

KB_ENTAILMENT

January 5, 2022

```
[35]: combination=[(True,True,True),(True,True,False),(True,False,True),(True,False,False),(False,Tr
```

```
[36]: variable={'p':0,'q':1,'r':2}
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[37]: kb= ''
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```
[38]: q= ''
```

```
[39]: priority={'~':3,'v':1,'^':2}
```

```
[40]: def input_rules():
    global kb,q
    kb=input('Enter the rule: ')
    q=input('Enter the query: ')
```

```
[52]: def entailment():
    global kb,q
    print("kb","alpha")
    print('*' * 10)
    print('POSTFIX OF KB IS ' + str(topostfix(kb)))
    print('POSTFIX OF THE QUERY IS ' + str(topostfix(q)))
    for comb in combination:

        s=evaluate_postfix(topostfix(kb),comb)

        f=evaluate_postfix(topostfix(q),comb)
        print(s,f)

        if s and not f:
            return False
    return True
```

```

[53]: def isoperand(c):
        return c.isalpha() and c!='v'

[54]: def isleftparenthesis(c):
        return c=='('

[55]: def isrightparenthesis(c):
        return c==')'

[56]: def isEmpty(stack):
        return len(stack)==0

[57]: def peek(stack):
        return stack[-1]

[58]: def has_less_or_equal_priority(c1,c2):
        try:
            return priority[c1]<=priority[c2]
        except KeyError: return False

[59]: def topostfix(infix):
        stack=[]
        postfix=''
        for c in infix:
            if isoperand(c):
                postfix+=c
            else:
                if isleftparenthesis(c):
                    stack.append(c)
                elif isrightparenthesis(c):
                    operator=stack.pop()
                    while not isleftparenthesis(operator):
                        postfix+=operator
                        operator=stack.pop()
                else:
                    while (not isEmpty(stack) and
↪has_less_or_equal_priority(c,peek(stack))):
                        postfix+=stack.pop()
                        stack.append(c)
        while(not isEmpty(stack)):
            postfix+=stack.pop();
        return postfix

```

```
[60]: def _eval(i,val1,val2):
        if i=='^':
            return val1 and val2
        return val1 or val2
```

```
[61]: def evaluate_postfix(exp,comb):
        stack=[]
        for i in exp:
            if isoperand(i):
                stack.append(comb[variable[i]])
            elif i=='~':
                val1=stack.pop();
                stack.append(not val1)
            else:
                val1=stack.pop()
                val2=stack.pop()
                stack.append(_eval(i,val1,val2))
        return stack.pop();
```

```
[62]: input_rules()
ans = entailment()
if ans: print("The Knowledge Base Entails Query")
else: print("The Knowledge Base Doesn't Entail Query")
```

Enter the rule: $(\sim q \vee \sim p \vee r) \wedge (\sim q \wedge p) \wedge q$

Enter the query: r

kb alpha

POSTFIX OF KB IS $q \sim p \sim v r v q \sim p \wedge q \wedge$

POSTFIX OF THE QUERY IS r

False True

False False

False True

False False

False True

False False

False True

False False

The Knowledge Base Entails Query

```
[ ]:
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KB_RESOLUTION

January 6, 2022

```
[31]: def disjunctify(clauses):  
    disjuncts=[]  
    for clause in clauses:  
        disjuncts.append(tuple(clause.split('v')))  
    return disjuncts
```

```
[32]: def getresolvent(ci,cj,di,dj):  
    resolvent=list(ci) + list(cj)  
    resolvent.remove(di)  
    resolvent.remove(dj)  
    return tuple(resolvent)
```

```
[33]: def resolve(ci,cj):  
    for di in ci:  
        for dj in cj:  
            if di == '~' + dj or dj == '~' + di:  
                return getresolvent(ci,cj,di,dj)
```

```
[38]: def check_resolution(clauses,query):  
    clauses+= [query if query.startswith('~') else '~' + query]  
    proposition='^'.join(['(' + clause + ')'] for clause in clauses)  
    print(f'Trying to prove {proposition} by contradiction...')  
    clauses=disjunctify(clauses)  
    resolved=False  
    new=set()  
  
    while not resolved:  
        n=len(clauses)  
        pairs = [(clauses[i], clauses[j]) for i in range(n) for j in range(i + 1, n)]  
        for (ci,cj) in pairs:  
            resolvent=resolve(ci,cj)  
            if not resolvent:  
                resolved=True  
                break
```

