§1 DOT-DIFF-EPS INTRODUCTION 1

(See https://cs.stanford.edu/~knuth/programs.html for date.)

1.* Introduction. This program prepares a METAFONT file for a special-purpose font that will approximate a given picture. The input file (stdin) is assumed to be an EPS file output by Adobe Photoshop TM on a Macintosh with the binary EPS option, containing m rows of n columns each; in Photoshop terminology the image is m pixels high and n pixels wide, in grayscale mode, with a resolution of 72 pixels per inch. The output file (stdout) will be a sequence of m lines like

```
row 10; data "d01...53";
```

this means that the pixel data for row 10 is the string of n bits 110100000001...01010011 encoded as a hexadecimal string of length n/4.

```
For simplicity, this program assumes that m = 512 and n = 440.
#define m 512
                       /* this many rows */
                      /* this many columns */
#define n 440
#include <stdio.h>
#include <time.h>
  time_t cur_clock;
  float a[m+2][n+2];
                              /* darknesses: 0.0 is white, 1.0 is black */
  ⟨Global variables 4⟩
  (Subroutines 12)
  main(argc, argv)
       int argc;
       char *argv[];
    register int i, j, k, l, ii, jj, w;
    register float err;
    float zeta = 0.2, sharpening = 0.9;
    \langle Check for nonstandard zeta and sharpening factors 2\rangle;
     (Check the beginning lines of the input file 3);
     \langle \text{Input the graphic data 5} \rangle;
      Translate input to output 15;
     \langle \text{Spew out the answers } 18^* \rangle;
```

2. Optional command-line arguments allow the user to change the zeta and/or sharpening parameters discussed below.

```
 \begin{split} &\langle \, \text{Check for nonstandard } \textit{zeta} \, \text{ and } \textit{sharpening factors } \, 2 \, \rangle \equiv \\ & \text{if } \, (\textit{argc} > 1 \land \textit{sscanf} \, (\textit{argv}[1], \text{"%g"}, \& \textit{zeta}) \equiv 1) \, \, \{ \\ & \textit{fprintf} \, (\textit{stderr}, \text{"Using}\_\text{zeta}\_=\_\%\text{g}^n, \textit{zeta}); \\ & \text{if } \, (\textit{argc} > 2 \land \textit{sscanf} \, (\textit{argv}[2], \text{"%g"}, \& \textit{sharpening}) \equiv 1) \\ & \textit{fprintf} \, (\textit{stderr}, \text{"}\_\square \text{and}\_\text{sharpening}\_\text{factor}\_\%\text{g}^n, \textit{sharpening}); \\ & \} \end{split}  This code is used in section 1*.
```

}

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3. Macintosh conventions indicate the end of a line by the ASCII \langle carriage return \rangle character (i.e., control-M, aka \backslash r), but the C library is set up to work best with newlines (i.e., control-J, aka \backslash n). We aren't worried about efficiency, so we simply input one character at a time. This program assumes Macintosh conventions.

The job here is to look for the sequence Box: in the input, followed by 0, 0, the number of columns, and the number of rows.

```
\#define panic(s)
           \textit{fprintf}\,(\textit{stderr}\,,s);\ \textit{exit}\,(-1);
\langle Check the beginning lines of the input file _3\rangle \equiv
  k=0;
scan:
  if (k ++ > 1000) panic ("Couldn't find the bounding box info! \n");
  if (getchar() \neq 'B') goto scan;
  if (getchar() \neq \circ) goto scan;
  if (getchar() \neq 'x') goto scan;
  if (getchar() \neq ':') goto scan;
  panic("Bad_{\sqcup}bounding_{\sqcup}box_{\sqcup}data!\n");
  if (urx \neq n \lor ury \neq m) panic("The_image_idoesn', t_have_the_icorrect_iwidth_and_height!\n");
This code is used in section 1*.
4. \langle Global variables 4\rangle \equiv
                            /* bounding box parameters */
  int llx, lly, urx, ury;
See also sections 8 and 11.
This code is used in section 1*.
```

