

# ELITES GRID

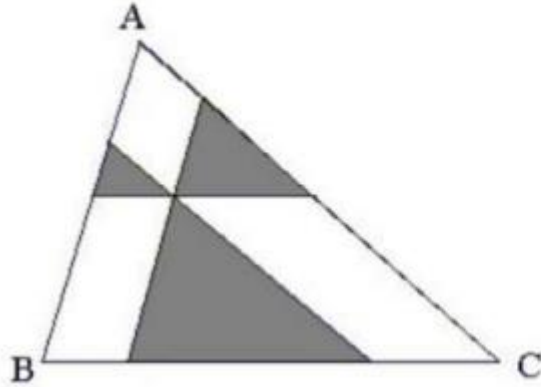
GEOMETRY ASSIGNMENT 4 (TRIANGLE – MIXED TOPICS)

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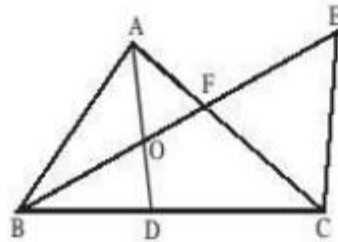
Q.1

Three lines are drawn parallel to each of the three sides of triangle  $ABC$  so that the three lines intersect in the interior of  $ABC$ . The resulting three smaller triangles have areas 1, 4, and 9. Find the area of triangle  $ABC$ .



Q2.

In the figure given below,  $AB = 4$  units,  $AC = 6$  units,  $AD = 3$  units,  $CF = 5$  units,  $BD = DC$  and  $BF$  is extended till  $E$  such that  $BF = FE = 4$  units.  $O$  is the point of intersection of  $AD$  and  $BF$ .



Find the measure of side  $CE$ .

a.  $\sqrt{14}$  cm

b. 4 cm

c. 3.5 cm

d.  $2\sqrt{3}$  cm

**Q3.**

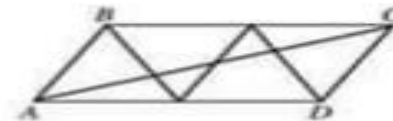
In triangle ABC, the internal angle bisector of  $\angle A$  meets BC at point D. If  $AB = 8$  cm,  $AD = 6$  cm and  $\angle BAC = 120^\circ$ , then what is the length of AC?

- (a) 24 cm                      (b) 12 cm                      (c)  $6\sqrt{3}$  cm                      (d) None of these

**Q4**

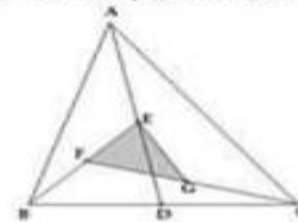
Parallelogram  $ABCD$  is made up of four equilateral triangles of side length 1. The length of diagonal  $AC$  is

- (A)  $\sqrt{5}$                       (B)  $\sqrt{7}$                       (C) 3  
(D)  $\sqrt{3}$                       (E)  $\sqrt{10}$

