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QUESTION 1

TO OBTAIN BFS USING ALGEBRAIC METHOD Question Max Z= 2x1+3x2+4x3+7x4 st: 2x1+3x2-x3+4x4=8 x1-2x2+6x3-7x4=-3 %xi>=0; i=1,2,3,4

```
clc
clear all
format short
% PHASE-1: Input the parameter
c=[2,3,4,7]; %Objective function
A=[2 3 -1 4; -1 2 -6 7]; %Coefficient Matrix
B=[8;3];%RHS of const
objective=1; %1 for max and -1 for minimization problem
%Number of possible solutions: nCm:nchoosek

% PHASE-2: Number of constraint and variable
m=size(A,1); %number of constraints
n=size(A,2); % number of variables

% PHASE-3: Compute the ncm Basic Solutions: The max number of basic
% solutions will always be nCm
nab=nchoosek(n,m); %total number of atmost basic solution
t=nchoosek(1:n,m); %from this we can extract our set of variables that we need to equate to zero

% PHASE-4:Construct the basic solution
% for this n>m must be satisfied
sol=[]; %default solution is zero (Empty Matrix)
if n>=m %if this is not statisfied then we can not have solutions
    for i=1:nab
    y=zeros(n,1);
    %selecting all rows for a specific column where for t we are taking all columns for a
    % specific row (which is basically the variables that are equated to zero)
    X=(A(:,t(i,:)))\B;
    %fetching values from A matrix for the rows correspond
    %checking feasibility condition
    if all(X>=0 & X~=inf & X~=-inf)
        y(t(i,:))=X;
        sol=[sol y];
    end
    end
    disp("Solution: ");
    disp(sol);
else
    error('No. of variables is less than number of constraints')
end
if any(X == 0)
        fprintf("DEGENERATE SOLUTION");
else
    fprintf('NON-DEGENERATE SOLUTION\n');
end
%PHASE 5: To find optimal solution
```

```
Z=c*sol; %finding the values corresponding to each point
if(objective==1)
    [Zmax,Zindex]=max(Z);%storing the max value of Z and the col in which this max value resides
else
    [Zmax,Zindex]=min(Z);%storing the min value of Z and the col in which this min value resides
end
BFS=sol(:,Zindex);%basic feasible solution
[Optimal_Value]=[BFS' Zmax];
Optimal_bfs=array2table(Optimal_Value);
Optimal_bfs.Properties.VariableNames(1:size(Optimal_bfs,2))={'x1','x2','x3','x4','Optimal Value of Z'};
disp(Optimal_bfs);
```

```
Solution:
    1.0000    2.4444         0         0
    2.0000         0    2.8125         0
         0         0    0.4375    2.5882
         0    0.7778         0    2.6471

NON-DEGENERATE SOLUTION
    x1    x2      x3        x4      Optimal Value of Z
    __    __    ______    ______    __________________

    0     0     2.5882    2.6471          28.882
```

