, 2], [2, 2], [2, 3]])
              \#>>> \# y = 1 * x 0 + 2 * x 1 + 3
            4
              \#>>> y = np.dot(X, np.array([1, 2])) + 3
            5
              reg = LinearRegression().fit(X train, y train)
              #reg.score(X, y)
In [434]:
              reg.score(X, y)
Out[434]: 0.8197513550724889
In [442]:
              reg.coef
Out[442]: array([ 3.21119912e-03, 2.00132715e-03, -1.57661894e+00, -1.97239820e-0
          2,
                  1.00552922e-01, 6.16509079e-02, 1.18951459e-04, -1.44508920e-0
          2,
                 -2.56680107e-05, 4.06253988e-02, -7.43388467e-02, 2.46560630e-0
          2,
                  2.73154781e-02, 3.75368626e-02, -4.80112235e-01, 2.88480648e-0
          5,
                 -6.30147861e-10, -7.79598914e-02, 2.81391552e-03, 6.26047718e+0
          0,
                  6.67670054e-011)
```

```
In [441]:
              reg.intercept_
Out[441]: 52.68181514202163
In [450]:
              y_pred = reg.predict(X_test)
           1
           2
In [458]:
              from sklearn.metrics import r2 score, mean squared error, mean absolute
           1
              from math import sqrt
           2
In [482]:
           1
              def print_score(y_test, y_pred):
                  print(" mean absolute error =
           2
                                                   {} ".format(round(mean absolute €
           3
                  print(" mean squared error
                                                   {} ".format(round(mean_squared_er
                                            =
           4
                  print(" root mean squared error = {} ".format(round(sqrt(mean squar
                  print(" r2_score =
           5
                                                   {} ".format(round(r2 score(y test
           6
In [459]:
              mean squared error?
In [510]:
              print score(y test, y pred)
           mean absolute error =
                                    2.937
          mean squared error
                                    16.022
           root_mean_squared_error = 4.003
           r2 score =
                                    0.826
              round(2.7817191, ndigits= 3)
In [466]:
Out[466]: 2.782
In [583]:
           1
              from sklearn import linear model
              clf = linear model.Lasso(alpha=1)
           2
              clf.fit(X train, y train)
Out[583]: Lasso(alpha=1, copy X=True, fit intercept=True, max iter=1000, normalize=
          False,
               positive=False, precompute=False, random state=None, selection='cyc
          lic',
               tol=0.0001, warm start=False)
 In [ ]:
           1
In [579]:
              print(clf.coef )
          8.85865351e-02 9.56471060e-02 1.66652748e-04 -1.25303024e-02
           -3.06587413e-05 5.35835119e-02 -6.58977372e-02 2.52542915e-02
            0.00000000e+00 4.32485363e-02 -4.34057521e-01
                                                          5.32035204e-05
            1.19951964e-10 -3.94846945e-02 -0.00000000e+00 0.00000000e+00
            8.27412021e-01]
```

```
In [580]:
               print(clf.intercept_)
          56.434209676507805
In [581]:
               y_pred_l = clf.predict(X_test)
In [582]:
               print_score(y_test, y_pred_1)
           mean absolute error =
                                      2.99
           mean squared error
                                      16.751
           root_mean_squared_error = 4.093
           r2_score =
                                      0.818
In [600]:
              from sklearn import linear model
            1
            2
              #sklearn.linear model.Ridge
              clf = linear model.Ridge(alpha=0.01)
            3
              clf.fit(X_train, y_train)
Out[600]: Ridge(alpha=0.01, copy_X=True, fit_intercept=True, max_iter=None,
                normalize=False, random state=None, solver='auto', tol=0.001)
In [601]:
              print(clf.coef_)
          [ 3.21118420e-03 2.00926971e-03 -1.57658134e+00 -1.97243352e-02
            1.00556085e-01 6.16596866e-02 1.18940852e-04 -1.44512583e-02
           -2.56688588e-05 4.06264691e-02 -7.43410472e-02 2.46558922e-02
            2.73047814e-02 3.75380577e-02 -4.80113387e-01
                                                             2.88533299e-05
           -6.30161628e-10 -7.79654641e-02 2.81619556e-03 6.25803872e+00
            6.67765661e-011
In [602]:
              y pred l = clf.predict(X test)
In [603]:
               print_score(y_test, y_pred_1)
           mean absolute error =
                                      2.937
           mean squared error
                                      16.022
                                =
           root mean squared error = 4.003
           r2 score =
                                      0.826
In [604]:
            1
               from sklearn.linear model import ElasticNet
            2
In [605]:
               regr = ElasticNet(random state=0)
            2
               regr.fit(X train, y train)
            3
Out[605]: ElasticNet(alpha=1.0, copy X=True, fit intercept=True, l1 ratio=0.5,
                     max iter=1000, normalize=False, positive=False, precompute=Fal
          se,
                     random state=0, selection='cyclic', tol=0.0001, warm start=Fal
          se)
In [610]:
               y pred r = regr.predict(X test)
```

