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(Downloaded from https://cs.stanford.edu/~knuth/programs.html and typeset on May 28, 2023)

1.\* Intro. This program generates clauses for the transition relation from time 0 to time r in Conway's Game of Life (thus simulating r steps), on an  $m \times n$  grid, given m, n, and r. The live cells are constrained to remain in this grid, and the configuration at time r is constrained to be exactly the same as it was at time 0.

Furthermore the entire grid isn't dead.

The Boolean variable for cell (x, y) at time t is named by its so-called "xty code," namely by the decimal value of x, followed by a code letter for t, followed by the decimal value of y. For example, if x = 10 and y = 11 and t = 0, the variable that indicates liveness of the cell is 10a11; and the corresponding variable for t = 1 is 10b11.

Up to 19 auxiliary variables are used together with each xty code, in order to construct clauses that define the successor state. The names of these variables are obtained by appending one of the following two-character combinations to the xty code: A2, A3, A4, B1, B2, B3, B4, C1, C2, C3, C4, D1, D2, E1, E2, F1, F2, G1, G2. These variables are derived from the Bailleux-Boufkhad method of encoding cardinality constraints: The auxiliary variable Ak stands for the condition "at least k of the eight neighbors are alive." Similarly, Bk stands for "at least k of the first four neighbors are alive," and Ck accounts for the other four neighbors. Codes Ck0, Ck1, Ck2, Ck3, Ck4, Ck3, Ck4, Ck5, Ck5, Ck6, Ck6, Ck6, Ck8, Ck8, Ck8, Ck8, Ck9, Ck

Those auxiliary variables receive values by means of up to 77 clauses per cell. For example, if u and v are the neighbors of cell z that correspond to a pairing of type D, there are six clauses

$$\bar{u}d_1$$
,  $\bar{v}d_1$ ,  $\bar{u}\bar{v}d_2$ ,  $uv\bar{d}_1$ ,  $u\bar{d}_2$ ,  $v\bar{d}_2$ .

The sixteen clauses

$$ar{d}_1b_1$$
,  $ar{e}_1b_1$ ,  $ar{d}_2b_2$ ,  $ar{d}_1ar{e}_1b_2$ ,  $ar{e}_2b_2$ ,  $ar{d}_2ar{e}_1b_3$ ,  $ar{d}_1ar{e}_2b_3$ ,  $ar{d}_2ar{e}_2b_4$ ,  $d_1e_1ar{b}_1$ ,  $d_1e_2ar{b}_2$ ,  $d_2e_1ar{b}_2$ ,  $d_1ar{b}_3$ ,  $d_2e_2ar{b}_3$ ,  $e_1ar{b}_3$ ,  $d_2ar{b}_4$ ,  $e_2ar{b}_4$ 

define b variables from d's and e's; and another sixteen define c's from f's and g's in the same fashion. A similar set of 21 clauses will define the a's from the b's and c's.

Once the a's are defined, thus essentially counting the live neighbors of cell z, the next state z' is defined by five further clauses

$$\bar{a}_4\bar{z}', \quad a_2\bar{z}', \quad a_3z\bar{z}', \quad \bar{a}_3a_4z', \quad \bar{a}_2a_4\bar{z}z'.$$

For example, the last of these states that z' will be true (i.e., that cell z will be alive at time t+1) if z is alive at time t and has  $\geq 2$  live neighbors but not  $\geq 4$ .

Nearby cells can share auxiliary variables, according to a tricky scheme that is worked out below. In consequence, the actual number of auxiliary variables and clauses per cell is reduced from 19 and 77 + 5 to 13 and 57 + 5, respectively, except at the boundaries.

