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## QUESTION 1

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TO OBTAIN BFS USING ALGEBRAIC METHOD Question Max  $Z = 2x_1 + 3x_2 + 4x_3 + 7x_4$  st:  $2x_1 + 3x_2 - x_3 + 4x_4 = 8$   $x_1 - 2x_2 + 6x_3 - 7x_4 = -3$   $x_i \geq 0$ ;  $i = 1, 2, 3, 4$

```
clc
clear all
format short
% PHASE-1: Input the parameter
c=[2,3,4,7]; %Objective function
A=[2 3 -1 4; 1 -2 6 -7]; %Coefficient Matrix
B=[8;-3];%RHS of const
objective=1; %1 for max and -1 for minimization problem
%Number of possible solutions: nCm:nchoosek

% PHASE-2: Number of constraint and variable
m=size(A,1); %number of constraints
n=size(A,2); % number of variables

% PHASE-3: Compute the ncm Basic Solutions: The max number of basic
% solutions will always be nCm
nab=nchoosek(n,m); %total number of atmost basic solution
t=nchoosek(1:n,m); %from this we can extract our set of variables that we need to equate to zero

% PHASE-4:Construct the basic solution
% for this n>m must be satisfied
sol=[]; %default solution is zero (Empty Matrix)
if n>=m %if this is not statisfied then we can not have solutions
    for i=1:nab
        y=zeros(n,1);
        %selecting all rows for a specific column where for t we are taking all columns for a
        % specific row (which is basically the variables that are equated to zero)
        X=(A(:,t(i,:)))\B;
        %fetching values from A matrix for the rows correspond
        %checking feasibility condition
        if all(X>=0 & X<=inf & X>=-inf)
            y(t(i,:))=X;
            sol=[sol y];
        end
    end
    disp("Solution: ");
    disp(sol);
else
    error('No. of variables is less than number of constraints')
end
if any(X == 0)
    fprintf("DEGENERATE SOLUTION");
else
    fprintf('NON-DEGENERATE SOLUTION\n');
end
%PHASE 5: To find optimal solution
```

```

Z=c*sol; %finding the values corresponding to each point
if(objective==1)
    [Zmax,Zindex]=max(Z);%storing the max value of Z and the col in which this max value resides
else
    [Zmax,Zindex]=min(Z);%storing the min value of Z and the col in which this min value resides
end
BFS=sol(:,Zindex);%basic feasible solution
[Optimal_Value]=[BFS' Zmax];
Optimal_bfs=array2table(Optimal_Value);
Optimal_bfs.Properties.VariableNames(1:size(Optimal_bfs,2))={'x1','x2','x3','x4','Optimal Value of Z'};
disp(Optimal_bfs);

```

Solution:

|        |        |        |        |
|--------|--------|--------|--------|
| 1.0000 | 2.4444 | 0      | 0      |
| 2.0000 | 0      | 2.8125 | 0      |
| 0      | 0      | 0.4375 | 2.5882 |
| 0      | 0.7778 | 0      | 2.6471 |

NON-DEGENERATE SOLUTION

| x1 | x2 | x3     | x4     | Optimal Value of Z |
|----|----|--------|--------|--------------------|
| 0  | 0  | 2.5882 | 2.6471 | 28.882             |

## QUESTION 2

TO OBTAIN BFS USING ALGEBRAIC METHOD Question 2 Max  $Z = -x_1 + 2x_2 - x_3$  st:  $x_1 + s_1 = 4$   $x_2 + s_2 = 4$   $-x_1 + x_2 + s_3 = 6$   $-x_1 + 2x_3 + s_4 = 4$   $x_1, x_2, x_3 \geq 0$

```

clc
clear all
format short
% PHASE-1: Input the parameter
c=[-1,2,-1,0,0,0,0]; %Objective function
A=[1,0,0,1,0,0,0;0,1,0,0,1,0,0;-1,1,0,0,0,1,0;-1,2,0,0,0,0,1]; %Coefficient Matrix
B=[4;4;6;4];%RHS of const
objective=1; %1 for max and -1 for minimization problem
%Number of possible solutions: nCm:nchoosek

% PHASE-2: Number of constraint and variable
m=size(A,1); %number of constraints
n=size(A,2); % number of variables

% PHASE-3: Compute the ncm Basic Solutions: The max number of basic
% solutions will always be nCm
nab=nchoosek(n,m); %total number of atmost basic solution
t=nchoosek(1:n,m); %from this we can extract our set of variables that we need to equate to zero

% PHASE-4:Construct the basic solution
% for this n>m must be satisfied
sol=[]; %default solution is zero (Empty Matrix)
if n>=m %if this is not statisfied then we can not have solutions
    for i=1:nab
        y=zeros(n,1);
        %selecting all rows for a specific column where for t we are taking all columns for a
        % specific row (which is basically the variables that are equated to zero)
        X=(A(:,t(i,:)))\B;
        %fetching values from A matrix for the rows correspond
        %checking feasibility condition
        if all(X>=0 & X<=inf & X<=-inf)

