1*   Introduction.   This program prepares a METAFONT file for a special-purpose font that will approxi-mate a given picture. The input file (*stdin*) is assumed to be an EPS file output by Adobe Photoshop$^{\text{TM}}$ on a Macintosh with the binary EPS option, containing m rows of n columns each; in Photoshop terminology the image is m pixels high and n pixels wide, in grayscale mode, with a resolution of 72 pixels per inch. The output file (*stdout*) will be a sequence of m lines like

$$\texttt{row 10; data "d01...53";}$$

this means that the pixel data for row 10 is the string of n bits $110100000001\ldots01010011$ encoded as a hexadecimal string of length $n/4$.

For simplicity, this program assumes that $m = 512$ and $n = 440$.

#**define** m 512   /* this many rows */
#**define** n 440   /* this many columns */
#**include** `<stdio.h>`
#**include** `<time.h>`
  time_t *cur_clock*;
  float $a[m + 2][n + 2]$;   /* darknesses: 0.0 is white, 1.0 is black */

  ⟨ Global variables 4 ⟩
  ⟨ Subroutines 12 ⟩

  main(*argc*, *argv*)
      int *argc*;
      char *argv[ ];
  {
    register int $i,\ j,\ k,\ l,\ ii,\ jj,\ w$;
    register float *err*;
    float $zeta = 0.2,\ sharpening = 0.9$;

    ⟨ Check for nonstandard *zeta* and *sharpening* factors 2 ⟩;
    ⟨ Check the beginning lines of the input file 3 ⟩;
    ⟨ Input the graphic data 5 ⟩;
    ⟨ Translate input to output 15 ⟩;
    ⟨ Spew out the answers 18* ⟩;
  }

2.   Optional command-line arguments allow the user to change the *zeta* and/or *sharpening* parameters discussed below.

⟨ Check for nonstandard *zeta* and *sharpening* factors 2 ⟩ ≡
  if $(argc > 1 \wedge sscanf(argv[1], \texttt{"\%g"}, \&zeta) \equiv 1)$ {
    fprintf(*stderr*, `"Using␣zeta␣=␣%g\n"`, *zeta*);
    if $(argc > 2 \wedge sscanf(argv[2], \texttt{"\%g"}, \&sharpening) \equiv 1)$
      fprintf(*stderr*, `"␣␣and␣sharpening␣factor␣%g\n"`, *sharpening*);
  }
This code is used in section 1*.

3.   Macintosh conventions indicate the end of a line by the ASCII ⟨carriage return⟩ character (i.e., control-M, aka `\r`), but the C library is set up to work best with newlines (i.e., control-J, aka `\n`). We aren't worried about efficiency, so we simply input one character at a time. This program assumes Macintosh conventions.

   The job here is to look for the sequence `Box:` in the input, followed by 0, 0, the number of columns, and the number of rows.

#**define** $panic(s)$
$$\{$$
$$fprintf(stderr, s); \; exit(-1);$$
$$\}$$

⟨Check the beginning lines of the input file 3⟩ ≡
   $k = 0;$
$scan$:
   if $(k{+}{+} > 1000)$ $panic($"Couldn't␣find␣the␣bounding␣box␣info!\n"$);$
   if $(getchar() \neq 'B')$ **goto** $scan;$
   if $(getchar() \neq 'o')$ **goto** $scan;$
   if $(getchar() \neq 'x')$ **goto** $scan;$
   if $(getchar() \neq ':')$ **goto** $scan;$
   if $(scanf($"%d␣%d␣%d␣%d"$, \& llx, \& lly, \& urx, \& ury) \neq 4 \vee llx \neq 0 \vee lly \neq 0)$
      $panic($"Bad␣bounding␣box␣data!\n"$);$
   if $(urx \neq n \vee ury \neq m)$ $panic($"The␣image␣doesn't␣have␣the␣correct␣width␣and␣height!\n"$);$
This code is used in section 1*.

4.   ⟨Global variables 4⟩ ≡
   int llx, lly, urx, ury;   /∗ bounding box parameters ∗/
See also sections 8 and 11.
This code is used in section 1*.

5.   After we've seen the bounding box, we look for `beginimage\r`; this will be followed by the pixel data, one character per byte.

