(See https://cs.stanford.edu/~knuth/programs.html for date.)

1. Generalized exact cover. This program implements an extension of the algorithm discussed in my paper about "dancing links." I hacked it together from the XCOVER program that I wrote in 1994; I apologize for not having time to apply spit and polish.

Given a matrix whose elements are 0 or 1, the problem in that paper was to find all subsets of its rows whose sum is at most 1 in all columns and exactly 1 in all "primary" columns. The matrix is specified in the standard input file as follows: Each column has a symbolic name, up to seven characters long. The first line of input contains the names of all primary columns, followed by '|', followed by the names of all other columns. (If all columns are primary, the '|' may be omitted.) The remaining lines represent the rows, by listing the columns where 1 appears.

Here I extend the idea so that nonprimary columns have a different sort of restriction: If a row specifies a "color" in a nonprimary column, it rules out rows of all other colors, but any number of rows with the same color are allowed. (The previous situation was the special case in which all rows had a different color.) If xx is a column name, a specification like xx:a as part of a row stands for color a in column xx. Each color is specified by a single character.

Also—very important—I assume here that the input data is totally symmetric in all colors (except perhaps the smallest). In other words, whenever there's a row specifying color attributes  $(\chi_1, \ldots, \chi_k)$  in columns  $(c_1, \ldots, c_k)$ , there's also a row that specifies attributes  $(\pi\chi_1, \ldots, \pi\chi_k)$  for those colors, for every permutation  $\pi$  that fixes the smallest color. Then if there are t colors, there will be (t-1)! equivalent solutions; this program speeds things up by finding exactly one of them. The smallest color is assumed to be 'a', and the others are assumed to be 'b', 'c', etc. This program is identical to GDANCE except for places where it refers to the new variables  $color\_thresh$ , conflict, and cthresh.

The program prints the number of solutions and the total number of link updates. It also prints every nth solution, if the integer command line argument n is given. A second command-line argument causes the full search tree to be printed, and a third argument makes the output even more verbose.

```
#define max\_level 1000
                                /* at most this many rows in a solution */
#define max_degree 1000
                                  /* at most this many branches per search tree node */
#define max\_cols 1000
                               /* at most this many columns */
#define max_nodes 200000
                                    /* at most this many nonzero elements in the matrix */
#include <stdio.h>
#include <ctype.h>
#include <string.h>
  ⟨ Type definitions 3⟩
   Global variables 2
  \langle \text{Subroutines } 6 \rangle;
  main(argc, argv)
       int argc;
       char *argv[];
     \langle \text{Local variables } 10 \rangle;
     verbose = argc - 1;
     if (verbose) sscanf (argv[1], "%d", &spacing);
     (Initialize the data structures 7);
     (Backtrack through all solutions 12);
     printf("Altogether_{\sqcup}%d_{\sqcup}solutions,_{\sqcup}after_{\sqcup}%u_{\sqcup}updates_{\sqcup}and_{\sqcup}%u_{\sqcup}cleansings.\n", count, updates,
     if (verbose) (Print a profile of the search tree 23);
     exit(0);
```

2

```
2. \langle \text{Global variables 2} \rangle \equiv
  int verbose;
                    /* > 0 to show solutions, > 1 to show partial ones too */
  int count = 0;
                   /* number of solutions found so far */
                               /* number of times we deleted a list element */
  unsigned int updates;
  unsigned int purifs;
                              /* number of times we purified a list element */
  int spacing = 1;
                        /* if verbose, we output solutions when count % spacing \equiv 0 *
  int profile[max_level][max_degree];
                                         /* tree nodes of given level and degree */
                                         /* updates at a given level */
/* purifications at a given level */
  unsigned int upd_prof [max_level];
  unsigned int pur_prof [max_level];
  int maxb = 0;
                     /* maximum branching factor actually needed */
  int maxl = 0;
                     /* maximum level actually reached */
See also sections 8 and 14.
This code is used in section 1.
```

§3 XGDANCE DATA STRUCTURES 3

**3. Data structures.** Each column of the input matrix is represented by a **column** struct, and each row is represented as a linked list of **node** structs. There's one node for each nonzero entry in the matrix.