```

        new=new.union(set(resolvant))
    if new.issubset(set(clauses)):
        break
    for clause in new:
        if clause not in clauses:
            clauses.append(clause)

    if resolved:
        print('SUCCESSFULLY PROVED BY RESOLUTION')
    else:
        print('CANNOT BE PROVED')

```

```

[39]: clauses = input('Enter the clauses ').split()
      query = input('Enter the query: ')
      check_resolution(clauses, query)

```

```

Enter the clauses AvB BvC ~C
Enter the query: B
Trying to prove (AvB)^(BvC)^(~C)^(~B) by contradiction...
SUCCESSFULLY PROVED BY RESOLUTION

```

```

[43]: clauses = input('Enter the clauses ').split()
      query = input('Enter the query: ')
      check_resolution(clauses, query)

```

```

Enter the clauses ~Qv~PvR ~Q^P Q
Enter the query: Q
Trying to prove (~Qv~PvR)^(~Q^P)^(Q)^(~Q) by contradiction...
SUCCESSFULLY PROVED BY RESOLUTION

```

```

[ ]:

```

FINAL_UNIFICATION

January 12, 2022

```
[495]: predicate=[]
```

```
[496]: no_of_arg=[]
```

```
[497]: arguement=[]
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```
[498]: no_of_predicat=0
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```
[499]: expressions=[]
```

```
[500]: fu=[]
```

```
[501]: lst=[]
```

```
[502]: def function1():  
    print('-----PROGRAM FOR UNIFICATION-----')  
    no_of_predicat=int(input('Enter the number of predicate '))  
    for i in range(no_of_predicat):  
        expr=input('Enter the expression ' + str(i) + " ")  
        expressions.append(expr)  
    for exp in expressions:  
        fu=exp.split('(')  
        one=fu[0]  
        predicate.append(one)  
        lst=fu[1]  
        lst=lst[:-1]  
        lst=lst.split(',')  
  
        if lst:  
            arguement.append(lst)  
    check_arg(no_of_predicat)
```

```
[503]: def check_arg(no_of_predicat):
```

```
    pred_flag=0
```

```

arg_flag=0
print('-----CHCEKING PREDICATES-----')

for i in range(no_of_predicat-1):

    if predicate[i]!=predicate[i+1]:
        print('PREDICAT NOT SAME')
        print('CANNOT BE UNIFIED')
        pred_flag=1
        break

if pred_flag!=1:
    for i in range(no_of_predicat-1):
        len1=len(arguement[i])
        len2=len(arguement[i+1])
        if len1!=len2:
            print('Arguement are not same cannot be unified')
            arg_flag=1
            break

if(arg_flag==0 and pred_flag==0):
    unify(no_of_predicat)

```

```

[504]: def unify(no_of_predicat):

    flag=0
    for i in range(no_of_predicat-1):

        for j in range(len(arguement[i])):

            if arguement[i][j]!=arguement[i+1][j]:

                print(' SUBSTITUTE ' + str(arguement[i][j]) + '/' +
↳str(arguement[i+1][j]))
                arguement[i][j]=arguement[i+1][j]
                flag+=1

    if flag==0:
        print(' AREGUEMENT ARE IDENTICAL NO SUBSTITUTION REQUIRED ')
        print(' NO NEED OF SUBSTITUTION ')

```

```

[493]: function1()

```

```

-----PROGRAM FOR UNIFICATION-----
Enter the number of predicate 2

```

```

Enter the expression 0 king(x,john)
Enter the expression 1 queen(y,jane)
-----CHCEKING PREDICATES-----
PREDICAT NOT SAME
CANNOT BE UNIFIED

```

[505]: function1()

```

-----PROGRAM FOR UNIFICATION-----
Enter the number of predicate 2
Enter the expression 0 knows(john,x)
Enter the expression 1 knows(y,bill)
-----CHCEKING PREDICATES-----
SUBSTITUTE john/y
SUBSTITUTE x/bill

```

[482]: function1()