```

```

        y(t(i,:))=X;
        sol=[sol y];
    end
end
disp("Solution: ");
disp(sol);
else
    error('No. of variables is less than number of constraints')
end
if any(X == 0)
    fprintf("DEGENERATE SOLUTION");
else
    fprintf('NON-DEGENERATE SOLUTION\n');
end
%PHASE 5: To find optimal solution
Z=c*sol; %finding the values corresponding to each point
if(objective==1)
    [Zmax,Zindex]=max(Z);%storing the max value of Z and the col in which this max value resides
else
    [Zmax,Zindex]=min(Z);%storing the min value of Z and the col in which this min value resides
end
BFS=sol(:,Zindex);%basic feasible solution
[Optimal_Value]=[BFS' Zmax];
Optimal_bfs=array2table(Optimal_Value);
Optimal_bfs.Properties.VariableNames(1:size(Optimal_bfs,2))={'x1','x2','x3','s1','s2','s3','s4','Optimal Value of Z'};
disp(Optimal_bfs);

```

|   |   |   |    |   |   |
|---|---|---|----|---|---|
| 4 | 4 | 4 | 4  | 0 | 0 |
| 4 | 4 | 4 | 0  | 2 | 0 |
| 0 | 0 | 0 | 0  | 0 | 0 |
| 0 | 0 | 0 | 0  | 4 | 4 |
| 0 | 0 | 0 | 4  | 2 | 4 |
| 6 | 6 | 6 | 10 | 4 | 6 |
| 0 | 0 | 0 | 8  | 0 | 4 |

### QUESTION 3

TO OBTAIN BFS USING ALGEBRAIC METHOD Question Max  $Z = 5x_2 - 2x_1$  st:  $2x_1 + 5x_2 + s_1 = 8$   $x_1 + x_2 + s_2 = 2$   $x_i \geq 0$

```

clc
clear all
format short
% PHASE-1: Input the parameter
c=[-2,5,0,0]; %Objective function
A=[2,5,1,0;1,1,0,1]; %Coefficient Matrix
B=[8;2];%RHS of const
objective=-1; %1 for max and -1 for minimization problem
%Number of possible solutions: nCm:nchoosek

% PHASE-2: Number of constraint and variable
m=size(A,1); %number of constraints
n=size(A,2); % number of variables

% PHASE-3: Compute the ncm Basic Solutions: The max number of basic
% solutions will always be nCm
nab=nchoosek(n,m); %total number of atmost basic solution
t=nchoosek(1:n,m); %from this we can extract our set of variables that we need to equate to zero

% PHASE-4:Construct the basic solution
% for this n>m must be satisfied
sol=[]; %default solution is zero (Empty Matrix)
if n>m %if this is not statisfied then we can not have solutions
    for i=1:nab
        y=zeros(n,1);
        %selecting all rows for a specific column where for t we are taking all columns for a
        % specific row (which is basically the variables that are equated to zero)
        X=(A(:,t(i,:)))\B;
        %fetching values from A matrix for the rows correspond
        %checking feasibility condition
        if all(X>=0 & X<=inf & X>=-inf)
            y(t(i,:))=X;
            sol=[sol y];
        end
    end
    disp("Solution: ");
    disp(sol);
else
    error('No. of variables is less than number of constraints')
end
if any(X == 0)
    fprintf("DEGENERATE SOLUTION");
else
    fprintf('NON-DEGENERATE SOLUTION\n');
end

%PHASE 5: To find optimal solution
Z=c*sol; %finding the values corresponding to each point
if(objective==1)
    [Zmax,Zindex]=max(Z);%storing the max value of Z and the col in which this max value resides
else
    [Zmax,Zindex]=min(Z);%storing the min value of Z and the col in which this min value resides
end
%Optimal BFS
BFS=sol(:,Zindex);%basic feasible solution