⟨Input the graphic data 5⟩ ≡
   $k = 0;$
$skan$:
   if $(k{+}{+} > 10000)$ $panic($"Couldn't␣find␣the␣pixel␣data!\n"$);$
   if $(getchar() \neq 'b')$ **goto** $skan;$
   if $(getchar() \neq 'e')$ **goto** $skan;$
   if $(getchar() \neq 'g')$ **goto** $skan;$
   if $(getchar() \neq 'i')$ **goto** $skan;$
   if $(getchar() \neq 'n')$ **goto** $skan;$
   if $(getchar() \neq 'i')$ **goto** $skan;$
   if $(getchar() \neq 'm')$ **goto** $skan;$
   if $(getchar() \neq 'a')$ **goto** $skan;$
   if $(getchar() \neq 'g')$ **goto** $skan;$
   if $(getchar() \neq 'e')$ **goto** $skan;$
   if $(getchar() \neq '\backslash r')$ **goto** $skan;$
   ⟨Input rectangular pixel data 6⟩;
   if $(getchar() \neq '\backslash r')$ $panic($"Wrong␣amount␣of␣pixel␣data!\n"$);$
This code is used in section 1*.

6.   Photoshop follows the conventions of photographers who consider 0 to be black and 1 to be white; but we follow the conventions of computer scientists who tend to regard 0 as devoid of ink (white) and 1 as full of ink (black).

   We use the fact that global arrays are initially zero to assume that there are all-white rows of 0s above, below, and to the left and right of the input data.

$\langle$ Input rectangular pixel data $6\rangle \equiv$
 for $(i = 1; \ i \leq ury; \ i{+}{+})$
  for $(j = 1; \ j \leq urx; \ j{+}{+}) \ a[i][j] = 1.0 - getchar(\,)/255.0;$

This code is used in section 5.

7. Dot diffusion.   Our job is to go from eight-bit pixels to one-bit pixels; that is, from 256 shades of gray to an approximation that uses only black and white. The method used here is called *dot diffusion* (see [D. E. Knuth, "Digital halftones by dot diffusion," *ACM Transactions on Graphics* **6** (1987), 245–273]); it works as follows: The pixels are divided into 64 classes, numbered from 0 to 63. We convert the pixel values to 0s and 1s by assigning values first to all the pixels of class 0, then to all the pixels of class 1, etc. The error incurred at each step is distributed to the neighbors whose class numbers are higher. This is done by means of precomputed tables *class_row*, *class_col*, *start*, *del_i*, *del_j*, and *alpha* whose function is easy to deduce from the following code segment.

$\langle$ Choose pixel values and diffuse the errors in the buffer 7 $\rangle \equiv$

```
    for (k = 0;  k < 64;  k++)
      for (i = class_row[k];  i ≤ m;  i += 8)
        for (j = class_col[k];  j ≤ n;  j += 8)  {
          ⟨ Decide the color of pixel [i, j] and the resulting err  9 ⟩;
          for (l = start[k];  l < start[k + 1];  l++)  a[i + del_i[l]][j + del_j[l]] += err * alpha[l];
        }
```

This code is used in section 15.

8.   We will use the following model for estimating the effect of a given bit pattern in the output: If a pixel is black, its darkness is 1.0; if it is white but at least one of its four neighbors is black, its darkness is *zeta*; if it is white and has four white neighbors, its darkness is 0.0. Laserprinters of the 1980s tended to spatter toner in a way that could be approximated roughly by taking *zeta* = 0.2 in this model. The value of *zeta* should be between -0.25 and $+1.0$.

An auxiliary array *aa* holds code values *white*, *gray*, or *black* to facilitate computations in this model. All cells are initially *white*; but when we decide to make a pixel *black*, we change its *white* neighbors (if any) to *gray*.

#**define** *white* 0   /∗ code for a white pixel with all white neighbors ∗/
#**define** *gray* 1   /∗ code for a white pixel with 1, 2, 3, or 4 black neighbors ∗/
#**define** *black* 2   /∗ code for a black pixel ∗/

$\langle$ Global variables 4 $\rangle$ $+\equiv$
    char $aa[m + 2][n + 2]$;   /∗ *white*, *gray*, or *black* status of final pixels ∗/

9.   In this step the current pixel's final one-bit value is determined. It presently is either *white* or *gray*; we either leave it as is, or we blacken it and gray its white neighbors, whichever minimizes the magnitude of the error.