More precisely, the nodes are linked circularly within each row, in both directions. The nodes are also linked circularly within each column; the column lists each include a header node, but the row lists do not. Column header nodes are part of a **column** struct, which contains further info about the column.

Each node contains five fields. Four are the pointers of doubly linked lists, already mentioned; the fifth points to the column containing the node.

```
⟨Type definitions 3⟩ ≡
  typedef struct node_struct {
    struct node_struct *left, *right; /* predecessor and successor in row */
    struct node_struct *up, *down; /* predecessor and successor in column */
    struct col_struct *col; /* the column containing this node */
    int color; /* color, if specified */
} node;
See also section 4.
This code is used in section 1.
```

**4.** Each **column** struct contains five fields: The *head* is a node that stands at the head of its list of nodes; the *len* tells the length of that list of nodes, not counting the header; the *name* is a one-, two-, or ... or seven-letter identifier; *next* and *prev* point to adjacent columns, when this column is part of a doubly linked list.

As backtracking proceeds, nodes will be deleted from column lists when their row has been blocked by other rows in the partial solution. But when backtracking is complete, the data structures will be restored to their original state.

```
⟨ Type definitions 3⟩ +≡
typedef struct col_struct {
  node head; /* the list header */
  int len; /* the number of non-header items currently in this column's list */
  char name[8]; /* symbolic identification of the column, for printing */
  struct col_struct *prev, *next; /* neighbors of this column */
  int color_thresh; /* used for backing up */
} column;
```

**5.** One **column** struct is called the root. It serves as the head of the list of columns that need to be covered, and is identifiable by the fact that its *name* is empty.

```
#define root col_array[0] /* gateway to the unsettled columns */
```

4 data structures xgdance  $\S 6$ 

**6.** A row is identified not by name but by the names of the columns it contains. Here is a routine that prints a row, given a pointer to any of its nodes. It also prints the position of the given node in its column.

```
\langle Subroutines _{6}\rangle \equiv
   print\_row(p)
           node *p;
   { register node *q = p;
       register int k;
       do {
           printf(" " ", q \rightarrow col \rightarrow name);
           if (q \rightarrow color) \langle Print the color of node <math>q \ 27 \rangle;
           q = q \rightarrow right;
       } while (q \neq p);
       \textbf{for} \ (q = p \text{-}col \text{-}head.down, k = 1; \ q \neq p; \ k \text{+++})
           if (q \equiv \&(p \rightarrow col \rightarrow head)) {
              printf("\n"); return 0;
                                                             /* row not in its column! */
           } else q = q \rightarrow down;
       printf(" \llcorner (\% \mathtt{d} \llcorner \mathtt{of} \llcorner \% \mathtt{d}) \backslash \mathtt{n} ", k, p \neg col \neg len);
See also sections 15, 16, 25, 26, and 28.
This code is used in section 1.
```

This code is used in section 1.

7. Inputting the matrix. Brute force is the rule in this part of the program.  $\langle \text{Initialize the data structures } 7 \rangle \equiv$  $\langle \text{Read the column names 9} \rangle;$  $\langle \text{ Read the rows } 11 \rangle$ ; This code is used in section 1. 8. #define  $buf\_size \ 4 * max\_cols + 3$ /\* upper bound on input line length \*/  $\langle \text{Global variables } 2 \rangle + \equiv$ **column**  $col\_array[max\_cols + 2];$ /\* place for column records \*/ /\* place for nodes \*/ **node**  $node\_array[max\_nodes];$ **char** buf [buf\_size]; #define panic(m){  $fprintf(stderr, "%s!\n%s", m, buf); exit(-1); }$  $\langle \text{ Read the column names } 9 \rangle \equiv$  $cur\_col = col\_array + 1;$  $fgets(buf, buf\_size, stdin);$ if  $(buf[strlen(buf) - 1] \neq `\n') panic("Input_line_too_long");$ for (p = buf, primary = 1; \*p; p++) { **while** (isspace(\*p)) p++;if  $(\neg *p)$  break; if  $(*p \equiv '|')$  { primary = 0;if  $(cur\_col \equiv col\_array + 1) \ panic("No\_primary\_columns");$  $(cur\_col - 1) \neg next = \&root, root.prev = cur\_col - 1;$ continue: for  $(q = p + 1; \neg isspace(*q); q \leftrightarrow)$ ; if (q > p + 7)  $panic("Column_name_too_long");$ if  $(cur\_col \ge \& col\_array[max\_cols])$   $panic("Too_lmany_lcolumns");$ for  $(q = cur\_col \neg name; \neg isspace(*p); q++, p++) *q = *p;$  $cur\_col \neg head.up = cur\_col \neg head.down = \& cur\_col \neg head;$  $cur\_col \rightarrow len = 0;$ if (primary)  $cur\_col \neg prev = cur\_col - 1, (cur\_col - 1) \neg next = cur\_col;$ else  $cur\_col \neg prev = cur\_col \neg next = cur\_col;$  $cur\_col +\!\!+;$ **if** (primary) { if  $(cur\_col \equiv col\_array + 1) \ panic("No\_primary\_columns");$  $(cur\_col - 1)$   $\neg next = \& root, root.prev = cur\_col - 1;$ } This code is used in section 7. 10.  $\langle \text{Local variables } 10 \rangle \equiv$ register column \*cur\_col; register char \*p, \*q;register node \**cur\_node*; int primary; See also sections 13 and 20.

