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(See https://cs.stanford.edu/~knuth/programs.html for date.)

1. Intro. This program produces a DLX file that corresponds to the problem of packing a given set of polyiamonds into a given two-dimensional box. The output file might be input directly to a DLX-solver; however, it often is edited manually, to customize a particular problem (for example, to avoid producing solutions that are equivalent to each other). (I hacked this from POLYOMINO-DLX.)

The triangular cells in the box are of two kinds,  $\Delta$  and  $\nabla$ . Both kinds have two coordinates xy, in the range  $0 \le x, y < 62$ , specified by means of the extended hexadecimal "digits"  $0, 1, \ldots, 9, a, b, \ldots, z, A, B, \ldots, Z$ . The ' $\nabla$ ' triangles, which appear immediately to the right of their ' $\Delta$ ' counterparts, are distinguished by having an apostrophe following the coordinates. (It may be helpful to think of a square cell xy, which has been subdivided into right triangles xy and xy' by its main diagonal, then slightly squashed so that the triangles become equilateral.)

As in DLX format, any line of stdin that begins with '|' is considered to be a comment.

The first noncomment line specifies the cells of the box. It's a list of pairs xy or xy', where each coordinate is either a single digit or a set of digits enclosed in square brackets. For example, '[02]b' specifies two cells, 0b, 2b. Brackets may also contain a range of items, with UNIX-like conventions; for instance, '[0-2][b-b]' specifies three cells, 0b', 1b', 2b'. A  $3 \times 4$  parallelogram, which contains 24 triangles, can be specified by '[1-3][1-4] [1-3][1-4]'.

Note: With square cells we had the luxury of regarding the pair xy in either of two ways: (i) "matrixwise" (with x denoting a row and y a column; increasing x meant going down, while increasing y meant going right); or (ii) "Cartesianwise" (with x and y denoting horizontal and vertical displacement; increasing x meant going right, while increasing y meant going up). However, with triangular cells, we're totally Cartesian.

Individual cells may be specified more than once, but they appear just once in the box. For example,

## [123]2 2[123][12][12],

specifies a noniamond that looks something like a fish. The cells of a box needn't be connected.

Cell specifications can optionally be followed by a suffix. For example, '[12]7suf' specifies two items named '17suf' and '27suf'. Such items will be *secondary*, unless the suffix is simply '''.

The other noncomment lines consist of a piece name followed by typical cells of that piece. These typical cells are specified in the same way as the cells of a box.

The typical cells lead to up to 12 "base placements" for a given piece, corresponding to rotations and/or reflections in two-dimensional space. The piece can then be placed by choosing one of its base placements and shifting it by an arbitrary amount, provided that all such cells fit in the box. The base placements themselves need not fit in the box.

All suffixes associated with a cell will be appended to the items generated by that cell. For example, a piece that has typical cells '00, 00', 00!, 00'! will generate options for every pair of adjacent cells in the box: When 33' and 34 are present, there will be an option '33' 34 33'! 34!'. If 00'! hadn't been specified, there would have been two options, '33' 34 33'!' and '34 33' 34!'.

Each piece name should be distinguishable from the coordinates of the cells in the box. (For example, a piece should not be named 00 unless cell 00 isn't in the box.) This condition is not fully checked by the program.

A piece that is supposed to occur more than once can be preceded by its multiplicity and a vertical line; for example, one can give its name as '12|Z'. (This feature will produce a file that can be handled only by DLX solvers that allow multiplicity.)

Several lines may refer to the same piece. In such cases the placements from each line are combined.

2 INTRO POLYIAMOND-DLX  $\S 2$ 

```
OK, here we go.
\#define bufsize 1024
                                /* input lines shouldn't be longer than this */
                                  /* at most this many pieces */
\#define maxpieces 100
                                      /* at most this many elements of lists */
#define maxnodes 100000
\#define maxbases 1000
                                   /* at most this many base placements */
                                   /* at most this many suffixes */
\#define maxsuffixes 10
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
  char buf[bufsize];
  \langle \text{Type definitions } 9 \rangle;
   \langle \text{Global variables 8} \rangle;
  \langle \text{Subroutines } 3 \rangle;
  main()
  {
     register int i, j, k, p, q, r, t, x, y, dx, dy, xy\theta, suf;
     register long long xa, ya;
     \langle \text{Read the box spec } 17 \rangle;
     \langle \text{ Read the piece specs 24} \rangle;
      \langle \text{ Output the DLX item-name line } 34 \rangle;
     \langle \text{ Output the DLX options 35} \rangle;
     \langle \text{ Bid farewell } 36 \rangle;
  }
```

§3 POLYIAMOND-DLX LOW-LEVEL OPERATIONS

**3.** Low-level operations. I'd like to begin by building up some primitive subroutines that will help to parse the input and to publish the output.

