§1 TICTACTOE6 INTRO 1

(See https://cs.stanford.edu/~knuth/programs.html for date.)

1. Intro. This program tries heuristically to construct a small circuit to decide when it is safe to move in the center in tictactoe. More precisely, we design about 1/8th of what is needed; we assume that eight copies of this circuit will be ORed together appropriately, taking account of the symmetries of the board.

In contrast to the circuit in TICTACTOE3, this program works entirely by statistical and formal methods rather than using any sort of logical intuition that makes sense.

There are 18 inputs, as in TICTACTOE3. I partition the truth table function into 2^6 rows indexed by $o_5x_5o_2o_6o_8o_4$ and 2^{12} columns indexed by $x_2x_6x_8x_4o_1o_3o_9o_7x_1x_3x_9x_7$, as suggested by the output of TICTACTOE5. Each column has a score (c, m) when it contains c cares and m ones among those cares. Low-scoring columns are the easiest to handle.

The computation proceeds in three phases.

Phase 1: For each equivalence class of positions $\{\alpha_1, \ldots, \alpha_k\}$ for which a center move is legitimate, let them correspond to columns $\{\beta_1, \ldots, \beta_k\}$ (which may not be distinct), and assume that β_1 has the lexicographically smallest score. Place a 1 in that position, and put don't-cares in the other k-1 positions. Repeating that process will yield a set of 2^{12} columns in which I hope there will be few columns that have many 1s.

Phase 2: Find a smallish set of vectors that matches every column. This is a covering problem, where a vector covers (or matches) a column if and only if it agrees with all of the care-bits in that column. When a column matches a vector, we essentially use that vector to fill in all the don't cares.

Phase 3: Build a circuit with Lupanov's method.

The standard input file should be the output of TICTACTOE4.

```
#define nn (1 \ll 12)
#define nnn \ (1 \ll 18)
\#define cases 4520
#define head (\&col[nn])
#include <stdio.h>
  typedef struct col_struct {
     int ah, al;
                      /* 64 asterisk specs, for don't cares */
                      /* 64 bit specs, for cares */
     int bh, bl;
                     /* the number of cares and the number of 1s */
     int c, m;
     struct col_struct *prev, *next;
                                             /* links for priority list */
  } column;
  ⟨Global variables 3⟩
  int count;
                   /* counter for miscellaneous purposes */
  (Subroutines 20)
  main()
     register int i, j, k, l, t;
     register column *p, *q;
     \langle Set up the initial columns 2\rangle;
     \langle \text{ Do phase 1 5} \rangle;
     \langle \text{ Do phase 2 } 13 \rangle;
     \langle \text{ Do phase 3 19} \rangle;
     \langle \text{ Check the results } 28 \rangle;
```

2 INTRO TICTACTOE6 §2

2. An important simplification occurs here: If $x_5 = 1$ or $o_5 = 1$, the output y_5 is guaranteed to be zero, so I can treat all such cases as don't-cares. (It follows that 48 of the 64 bits in every column are automatically don't-cares. Still, I've written the program to work with all 64 bits, because TICTACTOE7 will need that generality.)

```
#define bit(j,k) (((bits \gg j) & 1) \ll k)
\langle \text{ Set up the initial columns } 2 \rangle \equiv
       for (j = 0; j < nn; j ++) col[j].ah = col[j].al = #fffffffff,
                           col[j].next = \&col[j+1], col[j+1].prev = \&col[j];
       head \rightarrow next = \&col[0], col[0].prev = head;
       head \neg c = 99;
                                                         /* infinity */
       k=0;
       while (1) {
             if (\neg fgets(buf, 100, stdin)) break;
             if (buf[5] \neq ":" \lor sscanf(buf, "%x", \&bits) \neq 1) break;
             care[k] = bit(16, 17) + bit(17, 16) + bit(6, 15) + bit(4, 14) + bit(2, 13) + bit(0, 12) + bit(17, 16) + bit(17, 
                           bit(7,11) + bit(5,10) + bit(3,9) + bit(1,8) +
                           bit(14,7) + bit(12,6) + bit(10,5) + bit(8,4) +
                           bit(15,3) + bit(13,2) + bit(11,1) + bit(9,0);
             yval[k] = buf[11] - '0';
                                                                                          /* this is y_5 */
             if (yval[k] < 0 \lor yval[k] > 1) {
                    fprintf(stderr, "invalid_linput_line!_l%s", buf);
                    exit(-1);
             if (care[k] < #10000) (Make care[k] a "care" bit 4);
             k++;
      if (k \neq cases) {
             fprintf(stderr, "There\_were\_%d\_cases,\_not\_%d!\n", k, cases);
             exit(-2);
This code is used in section 1.
3. \langle \text{Global variables } 3 \rangle \equiv
      column col[nn+1];
      int care[cases], yval[cases];
       char buf[100];
      int bits;
See also sections 7, 14, 18, and 31.
```