QUESTION 2

TO OBTAIN BFS USING ALGEBRAIC METHOD Question 2 Max Z= -x1+2x2-x3 st: x1+s1=4 x2+s2=4 -x1+x2+s3=6 -x1+2x3+s4=4 x1,x2,x3>=0

```
clc
clear all
format short
% PHASE-1: Input the parameter
c=[-1,2,-1,0,0,0,0]; %Objective function
A=[1,0,0,1,0,0,0;0,1,0,0,1,0,0;-1,1,0,0,0,1,0;-1,0,2,0,0,0,1]; %Coefficient Matrix
B=[4;4;6;4];%RHS of const
objective=1; %1 for max and -1 for minimization problem
%Number of possible solutions: nCm:nchoosek

% PHASE-2: Number of constraint and variable
m=size(A,1); %number of constraints
n=size(A,2); % number of variables

% PHASE-3: Compute the ncm Basic Solutions: The max number of basic
% solutions will always be nCm
nab=nchoosek(n,m); %total number of atmost basic solution
t=nchoosek(1:n,m); %from this we can extract our set of variables that we need to equate to zero

% PHASE-4:Construct the basic solution
% for this n>m must be satisfied
sol=[]; %default solution is zero (Empty Matrix)
if n>=m %if this is not statisfied then we can not have solutions
    for i = 1:nab
        y = zeros(n, 1);
        % Check if the selected variables form a singular matrix
        if rank(A(:, t(i, :))) == m
            X = A(:, t(i, :)) \ B; % Solve for basic variables
            if all(X >= 0)
                y(t(i, :)) = X;
                sol = [sol y];
```

```
            end
        end
    end
    disp("Solution: ");
    disp(sol);
else
    error('No. of variables is less than number of constraints')
end
if any(X == 0)
        fprintf("DEGENERATE SOLUTION");
else
    fprintf('NON-DEGENERATE SOLUTION\n');
end
%PHASE 5: To find optimal solution
Z=c*sol; %finding the values corresponding to each point
if(objective==1)
    [Zmax,Zindex]=max(Z);%storing the max value of Z and the col in which this max value resides
else
    [Zmax,Zindex]=min(Z);%storing the min value of Z and the col in which this min value resides
end
BFS=sol(:,Zindex);%basic feasible solution
[Optimal_Value]=[BFS' Zmax];
Optimal_bfs=array2table(Optimal_Value);
Optimal_bfs.Properties.VariableNames(1:size(Optimal_bfs,2))={'x1','x2','x3','s1','s2','s3','s4','Optimal Value of Z'};
disp(Optimal_bfs);
```

```
Solution:
     4     4     4     4     0     0     0     0
     4     4     0     0     4     4     0     0
     4     0     4     0     2     0     2     0
     0     0     0     0     4     4     4     4
     0     0     4     4     0     0     4     4
     6     6    10    10     2     2     6     6
     0     8     0     8     0     4     0     4

NON-DEGENERATE SOLUTION
    x1    x2    x3    s1    s2    s3    s4    Optimal Value of Z
    __    __    __    __    __    __    __    __________________

    0     4     0     4     0     2     4             8
```

QUESTION 3

TO OBTAIN BFS USING ALGEBRAIC METHOD Question Min Z= 5x2-2x1 st: 2x1+5x2+s1=8 x1+x2+s2=2 %xi>=0

```
clc
clear all
format short
% PHASE-1: Input the parameter
c=[-2,5,0,0]; %Objective function
A=[2,5,1,0;1,1,0,1]; %Coefficient Matrix
B=[8;2];%RHS of const
objective=-1; %1 for max and -1 for minimization problem
%Number of possible solutions: nCm:nchoosek

% PHASE-2: Number of constraint and variable
m=size(A,1); %number of constraints
n=size(A,2); % number of variables
```

```
% PHASE-3: Compute the ncm Basic Solutions: The max number of basic
% solutions will always be nCm
nab=nchoosek(n,m); %total number of atmost basic solution
t=nchoosek(1:n,m); %from this we can extract our set of variables that we need to equate to zero

% PHASE-4:Construct the basic solution
% for this n>m must be satisfied
sol=[]; %default solution is zero (Empty Matrix)
if n>=m %if this is not statisfied then we can not have solutions
    for i=1:nab
    y=zeros(n,1);
    %selecting all rows for a specific column where for t we are taking all columns for a
    % specific row (which is basically the variables that are equated to zero)
    X=(A(:,t(i,:)))\B;
    %fetching values from A matrix for the rows correspond
    %checking feasibility condition
    if all(X>=0 & X~=inf & X~=-inf)
        y(t(i,:))=X;
        sol=[sol y];
    end
    end
    disp("Solution: ");
    disp(sol);
else
    error('No. of variables is less than number of constraints')
end
if any(X == 0)
        fprintf("DEGENERATE SOLUTION\n");
else
    fprintf('NON-DEGENERATE SOLUTION\n');
end

%PHASE 5: To find optimal solution
Z=c*sol; %finding the values corresponding to each point
if(objective==1)
    [Zmax,Zindex]=max(Z);%storing the max value of Z and the col in which this max value resides
else
    [Zmax,Zindex]=min(Z);%storing the min value of Z and the col in which this min value resides
end
%Optimal BFS
BFS=sol(:,Zindex);%basic feasible solution
[Optimal_Value]=[BFS' Zmax];
Optimal_bfs=array2table(Optimal_Value);
Optimal_bfs.Properties.VariableNames(1:size(Optimal_bfs,2))={'x1','x2','s1','s2','Optimal Value of Z'};
disp(Optimal_bfs);
```

```
Solution:
    0.6667    2.0000         0         0
    1.3333         0    1.6000         0
         0    4.0000         0    8.0000
         0         0    0.4000    2.0000

NON-DEGENERATE SOLUTION
    x1    x2    s1    s2    Optimal Value of Z
    __    __    __    __    __________________

    2     0     4     0             -4
```