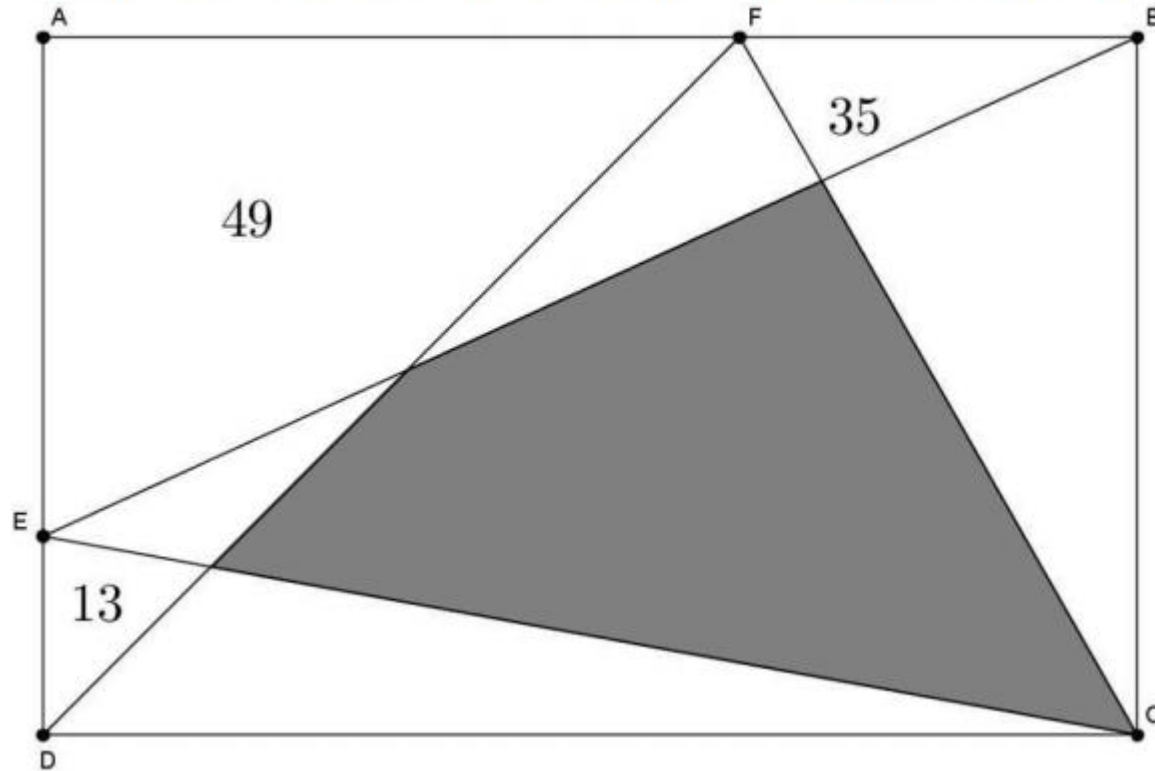
**Q5.**

In  $\triangle ABC$ , AD is a median. E is mid point of AD, F is mid point of BE and G is midpoint of CF. The ratio of areas of  $\triangle EFG$  to  $\triangle ABC$  is

- (a) 5:39  
(b) 4:31  
(c) 3:37  
(d) 2:16



Q6. Find the area of the shaded region, given the areas of three other regions.



**Q7.** Find the distance of the circum center to the vertex of a triangle with sides 20,21 and 29

**Q8.** If the sum of all altitudes of the triangle with sides 25,26 and 27 is represented as  $(a/b)(\sqrt{c})$  where  $a,b,c$  are integers, find  $a-bc$

**Q9** Determine the minimum value of the sum of inradius and circumradius of a right triangle with unit area

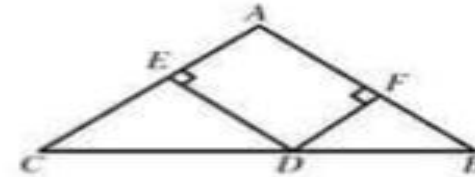
**Q10.** Two of the altitude of scalene triangle ABC have length 4 and 12 . If the length of third altitude is also an integer . find maximum value of third altitude.

**Q11.** In a quadrilateral ABCD, it is given that angle A =  $120^\circ$ , angle B & D =  $90^\circ$ , AB = 13, AD = 46, Find AC

**Q12.**

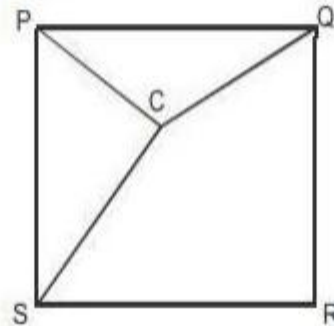
In  $\triangle ABC$ ,  $AC = AB = 25$  and  $BC = 40$ .  $D$  is a point chosen on  $BC$ . From  $D$ , perpendiculars are drawn to meet  $AC$  at  $E$  and  $AB$  at  $F$ .  $DE + DF$  equals

- (A) 12                      (B) 35                      (C) 24  
(D) 25                      (E)  $\frac{35}{2}\sqrt{2}$



**Q13.**

In the figure given below, C is a point inside the square PQRS. If PC = 6 m, QC = 8 m and SC = 10 m, then find the length of RC.