This code is used in section 1.

§4 TICTACTOE6 INTRO 3

4. A brute-force sorting method will keep the columns in lexicographic order by their (c, m) fields. Initially the m fields are all zero, so we don't worry about them here.

```
 \langle \, \text{Make } care[k] \, \, \text{a "care" bit 4} \rangle \equiv \\ \{ \\ j = care[k] \gg 12; \\ t = care[k] \& \, \text{\#fff}; \\ \text{if } (j \& \, \text{\#20}) \, \, col[t].ah \, -= 1 \ll (j - \, \text{\#20}); \\ \text{else } \, col[t].al \, -= 1 \ll j; \\ j = ++col[t].c; \\ p = col[t].prev, q = col[t].next; \\ p - next = q, q - prev = p; \\ \text{for } (\; ; \; j > q - c; \; q = q - next) \; ; \\ p = q - prev; \\ p - next = q - prev = \& col[t], col[t].prev = p, col[t].next = q; \\ \}
```

This code is used in section 2.

4 PHASE 1 TICTACTOE6 §5

```
Phase 1.
\langle \text{ Do phase 1 5} \rangle \equiv
  \langle Find the equivalence classes 6 \rangle;
  for (k = 0; k < cases; k++)
     if (yval[k]) {
        t = care[k];
        if (leader[t] \neq t) continue;
        for (j = t, t = link[t]; t \neq care[k]; t = link[t])
          if (col[t \& #fff].c \le col[j \& #fff].c \land (col[t \& #fff].c < col[j \& #fff].c \lor col[t \& #fff].m <
                   col[j \& #fff].m)) j = t;
        \langle \text{ Set care bit } j \text{ to } 1 \text{ 10} \rangle;
        for (t = j, j = link[j]; j \neq t; j = link[j]) (Change bit j to don't-care 11);
  \langle \text{ Print the results of Phase 1 12} \rangle;
This code is used in section 1.
6. Here I use the simplest union-find algorithm, without bells or whistles. (Years ago I never would have
imagined being so shamelessly wasteful of computer time and space as I am today.)
\langle Find the equivalence classes 6\rangle \equiv
  for (k = 0; k < cases; k++) dir[care[k]] = k, leader[care[k]] = link[care[k]] = care[k];
  for (k = 0; k < cases; k++) (Make care[k] equivalent to its rotation 8);
  for (k = 0; k < cases; k++) (Make care[k] equivalent to its reflection 9);
This code is used in section 5.
7. \langle \text{Global variables } 3 \rangle + \equiv
                                                     /* equivalence class structures */
  int dir[nnn], link[nnn], leader[nnn];
     \langle \text{ Make } care[k] \text{ equivalent to its rotation } 8 \rangle \equiv
  {
     t = care[k];
     j = t \oplus ((t \oplus (t \gg 1)) \& #7777) \oplus ((t \oplus (t \ll 3)) \& #8888);
     if (yval[dir[j]] \neq yval[k]) {
        fprintf(stderr, "Error: y [\%05x] = \%d, y [\%05x] = \%d! \n", t, yval[k], j, yval[dir[j]]);
        exit(-3);
     if (leader[j] \neq leader[t]) {
        do leader[j] = leader[t], j = link[j]; while (leader[j] \neq leader[t]);
        l = link[j], link[j] = link[t], link[t] = l;
```

This code is used in section 6.