QUESTION 4

TO OBTAIN BFS USING ALGEBRAIC METHOD Question Max Z= x1+x2+x3+0s1+0s2 st: x1+x2+s1=1 -x2+x3+s2=0 %xi>=0

```
clc
clear all
format short

% PHASE-1: Input the parameter
c=[1,1,1,0,0]; %Objective function
A=[1,1,0,1,0;0,-1,1,0,1]; %Coefficient Matrix
B=[1;0];%RHS of const
objective=1; %1 for max and -1 for minimization problem
%Number of possible solutions: nCm:nchoosek

% PHASE-2: Number of constraint and variable
m=size(A,1); %number of constraints
n=size(A,2); % number of variables

% PHASE-3: Compute the ncm Basic Solutions: The max number of basic
% solutions will always be nCm
nab=nchoosek(n,m); %total number of atmost basic solution
t=nchoosek(1:n,m); %from this we can extract our set of variables that we need to equate to zero

% PHASE-4:Construct the basic solution
% for this n>m must be satisfied
sol=[]; %default solution is zero (Empty Matrix)
if n>=m %if this is not statisfied then we can not have solutions
    for i = 1:nab
        y = zeros(n, 1);
        % Check if the selected variables form a singular matrix
        if rank(A(:, t(i, :))) == m
            X = A(:, t(i, :)) \ B; % Solve for basic variables
            if all(X >= 0)
                y(t(i, :)) = X;
                sol = [sol y];
            end
        end
    end
    disp("Solution: ");
    disp(sol);
else
    error('No. of variables is less than number of constraints')
end
if any(X == 0)
        fprintf("DEGENERATE SOLUTION\n");
else
    fprintf('NON-DEGENERATE SOLUTION\n');
end
%PHASE 5: To find optimal solution
Z=c*sol; %finding the values corresponding to each point
if(objective==1)
    [Zmax,Zindex]=max(Z);%storing the max value of Z and the col in which this max value resides
else
    [Zmax,Zindex]=min(Z);%storing the min value of Z and the col in which this min value resides
end
BFS=sol(:,Zindex);%basic feasible solution
[Optimal_Value]=[BFS' Zmax];
Optimal_bfs=array2table(Optimal_Value);
Optimal_bfs.Properties.VariableNames(1:size(Optimal_bfs,2))={'x1','x2','x3','s1','s2','Optimal Value of Z'};
disp(Optimal_bfs);
```

```
Solution:
     1     1     1     0     0     0     0     0
     0     0     0     1     0     1     0     0
     0     0     0     1     0     0     0     0
     0     0     0     0     1     0     1     1
     0     0     0     0     0     1     0     0

DEGENERATE SOLUTION
    x1    x2    x3    s1    s2    Optimal Value of Z
    __    __    __    __    __    __________________

    0     1     1     0     0              2
```

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