For example, I know that I'll need basic routines for the input and output of radix-62 digits.

```
\langle \text{ Subroutines } 3 \rangle \equiv
  int decode(\mathbf{char}\ c)
    if (c \leq 9)
       if (c \geq 0) return c - 0;
     } else if (c \ge 'a') {
       if (c \leq z') return c + 10 - a';
     } else if (c \ge 'A' \land c \le 'Z') return c + 36 - 'A';
     if (c \neq ' \n') return -1;
     fprintf(stderr, "Incomplete input line: "%s", buf);
     exit(-888);
  char encode(\mathbf{int} \ x)
    if (x < 0) return '-';
    if (x < 10) return '0' + x;
    if (x < 36) return 'a' -10 + x;
     if (x < 62) return 'A' -36 + x;
     return '?';
See also sections 4, 12, 13, 14, 15, 30, and 37.
This code is used in section 2.
```

4. I'll also want to decode the specification of a given set of digits, starting at position p in buf. Subroutine pdecode sets the global variable acc to a 64-bit number that represents the digit or digits mentioned there. Then it returns the next buffer position, so that I can continue scanning.

```
 \langle \text{Subroutines } 3 \rangle +\equiv \\ \text{int } pdecode(\text{register int } p) \\ \{ \\ \text{register int } x; \\ \text{if } (buf[p] \neq `[')') \{ \\ x = decode(buf[p]); \\ \text{if } (x \geq 0) \{ \\ acc = 1_{\text{LL}} \ll x; \\ \text{return } p+1; \\ \} \\ fprintf(stderr, "Illegal\_digit\_at\_position\_%d\_of\_%s", p, buf); \\ exit(-2); \\ \} \text{ else } \langle \text{Decode a bracketed specification } 5 \rangle; \\ \}
```

```
5. We want to catch illegal syntax such as '[-5]', '[1-]', '[3-2]', '[1-2-3]', '[3--5]', while allowing
'[7-z32-4A5-5]', etc. (The latter is equivalent to '[2-57-A]'.)
  Notice that the empty specification '[]' is legal, but useless.
\langle \text{ Decode a bracketed specification } 5 \rangle \equiv
     register int t, y;
     for (acc = 0, t = x = -1, p++; buf[p] \neq ']'; p++)
       if (buf[p] \equiv '\n') {
          fprintf(stderr, "Nouclosing_bracket_in_%s", buf);
          exit(-4);
       if (buf[p] \equiv ,-,) \land Get ready for a range 6)
        else {
          x = decode(buf[p]);
          if (x < 0) {
             fprintf(stderr, "Illegal_{\sqcup}bracketed_{\sqcup}digit_{\sqcup}at_{\sqcup}position_{\sqcup}%d_{\sqcup}of_{\sqcup}%s", p, buf);
             exit(-3);
          if (t < 0) acc |= 1_{LL} \ll x;
          else \langle Complete the range from t to x \cdot 7 \rangle;
     return p+1;
This code is used in section 4.
6. \langle \text{ Get ready for a range } 6 \rangle \equiv
  {
     if (x < 0 \lor buf[p+1] \equiv `]`) {
       fprintf(stderr, "Illegal \ range \ at \ position \ \ \ d \ of \ \ \ ", p, buf);
        exit(-5);
     t = x, x = -1;
This code is used in section 5.
    \langle Complete the range from t to x \rangle \equiv
     if (x < t) {
       fprintf(stderr, "Decreasing\_range\_at\_position\_%d\_of_L%s", p, buf);
        exit(-6);
     acc = (1_{LL} \ll (x+1)) - (1_{LL} \ll t);
     t = x = -1;
This code is used in section 5.
8. \langle \text{Global variables 8} \rangle \equiv
                         /* accumulated bits representing coordinate numbers */
  long long acc;
  long long accx, accy;
                                  /* the bits for each dimension of a partial spec */
See also sections 11, 22, and 23.
This code is used in section 2.
```

§9 POLYIAMOND-DLX DATA STRUCTURES

**9.** Data structures. The given box is remembered as a sorted list of cells xy, represented as a linked list of packed integers  $(x \ll 8) + y$ . The base placements of each piece are also remembered in the same way. All of the relevant information appears in a structure of type **box**.

```
⟨Type definitions 9⟩ ≡
  typedef struct {
   int list; /* link to the first of the packed triples xy */
   int size; /* the number of items in that list */
   int xmin, xmax, ymin, ymax; /* extreme coordinates */
   int pieceno; /* the piece, if any, for which this is a base placement */
  } box;
See also section 10.
This code is used in section 2.
```