So here's the overall outline of the program. #define maxx 50 /\* maximum number of lines in the pattern supplied by stdin \*/ #define maxy 50 /\* maximum number of columns per line in stdin \*/ #include <stdio.h> #include <stdlib.h> char p[maxx + 2][maxy + 2];/\* is cell (x, y) potentially alive? \*/ **char**  $have_b[maxx + 2][maxy + 2];$ /\* did we already generate b(x,y)? \*/ /\* did we already generate d(x,y)? \*/ char  $have_{-}d[maxx + 2][maxy + 2];$ **char**  $have_{-}e[maxx + 2][maxy + 4];$ /\* did we already generate e(x,y)? \*/ /\* did we already generate f(x-2,y)? \*/ char  $have_{-}f[maxx + 4][maxy + 2];$ /\* the time being considered \*/ int tt; int mm, nn, r; /\* the command-line parameters \*/ int xmax, ymax; /\* the number of rows and columns in the input pattern \*/ int xmin = maxx, ymin = maxy;/\* limits in the other direction \*/  $char \ timecode[] = "abcdefghijklmnopqrstuvwxyz"$ "ABCDEFGHIJKLMNOPQRSTUVWXYZ" "!\"#\$%&'()\*+,-./:;<=>?@[\\]^\_'{|}~"; /\* codes for  $0 \le t \le 83 */$ **char** buf[maxy + 2]; /\* input buffer \*/ unsigned int clause [4]; /\* clauses are assembled here \*/ /\* this many literals are in the current clause \*/ int clauseptr; ⟨Subroutines 6\*⟩  $main(\mathbf{int} \ argc, \mathbf{char} * argv[])$ register int j, k, x, y;  $\langle \text{Process the command line } 3^* \rangle$ ;  $\langle$  Avoid an all-dead grid  $16^*\rangle$ : for (tt = 0; tt < r; tt +++) { ymax = nn, ymin = 1;xmax = mm, xmin = 1;for  $(x = xmin - 1; x \le xmax + 1; x++)$ for  $(y = ymin - 1; y \le ymax + 1; y++)$  {  $\langle \text{ If cell } (x,y) \text{ is obviously dead at time } t+1, \text{ continue } 5^* \rangle;$ a(x,y); zprime(x, y);if  $(pp(x,y) \equiv 0)$  printf("~%d%c%d\n", x, timecode[(tt + 1) % r], y); /\* keep the configuration caged \*/  $\langle \text{Rule out smaller periods } 17^* \rangle;$  $\langle \text{Process the command line } 3^* \rangle \equiv$ if  $(argc \neq 4 \lor sscanf(argv[1], "%d", \&mm) \neq 1 \lor sscanf(argv[2], "%d", \&nn) \neq 1 \lor sscanf(argv[3], "%d", \&nn) \Rightarrow 1 \lor sscanf(argv[3],$  $\&r) \neq 1)$  { fprintf(stderr, "Usage: "%s m n n r n", argv[0]);exit(-1);  $printf("\"\sat-life-grid-cycle_\%d_\%d_\%d\n", mm, nn, r);$ This code is used in section 2\*.

 $\S4$  SAT-LIFE-GRID-CYCLE INTRO 3

```
4. \langle \text{Input the pattern 4} \rangle \equiv
      for (x = 1; ; x++) {
            if (\neg fgets(buf, maxy + 2, stdin)) break;
             if (x > maxx) {
                    fprintf(stderr, "Sorry, \_the\_pattern\_should\_have\_at\_most\_%d\_rows! \n", maxx);
             for (y = 1; buf[y - 1] \neq '\n'; y++)  {
                    if (y > maxy) {
                          fprintf(stderr, "Sorry, \bot the \_pattern \_should \_have \_at \_most \_%d \_columns! \n", maxy);
                           exit(-4);
                    if (buf[y-1] \equiv "") {
                          p[x][y] = 1;
                          if (y > ymax) ymax = y;
                          if (y < ymin) ymin = y;
                          if (x > xmax) xmax = x;
                          if (x < xmin) xmin = x;
                    } else if (buf[y-1] \neq '.') {
                          fprintf(stderr, "Unexpected_character_''%c'_found_in_the_pattern!\\n", buf[y-1]);
                          exit(-5);
                    }
             }
5* #define pp(xx, yy) (((xx) < xmin \vee (yy) < ymin \vee (xx) > xmax \vee (yy) > ymax) ? 0:1)
(If cell (x, y) is obviously dead at time t + 1, continue 5^*)
      if (pp(x-1,y-1)+pp(x-1,y)+pp(x-1,y+1)+pp(x,y-1)+pp(x,y)+pp(x,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1)+pp(x+1,y+1
                           (y-1) + pp(x+1,y) + pp(x+1,y+1) < 3) continue;
This code is used in section 2*.
```

**6.\*** Clauses are assembled in the *clause* array (surprise), where we put encoded literals.

The code for a literal is an unsigned 32-bit quantity, where the leading bit is 1 if the literal should be complemented. The next three bits specify the type of the literal (0 thru 7 for plain and A-G); the next three bits specify an integer k; and the next bit is zero. That leaves room for two 12-bit fields, which specify x and y.