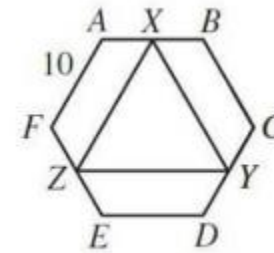
- (a)  $9\sqrt{2}$  m                      (b)  $8\sqrt{3}$  m                      (c)  $8\sqrt{2}$  m                      (d)  $9\sqrt{3}$  m

**Q14.** ABCD is a trapezium where BC is parallel to AD.  $AD=16$ ,  $BC=14$ ,  $AB=10$  and  $CD=15$  find sum of squares of diagonals

**Q15.** In a triangle ABC,  $AB = 8$  units,  $BC = 10$  units and  $CA = 12$  units. AD is angle bisector of angle A and I is the incenter, find AI:ID

**Q16**

In the diagram,  $ABCDEF$  is a regular hexagon with a side length of 10. If  $X$ ,  $Y$  and  $Z$  are the midpoints of  $AB$ ,  $CD$  and  $EF$ , respectively, what is the length of  $XZ$ ?



**Q17.** The shortest median of a right-angled triangle is 25 units. If the area of the triangle is 336 sq.units, what is the length (in units) of the longest median of the triangle?

**Q18.** In a  $\Delta PQR$ , PS is a median drawn from vertex P to QR. QT is internal angle bisector from Q to PR.  $PQ = 7$  units,  $QR = 18$  units,  $PT = TS$ . Find the side PR.

**Q19** In triangle ABC,  $AC = 12$ . If one of the trisectors of angle B is the median to AC and the other trisector of angle B is the altitude to AC, find the length of the altitude.

**Q20.** Two of the sides of a triangle are in the ratio 3:4. The medians to these sides are perpendicular to each other. If the third side of the triangle is  $12\sqrt{5}$ , find the smaller of the first two sides of the triangle

**Q21** The sides of a triangle measure 6, 10, and 14. Find the sum of the squares of the medians of the triangle. ?

**Q22.** In  $\triangle ABC$ ,  $\angle A = 45^\circ$  and  $\angle C = 30^\circ$ . If altitude BH intersects median AM at P, then  $AP : PM = 1 : k$ . Find k.

**Q23.** In  $\triangle ABC$ , angle C =  $90^\circ$  and  $AB = 60$ . The medians AD and BE intersect at G ( Centroid ) . If theta is the acute angle between the medians AD and BE whose tangent value is  $\frac{1}{3}$ , then the area of  $\triangle ABC$  is

**Q24.** In a triangle ABC, median AM is drawn such that it divides  $\angle BAC$  in the ratio 1:2. AM is extended to D such that  $\angle ABD = 90^\circ$ , Given  $AC=12$  Find AD.

**Q25.** If the circumradius and the inradius of a right-angled triangle are 25 cm and 6 cm respectively, find the area of the triangle. (A) 168 sq.cm. (B) 336 sq.cm. (C) 294 sq.cm. (D) Cannot be determined



# **ANSWER KEYS**

**BEFORE CHECKING ANSWER KEYS – TRY QUESTIONS ATLEAST 2-3 TIMES**

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- |               |                 |                    |
|---------------|-----------------|--------------------|
| 1) 36         | 11) 62          | 21) 249.           |
| 2) Sqrt 14    | 12) 24          | 22) $\sqrt{3} / 2$ |
| 3) 24         | 13) $8\sqrt{2}$ | 23) 400            |
| 4) Sqrt 7     | 14) 773         | 24) 24             |
| 5) 2:16       | 15) 2:1         | 25) 336            |
| 6) 97         | 16) 15          |                    |
| 7) 14.5       | 17) 48.5        |                    |
| 8) 904        | 18) 15          |                    |
| 9) $\sqrt{2}$ | 19) $3\sqrt{3}$ |                    |
| 10) 5         | 20) 36          |                    |

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