5. After we've seen the bounding box, we look for beginimage\r; this will be followed by the pixel data, one character per byte.

```
\langle \text{Input the graphic data 5} \rangle \equiv
  k=0;
skan:
  if (k ++ > 10000) panic("Couldn't_ifind_ithe_pixel_idata!\n");
  if (qetchar() \neq 'b') goto skan;
  if (getchar() \neq 'e') goto skan;
  if (getchar() ≠ 'g') goto skan;
  if (getchar() \neq 'i') goto skan;
  if (getchar() \neq 'n') goto skan;
  if (getchar() \neq 'i') goto skan;
  if (getchar() \neq 'm') goto skan;
  if (getchar() \neq 'a') goto skan;
  if (getchar() \neq 'g') goto skan;
  if (getchar() \neq 'e') goto skan;
  if (getchar() \neq '\r') goto skan;
  ⟨Input rectangular pixel data 6⟩;
  if (getchar() \neq '\r') panic("Wrong_amount_of_pixel_data!\n");
This code is used in section 1^*.
```

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6. Photoshop follows the conventions of photographers who consider 0 to be black and 1 to be white; but we follow the conventions of computer scientists who tend to regard 0 as devoid of ink (white) and 1 as full of ink (black).

We use the fact that global arrays are initially zero to assume that there are all-white rows of 0s above, below, and to the left and right of the input data.

```
\langle Input rectangular pixel data 6 \rangle \equiv for (i=1; i \leq ury; i++) for (j=1; j \leq urx; j++) a[i][j] = 1.0 - getchar()/255.0; This code is used in section 5.
```

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7. Dot diffusion. Our job is to go from eight-bit pixels to one-bit pixels; that is, from 256 shades of gray to an approximation that uses only black and white. The method used here is called *dot diffusion* (see [D. E. Knuth, "Digital halftones by dot diffusion," *ACM Transactions on Graphics* 6 (1987), 245–273]); it works as follows: The pixels are divided into 64 classes, numbered from 0 to 63. We convert the pixel values to 0s and 1s by assigning values first to all the pixels of class 0, then to all the pixels of class 1, etc. The error incurred at each step is distributed to the neighbors whose class numbers are higher. This is done by means of precomputed tables *class_row*, *class_col*, *start*, *del_i*, *del_j*, and *alpha* whose function is easy to deduce from the following code segment.

```
 \begin{array}{l} \langle \mbox{ Choose pixel values and diffuse the errors in the buffer } \mathbf{7} \rangle \equiv \\ \mbox{ for } (k=0; \ k<64; \ k++) \\ \mbox{ for } (i=class\_row[k]; \ i\leq m; \ i+=8) \\ \mbox{ for } (j=class\_col[k]; \ j\leq n; \ j+=8) \ \{ \\ \mbox{ } \langle \mbox{ Decide the color of pixel } [i,j] \mbox{ and the resulting } err \ 9 \rangle; \\ \mbox{ for } (l=start[k]; \ l<start[k+1]; \ l++) \ a[i+del\_i[l]][j+del\_j[l]] +=err*alpha[l]; \\ \mbox{ } \} \end{array}
```

This code is used in section 15.

8. We will use the following model for estimating the effect of a given bit pattern in the output: If a pixel is black, its darkness is 1.0; if it is white but at least one of its four neighbors is black, its darkness is zeta; if it is white and has four white neighbors, its darkness is 0.0. Laserprinters of the 1980s tended to spatter toner in a way that could be approximated roughly by taking zeta = 0.2 in this model. The value of zeta should be between -0.25 and +1.0.

An auxiliary array aa holds code values white, gray, or black to facilitate computations in this model. All cells are initially white; but when we decide to make a pixel black, we change its white neighbors (if any) to gray.

```
#define white 0 /* code for a white pixel with all white neighbors */
#define gray 1 /* code for a white pixel with 1, 2, 3, or 4 black neighbors */
#define black 2 /* code for a black pixel */
$$ Global variables 4$ \rightarrow \equiv \text{white, gray, or black status of final pixels */}$$
```

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9. In this step the current pixel's final one-bit value is determined. It presently is either *white* or *gray*; we either leave it as is, or we blacken it and gray its white neighbors, whichever minimizes the magnitude of the error.