§11

6

```
11. \langle \text{Read the rows } 11 \rangle \equiv
   cur\_node = node\_array;
   while (fgets(buf, buf_size, stdin)) {
      register column *ccol;
      register node *row\_start, *x;
      if (buf[strlen(buf) - 1] \neq '\n') panic("Input_line_too_long");
      row\_start = \Lambda;
      for (p = buf; *p; p++) {
        while (isspace(*p)) p ++;
        if (\neg *p) break;
        for (q = p + 1; \neg isspace(*q) \land *q \neq ':'; q++);
        if (q > p + 7) panic("Column_name_too_long");
        for (q = cur\_col \neg name; \neg isspace(*p) \land *p \neq ': '; q++, p++) *q = *p;
         *q = '\0';
        \mathbf{for}\ (\mathit{ccol} = \mathit{col\_array};\ \mathit{strcmp}(\mathit{ccol} \neg \mathit{name}, \mathit{cur\_col} \neg \mathit{name});\ \mathit{ccol} +\!\!\!\!+)\ ;
        if (ccol \equiv cur\_col) \ panic("Unknown\_column\_name");
        if (cur\_node \equiv \&node\_array[max\_nodes]) panic("Too_lmany_nodes");
        if (\neg row\_start) row\_start = cur\_node;
        else cur\_node \neg left = cur\_node - 1, (cur\_node - 1) \neg right = cur\_node;
        for (x = row\_start; x \neq cur\_node; x++)
           if (x \rightarrow col \equiv ccol) panic("A<sub>1</sub>|row<sub>1</sub>|can't<sub>1</sub>|use<sub>1</sub>|a<sub>1</sub>|column<sub>1</sub>|twice");
         cur\_node \neg col = ccol;
         cur\_node \neg up = ccol \neg head.up, ccol \neg head.up \neg down = cur\_node;
         ccol \neg head.up = cur\_node, cur\_node \neg down = \& ccol \neg head;
         ccol \neg len ++;
        if (*p \equiv ':') \langle \text{Read a color restriction } 24 \rangle;
         cur\_node ++;
      if (¬row_start) panic("Empty_row");
      row\_start \rightarrow left = cur\_node - 1, (cur\_node - 1) \rightarrow right = row\_start;
This code is used in section 7.
```

 $\S12$  XGDANCE BACKTRACKING '

12. Backtracking. Our strategy for generating all exact covers will be to repeatedly choose always the column that appears to be hardest to cover, namely the column with shortest list, from all columns that still need to be covered. And we explore all possibilities via depth-first search.

The neat part of this algorithm is the way the lists are maintained. Depth-first search means last-in-firstout maintenance of data structures; and it turns out that we need no auxiliary tables to undelete elements from lists when backing up. The nodes removed from doubly linked lists remember their former neighbors, because we do no garbage collection.