Type 0 literals have k=0 for the ordinary xty code. However, the value k=1 indicates that the time code should be for t+1 instead of t. And k=2 denotes a special "tautology" literal, which is always true. If the tautology literal is complemented, we omit it from the clause; otherwise we omit the entire clause. Finally, k=7 denotes an auxiliary literal, used to avoid clauses of length 4.

Here's a subroutine that outputs the current clause and resets the *clause* array.

```
#define taut (2 \ll 25)
#define sign (1_{\rm U} \ll 31)
\langle \text{Subroutines } 6^* \rangle \equiv
  void outclause(void)
     register int c, k, x, y, p;
     for (p = 0; p < clauseptr; p++)
       if (clause[p] \equiv taut) goto done;
     for (p = 0; p < clauseptr; p \leftrightarrow)
       if (clause[p] \neq taut + sign) {
          if (clause[p] \gg 31) printf("\square"); else printf("\square");
          c = (clause[p] \gg 28) \& #7;
          k = (clause[p] \gg 25) \& #7;
          x = (clause[p] \gg 12) \& #fff;
          y = clause[p] \& #fff;
          if (c) printf("%d%c%d%c%d", x, timecode[tt], y, c + '@', k);
          else if (k \equiv 7) printf ("%d%c%dx", x, timecode [tt], y);
          else printf("%d%c%d", x, timecode[(tt + k) \% r], y);
     printf("\n");
  done: clauseptr = 0;
See also sections 7*, 8, 9, 10, 11, 12, 14, and 15.
This code is used in section 2*.
    And here's another, which puts a type-0 literal into clause.
\langle Subroutines 6*\rangle + \equiv
  void applit(int x, int y, int bar, int k)
     if (k \equiv 0 \land pp(x,y) \equiv 0) clause [clauseptr++] = (bar ? 0 : sign) + taut;
     else clause[clauseptr ++] = (bar ? sign : 0) + (k \ll 25) + (x \ll 12) + y;
```

§8 SAT-LIFE-GRID-CYCLE INTRO 5

8. The d and e subroutines are called for only one-fourth of all cell addresses (x, y). Indeed, one can show that x is always odd, and that  $y \mod 4 < 2$ .

```
Therefore we remember if we've seen (x, y) before.
```

```
Slight trick: If yy is not in range, we avoid generating the clause d_k twice.
```

```
#define newlit(x, y, c, k) clause[clauseptr ++] = ((c) \ll 28) + ((k) \ll 25) + ((x) \ll 12) + (y)
#define newcomplit(x, y, c, k) clause[clauseptr ++] = sign + ((c) \ll 28) + ((k) \ll 25) + ((x) \ll 12) + (y)
\langle \text{Subroutines } 6^* \rangle + \equiv
  void d(\mathbf{int} \ x, \mathbf{int} \ y)
     register x1 = x - 1, x2 = x, yy = y + 1;
     if (have_{-}d[x][y] \neq tt + 1) {
        applit(x1, yy, 1, 0), newlit(x, y, 4, 1), outclause();
        applit(x2, yy, 1, 0), newlit(x, y, 4, 1), outclause();
        applit(x1, yy, 1, 0), applit(x2, yy, 1, 0), newlit(x, y, 4, 2), outclause();
        applit(x1, yy, 0, 0), applit(x2, yy, 0, 0), newcomplit(x, y, 4, 1), outclause();
        applit(x1, yy, 0, 0), newcomplit(x, y, 4, 2), outclause();
       if (yy \ge ymin \land yy \le ymax) applit (x^2, yy, 0, 0), newcomplit (x, y, 4, 2), outclause ();
       have_{-}d[x][y] = tt + 1;
     }
  }
  void e(\mathbf{int} \ x, \mathbf{int} \ y)
     register x1 = x - 1, x2 = x, yy = y - 1;
     if (have_{-}e[x][y] \neq tt + 1) {
        applit(x1, yy, 1, 0), newlit(x, y, 5, 1), outclause();
        applit(x2, yy, 1, 0), newlit(x, y, 5, 1), outclause();
        applit(x1, yy, 1, 0), applit(x2, yy, 1, 0), newlit(x, y, 5, 2), outclause();
        applit(x1, yy, 0, 0), applit(x2, yy, 0, 0), newcomplit(x, y, 5, 1), outclause();
        applit(x1, yy, 0, 0), newcomplit(x, y, 5, 2), outclause();
       if (yy \ge ymin \land yy \le ymax) applit (x2, yy, 0, 0), newcomplit (x, y, 5, 2), outclause ();
        have_{-}e[x][y] = tt + 1;
  }
```

