Thapar Institute of Engineering and Technology, Patiala

Department of Computer Science and Engineering

| B E- COE, CSE (VI Semester) MST | Course Code: UCS701 | |
|----------------------------------|--------------------------------------|--|
| | Course Name: Theory of Computation | |
| March 10, 2023, 3:30 PM | 9 | |
| Time: 2 Hours, M. Marks: 30 | Name Of Faculty: Sunita Garhwal, | |
| | Nitigya Sambyal, Chinmaya Panigrahy | |
| | Nidhi Kalra, Shashank Sheshar, Javed | |
| | Imran. | |

Note: Attempt all questions with proper justification. Assume missing data, if any, suitably.

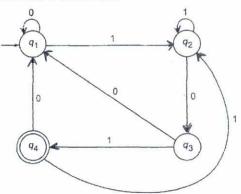
Q1. Given the regular expression $r = (101|10)^*$

(5)

- a) Convert the given r into NFA using Thompson's construction.
- b) Convert the obtained NFA into DFA using subset construction.
- c) Minimize the obtained DFA in 1 (b).
- Q2. Construct a deterministic finite automaton over $\Sigma = \{a, b\}$ such that

(6)

- a) It recognizes the language $G_1 = \{w \in \Sigma^*, \text{ where } |w| \ge 2 \text{ and the second symbol from right-hand side of } w \text{ is } b\}.$
- b) It recognizes the language $G_2 = \{ w \in \Sigma^* \mid w = \text{saba for some string } s \in \Sigma^* \}$.
- c) It recognizes the language $G_3 = \{a^nb^m \mid n, m \ge 1 \text{ and } n+m \text{ is even}\}.$
- Q3. a) Construct a Moore machine over $\Sigma = \{a, b\}$ which counts the occurrences of substring "baba" in the input string. Convert it into an equivalent Mealy machine. (3)
- Q3 b) Write a regular expression to represent all the even length strings over $\Sigma = \{0,1\}$ and ensure the number of zeros and ones are also even. (2)
- Q4. a) Write down regular expression corresponding to the following finite automaton using Arden's Theorem. (3)



[P.T.O.]

Q4. (b) Convert the given NFA with q_1 as initial and q_f as final state into its equivalent DFA:

| Current State | Input symbol | |
|----------------|--------------|----------------|
| | a | b |
| qı | q_1, q_2 | q_1 |
| q ₂ | - | q _f |
| qf | - | - |

(2)

Q5. (a) Find all strings in language
$$L=((a+b)*b(a+ab)*)$$
 of length less than four. Q5. (b) Consider the following productions of the regular grammar G:

 $S \rightarrow aA \mid a$

 $A \rightarrow aA \mid aB \mid a$

 $B \rightarrow bB \mid c$

Q5. (c) Write right linear grammar for
$$L = ba + (a + bb) a*b$$
.

(2)

Q6. (a) Using Pumping Lemma, prove that the language L is not regular
$$L = \{a^{n!} | n \ge 0\}$$
 (3)

Q6. (b) Consider languages L₁ and L₂ respectively where

(2)

 $L_1 = \{ w \mid 00 \text{ is not a substring of } w \}$ $L_2 = \{ w \mid w \text{ ends with } 01 \}$

Construct a DFA for the language L₁ - L₂.