10. Elements of the linked lists appear in structures of type node.

All of the lists will be rather short. So I make no effort to devise methods that are asymptotically efficient as things get infinitely large. My main goal is to have a program that's simple and correct. (And I hope that it will also be easy and fun to read, when I need to refer to it or modify it.)

```
⟨Type definitions 9⟩ +≡
typedef struct {
  int xy; /* position data stored in this node */
  int suf; /* suffix data for this node */
  int link; /* the next node of the list, if any */
} node;
```

11. All of the nodes appear in the array elt. I allocate it statically, because it doesn't need to be very big.

```
⟨Global variables 8⟩ +≡
node elt[maxnodes]; /* the nodes */
int curnode; /* the last node that has been allocated so far */
int avail; /* the stack of recycled nodes */
```

**12.** Subroutine *getavail* allocates a new node when needed.

```
 \begin{array}{l} \langle \operatorname{Subroutines} \; 3 \rangle \; + \equiv \\ & \operatorname{int} \; \operatorname{getavail}(\operatorname{void}) \\ \{ \\ & \operatorname{register} \; \operatorname{int} \; p = \operatorname{avail}; \\ & \operatorname{if} \; (p) \; \{ \\ & \operatorname{avail} = \operatorname{elt}[\operatorname{avail}].\operatorname{link}; \\ & \operatorname{return} \; p; \\ \} \\ & p = + \operatorname{curnode}; \\ & \operatorname{if} \; (p < \operatorname{maxnodes}) \; \operatorname{return} \; p; \\ & \operatorname{fprintf} \left( \operatorname{stderr}, "\operatorname{Overflow!} \sqcup \operatorname{Recompile} \sqcup \operatorname{by} \sqcup \operatorname{maxnodes} \sqcup \operatorname{bigger} \sqcup \operatorname{than} \sqcup \operatorname{\%d}. \\ \setminus \operatorname{n"}, \; \operatorname{maxnodes} \right); \\ & \operatorname{exit} \left( -666 \right); \\ \} \end{array}
```

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Conversely, putavail recycles a list of nodes that are no longer needed.  $\langle \text{Subroutines } 3 \rangle + \equiv$ **void** putavail(**int** p) register int q; **if** (p) { for (q = p; elt[q].link; q = elt[q].link); elt[q].link = avail;avail = p;} **14.** The *insert* routine puts new (x,y) data into the list of *newbox*, unless (x,y) is already present.  $\langle \text{Subroutines } 3 \rangle + \equiv$ void insert(int x, int y, int s)register int p, q, r, xy;  $xy = (x \ll 8) + y;$ for (q = 0, p = newbox.list; p; q = p, p = elt[p].link) { if  $(elt[p].xy \equiv xy)$  { /\* nothing to be done \*/ if  $(elt[p].suf \equiv s)$  return; if (elt[p].suf > s) break; /\* we've found the insertion point \*/ } else if (elt[p].xy > xy) break; /\* we've found the insertion point \*/ } r = getavail();elt[r].xy = xy, elt[r].suf = s, elt[r].link = p;**if** (q) elt[q].link = r;else newbox.list = r; newbox.size ++;**if** (x < newbox.xmin) newbox.xmin = x; **if** (y < newbox.ymin) newbox.ymin = y; **if** (x > newbox.xmax) newbox.xmax = x; **if** (y > newbox.ymax) newbox.ymax = y; } 15. Although this program is pretty simple, I do want to watch it in operation before I consider it to be reasonably well debugged. So here's a subroutine that's useful for diagnostic purposes.  $\langle \text{Subroutines } 3 \rangle + \equiv$ **void**  $printbox(\mathbf{box} *b)$ register int p, x, y; $b \rightarrow y max$ ); for  $(p = b \rightarrow list; p; p = elt[p].link)$  {

 $fprintf(stderr, "\_\%c\%c\%s", encode(x), encode(y), elt[p].suf? suffix[elt[p].suf-1]: "");$ 

