§1 POLYSTICKS DATA FOR DANCING 1

(See https://cs.stanford.edu/~knuth/programs.html for date.)

1. Data for dancing. This program creates data suitable for the DANCE routine, given the description of edges and junctions to be covered and a set of polystick shapes.

The first line of input names all the pieces. Each piece name consists of at most three characters; the name should also be distinguishable from a board position. (The program does not check this.)

The second line of input names all the board positions, in any order except that interior junction points must follow a '|'. Each position is of the form Hxy or Vxy or Ixy, where x and y are digits that represent coordinates; each "digit" is a single character, 0-9 or a-z representing the numbers 0-35. Position Hxy is the edge from (x, y) to (x, y + 1); position Ixy is the interior point (x, y). For example,

```
HO1 H11 V10 V11 | I11
```

is one way to describe a board that makes a small cross shape.

The remaining lines of input describe the polysticks. First comes the name, followed by two integers s and t, meaning that the shape should appear in s rotations and t transpositions. Then come board positions for each cell of the shape. For example, the line

C 4 1 HOO VOO IO1 VO1 HO2

```
describes a hexiamond that can appear in 4 orientations. (See the analogous program for polyominoes.)
                                 /* at most this many shapes */
#define max\_pieces 100
#define buf\_size = 3 * 36 * 36 * 4 + 10
                                              /* upper bound on line length */
#include <stdio.h>
#include <ctype.h>
  (Global variables 5)
  \langle \text{Subroutines 4} \rangle;
  main()
     register char *p, *q;
     register int j, k, n, x, y, z, bar;
     \langle \text{Read and output the piece names } 2 \rangle;
     \langle \text{Read and output the board } 3 \rangle;
     \langle \text{ Read and output the pieces 6} \rangle:
  }
     \#define panic(m)
          \{ fprintf(stderr, "%s!\n%s", m, buf); exit(-1); \}
\langle \text{Read and output the piece names } 2 \rangle \equiv
  if (\neg fgets(buf, buf\_size, stdin)) panic("No\_piece\_names");
  if (buf[strlen(buf) - 1] \neq '\n') panic("Input_line_too_long");
  fwrite(buf, 1, strlen(buf) - 1, stdout);
                                                 /* output all but the newline */
This code is used in section 1.
```

