§1 POLYSTICKS DATA FOR DANCING

(Downloaded from https://cs.stanford.edu/~knuth/programs.html and typeset on May 28, 2023)

1. Data for dancing. This program creates data suitable for the DANCE routine, given the description of edges and junctions to be covered and a set of polystick shapes.

The first line of input names all the pieces. Each piece name consists of at most three characters; the name should also be distinguishable from a board position. (The program does not check this.)

The second line of input names all the board positions, in any order except that interior junction points must follow a '|'. Each position is of the form Hxy or Vxy or Ixy, where x and y are digits that represent coordinates; each "digit" is a single character, 0-9 or a-z representing the numbers 0-35. Position Hxy is the edge from (x, y) to (x, y + 1); position Ixy is the interior point (x, y). For example,

```
HO1 H11 V10 V11 | I11
```

is one way to describe a board that makes a small cross shape.

This code is used in section 1.

The remaining lines of input describe the polysticks. First comes the name, followed by two integers s and t, meaning that the shape should appear in s rotations and t transpositions. Then come board positions for each cell of the shape. For example, the line

## C 4 1 HOO VOO IO1 VO1 HO2

```
describes a hexiamond that can appear in 4 orientations. (See the analogous program for polyominoes.)
                                /* at most this many shapes */
#define max_pieces 100
#define buf\_size \ 3*36*36*4+10
                                            /* upper bound on line length */
#include <stdio.h>
#include <ctype.h>
  (Global variables 5)
  \langle \text{Subroutines 4} \rangle;
  main()
     register char *p, *q;
     register int j, k, n, x, y, z, bar;
     \langle \text{Read and output the piece names } 2 \rangle;
     \langle \text{Read and output the board } 3 \rangle;
     \langle \text{ Read and output the pieces 6} \rangle:
  }
     \#define panic(m)
          \{ fprintf(stderr, "%s!\n%s", m, buf); exit(-1); \}
\langle \text{Read and output the piece names } 2 \rangle \equiv
  if (\neg fgets(buf, buf\_size, stdin)) panic("No\_piece\_names");
  if (buf[strlen(buf) - 1] \neq '\n') panic("Input_line_too_long");
  fwrite(buf, 1, strlen(buf) - 1, stdout);
                                                /* output all but the newline */
```

2 data for dancing polysticks  $\S 3$ 

```
3. \langle \text{Read and output the board 3} \rangle \equiv
  if (\neg fgets(buf, buf\_size, stdin)) panic("No\_board");
  if (buf[strlen(buf) - 1] \neq "\n") panic("Input_line_too_long");
  bxmin = bymin = 35; bxmax = bymax = 0;
  for (p = buf, bar = 0; *p; p += 4) {
     while (isspace(*p)) p++;
    if (\neg *p) break;
     if (*p \equiv ' \mid ' \wedge isspace(*(p+1))) {
       bar = 1;
       p -= 2;
       continue;
     x = decode(*(p+1));
     if (x < 0) panic("Bad_\\\x_\\\coordinate");
     y = decode(*(p+2));
     if (y < 0) panic("Bad_{\sqcup}y_{\sqcup}coordinate");
     if (\neg isspace(*(p+3))) \ panic("Bad_lboard_lposition");
    if (*p \equiv 'H' \land \neg bar) z = 0;
    else if (*p \equiv "V" \land \neg bar) z = 2;
     else if (*p \equiv 'I' \wedge bar) z = 1;
     else panic("Illegal_board_position");
    if (board[x][y][z]) panic("Duplicate_board_position");
    if (x < bxmin) bxmin = x;
     if (x > bxmax) bxmax = x;
     if (y < bymin) bymin = y;
    if (y > bymax) bymax = y;
     board[x][y][z] = 1;
  if (bxmin > bxmax) panic("Empty_board");
  printf("_{\sqcup}\%s", buf);
                            /* just pass the board names through */
This code is used in section 1.
4. \langle \text{Subroutines 4} \rangle \equiv
  int decode(c)
       char c;
    if (c \leq 9)
       if (c \geq 0) return c - 0;
     } else if (c \ge `a") {
       if (c \leq z') return c + 10 - a';
     return -1;
See also section 12.
This code is used in section 1.
5. \langle Global variables 5\rangle \equiv
  char buf [buf_size];
  int board [36][36][3];
                            /* positions present */
  int bxmin, bxmax, bymin, bymax; /* used portion of the board */
See also section 7.
This code is used in section 1.
```