 $x = elt[p].xy \gg 8, y = elt[p].xy \& #ff;$ 

 $fprintf(stderr, "\n");$ 

16. Inputting the given box. Now we're ready to look at the xy specifications of the box to be filled. As we read them, we remember the cells in the box called newbox. Then, for later convenience, we also record them in a three-dimensional array called occupied.

```
17. \langle \text{Read the box spec } 17 \rangle \equiv
  while (1) {
     if (\neg fgets(buf, bufsize, stdin)) {
        fprintf(stderr, "Input_{\square}file_{\square}ended_{\square}before_{\square}the_{\square}box_{\square}specification! \n");
        exit(-9);
     if (buf[strlen(buf) - 1] \neq `\n') {
       fprintf(stderr, "Overflow!_Recompile_me_by_making_bufsize_bigger_than_%d.\n", bufsize);
        exit(-667);
     printf("| \underset \kappas", buf); /* all input lines are echoed as DLX comments */
     if (buf[0] \neq '|') break;
  }
  p = 0;
  \langle Put the specified cells into newbox, starting at buf[p] 18\rangle;
  givenbox = newbox;
  \langle Set up the occupied table 21\rangle;
This code is used in section 2.
18. This spec-reading code will also be useful later when I'm inputting the typical cells of a piece.
\langle \text{Put the specified cells into } newbox, \text{ starting at } buf[p] | 18 \rangle \equiv
  newbox.list = newbox.size = 0;
  newbox.xmin = newbox.ymin = 62;
  newbox.xmax = newbox.ymax = -1;
  for (; buf[p] \neq '\n'; p++) {
     if (buf[p] \neq ' \cup ') \langle Scan \ an \ xy \ spec \ 19 \rangle;
This code is used in sections 17 and 25.
19. I could make this faster by using bitwise trickery. But what the heck.
\langle \text{Scan an } xy \text{ spec } 19 \rangle \equiv
     p = pdecode(p), accx = acc;
     p = pdecode(p), accy = acc;
     \langle \text{ Digest the optional suffix, } suf 20 \rangle;
     if (buf[p] \equiv '\n') p--; /* we'll reread the newline character */
     for (x = 0, xa = accx; xa; x++, xa \gg = 1)
       if (xa & 1) {
          for (y = 0, ya = accy; ya; y++, ya \gg = 1)
             if (ya \& 1) insert(x, y, suf);
        }
This code is used in section 18.
```

**char** occupied[massuffixes + 1][64][64];

**box** *givenbox*;

int sfxpresent;

Suffixes will be stored in pairs, both with and without ',' at the front.  $\langle \text{ Digest the optional suffix, } suf | 20 \rangle \equiv$ for  $(q=0; buf[p+q] \neq ' \cup ' \land buf[p+q] \neq ' \setminus n'; q++)$  { if  $(q \equiv 6)$  {  $fprintf(stderr, "Suffix_too_long, _starting_at_position_%d_of_%s", p, buf);$ exit(-11);suffix[scount][q] = buf[p+q];**if** (q) { suffix[scount][q] = 0;p += q; for (i = 0; ; i++)if  $(strcmp(suffix[i], suffix[scount]) \equiv 0)$  break; if  $(i \equiv scount)$  { scount += 2;**if** (scount > maxsuffixes) { fprintf(stderr, "Overflow!\_Recompile\_me\_by\_making\_maxsuffixes>%d.\n", massuffixes); exit(-7); if  $(suffix[i][0] \equiv '\'$ '') strcpy(suffix[scount-1], suffix[i]), strcpy(suffix[i], &suffix[scount-1][1]), i++;strcpy(&suffix[scount-1][1], suffix[i]), suffix[scount-1][0] = ```;if (strlen(suffix[scount - 1]) > 6) {  $fprintf(stderr, "Implied_suffix_'%s'_sis_too_long!\n", suffix[scount-1]);$ exit(-9); } } suf = i + 1;} else suf = 0; This code is used in section 19. **21.**  $\langle$  Set up the *occupied* table  $21 \rangle \equiv$ for (p = givenbox.list; p; p = elt[p].link) {  $x = elt[p].xy \gg 8, y = elt[p].xy \& #ff;$ occupied[elt[p].suf][x][y] = 1;This code is used in section 17. **22.**  $\langle \text{Global variables } 8 \rangle + \equiv$ /\* the current specifications are placed here \*/ **box** newbox; char  $suffix[maxsuffixes + 1][8] = {"\"};$ /\* table of suffixes seen \*/ int scount = 1; /\* this many nonempty suffixes seen \*/

/\* this many items in *qivenbox* have suffixes \*/

/\* does the box occupy a given cell? \*/

23. Inputting the given pieces. After I've seen the box, the remaining noncomment lines of the input file are similar to the box line, except that they begin with a piece name.

This name can be any string of one to eight nonspace characters allowed by DLX format, followed by a space. It should also not be the same as a position of the box.

I keep a table of the distinct piece names that appear, and their multiplicities.