The basic operation is "covering a column." This means removing it from the list of columns needing to be covered, and "blocking" its rows: removing nodes from other lists whenever they belong to a row of a node in this column's list.

```
\langle \text{ Backtrack through all solutions } 12 \rangle \equiv
  level = 0;
  cthresh = 'a';
forward: \langle \text{Set } best\_col \text{ to the best column for branching } 19 \rangle;
  cover(best\_col);
  cur\_node = choice[level] = best\_col \rightarrow head.down;
advance:
  if (cur\_node \equiv \&(best\_col \neg head)) goto backup;
  if (verbose > 1) {
     printf("L%d:", level);
     print\_row(cur\_node);
  conflict = 0;
  \langle \text{ Cover all other columns of } cur\_node 17 \rangle;
  if (conflict) goto recover;
  if (root.next \equiv \& root) (Record solution and goto recover 21);
  level++;
  goto forward;
backup: uncover(best_col);
  if (level \equiv 0) goto done;
  level--;
  cur\_node = choice[level]; best\_col = cur\_node \neg col;
recover: (Uncover all other columns of cur_node 18);
  cur\_node = choice[level] = cur\_node \neg down; goto advance;
done:
  if (verbose > 3) (Print column lengths, to make sure everything has been restored 22);
This code is used in section 1.
13. \langle \text{Local variables } 10 \rangle + \equiv
  register column *best\_col;
                                       /* column chosen for branching */
  register node *pp;
                              /* traverses a row */
14. \langle \text{Global variables 2} \rangle + \equiv
  int level:
                  /* number of choices in current partial solution */
  int cthresh;
                     /* smallest color allowable when extending a solution */
  int conflict;
                     /* set nonzero if a conflict arises while covering */
  node *choice[max_level]; /* the row and column chosen on each level */
```

8 BACKTRACKING XGDANCE  $\S15$ 

15. When a row is blocked, it leaves all lists except the list of the column that is being covered. Thus a node is never removed from a list twice.

```
\langle \text{Subroutines } 6 \rangle + \equiv
   cover(c)
         column *c;
   { register column *l, *r;
      register node *rr, *nn, *uu, *dd;
      register int k = 1;
                                       /* updates */
      l = c \neg prev; \ r = c \neg next;
      l \rightarrow next = r; r \rightarrow prev = l;
      for (rr = c \rightarrow head.down; rr \neq \&(c \rightarrow head); rr = rr \rightarrow down)
         for (nn = rr \rightarrow right; nn \neq rr; nn = nn \rightarrow right) {
            uu = nn \neg up; dd = nn \neg down;
            uu \rightarrow down = dd; dd \rightarrow up = uu;
            k++;
            nn \rightarrow col \rightarrow len --;
      updates += k;
      upd\_prof[level] += k;
```

16. Uncovering is done in precisely the reverse order. The pointers thereby execute an exquisitely choreographed dance which returns them almost magically to their former state.

```
\langle \text{Subroutines } 6 \rangle + \equiv
   uncover(c)
         column *c;
   { register column *l, *r;
      register node *rr, *nn, *uu, *dd;
      for (rr = c \rightarrow head.up; rr \neq \&(c \rightarrow head); rr = rr \rightarrow up)
         for (nn = rr \rightarrow left; nn \neq rr; nn = nn \rightarrow left) {
             uu = nn \neg up; dd = nn \neg down;
             uu \neg down = dd \neg up = nn;
            nn \neg col \neg len ++;
      l = c \rightarrow prev; \ r = c \rightarrow next;
      l \rightarrow next = r \rightarrow prev = c;
17. \langle \text{Cover all other columns of } cur\_node | 17 \rangle \equiv
   for (pp = cur\_node \neg right; pp \neq cur\_node; pp = pp \neg right)
      if (\neg pp \neg color) cover(pp \neg col);
      else if (pp \neg color > 0) {
         if (pp \rightarrow color > cthresh) conflict = 1;
         else purify(pp);
This code is used in section 12.
```