POLYSTICKS DATA FOR DANCING

ξ6

```
6. \langle \text{Read and output the pieces 6} \rangle \equiv
  while (fgets(buf, buf_size, stdin)) {
     if (buf[strlen(buf) - 1] \neq '\n') panic("Input_line_too_long");
     for (p = buf; isspace(*p); p++);
     if (\neg *p) panic("Empty_line");
     for (q = p + 1; \neg isspace(*q); q \leftrightarrow);
     \textbf{if } (q>p+3) \ \textit{panic}(\texttt{"Piece} \_ \texttt{name} \_ \texttt{too} \_ \texttt{long"});\\
     for (q = name; \neg isspace(*p); p++, q++) *q = *p;
     *q = '\0';
     for (p++; isspace(*p); p++);
     s = *p - '0';
     if ((s \neq 1 \land s \neq 2 \land s \neq 4) \lor \neg isspace(*(p+1))) panic("Bad_\suvalue");
     for (p += 2; isspace(*p); p++);
     t = *p - '0';
     if ((t \neq 1 \land t \neq 2) \lor \neg isspace(*(p+1))) panic("Bad_\t_value");
     n=0;
     xmin = ymin = 35; xmax = ymax = 0;
     for (p += 2; *p; p += 4, n++)
       while (isspace(*p)) p++;
       if (\neg *p) break;
       x = decode(*(p+1));
       if (x < 0) panic("Bad_{\sqcup}x_{\sqcup}coordinate");
       y = decode(*(p+2));
       if (y < 0) panic("Bad_y_coordinate");
       if (\neg isspace(*(p+3))) panic("Bad_{\sqcup}board_{\sqcup}position");
       if (*p \equiv 'H') z = 0;
       else if (*p \equiv "V") z = 2;
       else if (*p \equiv 'I') z = 1;
       else panic("Illegal board position");
       if (n \equiv 36 * 36 * 2) panic("Pigeonhole_{\square}principle_{\square}says_{\square}you_{\square}repeated_{\square}a_{\square}position");
       xx[n] = x, yy[n] = y, zz[n] = z;
       if (x < xmin) \ xmin = x;
       if (x > xmax) xmax = x;
       if (y < ymin) ymin = y;
       if (y > ymax) ymax = y;
     if (n \equiv 0) panic("Empty_piece");
     (Generate the possible piece placements 8);
This code is used in section 1.
7. \langle \text{Global variables 5} \rangle + \equiv
  char name[4];
                       /* name of current piece */
               /* symmetry type of current piece */
  int s, t;
  int xx[36*36*3], yy[36*36*3], zz[36*36*3];
                                                               /* coordinates of current piece */
  int xmin, xmax, ymin, ymax;
                                        /* range of coordinates */
```

4 data for dancing polysticks §8

```
8. \langle Generate the possible piece placements 8\rangle \equiv
  while (t) {
     for (k = 1; k \le 4; k++) {
       if (k \leq s) (Output translates of the current piece 11);
       \langle Rotate the current piece 10\rangle;
     ⟨Transpose the current piece 9⟩;
This code is used in section 6.
9. \langle \text{Transpose the current piece } 9 \rangle \equiv
  for (j = 0; j < n; j ++) {
     z = xx[j];
     xx[j] = yy[j];
     yy[j] = z;
     zz[j] = 2 - zz[j];
  z = xmin; xmin = ymin; ymin = z;
  z = xmax; xmax = ymax; ymax = z;
This code is used in section 8.
10. \langle \text{Rotate the current piece } 10 \rangle \equiv
  xmin = ymin = 1000; xmax = ymax = -1000;
  for (j = 0; j < n; j ++) {
     z = xx[j];
     xx[j] = -yy[j];
    if (zz[j] \equiv 2) xx[j]—;
     yy[j] = z;
     zz[j] = 2 - zz[j];
    if (xx[j] < xmin) xmin = xx[j];
    if (xx[j] > xmax) xmax = xx[j];
    if (yy[j] < ymin) ymin = yy[j];
    if (yy[j] > ymax) ymax = yy[j];
This code is used in section 8.
```