```

```
[Optimal_Value]=[BFS' Zmax];
Optimal_bfs=array2table(Optimal_Value);
Optimal_bfs.Properties.VariableNames(1:size(Optimal_bfs,2))={'x1','x2','s1','s2','Optimal Value of Z'};
disp(Optimal_bfs);
```

Solution:

|        |        |        |        |
|--------|--------|--------|--------|
| 0.6667 | 2.0000 | 0      | 0      |
| 1.3333 | 0      | 1.6000 | 0      |
| 0      | 4.0000 | 0      | 8.0000 |
| 0      | 0      | 0.4000 | 2.0000 |

NON-DEGENERATE SOLUTION

| x1 | x2 | s1 | s2 | Optimal Value of Z |
|----|----|----|----|--------------------|
| —  | —  | —  | —  | —                  |
| 2  | 0  | 4  | 0  | -4                 |

## QUESTION 4

TO OBTAIN BFS USING ALGEBRAIC METHOD Question Max  $Z = x_1 + x_2 + x_3 + 0s_1 + 0s_2$  st:  $x_1 + x_2 + s_1 = 1$   $-x_2 + x_3 + s_2 = 0$   $x_i \geq 0$

```
clc
clear all
format short
% PHASE-1: Input the parameter
c=[1,1,1,0,0]; %Objective function
A=[1,1,0,1,0;0,-1,1,0,1]; %Coefficient Matrix
B=[1;0];%RHS of const
objective=1; %1 for max and -1 for minimization problem
%Number of possible solutions: nCm:nchoosek

% PHASE-2: Number of constraint and variable
m=size(A,1); %number of constraints
n=size(A,2); % number of variables

% PHASE-3: Compute the ncm Basic Solutions: The max number of basic
% solutions will always be nCm
nab=nchoosek(n,m); %total number of atmost basic solution
t=nchoosek(1:n,m); %from this we can extract our set of variables that we need to equate to zero

% PHASE-4:Construct the basic solution
% for this n>m must be satisfied
sol=[]; %default solution is zero (Empty Matrix)
if n>m %if this is not statisfied then we can not have solutions
    for i=1:nab
        y=zeros(n,1);
        %selecting all rows for a specific column where for t we are taking all columns for a
        % specific row (which is basically the variables that are equated to zero)
        X=(A(:,t(i,:)))\B;
        %fetching values from A matrix for the rows correspond
        %checking feasibility condition
        if all(X>=0 & X<=inf & X<=-inf)
            y(t(i,:))=X;
            sol=[sol y];
        end
    end
    disp('Solution: ');
    disp(sol);
else
```

```

    error('No. of variables is less than number of constraints')
end
if any(X == 0)
    fprintf("DEGENERATE SOLUTION\n");
else
    fprintf('NON-DEGENERATE SOLUTION\n');
end
%PHASE 5: To find optimal solution
Z=c*sol; %finding the values corresponding to each point
if(objective==1)
    [Zmax,Zindex]=max(Z);%storing the max value of Z and the col in which this max value resides
else
    [Zmax,Zindex]=min(Z);%storing the min value of Z and the col in which this min value resides
end
BFS=sol(:,Zindex);%basic feasible solution
[Optimal_Value]=[BFS' Zmax];
Optimal_bfs=array2table(Optimal_Value);
Optimal_bfs.Properties.VariableNames(1:size(Optimal_bfs,2))={'x1','x2','x3','s1','s2','Optimal Value of Z'};
disp(Optimal_bfs);

```

Warning: Matrix is singular to working precision.  
Warning: Matrix is singular to working precision.  
Solution:

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 |
| 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |

DEGENERATE SOLUTION

| x1 | x2 | x3 | s1 | s2 | Optimal Value of Z |
|----|----|----|----|----|--------------------|
| —  | —  | —  | —  | —  | —                  |
| 0  | 1  | 1  | 0  | 0  | 2                  |