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```
3. \langle \text{Read and output the board 3} \rangle \equiv
  if (\neg fgets(buf, buf\_size, stdin)) panic("No\_board");
  if (buf[strlen(buf) - 1] \neq "\n") panic("Input_line_too_long");
  bxmin = bymin = 35; bxmax = bymax = 0;
  for (p = buf, bar = 0; *p; p += 4) {
     while (isspace(*p)) p++;
    if (\neg *p) break;
     if (*p \equiv ' \mid ' \wedge isspace(*(p+1))) {
       bar = 1;
       p -= 2;
       continue;
     x = decode(*(p+1));
     if (x < 0) panic("Bad_\\\x_\\\coordinate");
     y = decode(*(p+2));
     if (y < 0) panic("Bad_{\sqcup}y_{\sqcup}coordinate");
     if (\neg isspace(*(p+3))) \ panic("Bad_lboard_lposition");
    if (*p \equiv 'H' \land \neg bar) z = 0;
    else if (*p \equiv "V" \land \neg bar) z = 2;
     else if (*p \equiv 'I' \wedge bar) z = 1;
     else panic("Illegal_board_position");
    if (board[x][y][z]) panic("Duplicate_board_position");
    if (x < bxmin) bxmin = x;
     if (x > bxmax) bxmax = x;
     if (y < bymin) bymin = y;
    if (y > bymax) bymax = y;
     board[x][y][z] = 1;
  if (bxmin > bxmax) panic("Empty_board");
  printf("_{\sqcup}\%s", buf);
                            /* just pass the board names through */
This code is used in section 1.
4. \langle \text{Subroutines 4} \rangle \equiv
  int decode(c)
       char c;
    if (c \leq 9)
       if (c \geq 0) return c - 0;
     } else if (c \ge `a") {
       if (c \leq z') return c + 10 - a';
     return -1;
See also section 12.
This code is used in section 1.
5. \langle \text{Global variables 5} \rangle \equiv
  char buf [buf_size];
  int board [36][36][3];
                            /* positions present */
  int bxmin, bxmax, bymin, bymax; /* used portion of the board */
See also section 7.
This code is used in section 1.
```

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```
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6. \langle \text{Read and output the pieces 6} \rangle \equiv
  while (fgets(buf, buf_size, stdin)) {
     if (buf[strlen(buf) - 1] \neq '\n') panic("Input_line_too_long");
     for (p = buf; isspace(*p); p++);
     if (\neg *p) panic("Empty_line");
     for (q = p + 1; \neg isspace(*q); q \leftrightarrow);
     \textbf{if } (q>p+3) \ \textit{panic}(\texttt{"Piece} \_ \texttt{name} \_ \texttt{too} \_ \texttt{long"});\\
     for (q = name; \neg isspace(*p); p++, q++) *q = *p;
     *q = '\0';
     for (p++; isspace(*p); p++);
     s = *p - '0';
     if ((s \neq 1 \land s \neq 2 \land s \neq 4) \lor \neg isspace(*(p+1))) panic("Bad_\suvalue");
     for (p += 2; isspace(*p); p++);
     t = *p - '0';
     if ((t \neq 1 \land t \neq 2) \lor \neg isspace(*(p+1))) panic("Bad_\t_value");
     n=0;
     xmin = ymin = 35; xmax = ymax = 0;
     for (p += 2; *p; p += 4, n++)
        while (isspace(*p)) p++;
       if (\neg *p) break;
       x = decode(*(p+1));
       if (x < 0) panic("Bad_{\sqcup}x_{\sqcup}coordinate");
        y = decode(*(p+2));
       if (y < 0) panic("Bad_y_coordinate");
       if (\neg isspace(*(p+3))) panic("Bad_{\sqcup}board_{\sqcup}position");
       if (*p \equiv 'H') z = 0;
        else if (*p \equiv "V") z = 2;
        else if (*p \equiv 'I') z = 1;
        else panic("Illegal board position");
       if (n \equiv 36 * 36 * 2) panic("Pigeonhole_{\square}principle_{\square}says_{\square}you_{\square}repeated_{\square}a_{\square}position");
        xx[n] = x, yy[n] = y, zz[n] = z;
       if (x < xmin) \ xmin = x;
       if (x > xmax) xmax = x;
       if (y < ymin) ymin = y;
       if (y > ymax) ymax = y;
     if (n \equiv 0) panic("Empty_piece");
     (Generate the possible piece placements 8);
This code is used in section 1.
7. \langle \text{Global variables 5} \rangle + \equiv
```

```
char name[4];
                 /* name of current piece */
          /* symmetry type of current piece */
int s, t;
int xx[36*36*3], yy[36*36*3], zz[36*36*3];
                                                /* coordinates of current piece */
int xmin, xmax, ymin, ymax; /* range of coordinates */
```

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```
8. \langle Generate the possible piece placements 8\rangle \equiv
  while (t) {
     for (k = 1; k \le 4; k++) {
       if (k \leq s) (Output translates of the current piece 11);
       \langle Rotate the current piece 10\rangle;
     ⟨Transpose the current piece 9⟩;
This code is used in section 6.
9. \langle Transpose the current piece 9 \rangle \equiv
  for (j = 0; j < n; j ++) {
     z = xx[j];
     xx[j] = yy[j];
     yy[j] = z;
     zz[j] = 2 - zz[j];
  z = xmin; xmin = ymin; ymin = z;
  z = xmax; xmax = ymax; ymax = z;
This code is used in section 8.
10. \langle \text{Rotate the current piece } 10 \rangle \equiv
  xmin = ymin = 1000; xmax = ymax = -1000;
  for (j = 0; j < n; j ++) {
     z = xx[j];
     xx[j] = -yy[j];
    if (zz[j] \equiv 2) xx[j]—;
     yy[j] = z;
     zz[j] = 2 - zz[j];
    if (xx[j] < xmin) xmin = xx[j];
    if (xx[j] > xmax) xmax = xx[j];
    if (yy[j] < ymin) ymin = yy[j];
    if (yy[j] > ymax) ymax = yy[j];
This code is used in section 8.
```

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11. Interior points don't have to be on the board; they might, for example, lie on the boundary after translation.