§9 TICTACTOE6 PHASE 1 5

```
\langle \text{ Make } care[k] \text{ equivalent to its reflection } 9 \rangle \equiv
  {
     t = care[k];
     j = t \oplus ((t \oplus (t \gg 1)) \& #55) \oplus ((t \oplus (t \ll 1)) \& #aa) \oplus
          ((t \oplus (t \gg 2)) \& #1100) \oplus ((t \oplus (t \ll 2)) \& #4400);
     if (yval[dir[j]] \neq yval[k]) {
        fprintf(stderr, "Error: y [\%05x] = \%d, y [\%05x] = \%d! \n", t, yval[k], j, yval[dir[j]]);
        exit(-4);
     if (leader[j] \neq leader[t]) {
        do leader[j] = leader[t], j = link[j]; while (leader[j] \neq leader[t]);
        l = link[j], link[j] = link[t], link[t] = l;
This code is used in section 6.
10. \langle Set care bit j to 1 10 \rangle \equiv
  l = j \gg 12, i = j \& \#fff;
  if (l \& #20) col[i].bh += 1 \ll (l - #20);
  else col[i].bl += 1 \ll l;
  col[i].m++;
  p = col[i].prev, q = col[i].next, p \rightarrow next = q, q \rightarrow prev = p;
  for (l = col[i].c; l \equiv q \rightarrow c \land col[i].m > q \rightarrow m; q = q \rightarrow next);
  p \rightarrow next = q \rightarrow prev = \& col[i], col[i].prev = p, col[i].next = q;
This code is used in section 5.
      \langle Change bit j to don't-care 11\rangle \equiv
11.
     l = j \gg 12, i = j \& \# fff;
     if (l \& #20) col[i].ah += 1 \ll (l - #20);
     else col[i].al += 1 \ll l;
     col[i].c--;
     p = col[i].prev, q = col[i].next, p \rightarrow next = q, q \rightarrow prev = p;
     for (l = col[i].c; l ;
     p \rightarrow next = q \rightarrow prev = \& col[i], col[i].prev = p, col[i].next = q;
This code is used in section 5.
12. \langle \text{ Print the results of Phase 1 } 12 \rangle \equiv
  for (p = head \neg prev; p \neg c > 1; p = p \neg prev)
     for (count = 0, p = head \neg prev; p \neq head; p = p \neg prev)
     if (p \rightarrow m) count ++;
  printf("%d_{\square}columns_{\square}contain_{\square}1s\n", count);
This code is used in section 5.
```

6 Phase 2 tictactoe6 $\S13$

13. Phase 2. It turns out that Phase 1 does such a good job, there's really no need for a fancy Phase 2; all nonzero columns are simply covered by unit vectors or the all-1s vector. But I'll implement a greedy covering algorithm anyway, because it will be needed in TICTACTOE7.