```
In [607]:
            1
               print(regr.coef_)
          [ 3.07948392e-03 8.03124380e-03 -0.00000000e+00 -2.27788706e-02
            9.99014440e-02 1.28906758e-01 1.51438845e-04 -1.40664886e-02
           -2.97554470e-05 5.10817223e-02 -7.38323401e-02
                                                              2.57368590e-02
            0.00000000e+00 4.31514582e-02 -4.46882496e-01
                                                              5.28701233e-05
           -3.18901057e - 10 \quad -7.04940446e - 02 \quad -0.00000000e + 00 \quad 0.00000000e + 00
            8.08000374e-01]
In [608]:
            1
               print(regr.intercept_)
            2
            3
          40.646272811209904
In [612]:
               print score(y test, y pred r)
           mean_absolute_error =
                                      2.987
           mean squared error
                                      16.614
           root mean squared error = 4.076
           r2 score =
                                      0.819
In [637]:
               from sklearn.tree import DecisionTreeRegressor
            1
            2
            3
              # create a regressor object
              regressor = DecisionTreeRegressor(random_state = 0, max_depth = 6)
            5
               # fit the regressor with X and Y data
               regressor.fit(X train, y train)
Out[637]: DecisionTreeRegressor(criterion='mse', max depth=6, max features=None,
                                 max leaf nodes=None, min impurity decrease=0.0,
                                 min impurity split=None, min samples leaf=1,
                                 min samples split=2, min weight fraction leaf=0.0,
                                 presort=False, random state=0, splitter='best')
In [638]:
               y pred tree = regressor.predict(X test)
In [639]:
               print_score(y_test, y_pred_tree)
           mean absolute error =
           mean squared error
                                      7.032
           root mean squared error = 2.652
           r2 score =
                                      0.923
```

```
In [640]:
               from sklearn.externals.six import StringIO
            2
               from IPython.display import Image
              from sklearn.tree import export_graphviz
            3
            4
              import pydotplus
            5
              dot_data = StringIO()
              export_graphviz(regressor, out_file=dot_data,
            7
                               filled=True, rounded=True,
                               special characters=True)
            8
            9
               graph = pydotplus.graph from dot data(dot data.getvalue())
           10
               Image(graph.create_png())
Out[640]:
In [642]:
               graph.write_pdf("iris.pdf")
            1
            2
Out[642]: True
In [644]:
               #Image(graph.create png())
In [645]:
            1
               from sklearn.ensemble import ExtraTreesRegressor
In [682]:
              regressor = ExtraTreesRegressor(random state = 0, max depth = 10)
            1
            2
            3
               # fit the regressor with X and Y data
               regressor.fit(X train, y train)
Out[682]: ExtraTreesRegressor(bootstrap=False, criterion='mse', max depth=10,
                               max features='auto', max leaf nodes=None,
                               min impurity decrease=0.0, min impurity split=None,
                               min samples leaf=1, min samples split=2,
                               min weight fraction leaf=0.0, n estimators=10, n jobs
          =None,
                               oob score=False, random state=0, verbose=0,
                               warm start=False)
In [683]:
               y_pred_extra = regressor.predict(X_test)
In [684]:
               print_score(y_test, y_pred_extra)
           mean absolute error =
                                      1.311
           mean squared error
                                      3.751
           root mean squared error = 1.937
           r2 score =
                                      0.959
In [685]:
               from sklearn.ensemble import GradientBoostingRegressor
```

```
In [690]:
            1
              regressor = GradientBoostingRegressor(random_state = 0, max_depth = 11)
            2
            3
               # fit the regressor with X and Y data
               regressor.fit(X_train, y_train)
Out[690]: GradientBoostingRegressor(alpha=0.9, criterion='friedman mse', init=None,
                                     learning rate=0.1, loss='ls', max depth=11,
                                     max_features=None, max_leaf_nodes=None,
                                     min_impurity_decrease=0.0, min_impurity_split=N
          one,
                                     min_samples_leaf=1, min_samples_split=2,
                                     min_weight_fraction_leaf=0.0, n_estimators=100,
                                     n iter_no_change=None, presort='auto', random_s
          tate=0,
                                     subsample=1.0, tol=0.0001, validation_fraction=
          0.1,
                                     verbose=0, warm_start=False)
In [691]:
               y pred xg = regressor.predict(X_test)
In [692]:
               print score(y test, y pred extra)
           mean absolute error =
                                      1.058
           mean squared error
                                      2.939
           root mean squared error = 1.714
           r2_score =
                                      0.968
            1
  In [ ]:
```