Potentially gray values near the newly chosen pixel make this calculation slightly tricky. Notice, for example, that the very first black pixel to be created will increase the local darkness of the image by 1+4zeta. Suppose the original image is entirely black, so that a[i][j] is 1.0 for $1 \le i \le m$ and $1 \le j \le n$. If a pixel of class 0 is set to white, the error (i.e., the darkness that needs to be diffused to its upperclass neighbors) is 1.0; but if it is set to black, the error is -4zeta. The algorithm will choose black unless $zeta \ge .25$.

```
(Decide the color of pixel [i, j] and the resulting err \ 9) \equiv
  if (aa[i][j] \equiv white) \ err = a[i][j] - 1.0 - 4 * zeta;
             /* aa[i][j] \equiv gray */
     err = a[i][j] - 1.0 + zeta;
      \textbf{if} \ (aa[i-1][j] \equiv white) \ err \ -= zeta; \\
     if (aa[i+1][j] \equiv white) err -= zeta;
     if (aa[i][j-1] \equiv white) err = zeta;
     if (aa[i][j+1] \equiv white) err -= zeta;
  if (err + a[i][j] > 0) { /* black is better */
     aa[i][j] = black;
     if (aa[i-1][j] \equiv white) aa[i-1][j] = gray;
     if (aa[i+1][j] \equiv white) aa[i+1][j] = gray;
     \textbf{if } (aa[i][j-1] \equiv white) \ aa[i][j-1] = gray;
     if (aa[i][j+1] \equiv white) aa[i][j+1] = gray;
  else err = a[i][j];
                            /* keep it white or gray */
This code is used in section 7.
```

6

10. Computing the diffusion tables. The tables for dot diffusion could be specified by a large number of boring assignment statements, but it is more fun to compute them by a method that reveals some of the mysterious underlying structure.

```
\langle Initialize the diffusion tables 10 \rangle \equiv
  (Initialize the class number matrix 13);
  (Compile "instructions" for the diffusion operations 14);
This code is used in section 15.
11. \langle \text{Global variables 4} \rangle + \equiv
  char class_row [64], class_col [64];
                                           /* first row and column for a given class */
  char class\_number[10][10];
                                     /* the number of a given position */
  int kk = 0;
                    /* how many classes have been done so far */
  int start [65];
                      /* the first instruction for a given class */
  int del_i[256], del_j[256];
                                  /* relative location of a neighbor */
  float alpha[256];
                       /* diffusion coefficient for a neighbor */
```

12. The order of classes used here is the order in which pixels might be blackened in a font for halftones based on dots in a 45° grid. In fact, it is precisely the pattern used in the font ddith300, discussed in the author's paper "Fonts for Digital Halftones" [Chapter 21 of Selected Papers on Digital Typography].

```
 \begin{array}{l} \text{ void } store(i,j) \\ & \text{ int } i,j; \\ \{ \\ & \text{ if } (i<1) \ i+=8; \ \text{else if } (i>8) \ i-=8; \\ & \text{ if } (j<1) \ j+=8; \ \text{else if } (j>8) \ j-=8; \\ & class\_number[i][j] = kk; \\ & class\_row[kk] = i; \ class\_col[kk] = j; \\ & kk++; \\ \} \\ & \text{ void } store\_eight(i,j) \\ & \text{ int } i,j; \\ \{ \\ & store(i,j); \ store(i-4,j+4); \ store(1-j,i-4); \ store(5-j,i); \\ & store(j,5-i); \ store(4+j,1-i); \ store(5-i,5-j); \ store(1-i,1-j); \\ \} \\ \end{array}
```

This code is used in section 1^* .

13. \langle Initialize the class number matrix $13 \rangle \equiv store_eight(7,2); store_eight(8,3); store_eight(8,2); store_eight(8,1); store_eight(1,4); store_eight(1,3); store_eight(1,2); store_eight(2,3);$ for $(i=1;\ i\leq 8;\ i++)\ class_number[i][0]=class_number[i][8], class_number[i][9]=class_number[i][1];$ for $(j=0;\ j\leq 9;\ j++)\ class_number[0][j]=class_number[8][j], class_number[9][j]=class_number[1][j];$ This code is used in section 10.

14. The "compilation" in this step simulates going through the diffusion process the slow way, recording the actions it performs. Then those actions can all be done at high speed later.

```
\langle Compile "instructions" for the diffusion operations 14\rangle \equiv
  for (k = 0, l = 0; k < 64; k++)
                       /\!*\ l is the number of instructions compiled so far */
     start[k] = l;
     i = class\_row[k]; j = class\_col[k]; w = 0;
     for (ii = i - 1; ii \le i + 1; ii ++)
       for (jj = j - 1; jj \le j + 1; jj ++)
          if (class\_number[ii][jj] > k) {
             del_{-}i[l] = ii - i; \ del_{-}j[l] = jj - j; \ l++;
            if (ii \neq i \land jj \neq j) w++; /* diagonal neighbors get weight 1 */
            else w += 2; /* orthogonal neighbors get weight 2 */
     for (jj = start[k]; jj < l; jj \leftrightarrow)
       if (del_{-}i[jj] \neq 0 \land del_{-}j[jj] \neq 0) alpha[jj] = 1.0/w;
       else alpha[jj] = 2.0/w;
                     /* at this point l will be 256 */
  start[64] = l;
This code is used in section 10.
```