And of course I also compute and store all of the base placements that correspond to the typical cells that are specified.

```
\langle \text{Global variables 8} \rangle + \equiv
  char names[maxpieces][8];
                                     /* the piece names seen so far */
                        /* how many of them are there? */
  int piececount:
                                   /* what is the multiplicity? */
  char mult[maxpieces][8];
                         /* current multiplicity */
  char multip[8];
  box base[maxbases];
                               /* the base placements seen so far */
                        /* how many of them are there? */
  int basecount;
24. \langle Read the piece specs 24 \rangle \equiv
  while (1) {
     if (\neg fgets(buf, bufsize, stdin)) break;
     if (buf[strlen(buf) - 1] \neq '\n') {
       fprintf(stderr, "Overflow!_Recompile_me_by_making_bufsize_bigger_than_%d.\n", bufsize);
       exit(-777);
     printf("|_%s", buf); /* all input lines are echoed as DLX comments */
     if (buf[0] \equiv ')' continue;
     \langle \text{Read a piece spec 25} \rangle;
This code is used in section 2.
25. \langle \text{Read a piece spec 25} \rangle \equiv
  \langle Read the piece name, and find it in the names table at position k \geq 27 \rangle;
  newbox.pieceno = k; /* now buf[p] is the space following the name */
  \langle \text{ Put the specified cells into } newbox, \text{ starting at } buf[p] | 18 \rangle;
  \langle \text{ Normalize the cells of } newbox 29 \rangle;
  base[basecount] = newbox;
  \langle Create the other base placements equivalent to newbox 31\rangle;
This code is used in section 24.
```

**26.** We accept any string of characters followed by '|' as a multiplicity.

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```
\langle Read the piece name, and find it in the names table at position k = 27 \rangle \equiv
     for (p = 0; buf[p] \neq '\n'; p++)
          if (buf[p] \equiv '|') break;
          else multip[p] = buf[p];
     if (buf[p] \equiv '|') multip[p] = '0', p++;
     else p = 0, multip[0] = '1', multip[1] = '\0';
     for (q = p; buf[p] \neq '\n'; p++) {
          if (buf[p] \equiv ' \sqcup ') break;
          if (buf[p] \equiv ' \mid ' \vee buf[p] \equiv ' : ')  {
               fprintf(stderr, "Illegal_{\sqcup}character_{\sqcup}in_{\sqcup}piece_{\sqcup}name:_{\sqcup}%s", buf);
                exit(-8);
     if (buf[p] \equiv '\n') {
          fprintf(stderr, "(Empty_\%s_\is_\being_\ignored)\n", p \equiv 0? "line": "piece");
          continue;
     \langle Store the name in names [piececount] and check its validity 28\rangle;
     for (k = 0; ; k++)
          if (strncmp(names[k], names[piececount], 8) \equiv 0) break;
     if (k \equiv piececount) {
                                                                 /* it's a new name */
          if (++piececount > maxpieces) {
                fprintf(stderr, "Overflow! LRecompile LMe Lby LMaking LMaxpieces Lbigger Lthan L%d. n", maxpieces);
                exit(-668);
     if (\neg mult[k][0]) strcpy(mult[k], multip);
     else if (strcmp(mult[k], multip)) {
          fprintf(stderr, "Inconsistent_multiplicities\_for\_piece\_%.8s,\_%s\_vs\_%s!\n", names[k], mult[k],
                     multip);
          exit(-6);
This code is used in section 25.
28. \langle Store the name in names [piececount] and check its validity 28\rangle \equiv
     if (p \equiv q \lor p > q + 8) {
          fprintf(stderr, "Piece in ame is in one xistent in or itoo in or ito or itoo in or ito or i
          exit(-7);
     for (j = q; j < p; j ++) names [piececount][j - q] = buf[j];
     if (p \equiv q + 2) {
          x = decode(names[piececount][0]);
          y = decode(names[piececount][1]);
          if (x \ge 0 \land y \ge 0 \land occupied[0][x][y]) {
               fprintf(stderr, "Piece\_name\_conflicts\_with\_board\_position: \_\%s", buf);
                exit(-333);
     }
This code is used in section 27.
```

**29.** It's a good idea to "normalize" the typical cells of a piece, by making the xmin and ymin fields of newbox both zero.

```
 \langle \text{ Normalize the cells of } newbox \ 29 \rangle \equiv \\ xy\theta = (newbox.xmin \ll 8) + newbox.ymin; \\ \text{if } (xy\theta) \ \{ \\ \text{for } (p = newbox.list; \ p; \ p = elt[p].link) \ elt[p].xy -= xy\theta; \\ newbox.xmax -= newbox.xmin, newbox.ymax -= newbox.ymin; \\ newbox.xmin = newbox.ymin = 0; \\ \} \\ \text{This code is used in sections 25 and 32.}
```

12 Transformations polyiamond-dlx §30

**30.** Transformations. Now we get to the interesting part of this program, as we try to find all of the base placements that are obtainable from a given set of typical cells.

The method is a simple application of breadth-first search: Starting at the newly created base, we make sure that every elementary transformation of every known placement is also known.

This procedure requires a simple subroutine to check whether or not two placements are equal. We can assume that both placements are normalized, and that both have the same size. Equality testing is easy because the lists have been sorted.

