

Regression Models - Quiz 01

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Quiz 01

Attempts	Score
1/3	10/10

Question 01

Consider the data set given below:

```
x <- c(0.18, -1.54, 0.42, 0.95)
```

And weights given by:

```
w <- c(2, 1, 3, 1)
```

Give the value of μ that minimizes the least squares equation $\sum_{i=1}^n w_i(x_i - \mu)^2$

Answer

0.1471

Explanation

```
weighted.mean(x, w)
```

```
## [1] 0.1471429
```

Question 02

Consider the following data set:

```
x <- c(0.8, 0.47, 0.51, 0.73, 0.36, 0.58, 0.57, 0.85, 0.44, 0.42)
y <- c(1.39, 0.72, 1.55, 0.48, 1.19, -1.59, 1.23, -0.65, 1.49, 0.05)
```

Fit the regression through the origin and get the slope treating y as the outcome and x as the regressor. (Hint, do not center the data since we want regression through the origin, not through the means of the data.)

Answer

0.8263

Explanation

```
lm(y ~ x - 1)

##
## Call:
## lm(formula = y ~ x - 1)
##
## Coefficients:
##      x
## 0.8263
```

Question 03

Do `data(mtcars)` from the `datasets` package and fit the regression model with `mpg` as the outcome and `weight` as the predictor. Give the slope coefficient.

Answer

-5.344

Explanation

```
data(mtcars)
lm(mpg ~ wt, mtcars)

##
## Call:
## lm(formula = mpg ~ wt, data = mtcars)
##
## Coefficients:
## (Intercept)          wt
##      37.285      -5.344
```

Question 04

Consider data with an outcome (Y) and a predictor (X). The standard deviation of the predictor is one half that of the outcome. The correlation between the two variables is .5. What value would the slope coefficient for the regression model with Y as the outcome and X as the predictor?

Answer

1

Explanation

```
corOfYandX <- 0.5
sdYoverX <- 2
corOfYandX*sdYoverX

## [1] 1
```

Question 05

Students were given two hard tests and scores were normalized to have empirical mean 0 and variance 1. The correlation between the scores on the two tests was 0.4. What would be the expected score on Quiz 2 for a student who had a normalized score of 1.5 on Quiz 1?

Answer

0.6

Explanation

```
corOfYandX <- 0.4
quiz1 <- 1.5
quiz1*corOfYandX*1 + 0
```

```
## [1] 0.6
```

Question 06

Consider the data given by the following:

```
x <- c(8.58, 10.46, 9.01, 9.64, 8.86)
```

What is the value of the first measurement if x were normalized (to have mean 0 and variance 1)?

Answer

-0.9719

Explanation

```
mean <- mean(x)
sd <- sd(x)
(x[1] - mean)/sd
```

```
## [1] -0.9718658
```

Question 07

Consider the following data set (used above as well). What is the intercept for fitting the model with x as the predictor and y as the outcome?

```
x <- c(0.8, 0.47, 0.51, 0.73, 0.36, 0.58, 0.57, 0.85, 0.44, 0.42)
y <- c(1.39, 0.72, 1.55, 0.48, 1.19, -1.59, 1.23, -0.65, 1.49, 0.05)
```

Answer

1.567

Explanation

```
lm(y ~ x)

##
## Call:
## lm(formula = y ~ x)
##
## Coefficients:
## (Intercept)          x
##      1.567      -1.713
```

Question 08

You know that both the predictor and response have mean 0. What can be said about the intercept when you fit a linear regression?

Answer

It must be identically 0.

Question 09

Consider the data given by:

```
x <- c(0.8, 0.47, 0.51, 0.73, 0.36, 0.58, 0.57, 0.85, 0.44, 0.42)
```

What value minimizes the sum of the squared distances between these points and itself?

Answer

0.573

Explanation

```
mean(x)

## [1] 0.573
```

Question 10

Let the slope having fit Y as the outcome and X as the predictor be denoted as β_1 . Let the slope from fitting X as the outcome and Y as the predictor be denoted as γ_1 . Suppose that you divide β_1 by γ_1 , in other words consider β_1/γ_1 . What is this ratio always equal to?

Answer

$$\text{Var}(Y) / \text{Var}(X)$$

Explanation

```
cor(X, Y)*sd(Y)/sd(X) / (cor(X,Y)*sd(X)/sd(Y))  
= sd(Y)^2/(sd(X)^2)  
= var(Y)/var(X)
```