§18 XGDANCE BACKTRACKING 9

18. We included *left* links, thereby making the rows doubly linked, so that columns would be uncovered in the correct LIFO order in this part of the program. (The *uncover* routine itself could have done its job with *right* links only.) (Think about it.)

```
\langle Uncover all other columns of cur_node 18\rangle \equiv
  for (pp = cur\_node \neg left; pp \neq cur\_node; pp = pp \neg left)
     if (\neg pp \neg color) uncover(pp \neg col);
     else if (pp \neg color > 0 \land pp \neg color \leq cthresh) unpurify(pp);
This code is used in section 12.
     \langle \text{Set } best\_col \text{ to the best column for branching } 19 \rangle \equiv
  minlen = max\_nodes;
  if (verbose > 2) printf("Level", level);
  for (cur\_col = root.next; cur\_col \neq \&root; cur\_col = cur\_col \neg next) {
     if (verbose > 2) printf ("\\\sumset \( \)\subset (\( \)\d\) ", cur\_col \neg name, cur\_col \neg len);
     if (cur\_col \neg len < minlen) best_col = cur\_col, minlen = cur\_col \neg len;
  if (verbose) {
     if (level > maxl) {
        if (level \ge max\_level) panic("Too_{\perp}many_{\perp}levels");
        maxl = level;
     if (minlen > maxb) {
        if (minlen \ge max\_degree) panic("Too_{\square}many_{\square}branches");
        maxb = minlen;
     profile[level][minlen]++;
     if (verbose > 2) printf("\_branching\_on\_\%s(%d)\n", best\_col¬name, minlen);
This code is used in section 12.
20. \langle \text{Local variables } 10 \rangle + \equiv
  register int minlen;
  register int j, k, x;
      \langle \text{Record solution and goto } recover 21 \rangle \equiv
     count ++:
     if (verbose) {
        profile[level + 1][0] ++;
        if (count \% spacing \equiv 0) {
          printf("%d: \n", count);
           for (k = 0; k \leq level; k++) print_row(choice[k]);
     goto recover;
This code is used in section 12.
```

10 BACKTRACKING XGDANCE §22

```
\langle \text{Print column lengths, to make sure everything has been restored } 22 \rangle \equiv
22.
    printf("Final_column_lengths");
    for (cur\_col = root.next; cur\_col \neq \&root; cur\_col = cur\_col \neg next)
      printf(" \_ \%s(\%d)", cur\_col \neg name, cur\_col \neg len);
    printf("\n");
This code is used in section 12.
23. \langle \text{Print a profile of the search tree 23} \rangle \equiv
              /* the root node doesn't show up in the profile */
    x=1;
    for (level = 1; level \leq maxl + 1; level ++) {
      j = 0;
      for (k = 0; k \le maxb; k++) {
         printf("\%6d", profile[level][k]);
         j += profile[level][k];
      printf("Total_{\sqcup}%d_{\sqcup}nodes.\n",x);
This code is used in section 1.
```

§24 XGDANCE COLOR BARRIERS 11

24. Color barriers. Finally, here's the new material related to coloring.

```
 \langle \, \operatorname{Read} \, \operatorname{a} \, \operatorname{color} \, \operatorname{restriction} \, {}^{24} \rangle \equiv \\ \{ & \quad \text{if} \, (primary) \, \, panic(\texttt{"Color} \sqcup \operatorname{isn't} \sqcup \operatorname{allowed} \sqcup \operatorname{in} \sqcup \operatorname{a} \sqcup \operatorname{primary} \sqcup \operatorname{column"}); \\ & \quad \text{if} \, (isspace(*(p+1)) \vee \neg isspace(*(p+2))) \, \, panic(\texttt{"Color} \sqcup \operatorname{should} \sqcup \operatorname{be} \sqcup \operatorname{a} \sqcup \operatorname{single} \sqcup \operatorname{character"}); \\ & \quad cur\_node \neg color = *(p+1); \\ & \quad p += 2; \\ \}
```

This code is used in section 11.