```
 \begin{array}{l} \langle \, \text{Subroutines } \, 3 \, \rangle \, + \equiv \\ \quad \text{int } \, equality (\text{int } b) \\ \{ \quad / * \, \, \text{return } 1 \, \, \text{if } \, base[b] \, \, \text{matches } \, newbox \, \, * / \\ \quad \text{register int } \, p, \, \, q; \\ \quad \text{for } \, (p = base[b].list, q = newbox.list; \, \, p; \, p = elt[p].link, q = elt[q].link) \\ \quad \text{if } \, (elt[p].xy \neq elt[q].xy \vee elt[p].suf \neq elt[q].suf) \, \, \text{return } \, 0; \\ \quad \text{return } \, 1; \\ \} \end{array}
```

31. Just two elementary transformations suffice to generate them all. These transformations depend (in a somewhat subtle-but-nice way) on whether or not there's a suffix that begins with ''.

```
\langle Create the other base placements equivalent to newbox 31\rangle \equiv
  j = basecount, k = basecount + 1; /* bases j thru k - 1 have been checked */
  while (i < k) {
     \langle \text{ Set } newbox \text{ to } base[j] \text{ transformed by } 60^{\circ} \text{ rotation } 32 \rangle;
     for (i = basecount; i < k; i \leftrightarrow)
       if (equality(i)) break;
     if (i < k) putavail(newbox.list);
                                              /* already known */
     else base[k++] = newbox; /* we've found a new one */
     \langle \text{ Set } newbox \text{ to } base[j] \text{ transformed by } xy \text{ transposition } 33 \rangle;
     for (i = basecount; i < k; i++)
       if (equality(i)) break;
     if (i < k) putavail(newbox.list);
                                            /* already known */
     else base[k++] = newbox; /* we've found a new one */
     j++;
  basecount = k;
  if (basecount + 12 > maxbases) {
     fprintf(stderr, "Overflow!_LRecompile_Lme_Lby_Lmaking_Lmaxbases_Lbigger_Lthan_L%d.\n",
          basecount + 23);
     exit(-669);
This code is used in section 25.
```

§32 POLYIAMOND-DLX TRANSFORMATIONS 13

**32.** The first elementary transformation replaces (x, y) by (x + y - 1, 1 - x)' and (x, y)' by (x + y, 1 - x). It corresponds to 60-degree rotation about the "origin" (the point between (0, 0)' and (1, 1)) in our coordinates). Actually I add a constant, then normalize afterwards, so that the coordinates don't go negative.

```
 \langle \text{Set } newbox \text{ to } base[j] \text{ transformed by } 60^{\circ} \text{ rotation } 32 \rangle \equiv newbox.size = newbox.list = 0; \\ t = newbox.ymax = base[j].xmax; newbox.xmax = 0; \\ newbox.xmin = newbox.ymin = 64; \\ \textbf{for } (p = base[j].list; p; p = elt[p].link) \; \{ \\ x = elt[p].xy \gg 8, y = elt[p].xy \& \#ff; \\ \textbf{if } (elt[p].suf \& 1) \; \{ \\ /* \text{ suffix starts with prime } */ \\ insert(x+y+1,t-x,elt[p].suf-1); \\ \} \; \textbf{else } \{ \\ insert(x+y,t-x,elt[p].suf+1); \\ \} \\ \langle \text{Normalize the cells of } newbox \; 29 \rangle; \\ \text{This code is used in section } 31.
```

**33.** The other elementary transformation replaces (x, y) by (y, x) and (x, y)' by (y, x)'. It corresponds to reflection about the line at slope 30° through the origin—a nice reflection that doesn't interchange  $\Delta$  with  $\nabla$ .

```
[I like to think of the barycentric coordinates (x,y,z) such that x+y+z=1 or 2, with (x,y)\leftrightarrow (x,y,2-x,y) and (x,y)'\leftrightarrow (x,y,1-x-y). With such coordinates the simplest transformations take (x,y,z) to (y,x,z), (y,z,x), and (1-x,1-y,1-z).]

\langle Set newbox to base[j] transformed by xy transposition 33\rangle \equiv newbox.size = newbox.list = 0;
newbox.size = newbox.list = 0;
newbox.xmax = base[j].ymax, newbox.ymax = base[j].xmax;
for (p = base[j].list; \ p; \ p = elt[p].link) {
x = elt[p].xy \gg 8, y = elt[p].xy \& #ff;
insert(y, x, elt[p].suf);
}
```

This code is used in section 31.

14 FINISHING UP POLYIAMOND-DLX §34

**34.** Finishing up. In previous parts of this program, I've terminated abruptly when finding malformed input.

But when everything on *stdin* passes muster, I'm ready to publish all the information that has been gathered.