The idea of this algorithm is to cover columns one by one, in decreasing order of (c, m). At each step we try to augment the current set of covering vectors in such a way as to minimize the number of 1s added, and (for a fixed number of 1s) the number of asterisks subtracted.

```
\langle \text{ Do phase 2 } 13 \rangle \equiv
   \langle Compute the pop table for population counts 15\rangle;
   vec[0].ah = vec[0].al = 0, vec[0].bh = vec[0].bl = #fffffffff;
                                                                                    /* all 1s vector */
   p = head \neg prev:
                           /* the next column to be covered */
newvec: v++:
   vec[v].ah = vec[v].al = #ffffffff, vec[v].bh = vec[v].bl = 0;
                                                                                    /* all *s vector */
coverit: l = 0;
  if (p - m \equiv 0) goto advancep;
   for (k = 0, count = #990099; k < v; k++)  {
     \langle \text{ If } p \text{ is incompatible with } vec[k], \text{ continue } 16 \rangle;
     t = p - bh \& \sim vec[k].bh, j = pop[((\mathbf{unsigned\ int})\ t) \gg 16] + pop[t \& \#ffff]; /* count new 1s */
     t = p \neg bl \& \sim vec[k].bl, j += pop[((\mathbf{unsigned\ int})\ t) \gg 16] + pop[t \& \#ffff], j \ll 16;
     t = vec[k].ah \& \sim p \rightarrow ah, j += pop[((unsigned int) t) \gg 16] + pop[t \& #ffff];
                                                                                                          /* count lost *s */
     t = vec[k].al \& \sim p \neg al, j += pop[((unsigned int) t) \gg 16] + pop[t \& #ffff];
     if (j < count) count = j, l = k;
   \langle \text{Cover column } p \text{ with vector } l \mid 17 \rangle;
advancep: p = p \neg prev;
  if (p \rightarrow c) {
     if (l \equiv v) goto newvec;
     goto coverit;
   printf("there_{\square}are_{\square}%d_{\square}covering_{\square}vectors\n", v);
This code is used in section 1.
14. #define vecs 500
\langle \text{Global variables } 3 \rangle + \equiv
  int pop[1 \ll 16];
                             /* table of 16-bit population counts */
   column vec[vecs];
                               /* covering vectors */
  int v:
               /* the current number of vectors */
15. \langle Compute the pop table for population counts |15\rangle \equiv
   for (k = 1; k < \text{#10000}; k += k)
     for (j = 0; j < k; j++) pop[k+j] = 1 + pop[j];
This code is used in section 13.
16. \langle \text{ If } p \text{ is incompatible with } vec[k], \text{ continue } 16 \rangle \equiv
   t = p \rightarrow bl \oplus vec[k].bl;
  if (t \& (\sim vec[k].al) \& (\sim p \rightarrow al)) continue;
   t = p \rightarrow bh \oplus vec[k].bh;
  if (t \& (\sim vec[k].ah) \& (\sim p \rightarrow ah)) continue;
This code is used in section 13.
```

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17. The *next* field is now changed to point to the covering vector.

```
 \begin{split} &\langle \, \text{Cover column } p \, \, \text{with vector } l \, \, 17 \, \rangle \equiv \\ &q = \& \, vec[l]; \\ &p \neg next = q; \\ &q \neg bl \mid = p \neg bl, q \neg bh \mid = p \neg bh; \\ &q \neg al \, \, \& = p \neg al, q \neg ah \, \, \& = p \neg ah; \\ &p \neg intf \, (\texttt{"cover} \sqsubseteq \%03x : \%08x\%08x , \%08x\%08x \_ with \_ \%d : \%08x\%08x , \%08x\%08x \backslash n^{\texttt{"}}, p - col, p \neg ah, p \neg al, p \neg bh, p \neg bl, l, q \neg ah, q \neg al, q \neg bh, q \neg bl); \end{split}
```

This code is used in section 13.

8 PHASE 3 TICTACTOE6 §18

Phase 3. Finally, we construct the Boolean chain by using the methods of TICTACTOE3. #define gates 1000 $\langle \text{Global variables } 3 \rangle + \equiv$ typedef enum { inp, and, or, xor, butnot, nor char *opcode_name[] = {"input", "&", "|", "^", ">", "\$"}; **opcode** op[gates]; **char** val[gates]; int jx[gates], kx[gates], p[gates]; **char** name[gates][8];int x[10], o[10], vx[20], uu[vecs], vv[vecs], $colgate[1 \ll 12]$; /* addresses of named gates */ /* addresses of columns, if generated */ int $colgate[1 \ll 12];$ int g; /* address of the most recently generated gate */ int rowbase, colbase0, colbase1; /* addresses of key gates */ **19.** #define makegate(l, o, r) op[++g] = o, jx[g] = l, kx[g] = r#define $make\theta(l, o, r)$ $makegate(l, o, r), name[g][0] = '\0'$ #define make1(s, j, l, o, r, v) makeqate(l, o, r), sprintf(name[q], s, j), v = q#define make2(s, j, k, l, o, r, v) makegate(l, o, r), sprintf(name[g], s, j, k), v = g $\langle \text{ Do phase 3 19} \rangle \equiv$ for $(j = 1; j \le 9; j++)$ make1 ("x\d", j, 0, inp, 0, x[j]); for $(j = 1; j \le 9; j++) make1("o%d", j, 0, inp, 0, o[j]);$ vx[0] = o[5], vx[1] = x[5];vx[2] = o[1], vx[3] = o[3], vx[4] = o[9], vx[5] = o[7];vx[6] = x[1], vx[7] = x[3], vx[8] = x[9], vx[9] = x[7];vx[10] = o[2], vx[11] = o[6], vx[12] = o[8], vx[13] = o[4];vx[14] = x[2], vx[15] = x[6], vx[16] = x[8], vx[17] = x[4]; \langle Make minterms for the rows $22 \rangle$; $\langle Make minterms for the columns 23 \rangle;$ \langle Make the row selector functions 24 \rangle ; \langle Make the column selector functions $25 \rangle$; (Combine the selector functions to make the output 26); This code is used in section 1.