8 SYNTHESIS DOT-DIFF-EPS §15

15. Synthesis. Now we're ready to put the pieces together.

```
⟨Translate input to output 15⟩ ≡
⟨Initialize the diffusion tables 10⟩;
if (sharpening) ⟨Sharpen the input 16⟩;
⟨Choose pixel values and diffuse the errors in the buffer 7⟩;
This code is used in section 1*.
```

16. Experience shows that dot diffusion often does a better job if we apply a filtering operation that exaggerates the differences between the intensities of a pixel and its neighbors:

$$a_{ij} \leftarrow \frac{a_{ij} - \alpha \bar{a}_{ij}}{1 - \alpha},$$

where $\bar{a}_{ij} = \frac{1}{9} \sum_{\delta=-1}^{+1} \sum_{\epsilon=-1}^{+1} a_{(i+\delta)(j+\epsilon)}$ is the average value of a_{ij} and its eight neighbors. (See the discussion in the Transactions on Graphics paper cited earlier. The parameter α is the sharpening value, which must obviously be less than 1.0.)

We could use a buffering scheme to apply this transformation in place, but it's easier to store the new value of a_{ij} in $a_{(i-1)(j-1)}$ and then shift everything back into position afterwards. The values of a_{i0} and a_{0j} don't have to be restored to zero after this step, because they will not be examined again.

```
 \begin{cases} \text{for } (i=1;\ i\leq m;\ i++) \\ \text{for } (j=1;\ j\leq n;\ j++) \end{cases} \text{ float } abar; \\ abar = (a[i-1][j-1]+a[i-1][j]+a[i-1][j+1]+a[i][j-1]+\\ a[i][j]+a[i][j+1]+a[i+1][j-1]+a[i+1][j]+a[i+1][j+1])/9.0; \\ a[i-1][j-1] = (a[i][j]-sharpening*abar)/(1.0-sharpening); \\ \} \\ \text{for } (i=m;\ i>0;\ i--) \\ \text{for } (j=n;\ j>0;\ j--)\ a[i][j] = (a[i-1][j-1]\leq 0.0\ ?\ 0.0: a[i-1][j-1]\geq 1.0\ ?\ 1.0: a[i-1][j-1]); \\ \} \\ \text{This code is used in section 15.}
```

17.* Here I'm assuming that n is a multiple of 4.

```
 \begin{split} &\langle \text{Forget this } 17^* \rangle \equiv \\ & \textbf{for } (i=1; \ i \leq m; \ i++) \ \ \{ \\ & \ printf(\texttt{"row} \_ \% \texttt{d}; \_ \texttt{data} \_ \backslash \texttt{""}, i); \\ & \textbf{for } (j=1; \ j \leq n; \ j+=4) \ \ \{ \\ & \ \textbf{for } (k=0, w=0; \ k < 4; \ k++) \ \ w = w + w + (aa[i][j+k] \equiv black \ ? \ 1:0); \\ & \ printf(\texttt{"}\%x\texttt{"}, w); \\ & \ \} \\ & \ printf(\texttt{"}\\texttt{"}, \texttt{"}); \\ & \ \} \end{split}
```

18.* Here I'm writing an encapsulated PostScript file instead of a kludgy METAFONT file.

```
\langle Spew out the answers 18^*\rangle \equiv \langle Output the header of the EPS file 19^*\rangle; \langle Output the image 20^*\rangle; \langle Output the trailer of the EPS file 21^*\rangle; This code is used in section 1^*.
```