Potentially *gray* values near the newly chosen pixel make this calculation slightly tricky. Notice, for example, that the very first black pixel to be created will increase the local darkness of the image by $1 + 4zeta$. Suppose the original image is entirely black, so that $a[i][j]$ is 1.0 for $1 \leq i \leq m$ and $1 \leq j \leq n$. If a pixel of class 0 is set to *white*, the error (i.e., the darkness that needs to be diffused to its upperclass neighbors) is 1.0; but if it is set to *black*, the error is $-4zeta$. The algorithm will choose *black* unless $zeta \geq .25$.

⟨ Decide the color of pixel $[i, j]$ and the resulting *err* 9 ⟩ ≡
```
  if (aa[i][j] ≡ white)  err = a[i][j] − 1.0 − 4 ∗ zeta;
  else {      /∗ aa[i][j] ≡ gray ∗/
    err = a[i][j] − 1.0 + zeta;
    if (aa[i − 1][j] ≡ white)  err −= zeta;
    if (aa[i + 1][j] ≡ white)  err −= zeta;
    if (aa[i][j − 1] ≡ white)  err −= zeta;
    if (aa[i][j + 1] ≡ white)  err −= zeta;
  }
  if (err + a[i][j] > 0) {      /∗ black is better ∗/
    aa[i][j] = black;
    if (aa[i − 1][j] ≡ white)  aa[i − 1][j] = gray;
    if (aa[i + 1][j] ≡ white)  aa[i + 1][j] = gray;
    if (aa[i][j − 1] ≡ white)  aa[i][j − 1] = gray;
    if (aa[i][j + 1] ≡ white)  aa[i][j + 1] = gray;
  }
  else  err = a[i][j];      /∗ keep it white or gray ∗/
```
This code is used in section 7.

10.   Computing the diffusion tables.   The tables for dot diffusion could be specified by a large number of boring assignment statements, but it is more fun to compute them by a method that reveals some of the mysterious underlying structure.

⟨ Initialize the diffusion tables 10 ⟩ ≡
  ⟨ Initialize the class number matrix 13 ⟩;
  ⟨ Compile "instructions" for the diffusion operations 14 ⟩;
This code is used in section 15.

11.   ⟨ Global variables 4 ⟩ +≡
  char $class\_row[64]$, $class\_col[64]$;   /∗ first row and column for a given class ∗/
  char $class\_number[10][10]$;   /∗ the number of a given position ∗/
  int $kk = 0$;   /∗ how many classes have been done so far ∗/
  int $start[65]$;   /∗ the first instruction for a given class ∗/
  int $del\_i[256]$, $del\_j[256]$;   /∗ relative location of a neighbor ∗/
  float $alpha[256]$;   /∗ diffusion coefficient for a neighbor ∗/

12.   The order of classes used here is the order in which pixels might be blackened in a font for halftones based on dots in a 45° grid. In fact, it is precisely the pattern used in the font `ddith300`, discussed in the author's paper "Fonts for Digital Halftones" [Chapter 21 of *Selected Papers on Digital Typography*].

⟨ Subroutines 12 ⟩ ≡
  void $store(i, j)$
      int i, j;
  {
    if $(i < 1)$ $i \mathrel{+}= 8$; **else if** $(i > 8)$ $i \mathrel{-}= 8$;
    if $(j < 1)$ $j \mathrel{+}= 8$; **else if** $(j > 8)$ $j \mathrel{-}= 8$;
    $class\_number[i][j] = kk$;
    $class\_row[kk] = i$; $class\_col[kk] = j$;
    $kk\mathbin{++}$;
  }
  void $store\_eight(i, j)$
      int i, j;
  {
    $store(i, j)$; $store(i - 4, j + 4)$; $store(1 - j, i - 4)$; $store(5 - j, i)$;
    $store(j, 5 - i)$; $store(4 + j, 1 - i)$; $store(5 - i, 5 - j)$; $store(1 - i, 1 - j)$;
  }
This code is used in section 1*.