 $\S20$ TICTACTOE6 PHASE 3 9

20. Here's a simple recursive subroutine that makes minterms for n > 1 variables $v[0], \ldots, v[n-1]$. The minterms appear in gates $o, o+1, \ldots, o+2^n-1$, where o is the output.

```
\langle \text{Subroutines } 20 \rangle \equiv
  int makemins(int *v, int n)
     register int j, k, g\theta, g1, fn, cn;
     if (n < 4) (Handle the base cases 21)
     else {
       fn = n/2, cn = n - fn;
       g\theta = makemins(v, cn);
        g1 = makemins(v + cn, fn);
       for (j = 0; j < 1 \ll cn; j++)
          for (k = 0; k < 1 \ll fn; k++) make0(g0 + j, and, g1 + k);
     return g - (1 \ll n) + 1;
This code is used in section 1.
     \langle Handle the base cases 21 \rangle \equiv
     make\theta(v[0], nor, v[1]);
     make\theta(v[1], butnot, v[0]);
     make\theta(v[0], butnot, v[1]);
     make\theta(v[0], and, v[1]);
     if (n > 2) {
        g\theta = g - 3;
       for (j = 0; j < 4; j++) {
          make\theta(g\theta + j, butnot, v[2]);
          make\theta(g\theta + j, and, v[2]);
```

This code is used in section 20.

22. We're using only 16 of the 64 rows, as remarked earlier. But we'll want to share logic with the output of TICTACTOE7, so all 64 minterms are made at this step. I will figure out later which are them aren't really needed.

```
\langle Make minterms for the rows 22 \rangle \equiv rowbase = makemins(vx, 6); for (j = 0; j < 64; j++) sprintf (name[rowbase + j], "r%x", j); This code is used in section 19.
```

23. Most of the 2^{12} columns will not be used. So we only make base addresses from which full minterms can be generated as needed.

```
\langle Make minterms for the columns 23\rangle \equiv colbase0 = makemins(vx + 6, 6); colbase1 = makemins(vx + 12, 6); This code is used in section 19.
```

10 Phase 3 Tictactoe6 $\S24$

```
\langle Make the row selector functions 24 \rangle \equiv
  vv[0] = 19;
                    /* kludge: this is '\bar{o}_5 \wedge \bar{x}_5' */
  sprintf (name [19], "v0");
  for (j = 1; j < v; j ++) {
     for (k = 0; k < 32; k++)
       if (vec[j].bl \& (1 \ll k)) {
          if (\neg vv[j]) vv[j] = rowbase + k;
             make\theta(vv[j], or, rowbase + k);
             vv[j] = g;
     for (k = 0; k < 32; k++)
       if (vec[j].bh \& (1 \ll k)) {
          if (\neg vv[j]) vv[j] = rowbase + k + 32;
          else {
             make\theta(vv[j], or, rowbase + k + 32);
             vv[j] = g;
     sprintf(name[vv[j]], "v%d", j);
This code is used in section 19.
25. \langle Make the column selector functions 25\rangle \equiv
  for (j = 0; j < nn; j++)
     if (col[j].m) {
       l = col[j].next - vec;
       if (\neg colgate[j]) {
          make0 (colbase0 + (j \gg 6), and, colbase1 + (j \& #3f));
          sprintf(name[g], "c%03x", j);
          colgate[j] = g;
        }
       if (\neg uu[l]) uu[l] = colgate[j];
       else {
          make0 (uu[l], or, colgate[j]);
          uu[l] = g;
  for (j = 0; j < v; j \leftrightarrow) sprintf (name[uu[j]], "u\%d", j);
This code is used in section 19.
26. \langle Combine the selector functions to make the output 26 \rangle \equiv
  for (j = k = 0; j < v; j ++) {
     make\theta(uu[j], and, vv[j]);
     if (k) make \theta(k, or, g-1);
     k = g;
  sprintf(name[g], "y5");
  printf("Phase_{\square}3_{\square}created_{\square}%d_{\square}gates.\n", g);
This code is used in section 19.
```

§27 TICTACTOE6 CHECKING 11

27. Checking. Now comes the proof of the pudding: We run through all 4520 inputs, and make sure that we've produced the desired output.