§11 POLYSTICKS DATA FOR DANCING 5

11. Interior points don't have to be on the board; they might, for example, lie on the boundary after translation.

```
\langle Output translates of the current piece 11\rangle \equiv
  for (x = bxmin - xmin; x \le bxmax - xmax; x++)
    for (y = bymin - ymin; y \le bymax - ymax; y++) {
      for (j = 0; j < n; j++)
        if (zz[j] \neq 1 \land \neg board[x + xx[j]][y + yy[j]][zz[j]]) goto nope;
      printf(name);
      for (j = 0; j < n; j ++)
        if (board[x + xx[j]][y + yy[j]][zz[j]]) {
          printf("\n");
    nope:;
This code is used in section 8.
12. \langle \text{Subroutines 4} \rangle + \equiv
  char codeletter[3] = \{ 'H', 'I', 'V' \};
  char encode(x)
      int x;
    if (x < 10) return '0' + x;
    return 'a' -10 + x;
```

6 INDEX POLYSTICKS §13

## 13. Index.

```
bar: \underline{1}, \underline{3}.
board: 3, 5, 11.
buf: 2, 3, 5, 6.
buf_size: 1, 2, 3, 5, 6.
bxmax: 3, \underline{5}, 11.
bxmin: 3, 5, 11.
by max: 3, 5, 11.
bymin: 3, \underline{5}, 11.
c: \underline{4}.
codeletter: 11, \underline{12}.
decode: 3, \underline{4}, 6.
encode: 11, \underline{12}.
exit: 2.
fgets: 2, 3, 6.
fprintf: 2.
fwrite: 2.
isspace: 3, 6.
j: \underline{1}.
k: \underline{1}.
main: \underline{1}.
max\_pieces: 1.
n: \underline{1}.
name \colon \ 6, \ \underline{7}, \ 11.
nope: \underline{11}.
p: <u>1</u>.
panic: \underline{2}, \underline{3}, \underline{6}.
printf: 3, 11.
q: \underline{1}.
s: <u>7</u>.
stderr: 2.
stdin: 2, 3, 6.
stdout: 2.
strlen: 2, 3, 6.
t: \underline{7}.
x: \quad \underline{1}, \quad \underline{12}.
xmax: 6, 7, 9, 10, 11.
xmin: 6, <u>7</u>, 9, 10, 11.
xx: 6, <u>7</u>, 9, 10, 11.
y: <u>1</u>.
ymax: 6, 7, 9, 10, 11.
ymin: 6, <u>7</u>, 9, 10, 11.
yy: 6, 7, 9, 10, 11.
z: \underline{1}.
zz: 6, 7, 9, 10, 11.
```

POLYSTICKS NAMES OF THE SECTIONS 7

```
\label{eq:continuous} \left\langle \begin{array}{ll} \text{Generate the possible piece placements 8} \right\rangle \quad \text{Used in section 6.} \\ \left\langle \begin{array}{ll} \text{Global variables 5, 7} \right\rangle \quad \text{Used in section 1.} \\ \left\langle \begin{array}{ll} \text{Output translates of the current piece 11} \right\rangle \quad \text{Used in section 8.} \\ \left\langle \begin{array}{ll} \text{Read and output the board 3} \right\rangle \quad \text{Used in section 1.} \\ \left\langle \begin{array}{ll} \text{Read and output the piece names 2} \right\rangle \quad \text{Used in section 1.} \\ \left\langle \begin{array}{ll} \text{Read and output the pieces 6} \right\rangle \quad \text{Used in section 1.} \\ \left\langle \begin{array}{ll} \text{Rotate the current piece 10} \right\rangle \quad \text{Used in section 8.} \\ \left\langle \begin{array}{ll} \text{Subroutines 4, 12} \right\rangle \quad \text{Used in section 1.} \\ \left\langle \begin{array}{ll} \text{Transpose the current piece 9} \right\rangle \quad \text{Used in section 8.} \\ \end{array} \right.
```

## POLYSTICKS

	Section	Page
Data for dancing	1	]
Index	13	$\epsilon$