**9.** The f subroutine can't be shared quite so often. But we do save a factor of 2, because x + y is always even.

```
 \begin{array}{l} \text{Void } f(\textbf{int } x, \textbf{int } y) \\ \{ \\ \textbf{register } xx = x - 1, \ y1 = y, \ y2 = y + 1; \\ \textbf{if } (have\_f[x][y] \neq tt + 1) \ \{ \\ applit(xx, y1, 1, 0), newlit(x, y, 6, 1), outclause(); \\ applit(xx, y2, 1, 0), newlit(x, y, 6, 1), outclause(); \\ applit(xx, y1, 1, 0), applit(xx, y2, 1, 0), newlit(x, y, 6, 2), outclause(); \\ applit(xx, y1, 0, 0), applit(xx, y2, 0, 0), newcomplit(x, y, 6, 1), outclause(); \\ applit(xx, y1, 0, 0), newcomplit(x, y, 6, 2), outclause(); \\ applit(xx, y1, 0, 0), newcomplit(x, y, 6, 2), outclause(); \\ if (xx \geq xmin \land xx \leq xmax) \ applit(xx, y2, 0, 0), newcomplit(x, y, 6, 2), outclause(); \\ have\_f[x][y] = tt + 1; \\ \} \\ \} \end{array}
```

10. The g subroutine cleans up the dregs, by somewhat tediously locating the two neighbors that weren't handled by d, e, or f. No sharing is possible here.

```
 \begin{array}{l} & \text{ void } g(\textbf{int } x, \textbf{int } y) \\ \{ & \text{ register } x1, \ x2, \ y1, \ y2; \\ & \textbf{ if } (x \& 1) \ x1 = x - 1, y1 = y, x2 = x + 1, y2 = y \oplus 1; \\ & \textbf{ else } \ x1 = x + 1, y1 = y, x2 = x - 1, y2 = y - 1 + ((y \& 1) \ll 1); \\ & applit(x1, y1, 1, 0), newlit(x, y, 7, 1), outclause(); \\ & applit(x2, y2, 1, 0), newlit(x, y, 7, 1), outclause(); \\ & applit(x1, y1, 1, 0), applit(x2, y2, 1, 0), newlit(x, y, 7, 2), outclause(); \\ & applit(x1, y1, 0, 0), applit(x2, y2, 0, 0), newcomplit(x, y, 7, 1), outclause(); \\ & applit(x2, y2, 0, 0), newcomplit(x, y, 7, 2), outclause(); \\ & applit(x2, y2, 0, 0), newcomplit(x, y, 7, 2), outclause(); \\ \} \end{array}
```

11. Fortunately the b subroutine can be shared (since x is always odd), thus saving half of the sixteen clauses generated.

```
 \begin{array}{l} \text{Void } b(\text{int } x, \text{int } y) \\ \{ \\ \text{register } j, \ k, \ xx = x, \ y1 = y - (y \& 2), \ y2 = y + (y \& 2); \\ \text{if } (have\_b[x][y] \neq tt + 1) \ \{ \\ d(xx,y1); \\ e(xx,y2); \\ \text{for } (j=0; \ j < 3; \ j++) \\ \text{for } (k=0; \ k < 3; \ k++) \\ \text{if } (j) \ newcomplit(xx,y1,4,j); \ \ /* \ \bar{d}_j \ */ \\ \text{if } (k) \ newcomplit(xx,y2,5,k); \ \ /* \ \bar{e}_k \ */ \\ newlit(x,y,2,j+k); \ \ /* \ b_{j+k} \ */ \\ outclause(); \\ \text{if } (j) \ newlit(xx,y2,5,3-k); \ \ /* \ d_{3-j} \ */ \\ \text{if } (k) \ newlit(xx,y2,5,3-k); \ \ /* \ \bar{b}_{5-j-k} \ */ \\ outclause(); \\ \} \\ newcomplit(x,y,2,5-j-k); \ \ /* \ \bar{b}_{5-j-k} \ */ \\ outclause(); \\ \} \\ have\_b[x][y] = tt+1; \\ \} \\ \} \end{array}
```