25. When we choose a row that specifies colors in one or more columns, we "purify" those columns by removing all incompatible rows. All rows that want the same color in a purified column will now be given the color code -1 so that we need not purify the column again.

```
\langle \text{Subroutines } 6 \rangle + \equiv
   purify(p)
         node *p;
   { register column *c = p \rightarrow col;
      register int x = p \rightarrow color;
      register node *rr, *nn, *uu, *dd;
      register int k = 0, kk = 1; /* updates */
                                   /* this is used only to help print_row */
      c \rightarrow head.color = x;
      c \rightarrow color\_thresh = cthresh;
      if (cthresh \equiv x) cthresh \leftrightarrow;
      for (rr = c \rightarrow head.down; rr \neq \&(c \rightarrow head); rr = rr \rightarrow down)
         if (rr \rightarrow color \neq x) {
            for (nn = rr \rightarrow right; nn \neq rr; nn = nn \rightarrow right) {
               uu = nn \neg up; dd = nn \neg down;
               uu \rightarrow down = dd; dd \rightarrow up = uu;
               k++;
               nn \rightarrow col \rightarrow len --;
         } else if (rr \neq p) kk++, rr \neg color = -1;
      updates += k, purifs += kk;
      upd\_prof[level] += k, pur\_prof[level] += kk;
```

12 COLOR BARRIERS XGDANCE §26

```
26. Just as purify is analogous to cover, the inverse process is analogous to uncover.
\langle Subroutines _{6}\rangle +\equiv
   unpurify(p)
         node *p;
   { register column *c = p \rightarrow col;
      register int x = p \neg color;
      \textbf{register node} *rr, *nn, *uu, *dd;
      for (rr = c \rightarrow head.up; rr \neq \&(c \rightarrow head); rr = rr \rightarrow up)
         if (rr \rightarrow color < 0) rr \rightarrow color = x;
         else if (rr \neq p) {
            for (nn = rr \rightarrow left; nn \neq rr; nn = nn \rightarrow left) {
                uu = nn \neg up; dd = nn \neg down;
               uu \rightarrow down = dd \rightarrow up = nn;
               nn \neg col \neg len ++;
      c \rightarrow head.color = 0;
      cthresh = c \neg color\_thresh;
27. \langle Print the color of node q 27\rangle \equiv
   printf(":%c", q\rightarrow color > 0 ? q\rightarrow color : q\rightarrow col\rightarrow head.color);
This code is used in section 6.
```

 $\S28$  XGDANCE HELP FOR DEBUGGING 13

28. Help for debugging. Here's a subroutine for when I'm doing a long run and want to check the current progress.

```
 \begin{split} &\langle \, \text{Subroutines 6} \, \rangle + \equiv \\ & \quad \text{void } show\_state(\,) \\ &\{ \\ & \quad \text{register int } k; \\ & \quad printf(\, \text{"Current} \sqcup \text{state} \sqcup (\text{level} \sqcup \% \text{d}) : \n^{\texttt{"}}, level); \\ & \quad \text{for } (k=0; \ k < level; \ k++) \ print\_row(choice[k]); \\ & \quad printf(\, \text{"Max} \sqcup \text{level} \sqcup \text{so} \sqcup \text{far:} \sqcup \% \text{d} \cap \text{"}, maxl); \\ & \quad printf(\, \text{"Max} \sqcup \text{branching} \sqcup \text{so} \sqcup \text{far:} \sqcup \% \text{d} \cap \text{"}, maxb); \\ & \quad printf(\, \text{"Solutions} \sqcup \text{so} \sqcup \text{far:} \sqcup \% \text{d} \cap \text{"}, count); \\ & \quad \} \end{split}
```