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```
19* \langle Output the header of the EPS file 19*\rangle \equiv
  printf("%%!PS\n");
  printf("%%%BoundingBox: 0.0.0.%d\n", (int)(.5 + n * 72.0/300.0), (int)(.5 + m * 72.0/300.0));
  printf("%%%Creator:_dot_diff-eps\n");
  cur\_clock = time(0);
  printf("\%\%CreationDate: \ \ \ \ \ \ \ ctime(\&cur\_clock));
  printf("\%\%\%Pages: 1\n");
  printf("%%%%EndProlog\n");
  printf("\%\%\%Page: l1l1\n");
  printf("/picstr_{\square}%d_{\square}string_{\square}def\n", n \gg 3);
  printf("72 \cup 300 \cup div_{\cup}dup_{\cup}scale_{\cup}%d_{\cup}%d_{\cup}scale_{n}", n, m);
  printf("%d_{\sqcup}%d_{\sqcup}true_{\sqcup}[%d_{\sqcup}0_{\sqcup}0_{\sqcup}-%d_{\sqcup}0_{\sqcup}%d] \n", n, m, n, m, m);
  printf("u{currentfileupicstrureadhexstringupop}uimagemask\n");
This code is used in section 18*.
20* \langle \text{Output the image } 20^* \rangle \equiv
  for (i = 1; i \le m; i++)
     for (j = 1; j \le n; j += 4) {
        for (k = 0, w = 0; k < 4; k++) w = w + w + (aa[i][j + k] \equiv black ? 1 : 0);
        printf("%x", w);
This code is used in section 18*.
21* \(\right\) Output the trailer of the EPS file 21^*\\ \(\text{\in}\)
  printf("%%%%EOF\n");
This code is used in section 18*.
```

10 INDEX DOT-DIFF-EPS §22

22* Index.

The following sections were changed by the change file: 1, 17, 18, 19, 20, 21, 22. a: <u>1</u>* *aa*: <u>8, 9, 17*, 20*</u> abar: 16.alpha: 7, $\underline{11}$, 14. $argc: \underline{1}, \underline{2}.$ argv: $\underline{1}^*$, 2. black: 8, 9, 17, 20* $class_col$: 7, $\underline{11}$, 12, 14. class_number: <u>11</u>, 12, 13, 14. $class_row\colon \ \ 7,\ \underline{11},\ 12,\ 14.$ ctime: 19.* *cur_clock*: 1* 19* $\textit{del_i}\colon \ \ 7, \ \underline{11}, \ 14.$ $del_{-}j$: 7, <u>11</u>, 14. err: 1^* , 7, 9. exit: 3. fprintf: 2, 3.getchar: 3, 5, 6.gray: 8, 9. $i: \quad \underline{1}, \quad \underline{12}.$ $ii: \ \underline{1}^*, \ 14.$ $j: 1^*, 12.$ $jj: 1^*, 14.$ k: <u>1</u>* kk: 11, 12.*l*: 1* $llx: 3, \underline{4}.$ lly: $\frac{1}{3}$, $\frac{1}{4}$. $m: \underline{1}^*$ $main: \underline{1}^*$ n: <u>1</u>* panic: $\underline{3}$, $\underline{5}$. printf: 17,* 19,* 20,* 21.* $scan: \underline{3}.$ scan f: 3.sharpening: $\underline{1}$, $\underline{2}$, $\underline{15}$, $\underline{16}$. $skan: \underline{5}.$ sscanf: 2.start: 7, <u>11</u>, 14. stderr: 2, 3.stdin: 1.*stdout: 1* store: $\underline{12}$. $store_eight: \underline{12}, \underline{13}.$ time: 19* $urx: 3, \underline{4}, 6.$ $ury: 3, \underline{4}, 6.$ $w: \underline{1}^*$ white: 8, 9. zeta: 1^* , 2, 8, 9.

DOT-DIFF-EPS NAMES OF THE SECTIONS 11

```
\langle Check for nonstandard zeta and sharpening factors 2\rangle Used in section 1*.
(Check the beginning lines of the input file 3) Used in section 1*.
(Choose pixel values and diffuse the errors in the buffer 7) Used in section 15.
Compile "instructions" for the diffusion operations 14 \( \) Used in section 10.
Decide the color of pixel [i, j] and the resulting err \ 9 Used in section 7.
(Forget this 17*)
Global variables 4, 8, 11 Used in section 1^*.
(Initialize the class number matrix 13) Used in section 10.
\langle Initialize the diffusion tables 10 \rangle Used in section 15.
(Input rectangular pixel data 6) Used in section 5.
(Input the graphic data 5) Used in section 1*.
Output the header of the EPS file 19* Used in section 18*.
(Output the image 20^*) Used in section 18^*.
Output the trailer of the EPS file 21* Used in section 18*.
\langle \text{Sharpen the input 16} \rangle Used in section 15.
\langle Spew out the answers 18^* \rangle Used in section 1^*.
\langle Subroutines 12\rangle Used in section 1*.
(Translate input to output 15) Used in section 1*.
```

DOT-DIFF-EPS

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