**12.** The (unshared) c subroutine handles the other four neighbors, by working with f and q instead of d and e.

If y=0, the overlap rules set y1=-1, which can be problematic. I've decided to avoid this case by omitting f when it is guaranteed to be zero.

```
\langle Subroutines 6*\rangle + \equiv
  void c(\mathbf{int} \ x, \mathbf{int} \ y)
  {
     register j, k, x1, y1;
     if (x \& 1) x1 = x + 2, y1 = (y - 1) | 1;
     else x1 = x, y1 = y \& -2;
     if (x1-1 < xmin \lor x1-1 > xmax \lor y1+1 < ymin \lor y1 > ymax) (Set c equal to g 13)
     else {
        f(x1, y1);
        for (j = 0; j < 3; j ++)
          for (k = 0; k < 3; k ++)
             if (j+k) {
               if (j) newcomplit (x1, y1, 6, j); /* \bar{f}_j */
               if (k) newcomplit(x, y, 7, k); /* \bar{g}_k */
                newlit(x, y, 3, j + k); /* c_{j+k} */
                outclause();
               if (j) newlit(x1, y1, 6, 3 - j); /* f_{3-j} */
               if (k) newlit(x, y, 7, 3 - k); /* g_{3-k} */
                newcomplit(x, y, 3, 5 - j - k); /* \bar{c}_{5-j-k} */
                outclause();
             }
     }
  }
13. \langle \text{Set } c \text{ equal to } g \text{ 13} \rangle \equiv
     for (k = 1; k < 3; k ++) {
        newcomplit(x, y, 7, k), newlit(x, y, 3, k), outclause();
                                                                       /* \bar{g}_k \vee c_k */
                                                                        /* g_k \vee \bar{c}_k */
        newlit(x, y, 7, k), newcomplit(x, y, 3, k), outclause();
     newcomplit(x, y, 3, 3), outclause();
                                                  /* \bar{c}_3 */
     newcomplit(x, y, 3, 4), outclause();
                                                  /* \bar{c}_4 */
This code is used in section 12.
```

14. Totals over all eight neighbors are then deduced by the a subroutine.

```
\langle Subroutines 6*\rangle + \equiv
   void a(\mathbf{int} \ x, \mathbf{int} \ y)
      register j, k, xx = x \mid 1;
      b(xx,y);
      c(x,y);
      for (j = 0; j < 5; j++)
         for (k = 0; k < 5; k++)
            if (j + k > 1 \land j + k < 5) {
               \begin{array}{lll} \textbf{if} \ (j) \ \ newcomplit(xx,y,2,j); & /* \ \bar{b}_j \ */ \\ \textbf{if} \ (k) \ \ newcomplit(x,y,3,k); & /* \ \bar{c}_k \ */ \end{array}
               newlit(x, y, 1, j + k); /* a_{j+k} */
               outclause();
      for (j = 0; j < 5; j++)
         for (k = 0; k < 5; k++)
            if (j + k > 2 \land j + k < 6 \land j * k) {
               \begin{array}{lll} \textbf{if} \ (j) \ \ newlit(xx,y,2,j); & /* \ b_j \ */ \\ \textbf{if} \ (k) \ \ newlit(x,y,3,k); & /* \ c_k \ */ \end{array}
               newcomplit(x, y, 1, j + k - 1); /* \bar{a}_{j+k-1} */
               outclause();
            }
   }
15. Finally, as mentioned at the beginning, z' is determined from z, a_2, a_3, and a_4.
   I actually generate six clauses, not five, in order to stick to 3SAT.
\langle Subroutines 6*\rangle + \equiv
   void zprime(\mathbf{int} \ x, \mathbf{int} \ y)
      newcomplit(x, y, 1, 4), applit(x, y, 1, 1), outclause();
                                                                                  /* \bar{a}_4 \bar{z}' */
      newlit(x, y, 1, 2), applit(x, y, 1, 1), outclause(); /* <math>a_2\bar{z}' */
      newlit(x, y, 1, 3), applit(x, y, 0, 0), applit(x, y, 1, 1), outclause();
                                                                                                /* a_3 z \bar{z}' */
      newcomplit(x, y, 1, 3), newlit(x, y, 1, 4), applit(x, y, 0, 1), outclasse(); /* \bar{a}_3 a_4 z' */
      applit(x, y, 0, 7), newcomplit(x, y, 1, 2), newlit(x, y, 1, 4), outclause(); /* <math>x\bar{a}_2a_4 */
      applit(x, y, 1, 7), applit(x, y, 1, 0), applit(x, y, 0, 1), outclause(); /* <math>\bar{x}\bar{z}z' */
16* \langle Avoid an all-dead grid 16^* \rangle \equiv
   for (x = 1; x \le mm; x++)
      for (y = 1; y \le nn; y ++) printf ("\\da\d\d\", x, y);
```

