1. Intro. This program computes the up-up-or-down-down permutation of $\{1, 2, \ldots, 2n-1\}$ that corresponds to a given $2 \times n$ whirlpool permutation. The latter permutation appears on the command line, as a permutation of $\{0, 1, \ldots, 2n-1\}$, with 0 in the bottom left corner.

(I've made no attempt to be efficient.)

(But I didn't go out of my way to be inefficient.)

(Apologies for doing this hurriedly.)

```
#define maxn 100
#include <stdio.h>
#include <stdlib.h>
  int a[2 * maxn];
  int used[2 * maxn];
  int answer[2 * maxn];
  main(int argc, char *argv[])
  {
    register int i, j, k, n, nn, t, saven;
    ⟨ Process the command line 2 ⟩;
    for ( ; n > 1; n--) ⟨ Reduce the problem from n to n − 1 4 ⟩;
    ⟨ Print the answer 5 ⟩;
  }
```

2. ⟨ Process the command line 2 ⟩ ≡

```
if (argc < 5 ∨ ((argc & 1) ≡ 0)) {
  fprintf(stderr, "Usage: %s a11 a12 ... a1n 0 a22 ... a2n\n", argv[0]);
  exit(−1);
}
nn = argc − 1, n = saven = nn/2;
if (n > maxn) {
  fprintf(stderr, "Recompile me: This program has maxn=%d!\n", maxn);
  exit(−99);
}
for (k = 0; k < nn; k++) {
  if (sscanf(argv[k + 1], "%d", &a[k]) ≠ 1) {
    fprintf(stderr, "Bad matrix entry '%s'!\n", argv[k + 1]);
    exit(−2);
  }
  if (a[k] < 0 ∨ a[k] ≥ nn) {
    fprintf(stderr, "Matrix entry '%d' out of range!\n", a[k]);
    exit(−3);
  }
  if (used[a[k]]) {
    fprintf(stderr, "Duplicate matrix entry '%d'!\n", a[k]);
    exit(−4);
  }
  used[a[k]] = 1;
}
if (a[n]) {
  fprintf(stderr, "Matrix entry a21 should be zero, not %d!\n", a[n]);
  exit(−5);
}
⟨ Verify the whirlpool criteria 3 ⟩;
```

This code is used in section 1.

3. ⟨ Verify the whirlpool criteria 3 ⟩ ≡

```
for (k = n + 1; k < nn; k++) {
  if ((((a[k − n − 1] < a[k − n]) + (a[k − n] < a[k]) + (a[k] < a[k − 1]) + (a[k − 1] < a[k − n − 1])) & 1) ≡ 0)
    {
    fprintf(stderr, "Not a vortex! (%d %d / %d %d)\n", a[k − n − 1], a[k − n], a[k − 1], a[k]);
    exit(−6);
  }
}
```

This code is used in section 2.

4. ⟨ Reduce the problem from n to $n-1$ 4 ⟩ ≡

```
{
  register int t, nnp;
  nnp = n + n - 2;
  answer[nnp + 1] = a[0], answer[nnp] = a[1];
  for (k = 1; k < n; k++) {
    t = a[k];
    if (t > answer[nnp + 1]) t--;
    a[k - 1] = t - 1;
    t = a[k + saven];
    if (t > answer[nnp + 1]) t--;
    a[k + saven - 1] = t - 1;
  }
  for (t = nnp - a[saven], k = 0; k < n - 1; k++) {
    a[k] = (a[k] + t) % nnp;
    a[k + saven] = (a[k + saven] + t) % nnp;
  }
}
```

This code is used in section 1.

5. At this point $n = 1$, and *answer* contains numbers that need to be "uncompressed" because they were the results of a recursive computation on a compressed problem.

⟨ Print the answer 5 ⟩ ≡

```
n = saven;
answer[1] = 1;
for (k = 0; k < nn; k++) used[k] = 0;
used[answer[nn - 1]] = used[answer[nn - 2]] = 1;
for (k = nn - 4; k ≥ 0; k -= 2) {
  t = answer[k + 1];
  for (j = 1; j ≤ t; j++)
    if (used[j]) t++;
  answer[k + 1] = t;
  t = answer[k];
  for (j = 1; j ≤ t; j++)
    if (used[j]) t++;
  answer[k] = t;
  used[t] = used[answer[k + 1]] = 1;
}
for (k = nn - 1; k; k--) printf("␣%d", answer[k]);
printf("\n");
```

This code is used in section 1.

6. Index.

⟨ Print the answer 5 ⟩ Used in section 1.
⟨ Process the command line 2 ⟩ Used in section 1.
⟨ Reduce the problem from n to $n-1$ 4 ⟩ Used in section 1.
⟨ Verify the whirlpool criteria 3 ⟩ Used in section 2.

WHIRLPOOL2N-ENCODE