The tricky thing is that we want to hook up eight copies of our circuit. So we evaluate eight times, and OR the results together.

```
28. \langle Check the results 28 \rangle \equiv
   count = 0;
   for (l = 0; l < cases; l++) {
      grandval = 0;
      for (i = 0, t = care[l]; i < 4; i++) {
         \langle \operatorname{Set} x_i \text{ and } o_i \text{ from } t \text{ 29} \rangle;
         \langle Evaluate the chain 30\rangle;
         grandval \mid = val[g];
         t = t \oplus ((t \oplus (t \gg 1)) \& \text{#7777}) \oplus ((t \oplus (t \ll 3)) \& \text{#8888});
      t = t \oplus ((t \oplus (t \gg 1)) \& #55) \oplus ((t \oplus (t \ll 1)) \& #aa) \oplus 
            ((t \oplus (t \gg 2)) \& #1100) \oplus ((t \oplus (t \ll 2)) \& #4400);
      for (i = 0; i < 4; i++) {
         \langle \operatorname{Set} x_i \text{ and } o_i \text{ from } t \text{ 29} \rangle;
         \langle Evaluate the chain 30\rangle;
         grandval = val[g];
         t = t \oplus ((t \oplus (t \gg 1)) \& #7777) \oplus ((t \oplus (t \ll 3)) \& #8888);
      if (grandval \neq yval[l]) printf("Failure_at_%05x_a(should_be_%d)!\n", care[l], yval[l]);
      count ++;
   printf("%d_{\square}cases_{\square}checked.\n", count);
This code is used in section 1.
29. #define setx(i, j) \ val[x[i]] = (t \gg j) \& 1
#define seto(i, j) val[o[i]] = (t \gg j) \& 1
\langle \operatorname{Set} x_i \text{ and } o_i \operatorname{from} t \ 29 \rangle \equiv
   seto(5, 17), setx(5, 16);
   seto(1, 15), seto(3, 14), seto(9, 13), seto(7, 12);
   setx(1, 11), setx(3, 10), setx(9, 9), setx(7, 8);
   seto(2,7), seto(6,6), seto(8,5), seto(4,4);
   setx(2,3), setx(6,2), setx(8,1), setx(4,0);
This code is used in section 28.
```