 $printf("\n");$ 

This code is used in section 2\*.

```
 \begin{array}{l} \textbf{17.*} \quad \langle \text{Rule out smaller periods } \textbf{17.*} \rangle \equiv \\ \textbf{for } (k=1; \ k < r; \ k++) \\ \textbf{if } (r \% \ k \equiv 0) \ \{ \\ \text{ } /* \ \text{generation } k \ \text{shouldn't equal gen } 0 \ */ \\ \textbf{for } (x=1; \ x \leq mm; \ x++) \\ \textbf{for } (y=1; \ y \leq nn; \ y++) \ \{ \\ \text{ } printf("\%da\%d_{\square}\%d\%c\%d_{\square}\%d\%c\%d^{-}\%da\%c\%d^{-}, x, y, x, timecode[k], y, x, timecode[k], y); \\ \text{ } printf("~\%da\%d_{\square}\%d\%c\%d_{\square}\%d\%c\%d^{-}, x, y, x, timecode[k], y, x, timecode[k], y); \\ \} \\ \textbf{for } (x=1; \ x \leq mm; \ x++) \\ \textbf{for } (y=1; \ y \leq nn; \ y++) \ printf("_{\square}\%da\%c\%d", x, timecode[k], y); \\ printf("^n"); \\ \} \\ \text{This code is used in section } 2^*. \\ \end{array}
```

## 18\* Index.

The following sections were changed by the change file: 1, 2, 3, 5, 6, 7, 16, 17, 18.

```
ymax: 2, 4, 5, 8, 12.
applit: 7, 8, 9, 10, 15.
                                                                                      ymin: \ \underline{2}, 4, 5, 8, 12.
argc: 2* 3*
                                                                                      yy: 5, 8.
argv: \underline{2}^*, \underline{3}^*
                                                                                      y1: \ \underline{9}, \ \underline{10}, \ \underline{11}, \ \underline{12}.
b: <u>11</u>.
                                                                                      y2: \ \ \underline{9}, \ \underline{10}, \ \underline{11}.
                                                                                     zprime: 2, 15.
bar: \underline{7}^*
buf: \underline{2}^*, 4.
c: \ \underline{6}^*, \ \underline{12}.
clause: 2, 6, 7, 8.
clauseptr: 2,* 6,* 7,* 8.
d: 8.
done: \underline{\mathbf{6}}^*
e: 8.
exit: 3^*, 4.
f: \underline{9}.
fgets: 4.
fprintf: 3, 4.
g: \underline{10}.
have_{-}d: \quad \underline{2}^*, \quad 8.
have_e: \underline{2}, 8.
have_f: 2^*, 9.
j: \ \underline{2}^*, \ \underline{11}, \ \underline{12}, \ \underline{14}.
k: \quad \underline{2}, \, \underline{6}, \, \underline{7}, \, \underline{11}, \, \underline{12}, \, \underline{14}.
main: \underline{2}^*
maxx: 2^*, 4.
maxy: 2^*, 4.
mm: <u>2</u>*, 3*, 16*, 17*.
newcomplit: 8, 9, 10, 11, 12, 13, 14, 15.
newlit: 8, 9, 10, 11, 12, 13, 14, 15.
nn: 2*, 3*, 16*, 17*
outclause: 6, 8, 9, 10, 11, 12, 13, 14, 15.
p: 2* 6*
pp: 2*, <u>5</u>*, <u>7</u>*
printf: 2,* 3,* 6,* 16,* 17.*
r: \underline{2}^*
sign: 6, 7, 8.
sscanf: 3*
stderr: 3* 4.
stdin: 2^*, 4.
taut: 6, 7*
timecode: \underline{2}, 6, 17.
tt: \ \underline{2}^*, 6^*, 8, 9, 11.
x: \quad 2, 6, 7, 8, 9, 10, 11, 12, 14, 15.
xmax: \ \underline{2}^*, 4, 5^*, 9, 12.
xmin: \ \underline{2}, 4, 5, 9, 12.
xx: 5, 9, 11, 14.
x2: 8, 10.
y: \quad 2, 6, 7, 8, 9, 10, 11, 12, 14, 15.
```

SAT-LIFE-GRID-CYCLE NAMES OF THE SECTIONS 11

## SAT-LIFE-GRID-CYCLE

	Sect	ion	Page
Intro		1	1
Indov		1.2	10