```
\langle \text{Output the DLX item-name line } 34 \rangle \equiv
  printf("|uthisufileuwasucreatedubyupolyiamond-dlxufromuthatudata\n");
  for (p = givenbox.list; p; p = elt[p].link)
    if (elt[p].suf < 2) {
       x = elt[p].xy \gg 8, y = elt[p].xy \& #ff;
       printf("_{\sqcup}\%c\%c\%s", encode(x), encode(y), elt[p].suf?"":"");
  for (k = 0; k < piececount; k++) {
    if (mult[k][0] \equiv '1' \land mult[k][1] \equiv '\0') printf("\\\.8s", names[k]);
    if (scount > 1) {
    printf(" \sqcup | ");
    for (sfxpresent = 0, p = givenbox.list; p; p = elt[p].link)
       if (elt[p].suf > 1) {
         x = elt[p].xy \gg 8, y = elt[p].xy \& #ff, sfxpresent ++;
         printf(" " \& c \& c \& s", encode(x), encode(y), suffix[elt[p].suf - 1]);
  }
  printf("\n");
This code is used in section 2.
35. \langle \text{ Output the DLX options 35} \rangle \equiv
  for (j = 0; j < basecount; j \leftrightarrow) {
    for (dx = givenbox.xmin; dx \leq givenbox.xmax - base[j].xmax; dx++)
       for (dy = givenbox.ymin; dy \leq givenbox.ymax - base[j].ymax; dy++) {
         for (p = base[j].list; p; p = elt[p].link) {
            x = elt[p].xy \gg 8, y = elt[p].xy \& #ff;
           if (\neg occupied[elt[p].suf][x + dx][y + dy]) break;
         if (\neg p) {
                        /* they're all in the box */
            printf("\%.8s", names[base[j].pieceno]);
           for (p = base[j].list; p; p = elt[p].link) {
              x = elt[p].xy \gg 8, y = elt[p].xy \& #ff;
              printf("u\%c\%c\%s", encode(x+dx), encode(y+dy), elt[p].suf? suffix[elt[p].suf-1]:"");
           printf("\n");
       }
  }
This code is used in section 2.
```

§36 POLYIAMOND-DLX FINISHING UP 15

**36.** Finally, when I've finished outputting the desired DLX file, it's time to say goodbye by summarizing what I did.