```
\langle Output translates of the current piece 11\rangle \equiv
  for (x = bxmin - xmin; x \le bxmax - xmax; x++)
    for (y = bymin - ymin; y \le bymax - ymax; y++) {
      for (j = 0; j < n; j++)
        if (zz[j] \neq 1 \land \neg board[x + xx[j]][y + yy[j]][zz[j]]) goto nope;
      printf(name);
      for (j = 0; j < n; j ++)
        if (board[x + xx[j]][y + yy[j]][zz[j]]) {
          printf("\n");
    nope:;
This code is used in section 8.
12. \langle \text{Subroutines 4} \rangle + \equiv
  char codeletter[3] = \{ 'H', 'I', 'V' \};
  char encode(x)
      int x;
    if (x < 10) return '0' + x;
    return 'a' -10 + x;
```

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```
bar: \underline{1}, \underline{3}.
board: 3, 5, 11.
buf: 2, 3, 5, 6.
buf_size: 1, 2, 3, 5, 6.
bxmax: 3, \underline{5}, 11.
bxmin: 3, 5, 11.
by max: 3, 5, 11.
bymin: 3, \underline{5}, 11.
c: \underline{4}.
codeletter: 11, \underline{12}.
decode: 3, \underline{4}, 6.
encode: 11, \underline{12}.
exit: 2.
fgets: 2, 3, 6.
fprintf: 2.
fwrite: 2.
isspace: 3, 6.
j: \underline{1}.
k: \underline{1}.
main: \underline{1}.
max\_pieces: 1.
n: \underline{1}.
name \colon \ 6, \ \underline{7}, \ 11.
nope: \underline{11}.
p: <u>1</u>.
panic: \underline{2}, \underline{3}, \underline{6}.
printf: 3, 11.
q: \underline{1}.
s: <u>7</u>.
stderr: 2.
stdin: 2, 3, 6.
stdout: 2.
strlen: 2, 3, 6.
t: \underline{7}.
x: \quad \underline{1}, \quad \underline{12}.
xmax: 6, 7, 9, 10, 11.
xmin: 6, <u>7</u>, 9, 10, 11.
xx: 6, <u>7</u>, 9, 10, 11.
y: <u>1</u>.
ymax: 6, 7, 9, 10, 11.
ymin: 6, <u>7</u>, 9, 10, 11.
yy: 6, 7, 9, 10, 11.
z: \underline{1}.
zz: 6, 7, 9, 10, 11.
```

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```
\label{eq:continuous} \left\langle \begin{array}{ll} \text{Generate the possible piece placements 8} \right\rangle \quad \text{Used in section 6.} \\ \left\langle \begin{array}{ll} \text{Global variables 5, 7} \right\rangle \quad \text{Used in section 1.} \\ \left\langle \begin{array}{ll} \text{Output translates of the current piece 11} \right\rangle \quad \text{Used in section 8.} \\ \left\langle \begin{array}{ll} \text{Read and output the board 3} \right\rangle \quad \text{Used in section 1.} \\ \left\langle \begin{array}{ll} \text{Read and output the piece names 2} \right\rangle \quad \text{Used in section 1.} \\ \left\langle \begin{array}{ll} \text{Read and output the pieces 6} \right\rangle \quad \text{Used in section 1.} \\ \left\langle \begin{array}{ll} \text{Rotate the current piece 10} \right\rangle \quad \text{Used in section 8.} \\ \left\langle \begin{array}{ll} \text{Subroutines 4, 12} \right\rangle \quad \text{Used in section 1.} \\ \left\langle \begin{array}{ll} \text{Transpose the current piece 9} \right\rangle \quad \text{Used in section 8.} \\ \end{array} \right.
```

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