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1. Intro. This program simply generates data for GDANCE to solve the problem of placing MacMahon's 24 triangles into a regular hexagon, as discussed in Martin Gardner in Chapter 16 of *Mathematical Magic Show*. But instead of making the outside edge a solid color, I'm trying for a solution with  $180^{\circ}$  symmetry when we map the colors  $a \leftrightarrow d$ ,  $b \leftrightarrow c$ .

And it should tile the plane too.

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char piece [24][4] = {{'a', 'a', 'a', 0}, {'d', 'd', 'd', 0}, {'b', 'b', 'b', 0}, {'c', 'c', 'c', 0}, {'a',
                'a', 'd', 0}, {'d', 'd', 'a', 0}, {'a', 'a', 'b', 0}, {'d', 'd', 'c', 0}, {'a', 'a', 'c', 0}, {'d', 'd',
                'b',0},{'b','b','c',0},{'c','c','d',0},{'b','b','c',0},{'c','c','b',0},{'b',0},{'b',0},
               0}, {'c', 'c', 'a', 0}, {'a', 'b', 'c', 0}, {'b', 'd', 'c', 0}, {'a', 'b', 'd', 0}, {'a', 'd', 'c', 0},
                {'a', 'c', 'd', 0}, {'a', 'd', 'b', 0}, {'a', 'c', 'b', 0}, {'b', 'c', 'd', 0}, };
     \mathbf{char} \ pos[36][4] = \{\{2,3,8,0\}, \{3,0,4,0\}, \{4,5,9,0\}, \{5,1,6,0\}, \{6,7,10,0\}, \{11,12,19,0\}, \{12,8,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, \{13,0,13,0\}, 
                \{13, 14, 20, 0\}, \{14, 9, 15, 0\}, \{15, 16, 21, 0\}, \{16, 10, 17, 0\}, \{17, 18, 22, 0\}, \};
     \mathbf{char} \ map[23] = \{0, 0, 11, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 7, 19, 20, 20, 19\};
     main()
          register int j, k;
          for (k = 12; k < 36; k++)
                pos[k][0] = pos[k-12][1], pos[k][1] = pos[k-12][2], pos[k][2] = pos[k-12][0];
           (Output the first line of dance data 3);
          for (j = 0; j < 24; j ++)
               for (k = 0; k < (j \ge 4 ? 36 : 12); k++) \langle Generate rows for piece j in position k 2 \rangle;
          \langle Generate rows for piece j in position k \mid 2 \rangle \equiv
     {
          printf("\%s_{\square}P\%02d", piece[j], k \% 12);
          if (map[pos[k][0]] \equiv pos[k][0]) printf (" \sqcup \%02d : \%c", pos[k][0], piece[j][0]);
          if (map[pos[k][1]] \equiv pos[k][1]) printf (" \cup \%02d : \%c", pos[k][1], piece[j][1]);
          if (map[pos[k][2]] \equiv pos[k][2]) printf (" \cup \%02d : \%c", pos[k][2], piece[j][2]);
          else printf(" " \%02d: \%c", map[pos[k][2]], `a' + 'd' - piece[j][2]);
          printf(" " ", piece[j \oplus 1]);
This code is used in section 1.
3. (Output the first line of dance data 3) \equiv
     for (j = 0; j < 24; j ++) printf("%s_{\( \)}", piece[j]);
     for (k = 0; k < 12; k++) printf("P%02d_{\perp}", k);
     printf("|");
     for (k = 0; k < 21; k++)
          if (k \neq 1 \land k \neq 2 \land k \neq 18) printf("\\\\\\\\\02d\\\,k);
     printf("\n");
This code is used in section 1.
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## 4. Index.

j:  $\underline{1}$ .  $k: \ 1.$   $main: \ 1.$   $map: \ 1, \ 2.$   $piece: \ 1, \ 2, \ 3.$   $pos: \ 1, \ 2.$   $printf: \ 2, \ 3.$   $\langle \, \text{Generate rows for piece} \, j \, \, \text{in position} \, k \, \, 2 \, \rangle \quad \text{Used in section 1.} \\ \langle \, \text{Output the first line of dance data} \, \, 3 \, \rangle \quad \text{Used in section 1.}$ 

## MACMAHON-TRIANGLES-SYM-TILE

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