```
 \begin{array}{l} \langle \operatorname{Bid} \ \operatorname{farewell} \ 36 \rangle \equiv \\ & \text{ if } (\neg s f x p r e s e n t) \\ & f p r int f (s t d e r r, "Altogether \ \%d \ cells, \ \%d \ pieces, \ \%d \ base \ placements, \ \%d \ nodes. \ 'n", \\ & g i v e n b o x. size, p i e e e count, base count, curnode + 1); \\ & \text{else } f p r int f (s t d e r r, "Altogether \ \%d \ \%d \ cells, \ \%d \ pieces, \ \%d \ base \ placements, \ \%d \ nodes. \ 'n", \\ & g i v e n b o x. size - s f x p r e s e nt, p i e e e count, base count, curnode + 1); \\ & \text{This code is used in section 2.} \\ & \textbf{37.} \quad \langle \operatorname{Subroutines} \ 3 \rangle \ + \equiv \\ & \textbf{void } de b u g (\textbf{int } m) \\ & \{ \\ & f p r int f (s t d e r r, " \ ... \ d e b u g \ stop \ \%d ... \ 'n", m); \\ & \} \end{array}
```

## 38. Index.

acc: 4, 5, 7, 8, 19. accx: 8, 19. accy: 8, 19.  $avail\colon \ \underline{11},\ 12,\ 13.$ *b*: <u>15</u>, <u>30</u>. base: 23, 25, 30, 31, 32, 33, 35.  $basecount \colon \ \ \underline{23}, \ 25, \ 31, \ 35, \ 36.$ box: 9, 15, 22, 23. buf: 2, 3, 4, 5, 6, 7, 17, 18, 19, 20, 24, 25, 27, 28. bufsize:  $\underline{2}$ ,  $\underline{17}$ ,  $\underline{24}$ . c:  $\underline{3}$ .  $curnode: \underline{11}, \underline{12}, \underline{36}.$ debug: 37. $decode: \underline{3}, 4, 5, 28.$ dx:  $\underline{2}$ ,  $\underline{35}$ .  $dy: \ \ \underline{2}, \ 35.$ elt: 11, 12, 13, 14, 15, 21, 29, 30, 32, 33, 34, 35. encode: 3, 15, 34, 35. equality:  $\underline{30}$ ,  $\underline{31}$ . exit: 3, 4, 5, 6, 7, 12, 17, 20, 24, 27, 28, 31. fgets: 17, 24. fprintf: 3, 4, 5, 6, 7, 12, 15, 17, 20, 24, 27, 28, 31, 36, 37. getavail: 12, 14.givenbox: 17, 21, 22, 34, 35, 36. insert: 14, 19, 32, 33. j:  $\underline{2}$ . k: 2. *link*: 10, 12, 13, 14, 15, 21, 29, 30, 32, 33, 34, 35. list: 9, 14, 15, 18, 21, 29, 30, 31, 32, 33, 34, 35. $m: \ \ \frac{37}{}.$ main: 2.maxbases: 2, 23, 31.maxnodes: 2, 11, 12.maxpieces: 2, 23, 27. $\textit{maxsuffixes}\colon \ \underline{2},\ \underline{20},\ \underline{22}.$  $mult\colon \ \underline{23},\ 27,\ 34.$ multip:  $\underline{23}$ ,  $\underline{27}$ . names: 23, 27, 28, 34, 35. newbox: 14, 16, 17, 18, 22, 25, 29, 30, 31, 32, 33. node: 10, 11. occupied: 16, 21, <u>22</u>, 28, 35. p: 2, 4, 12, 13, 14, 15, 30.  $pdecode: \underline{4}, \underline{19}.$ piececount: 23, 27, 28, 34, 36. pieceno: 9, 15, 25, 35. $printbox: \underline{15}.$ printf: 17, 24, 34, 35. putavail: 13, 31.q: 2, 13, 14, 30.

 $r: \ \underline{2}, \ \underline{14}.$ s: <u>14</u>. scount: 20, 22, 34.sfxpresent: 22, 34, 36. size: 9, 14, 15, 18, 32, 33, 36. stderr: 3, 4, 5, 6, 7, 12, 15, 17, 20, 24, 27, 28, 31, 36, 37. stdin: 1, 17, 24, 34. strcmp: 20, 27. strcpy: 20, 27. strlen: 17, 20, 24. strncmp: 27.suf: 2, 10, 14, 15, 19, 20, 21, 30, 32, 33, 34, 35. suffix: 15, 20, 22, 34, 35. t:  $\underline{2}$ ,  $\underline{5}$ .  $x: \ \underline{2}, \ \underline{3}, \ \underline{4}, \ \underline{14}, \ \underline{15}.$  $xa: \ \underline{2}, \ 19.$ *xmax*: 9, 14, 15, 18, 29, 32, 33, 35. *xmin*: 9, 14, 15, 18, 29, 32, 35.  $xy: \quad \underline{10}, \, \underline{14}, \, 15, \, 21, \, 29, \, 30, \, 32, \, 33, \, 34, \, 35.$  $xy\theta: 2, 29.$  $y: \ \underline{2}, \ \underline{5}, \ \underline{14}, \ \underline{15}.$ ya: 2, 19.ymax: 9, 14, 15, 18, 29, 32, 33, 35. ymin: 9, 14, 15, 18, 29, 32, 35.

POLYIAMOND-DLX NAMES OF THE SECTIONS 17

```
\langle \text{ Bid farewell 36} \rangle Used in section 2.
(Complete the range from t to x 7) Used in section 5.
\langle Create the other base placements equivalent to newbox 31\rangle Used in section 25.
\langle \text{ Decode a bracketed specification 5} \rangle Used in section 4.
 Digest the optional suffix, suf(20) Used in section 19.
 Get ready for a range 6 Used in section 5.
 Global variables 8, 11, 22, 23 \ Used in section 2.
(Normalize the cells of newbox 29) Used in sections 25 and 32.
 Output the DLX item-name line 34 \rangle Used in section 2.
 Output the DLX options 35 \ Used in section 2.
\langle \text{ Put the specified cells into } newbox, \text{ starting at } buf[p] | 18 \rangle Used in sections 17 and 25.
(Read a piece spec 25) Used in section 24.
\langle \text{Read the box spec } 17 \rangle Used in section 2.
Read the piece name, and find it in the names table at position k = 27 Used in section 25.
\langle \text{ Read the piece specs 24} \rangle Used in section 2.
\langle \text{Scan an } xy \text{ spec } 19 \rangle Used in section 18.
\langle Set up the occupied table 21\rangle Used in section 17.
(Set newbox to base [i] transformed by 60^{\circ} rotation 32) Used in section 31.
(Set newbox to base[j] transformed by xy transposition 33) Used in section 31.
(Store the name in names[piececount] and check its validity 28) Used in section 27.
\langle Subroutines 3, 4, 12, 13, 14, 15, 30, 37\rangle Used in section 2.
\langle Type definitions 9, 10 \rangle Used in section 2.
```

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