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```
30.
     \langle Evaluate the chain 30\rangle \equiv
  if (tracing[t]) {
    printf("Tracing_case_w%05x:\n",t);
    for (k = 1; k < 19; k \leftrightarrow) printf("%d=%d_{\sqcup}(%s)\n", k, val[k], name[k]);
  for (k = 19; k \le g; k++) {
    switch (op[k]) {
     case and: val[k] = val[jx[k]] \& val[kx[k]]; break;
     case or: val[k] = val[jx[k]] \mid val[kx[k]]; break;
     case xor: val[k] = val[jx[k]] \oplus val[kx[k]]; break;
     case butnot: val[k] = val[jx[k]] \& \sim val[kx[k]]; break;
     case nor: val[k] = 1 - (val[jx[k]] \mid val[kx[k]]); break;
     if (tracing[t]) {
       printf("%d=", k);
       if (name[jx[k]][0]) printf (name[jx[k]]);
       else printf("%d", jx[k]);
       printf(opcode\_name[op[k]]);
       if (name[kx[k]][0]) printf (name[kx[k]]);
       else printf("%d", kx[k]);
       printf("=%d", val[k]);
       if (name[k][0]) printf("_{\sqcup}(%s)\n", name[k]);
       else printf("\n");
  }
This code is used in section 28.
31. \langle Global variables 3\rangle + \equiv
                    /* OR of the eight inputs */
  int grandval;
  char tracing[1 \ll 18]; /* selective verbose printouts */
```

§32 TICTACTOE6 INDEX 13

32. Index.

advancep: 13.ah: 1, 2, 4, 11, 12, 13, 16, 17. al: 1, 2, 4, 11, 12, 13, 16, 17. and: 18, 20, 21, 25, 26, 30. $bh: \underline{1}, 10, 12, 13, 16, 17, 24.$ bit: 2.bits: $2, \underline{3}$. $bl: \underline{1}, 10, 12, 13, 16, 17, 24.$ buf: $2, \underline{3}$. butnot: 18, 21, 30. c: <u>1</u>. care: $2, \underline{3}, 4, 5, 6, 8, 9, 28$. $cases \colon \ \, \underline{1}, \,\, 2, \,\, 3, \,\, 5, \,\, 6, \,\, 28.$ $cn: \underline{20}.$ $col: 1, 2, \underline{3}, 4, 5, 10, 11, 12, 17, 25.$ col_struct: 1. $colbase\theta$: 18, 23, 25. colbase1: 18, 23, 25. $colgate: \underline{18}, \underline{25}.$ column: $\underline{1}$, $\underline{3}$, $\underline{14}$. count: $\underline{1}$, 12, 13, 28. coverit: $\underline{13}$. dir: 6, 7, 8, 9.exit: 2, 8, 9.fgets: 2. $fn: \underline{20}.$ fprintf: 2, 8, 9.g: <u>18</u>. gates: 18. $\mathit{grandval}\colon \ \ \underline{31}.$ $g\theta: \ \ \underline{20}, \ 21.$ $g1: \underline{20}.$ $head\colon \ \underline{1},\ \underline{2},\ \underline{12},\ \underline{13}.$ *i*: <u>1</u>. inp: 18, 19. $j: \ \underline{1}, \ \underline{20}.$ jx: 18, 19, 30. $k: \ \ \underline{1}, \ \underline{20}.$ kx: 18, 19, 30.*l*: <u>1</u>. leader: $5, 6, \frac{7}{2}, 8, 9$. link: 5, 6, 7, 8, 9. $m: \underline{1}.$ $main: \underline{1}.$ $makegate: \underline{19}.$ makemins: 20, 22, 23. $make\theta$: 19, 20, 21, 24, 25, 26. $make1: \underline{19}.$ $make2: \underline{19}.$ $n: \underline{20}.$ name: 18, 19, 22, 24, 25, 26, 30.

 $newvec: \underline{13}.$ next: $\underline{1}$, 2, 4, 10, 11, 17, 25. $nn: \ \underline{1}, \ 2, \ 3, \ 25.$ $nnn: \underline{1}, 7.$ nor: 18, 21, 30. o: <u>18</u>. op: 18, 19, 30.opcode: 18. $opcode_name: \underline{18}, 30.$ or: 18, 24, 25, 26, 30. $p: \ \ \underline{1}, \ \underline{18}.$ pop: 13, <u>14</u>, 15. prev: $\underline{1}$, 2, 4, 10, 11, 12, 13. printf: 12, 13, 17, 26, 28, 30. $q: \underline{1}$. rowbase: 18, 22, 24.seto: $\underline{29}$. setx: 29.sprintf: 19, 22, 24, 25, 26. sscanf: 2.stderr: 2, 8, 9. stdin: 2.t: $\underline{1}$. tracing: $30, \underline{31}$. uu: 18, 25, 26. $v: \ \underline{14}, \ \underline{20}.$ val: 18, 28, 29, 30.vec: 13, <u>14</u>, 16, 17, 24, 25. $vecs: \underline{14}, 18.$ vv: 18, 24, 26.vx: 18, 19, 22, 23. $x: \underline{18}$. xor: 18, 30. yval: 2, 3, 5, 8, 9, 28.

14 NAMES OF THE SECTIONS TICTACTOE6

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\langle \text{ Make } care[k] \text{ equivalent to its reflection } 9 \rangle Used in section 6.
\langle \text{ Make } care[k] \text{ equivalent to its rotation } 8 \rangle Used in section 6.
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\langle \text{Subroutines 20} \rangle Used in section 1.
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