```

-----PROGRAM FOR UNIFICATION-----
Enter the number of predicate 2
Enter the expression 0 studies(x,g(x))
Enter the expression 1 studies(z,g(z))
-----CHCEKING PREDICATES-----
2
range(0, 1)
SUBSTITUTE x/z

```

[]:

FOL_TO_CNF

January 13, 2022

```
[1]: def getAttributes(string):
    expr = '\([^~]+\)'
    matches = re.findall(expr, string)
    return [m for m in str(matches) if m.isalpha()]

def getPredicates(string):
    expr = '[a-z~]+\([A-Za-z,]+\)'
    return re.findall(expr, string)

def DeMorgan(sentence):
    string = ''.join(list(sentence).copy())
    string = string.replace('~', '')
    flag = '[' in string
    string = string.replace('~[', '')
    string = string.strip(']')
    for predicate in getPredicates(string):
        string = string.replace(predicate, f'~{predicate}')
    s = list(string)
    for i, c in enumerate(string):
        if c == '|':
            s[i] = '&'
        elif c == '&':
            s[i] = '|'
    string = ''.join(s)
    string = string.replace('~', '')
    return f'[{string}]' if flag else string

def Skolemization(sentence):
    SKOLEM_CONSTANTS = [f'{chr(c)}' for c in range(ord('A'), ord('Z')+1)]
    statement = ''.join(list(sentence).copy())
    matches = re.findall('[ ].', statement)
    for match in matches[::-1]:
        statement = statement.replace(match, '')
        statements = re.findall('\[\[\^]+\]', statement)
        for s in statements:
            statement = statement.replace(s, s[1:-1])
        for predicate in getPredicates(statement):
```

```

        attributes = getAttributes(predicate)
        if ''.join(attributes).islower():
            statement = statement.replace(match[1], SKOLEM_CONSTANTS.pop(0))
        else:
            aL = [a for a in attributes if a.islower()]
            aU = [a for a in attributes if not a.islower()][0]
            statement = statement.replace(aU, f'{SKOLEM_CONSTANTS.
→pop(0)}({aL[0] if len(aL) else match[1]})')
        return statement

```

```

[2]: import re

def fol_to_cnf(fol):

    statement = fol.replace("<=>", "_")
    while '_' in statement:
        i = statement.index('_')
        new_statement = '[' + statement[:i] + '=>' + statement[i+1:] + ']&[' +
→statement[i+1:] + '=>' + statement[:i] + ']'
        statement = new_statement
    statement = statement.replace("=>", "-")
    expr = '\\([([~])+)\\)'
    statements = re.findall(expr, statement)
    for i, s in enumerate(statements):
        if '[' in s and ']' not in s:
            statements[i] += ']'
    for s in statements:
        statement = statement.replace(s, fol_to_cnf(s))
    while '-' in statement:
        i = statement.index('-')
        br = statement.index('(') if '[' in statement else 0
        new_statement = '~' + statement[br:i] + '|' + statement[i+1:]
        statement = statement[:br] + new_statement if br > 0 else new_statement
    while '~' in statement:
        i = statement.index('~')
        statement = list(statement)
        statement[i], statement[i+1], statement[i+2] = ' ', statement[i+2], '~'
        statement = ''.join(statement)
    while '~' in statement:
        i = statement.index('~')
        s = list(statement)
        s[i], s[i+1], s[i+2] = ' ', s[i+2], '~'
        statement = ''.join(s)
    statement = statement.replace('~[ ', '[~ ')
    statement = statement.replace('~[ ', '[~ ')
    expr = '(~[ | ].)'
    statements = re.findall(expr, statement)

```

```

for s in statements:
    statement = statement.replace(s, fol_to_cnf(s))
expr = '~\[[~]+\]'
statements = re.findall(expr, statement)
for s in statements:
    statement = statement.replace(s, DeMorgan(s))
return statement

```