13.   ⟨ Initialize the class number matrix 13 ⟩ ≡
  $store\_eight(7, 2)$; $store\_eight(8, 3)$; $store\_eight(8, 2)$; $store\_eight(8, 1)$;
  $store\_eight(1, 4)$; $store\_eight(1, 3)$; $store\_eight(1, 2)$; $store\_eight(2, 3)$;
  for $(i = 1;\ i \le 8;\ i\mathbin{++})$ $class\_number[i][0] = class\_number[i][8]$, $class\_number[i][9] = class\_number[i][1]$;
  for $(j = 0;\ j \le 9;\ j\mathbin{++})$ $class\_number[0][j] = class\_number[8][j]$, $class\_number[9][j] = class\_number[1][j]$;
This code is used in section 10.

14. The "compilation" in this step simulates going through the diffusion process the slow way, recording the actions it performs. Then those actions can all be done at high speed later.

⟨ Compile "instructions" for the diffusion operations 14 ⟩ ≡

```
for (k = 0, l = 0; k < 64; k++) {
    start[k] = l;        /* l is the number of instructions compiled so far */
    i = class_row[k];  j = class_col[k];  w = 0;
    for (ii = i − 1;  ii ≤ i + 1;  ii ++)
        for (jj = j − 1;  jj ≤ j + 1;  jj ++)
            if (class_number[ii][jj] > k) {
                del_i[l] = ii − i;  del_j[l] = jj − j;  l++;
                if (ii ≠ i ∧ jj ≠ j)  w++;       /* diagonal neighbors get weight 1 */
                else  w += 2;        /* orthogonal neighbors get weight 2 */
            }
    for (jj = start[k];  jj < l;  jj ++)
        if (del_i[jj] ≠ 0 ∧ del_j[jj] ≠ 0)  alpha[jj] = 1.0/w;
        else  alpha[jj] = 2.0/w;
}
start[64] = l;        /* at this point l will be 256 */
```

This code is used in section 10.

15.   Synthesis.   Now we're ready to put the pieces together.

⟨ Translate input to output 15 ⟩ ≡
   ⟨ Initialize the diffusion tables 10 ⟩;
   if (*sharpening*) ⟨ Sharpen the input 16 ⟩;
   ⟨ Choose pixel values and diffuse the errors in the buffer 7 ⟩;

This code is used in section 1*.

16.   Experience shows that dot diffusion often does a better job if we apply a filtering operation that exaggerates the differences between the intensities of a pixel and its neighbors:

$$a_{ij} \leftarrow \frac{a_{ij} - \alpha \bar{a}_{ij}}{1 - \alpha},$$

where $\bar{a}_{ij} = \frac{1}{9} \sum_{\delta=-1}^{+1} \sum_{\epsilon=-1}^{+1} a_{(i+\delta)(j+\epsilon)}$ is the average value of a_{ij} and its eight neighbors. (See the discussion in the *Transactions on Graphics* paper cited earlier. The parameter α is the *sharpening* value, which must obviously be less than 1.0.)

   We could use a buffering scheme to apply this transformation in place, but it's easier to store the new value of a_{ij} in $a_{(i-1)(j-1)}$ and then shift everything back into position afterwards. The values of a_{i0} and a_{0j} don't have to be restored to zero after this step, because they will not be examined again.

⟨ Sharpen the input 16 ⟩ ≡
   {
      for ($i = 1$; $i \leq m$; $i{+}{+}$)
         for ($j = 1$; $j \leq n$; $j{+}{+}$) { **float** *abar*;
            $abar = (a[i-1][j-1] + a[i-1][j] + a[i-1][j+1] + a[i][j-1] +$
               $a[i][j] + a[i][j+1] + a[i+1][j-1] + a[i+1][j] + a[i+1][j+1])/9.0$;
            $a[i-1][j-1] = (a[i][j] - sharpening * abar)/(1.0 - sharpening)$;
         }
      for ($i = m$; $i > 0$; $i{-}{-}$)
         for ($j = n$; $j > 0$; $j{-}{-}$) $a[i][j] = (a[i-1][j-1] \leq 0.0 \,?\, 0.0 : a[i-1][j-1] \geq 1.0 \,?\, 1.0 : a[i-1][j-1])$;
   }

This code is used in section 15.

17*.   Here I'm assuming that n is a multiple of 4.

