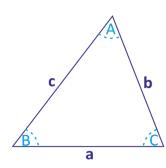
# Cheat Sheet – Solution of Triangles

## All sides (a, b, c)

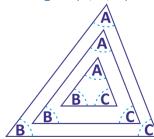


$$A = \cos^{-1} \frac{b^2 + c^2 - a^2}{2bc}$$

$$B = \cos^{-1} \frac{c^2 + a^2 - b^2}{2ca}$$

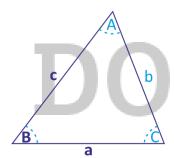
$$C = \cos^{-1} \frac{a^2 + b^2 - c^2}{2ab}$$

# All angles (A, B, C)



 $a: b: c = \sin A : \sin B : \sin C$ 

# Two sides and included angle (a, B, c)



$$b = \sqrt{c^2 + a^2 - 2ca\cos B}$$

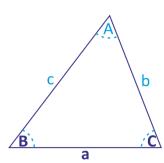
$$b = \sqrt{c^2 + a^2 - 2ca\cos B}$$

$$C = \cos^{-1}\frac{a^2 + b^2 - c^2}{2ab}$$

$$A = \pi - B - C$$

$$A = \pi - B - C$$

#### Two angles and included side (a, B, C)

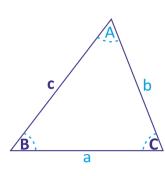


$$A = \pi - B - C$$

$$b = \frac{\sin B}{\sin A}a$$

$$c = \frac{\sin C}{\sin A}a$$

#### Two angles and non-included side (B, C, c)



$$A = \pi - B - C$$

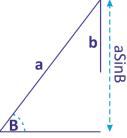
$$a = \frac{\sin A}{\sin C}c$$

$$b = \frac{\sin B}{\sin C}c$$

## Two sides and non-included angle (a, b, B)

#### b < asin B

No triangle possible



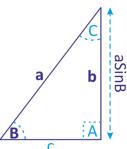
## $b = a \sin B$

One triangle possible

$$A = \pi/2$$

$$C = \pi/2 - A$$

$$c = a\cos B$$



## a > b > asin B, B acute

Two triangles possible

$$A_1 = \sin^{-1}\left(\frac{a\sin B}{b}\right)$$

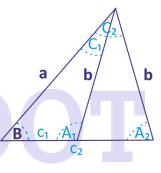
$$A_2 = \pi - \sin^{-1}\left(\frac{a\sin B}{b}\right)$$

$$c_1 = a\cos B + b\cos A_1$$

$$c_2 = a\cos B + b\cos A_2$$

$$C_1 = \pi - A_1 - B$$

$$C_1 = \pi - A_2 - B$$



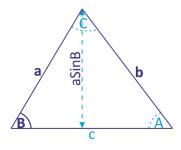
# b > a > a sin B, B acute

One triangle possible

$$A = \sin^{-1} \left( \frac{a \sin B}{b} \right)$$

$$c = a\cos B + b\cos A$$

$$C = \pi - A - B$$



#### $b > a > a \sin B$ , B obtuse

One triangle possible

$$A = \sin^{-1} \left( \frac{a \sin B}{b} \right)$$

$$c = a\cos B + b\cos A$$

$$C = \pi - A - B$$

# a > b > asin B, B obtuse

No triangle possible