```

[3]: n = int(input())
while n:
    statement = input("Enter FOL statement: ")
    print(f"FOL converted to CNF: {Skolemization(fol_to_cnf(statement))} \n\n")
    n -= 1

```

3

Enter FOL statement:

[american(x)&weapon(y)&sells(x,y,z)&hostile(z)]=>criminal(x)

FOL converted to CNF:

[~american(x)|~weapon(y)|~sells(x,y,z)|~hostile(z)]|criminal(x)

Enter FOL statement: x[y[animal(y)=>loves(x,y)]]=>[z[loves(z,x)]]

FOL converted to CNF: [animal(G(x))&~loves(x,G(x))]|[loves(F(x),x)]

Enter FOL statement: animal(y)<=>loves(x,y)

FOL converted to CNF: [~animal(y)|loves(x,y)]&[~loves(x,y)|animal(y)]

[]:

FOL_FORWARD_REASONING

January 13, 2022

- 1 Create a knowledgebase consisting of first order logic statements and prove the given query using forward reasoning

```
[1]: import re

def isVariable(x):
    return len(x) == 1 and x.islower() and x.isalpha()

def getAttributes(string):
    expr = '\\([~])+\\)'
    matches = re.findall(expr, string)
    return matches

def getPredicates(string):
    expr = '([a-z~]+)\\([~&|]+\\)'
    return re.findall(expr, string)

[2]: class Fact:
    def __init__(self, expression):
        self.expression = expression
        predicate, params = self.splitExpression(expression)
        self.predicate = predicate
        self.params = params
        self.result = any(self.getConstants())

    def splitExpression(self, expression):
        predicate = getPredicates(expression)[0]
        params = getAttributes(expression)[0].strip('()').split(',')
        return [predicate, params]

    def getResult(self):
        return self.result

    def getConstants(self):
        return [None if isVariable(c) else c for c in self.params]

    def getVariables(self):
```

```

        return [v if isVariable(v) else None for v in self.params]

    def substitute(self, constants):
        c = constants.copy()
        f = f"{self.predicate}({'.'.join([constants.pop(0) if isVariable(p)
→else p for p in self.params])})"
        return Fact(f)

class Implication:
    def __init__(self, expression):
        self.expression = expression
        l = expression.split('=>')
        self.lhs = [Fact(f) for f in l[0].split('&')]
        self.rhs = Fact(l[1])

    def evaluate(self, facts):
        constants = {}
        new_lhs = []
        for fact in facts:
            for val in self.lhs:
                if val.predicate == fact.predicate:
                    for i, v in enumerate(val.getVariables()):
                        if v:
                            constants[v] = fact.getConstants()[i]
                            new_lhs.append(fact)
        predicate, attributes = getPredicates(self.rhs.expression)[0],
→str(getAttributes(self.rhs.expression)[0])
        for key in constants:
            if constants[key]:
                attributes = attributes.replace(key, constants[key])
        expr = f'{predicate}{attributes}'
        return Fact(expr) if len(new_lhs) and all([f.getResult() for f in
→new_lhs]) else None

class KB:
    def __init__(self):
        self.facts = set()
        self.implications = set()

    def tell(self, e):
        if '=>' in e:
            self.implications.add(Implication(e))
        else:
            self.facts.add(Fact(e))
        for i in self.implications:
            res = i.evaluate(self.facts)
            if res:

```

```

        self.facts.add(res)

    def query(self, e):
        facts = set([f.expression for f in self.facts])
        i = 1
        print(f'Querying {e}:')
        for f in facts:
            if Fact(f).predicate == Fact(e).predicate:
                print(f'\t{i}. {f}')
                i += 1

    def display(self):
        print("All facts: ")
        for i, f in enumerate(set([f.expression for f in self.facts])):
            print(f'\t{i+1}. {f}')

```

```

[3]: kb = KB()
kb.tell('missile(x)=>weapon(x)')
kb.tell('missile(M1)')
kb.tell('enemy(x,America)=>hostile(x)')
kb.tell('american(West)')
kb.tell('enemy(Nono,America)')
kb.tell('owns(Nono,M1)')
kb.tell('missile(x)&owns(Nono,x)=>sells(West,x,Nono)')
kb.tell('american(x)&weapon(y)&sells(x,y,z)&hostile(z)=>criminal(x)')
kb.query('criminal(x)')
kb.display()

```

```

Querying criminal(x):
    1. criminal(West)
All facts:
    1. sells(West,M1,Nono)
    2. criminal(West)
    3. missile(M1)
    4. weapon(M1)
    5. enemy(Nono,America)
    6. american(West)
    7. hostile(Nono)
    8. owns(Nono,M1)

```

```

[ ]:

```