14 INDEX XGDANCE §29

## 29. Index.

advance: 12. $argc: \underline{1}.$  $argv: \underline{1}.$ backup:  $\underline{12}$ .  $best\_col$ : 12, <u>13</u>, 19. buf: 8, 9, 11.  $buf\_size: 8, 9, 11.$  $c: \ \underline{15}, \ \underline{16}, \ \underline{25}, \ \underline{26}.$ ccol:  $\underline{11}$ . choice: 12, <u>14</u>, 21, 28.  $col: \underline{3}, 6, 11, 12, 15, 16, 17, 18, 25, 26, 27.$  $col\_array$ : 5, 8, 9, 11. col\_struct: 3, 4. color: 3, 6, 17, 18, 24, 25, 26, 27.  $color\_thresh$ : 1,  $\underline{4}$ , 25, 26. **column**: <u>4</u>, 5, 8, 10, 11, 13, 15, 16, 25, 26. conflict: 1, 12, <u>14</u>, 17. count:  $1, \underline{2}, 21, 28.$ cover:  $12, \underline{15}, 17, 26.$ cthresh: 1, 12, <u>14</u>, 17, 18, 25, 26. *cur\_col*: 9, <u>10</u>, 11, 19, 22. cur\_node: <u>10</u>, 11, 12, 17, 18, 24. dd: 15, 16, 25, 26.done: 12.down:  $\underline{3}$ , 6, 9, 11, 12, 15, 16, 25, 26. exit: 1, 9.fgets: 9, 11.forward: 12.fprintf: 9.head: 4, 6, 9, 11, 12, 15, 16, 25, 26, 27. isspace: 9, 11, 24. j:  $\underline{20}$ . k: 6, 15, 20, 25, 28. kk: 25. *l*: <u>15</u>, <u>16</u>. *left*:  $\underline{3}$ , 11, 16, 18, 26. len: 4, 6, 9, 11, 15, 16, 19, 22, 25, 26. level: 12, <u>14</u>, 15, 19, 21, 23, 25, 28. main: 1. $max\_cols$ :  $\underline{1}$ , 8, 9.  $max\_degree: \underline{1}, \underline{2}, \underline{19}.$  $max\_level: 1, 2, 14, 19.$  $max\_nodes: \underline{1}, 8, 11, 19.$  $maxb: \ \underline{2}, \ 19, \ 23, \ 28.$ maxl: 2, 19, 23, 28.minlen: 19, 20. $name: \underline{4}, 5, 6, 9, 11, 19, 22.$  $next: \underline{4}, 9, 12, 15, 16, 19, 22.$  $nn: \ \underline{15}, \ \underline{16}, \ \underline{25}, \ \underline{26}.$ **node**: 3, 4, 6, 8, 10, 11, 13, 14, 15, 16, 25, 26.  $node\_array: 8, 11.$ 

node\_struct: 3. p: 6, 10, 25, 26. panic: 9, 11, 19, 24. *pp*: <u>13</u>, 17, 18. prev:  $\underline{4}$ , 9, 15, 16. primary: 9, 10, 24.*print\_row*: <u>6</u>, 12, 21, 25, 28. printf: 1, 6, 12, 19, 21, 22, 23, 27, 28. profile: 2, 19, 21, 23. $pur_prof: \underline{2}, \underline{23}, \underline{25}.$ purifs:  $1, \underline{2}, 25.$ purify:  $17, \ \underline{25}, \ 26.$  $q: \ \ \underline{6}, \ \underline{10}.$  $r: \ \underline{15}, \ \underline{16}.$  $recover: \underline{12}, \underline{21}.$  $right: \ \ \underline{3}, \ 6, \ 11, \ 15, \ 17, \ 18, \ 25.$ root: 5, 9, 12, 19, 22.  $row\_start: 11.$ rr: 15, 16, 25, 26. $show\_state: \underline{28}.$ spacing: 1, 2, 21. sscanf: 1.stderr: 9.stdin: 9, 11. strcmp: 11.*strlen*: 9, 11.  $uncover: 12, \underline{16}, 18, 26.$ unpurify:  $18, \underline{26}$ . up: 3, 9, 11, 15, 16, 25, 26. $upd\_prof: \ \ \underline{2}, \ 15, \ 23, \ 25.$  $updates: 1, \underline{2}, 15, 25.$ uu: 15, 16, 25, 26.verbose: 1, 2, 12, 19, 21. $x: \ \underline{11}, \ \underline{20}, \ \underline{25}, \ \underline{26}.$ 

XGDANCE NAMES OF THE SECTIONS 15

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\langle \text{Local variables 10, 13, 20} \rangle Used in section 1.
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(Print column lengths, to make sure everything has been restored 22) Used in section 12.
Print the color of node q 27 Used in section 6.
(Read a color restriction 24) Used in section 11.
\langle \text{ Read the column names 9} \rangle Used in section 7.
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\langle \text{Set } best\_col \text{ to the best column for branching } 19 \rangle Used in section 12.
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\langle Type definitions 3, 4\rangle Used in section 1.
\langle Uncover all other columns of cur\_node 18\rangle Used in section 12.
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## XGDANCE

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