⟨ Forget this 17* ⟩ ≡
   for ($i = 1$; $i \leq m$; $i{+}{+}$) {
      printf ("row␣%d;␣data␣\"", *i*);
      for ($j = 1$; $j \leq n$; $j \mathrel{+}= 4$) {
         for ($k = 0, w = 0$; $k < 4$; $k{+}{+}$) $w = w + w + (aa[i][j+k] \equiv black \,?\, 1 : 0)$;
         printf ("%x", *w*);
      }
      printf ("\";\n");
   }

18*.   Here I'm writing an encapsulated PostScript file instead of a kludgy METAFONT file.

⟨ Spew out the answers 18* ⟩ ≡
   ⟨ Output the header of the EPS file 19* ⟩;
   ⟨ Output the image 20* ⟩;
   ⟨ Output the trailer of the EPS file 21* ⟩;

This code is used in section 1*.

19* ⟨ Output the header of the EPS file 19* ⟩ ≡
   $printf$ ("%%!PS\n");
   $printf$ ("%%%%BoundingBox:␣0␣0␣%d␣%d\n", (**int**)(.5 + n * 72.0/300.0), (**int**)(.5 + m * 72.0/300.0));
   $printf$ ("%%%%Creator:␣dot_diff-eps\n");
   $cur\_clock = time(0);$
   $printf$ ("%%%%CreationDate:␣%s", $ctime(\&cur\_clock)$);
   $printf$ ("%%%%Pages:␣1\n");
   $printf$ ("%%%%EndProlog\n");
   $printf$ ("%%%%Page:␣1␣1\n");
   $printf$ ("/picstr␣%d␣string␣def\n", $n \gg 3$);
   $printf$ ("72␣300␣div␣dup␣scale␣%d␣%d␣scale\n", n, m);
   $printf$ ("%d␣%d␣true␣[%d␣0␣0␣-%d␣0␣%d]\n", n, m, n, m, m);
   $printf$ ("␣{currentfile␣picstr␣readhexstring␣pop}␣imagemask\n");
This code is used in section 18*.

20* ⟨ Output the image 20* ⟩ ≡
   for $(i = 1; \ i \leq m; \ i{+}{+})$
     for $(j = 1; \ j \leq n; \ j \mathrel{+}= 4)$ {
       for $(k = 0, w = 0; \ k < 4; \ k{+}{+})$ $w = w + w + (aa[i][j + k] \equiv black \ ? \ 1 : 0);$
       $printf$ ("%x", w);
     }
This code is used in section 18*.

21* ⟨ Output the trailer of the EPS file 21* ⟩ ≡
   $printf$ ("%%%%EOF\n");
This code is used in section 18*.

22.* Index.

The following sections were changed by the change file: 1, 17, 18, 19, 20, 21, 22.

⟨ Check for nonstandard *zeta* and *sharpening* factors 2 ⟩   Used in section 1*.
⟨ Check the beginning lines of the input file 3 ⟩   Used in section 1*.
⟨ Choose pixel values and diffuse the errors in the buffer 7 ⟩   Used in section 15.
⟨ Compile "instructions" for the diffusion operations 14 ⟩   Used in section 10.
⟨ Decide the color of pixel $[i, j]$ and the resulting *err* 9 ⟩   Used in section 7.
⟨ Forget this 17* ⟩
⟨ Global variables 4, 8, 11 ⟩   Used in section 1*.
⟨ Initialize the class number matrix 13 ⟩   Used in section 10.
⟨ Initialize the diffusion tables 10 ⟩   Used in section 15.
⟨ Input rectangular pixel data 6 ⟩   Used in section 5.
⟨ Input the graphic data 5 ⟩   Used in section 1*.
⟨ Output the header of the EPS file 19* ⟩   Used in section 18*.
⟨ Output the image 20* ⟩   Used in section 18*.
⟨ Output the trailer of the EPS file 21* ⟩   Used in section 18*.
⟨ Sharpen the input 16 ⟩   Used in section 15.
⟨ Spew out the answers 18* ⟩   Used in section 1*.
⟨ Subroutines 12 ⟩   Used in section 1*.
⟨ Translate input to output 15 ⟩   Used in section 1*.

DOT-DIFF-EPS